F# Training M

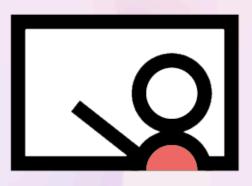
Monadic Types

2025 April



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Type
Option



Type Option

A.k.a Maybe (Haskell), Optional (Java 8)

Models the absence of value

→ Defined as a union with 2 cases

Option » Use cases

- 1. Modeling an optional field
- 2. Partial operation



Case 1: Modeling an optional field

```
type Civility = Mr | Mrs

type User = { Name: string; Civility: Civility option } with
    static member Create(name, ?civility) = { Name = name; Civility = civility }

let joey = User.Create("Joey", Mr)
let guest = User.Create("Guest")
```

- → Make it explicit that Name is mandatory and Civility optional
- Warning: this design does not prevent Name = null here (BCL limit)

Case 2. Partial operation

Operation where no output value is possible for certain inputs.

Example 1: inverse of a number

```
let inverse n = 1.0 / n

let tryInverse n =
    match n with
    | 0.0 → None
    | n → Some (1.0 / n)
```

Function	Operation	Signature	n = 0.5	n = 0.0
inverse	Partial	float → float	2.0	infinity ?
tryInverse	Total	$float \rightarrow float option$	Some 2.0	None 👌

Case 2. Partial operation (2)

Example 2: find an element in a collection

- → Partial operation: find predicate → 🛪 when item not found
- → Total operation: tryFind predicate → None or Some item

Benefits 👍

- → Explicit, honest / partial operation
 - → No special value: null, infinity
 - → No exception
- → Forces calling code to handle all cases:
 - → Some value → output value given
 - → None → output value missing

Option » Control flow

To test for the presence of the value (of type '7) in the option

- → X Do not use IsSome, IsNone and Value (🤞 🕸)
 - → if option.IsSome then option.Value...
- → d By hand with pattern matching.
- → ✓ Option.xxx functions ?

Manual control flow with pattern matching

Example:

Control flow with Option.xxx helpers

Mapping of the inner value (of type 'T) if present:

- \rightarrow map f option with f total operation 'T \rightarrow 'U
- ightarrow bind f option with f partial operation 'T ightarrow 'U option

Keep value if present and if conditions are met:

 \rightarrow filter predicate option with predicate: 'T \rightarrow bool called only if value present

Demo

→ Implementation of map, bind and filter with pattern matching

Demo » Solution

```
// (f: 'T \rightarrow 'U) \rightarrow 'T option \rightarrow 'U option
let map f option =
     match option with
        Some x \rightarrow Some (f x)
        None \rightarrow None
                                         // \uparrow \uparrow \uparrow 1. Why can't we write `None \rightarrow option`?
let bind f option =
                                         // (f: 'T \rightarrow 'U option) \rightarrow 'T option \rightarrow 'U option
     match option with
        Some x \rightarrow f x
        None \rightarrow None
let filter predicate option = // (predicate: 'T 
ightarrow bool) 
ightarrow 'T option 
ightarrow 'T option
     match option with
        Some x when predicate x \rightarrow option
                                         // ff 2. Implement `filter` with `bind`?
         \rightarrow None
```

T Bonus questions » Answers

```
let map (f: 'T \rightarrow 'U) (option: 'T option) : 'U option =
   match option with
     Some x \rightarrow Some (f x)
     None \rightarrow (*None*) option // \nearrow Type error: `'U option` given \neq `'T option` expected
```

```
// ## 2. Implement `filter` with `bind`?
let filter predicate option = // (predicate: 'T \rightarrow bool) \rightarrow 'T option \rightarrow 'T option
    option \triangleright bind (fun x \rightarrow if predicate x then option else None)
```

Integrated control flow » Example

```
// Question/answer console application
type \underline{Answer} = A \mid B \mid C \mid D
let tryParseAnswer =
    function
       "A" \rightarrow Some A
      "B" \rightarrow Some B
      "C" \rightarrow Some C
      "D" \rightarrow Some D
           → None
/// Called when the user types the answer on the keyboard
let checkAnswer (expectedAnswer: Answer) (givenAnswer: string) =
    tryParseAnswer givenAnswer
    ▷ Option.filter ((=) expectedAnswer)
    \triangleright Option.map (fun \_ \rightarrow " \checkmark ")
    > Option.defaultValue "X"
["X"; "A"; "B"] ▷ List.map (checkAnswer B) // ["X"; "X"; "V"]
```

Integrated control flow » Advantages

Makes business logic more readable

- → No if hasValue then / else
- → Highlight the happy path
- → Handle corner cases at the end
- The computation expressions ? provide an alternative syntax + lightweight

Option: comparison with other types

- 1. Option VS List
- 2. Option *VS* Nullable
- 3. Option *VS* null



Option *VS* List

Conceptually closed

- → Option ~ List of 0 or 1 items
- \rightarrow See Option.toList function: 't option \rightarrow 't list (None \rightarrow [], Some x \rightarrow [x])
- Option & List modules: many functions with the same name
- → contains, count, exist, filter, fold, forall, map
- A List can have more than 1 element
- → Type Option models absence of value better than type List

Option **VS** Nullable

System.Nullable<'T> ~ Option<'T> but more limited

- → Does not work for reference types
- → Lacks monadic behavior i.e. map and bind functions
- → Lacks built-in pattern matching Some x | None
- → In F#, no magic as in C# / keyword null
- ← C# uses nullable types whereas F# uses only Option

Option *VS* null

Due to the interop with the BCL, F# has to deal with null in some cases.

Good practice: isolate these cases and wrap them in an Option type.

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Type
Result



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Type Result

A.k.a Either (Haskell)

Models a double-track Success/Failure

Functional way of dealing with business errors (expected errors)

- → Allows exceptions to be used only for exceptional errors
- → As soon as an operation fails, the remaining operations are not launched

Railway-oriented programming (ROP)
https://fsharpforfunandprofit.com/rop/

Module Result

Contains less functions than Option !? map f result : to map the success \cdot ('T \rightarrow 'U) \rightarrow Result<'T, 'Error> \rightarrow Result<'U, 'Error> mapError f result : to map the error $('Err1 \rightarrow 'Err2) \rightarrow Result<'T, 'Err1> \rightarrow Result<'T, 'Err2>$ bind f result : same as map with f returning a Result $('T \rightarrow Result<'U, 'Error>) \rightarrow Result<'T, 'Error> \rightarrow Result<'U, 'Error>$ · The result is flattened, like the flatMap function on JS arrays · A Same type of 'Error for f and the input result.

Quiz Result 🚣

Implement Result.map and Result.bind

- Tips:
 - → Map the Success track
 - → Access the Success value using pattern matching



Quiz Result 🐶

Solution: implementation of Result.map and Result.bind

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Result: Success/Failure tracks

map: no track change

```
Track Input Operation Output Success - 0k \times \longrightarrow map(x \rightarrow y) \longrightarrow 0k \times Failure - Error e \longrightarrow map(\dots) \longrightarrow Error e
```

bind: eventual routing to Failure track, but never vice versa

```
Track Input Operation Output Success - Ok x \longrightarrow bind( x \rightarrow Ok y ) \longrightarrow Ok y \longrightarrow bind( x \rightarrow Error e2 ) \bigcirc Failure - Error e \longrightarrow bind( .... ) \longrightarrow Error \sim
```

The mapping/binding operation is never executed in track Failure.

Result *VS* Option

Option can represent the result of an operation that may fail But if it fails, the option doesn't contain the error, just None

```
Option<'T> \simeq Result<'T, unit>

→ Some x \simeq Ok x

→ None \simeq Error ()

→ See Result.toOption (built-in) and Result.ofOption (below)
```

```
[<RequireQualifiedAccess>]
module Result =
    let ofOption error option =
        match option with
        | Some x → Ok x
        | None → Error error
```

Result *VS* Option (2)

7 Dates:

- The Option type is part of F# from the get go
- · The Result type is more recent: introduced in F# 4.1 (2016)
 - → After numerous articles on F# for fun and profit

Memory:

- · The Option type (alias: option) is a regular union: a reference type
- · The Result type is a struct union: a value type
- · The ValueOption type (alias: voption) is a struct union
 - → ValueNone | ValueSome of 't

Result VS Option » Example

Let's change our previous checkAnswer to indicate the Error:

```
type Answer = A | B | C | D
type <u>Error</u> = InvalidInput of string | WrongAnswer of Answer
let tryParseAnswer =
    function
       "A" \rightarrow Ok A
       "B" \rightarrow 0k B
      "C" \rightarrow 0k C
      "D" \rightarrow Ok D
       s \rightarrow Error(InvalidInput s)
let checkAnswerIs expected actual =
    if actual = expected then Ok actual else Error(WrongAnswer actual)
```

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Result VS Option » Example (2)

```
let printAnswerCheck (givenAnswer: string) =
    tryParseAnswer givenAnswer

    ▷ Result.bind (checkAnswerIs B)

    > function
         0k x
                   → printfn $"%A{x}: 
✓ Correct
         Error(WrongAnswer x) \rightarrow printfn $"%A{x}: \times Wrong Answer"
         Error(InvalidInput s) \rightarrow printfn $"%s{s}: \times Invalid Input"
printAnswerCheck "X";; // X: X Invalid Input
printAnswerCheck "A";; // A: 🗙 Wrong Answer
printAnswerCheck "B";; // B: ✓ Correct
```

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5 Smart constructor



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Smart constructor: Purpose

- " Making illegal states unrepresentable
- https://kutt.it/MksmkG F♯ for fun and profit, Jan 2013
 - → Design to prevent invalid states
 - → Encapsulate state (all primitives) in an object
 - → Smart constructor guarantees a valid initial state
 - → Validates input data
 - → If Ko, returns "nothing" (Option) or an error (Result)
 - → If Ok, returns the created object wrapped in an Option / a Result

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Encapsulate the state in a type

- → Single-case (discriminated) union 👌 : Type X = private X of a: 'a...
- https://kutt.it/mmMXCo F♯ for fun and profit, Jan 2013
- → Record : Type X = private { a: 'a... }
- https://kutt.it/cYP4gY Paul Blasucci, Mai 2021
- private keyword:
- → Hide object content
- → Fields and constructor no longer visible from outside
- → Smart constructor defined in companion module or static method

Smart constructor » Example #1

Smart constructor:

- → tryCreate function in companion module
- → Returns an Option

Smart constructor » Example #2

Smart constructor:

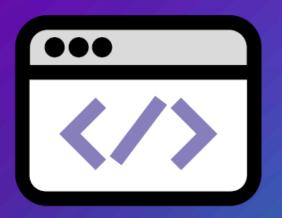
- → Static method of
- → Returns Result with error of type string

```
type Tweet =
    private { Tweet: string }

static member Of tweet =
    if System.String.IsNullOrEmpty tweet then
        Error "Tweet shouldn't be empty"
    elif tweet.Length > 280 then
        Error "Tweet shouldn't contain more than 280 characters"
    else Ok { Tweet = tweet }

let tweet1 = Tweet.Of "Hello world" // Ok { Tweet = "Hello world" }
```

Computation
expression



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Computation expression (CE)

Syntactic sugar hiding a "machinery"

- → Applies the Separation of Concerns principle
- → Code should be more readable inside the computation expression

```
Syntax: builder { expr }
```

- → builder instance of a "Builder"
- → expr can contain let, let!, do!, yield, yield!, return, return!
- Note: seq, async and task are CEs

Builder

A computation expression relies on an object called Builder.

→ This object can be used to store a background state.

For each supported keyword (let!, return ...), the *Builder* implements one or more related methods. Examples:

```
• builder { return expr } → builder.Return(expr)
```

```
• builder { let! x = expr; cexpr } → builder.Bind(expr, (fun x → {| cexpr |}))
```

The builder can also wrap the result in a type of its own:

- async { return x } returns an Async<'X> type
- seq { yield x } returns a type Seq<'X>

Builder desugaring

The compiler translates to the builder methods.

→ The CE hides the complexity of these calls, which are often nested:

Builder - Example: logger

Need: log the intermediate values of a calculation

```
let log value = printfn $"{value}"

let loggedCalc =
    let x = 42
    log x // 
    let y = 43
    log y // 
    let z = x + y
    log z // 
    z
```

Problems 1

- ① Verbose: the log x interfere with reading
- 2 Error prone: forget a log, log wrong value...

Builder - Example: logger (2)

Make logs implicit in a CE when let! / Bind :

```
type LoggingBuilder() =
    let log value = printfn $"{value}"; value
    member _.Bind(x, f) = x \triangleright log \triangleright f
    member _.Return(x) = x
let logger = LoggingBuilder()
// ---
let loggedCalc = logger {
    let! x = 42
    let! y = 43
    let! z = x + y
    return z
```

Builder - Example: maybe

Need: simplify the sequence of "trySomething" returning an Option

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Builder - Example: maybe (2)

```
// With CE
type MaybeBuilder() =
   member _.Bind(x, f) = x \triangleright Option.bind f
   member _.Return(x) = Some x
let maybe = MaybeBuilder()
let division' = maybe {
    let! v1 = 36 ▷ tryDivideBy 2
    let! v2 = v1 ▷ tryDivideBy 3
    let! v3 = v2 ▷ tryDivideBy 2
    return v3
```

Result: Symmetry, X Intermediate values

Limit: nested CEs

- Different CEs can be nested
- X But code becomes difficult to understand

Example: combining logger and maybe ?

Alternative solution 27 27:

Limit: combining CEs

```
How to combine Async + Option / Result ?

→ asyncResult CE + helpers in FsToolkit
```

```
type LoginError =
     InvalidUser InvalidPassword
     Unauthorized of AuthError | TokenErr of TokenError
let login username password =
   asyncResult {
        // tryGetUser: string → Async<User option>
        let! user = username > tryGetUser > AsyncResult.requireSome InvalidUser
        // isPasswordValid: string \rightarrow User \rightarrow bool
       do! user ▷ isPasswordValid password ▷ Result.requireTrue InvalidPassword
        // authorize: User → Async<Result<unit, AuthError>>
       do! user ▷ authorize ▷ AsyncResult.mapError Unauthorized
        // createAuthToken: User → Result<AuthToken, TokenError>
       return! user ▷ createAuthToken ▷ Result.mapError TokenErr
    } // Async<Result<AuthToken, LoginError>>
```

CE: the Swiss army knife 💝

The computation expressions serve different purposes:

- \cdot C# yield return \rightarrow F# seq {}
- C \sharp async/await → F \sharp async {}
- C♯ LINQ expressions from ... select → F♯ query {}

•

Underlying theoretical foundations:

- Monoid
- Monad
- Applicative



Monoid

- ≃ Type T defining a set with:
- 1. Operation $(+): T \rightarrow T \rightarrow T$
 - → To combine sets and keep the same "type"
 - \rightarrow Associative: a + (b + c) \equiv (a + b) + c
- 2. Neutral element (aka identity) \simeq empty set
 - → Combinable with any set without effect
 - \rightarrow a + e \equiv e + a \equiv a

CE monoidal

The builder of a monoidal CE (such as seq) has at least:

- → Yield to build the set element by element
- \rightarrow Combine \equiv (+) (Seq.append)
- → Zero = neutral element (Seq.empty`)

Generally added (among others):

- → For to support for x in xs do ...
- → YieldFrom to support yield!

Monad

- ≃ Generic type M<'T> with:
- 1. return construction function
 - → Signature: (value: 'T) → M<'T>
 - → ≃ Wrap a value
- 2. Link function bind (aka >= operator)
 - \rightarrow Signature: (f: 'T \rightarrow M<'U>) \rightarrow M<'T> \rightarrow M<'U>
 - → Use wrapped value, map with f function to a value of another type and re-wrap the result

Monad: laws

```
return ≡ neutral element for bind
      Left: return x \triangleright bind f \equiv f x
        Right: m ▷ bind return ≡ m
bind is associative
           \triangleright bind f \triangleright bind g \equiv m \triangleright bind (fun x \rightarrow f x \triangleright bind g)
```

Monads and languages

Haskell

- · Monads used a lot. Common ones: IO, Maybe, State, Reader.
- · Monad is a type class for easily creating your own monads.

F♯

- Some CEs allow monadic operations.
- · More rarely used directly (except by Haskellers, OCamlers...)

C#

- · Monad implicit in LINQ
- · <u>LanguageExt</u> library for functional programming

Monadic CE

The builder of a monadic CE has Return and Bind methods.

The Option and Result types are monadic.

→ We can create their own CE:

```
type OptionBuilder() =
    member _.Bind(x, f) = x > Option.bind f
    member _.Return(x) = Some x

type ResultBuilder() =
    member _.Bind(x, f) = x > Result.bind f
    member _.Return(x) = Ok x
```

Monadic and generic CE

FSharpPlus provides a monad CE

→ Works for all monadic types: Option, Result, ... and even Lazy!

```
#r "nuget: FSharpPlus"
open FSharpPlus
let lazyValue = monad {
    let! a = lazy (printfn "I'm lazy"; 2)
    let! b = lazy (printfn "I'm lazy too"; 10)
    return a + b
} // System.Lazy<int>
let result = lazyValue.Value
// I'm lazy
// I'm lazy too
   val result : int = 12
```

Monadic and generic CE (2)

Example with Option type:

```
#r "nuget: FSharpPlus"
open FSharpPlus

let addOptions x' y' = monad {
    let! x = x'
    let! y = y'
    return x + y
}

let v1 = addOptions (Some 1) (Some 2) // Some 3
let v2 = addOptions (Some 1) None // None
```

Monadic and generic CE (3)

Limit: several monadic types cannot be mixed!

```
#r "nuget: FSharpPlus"
open FSharpPlus
let v1 = monad {
    let! a = 0k 2
   let! b = Some 10
    return a + b
 // * Error FS0043 ...
let v2 = monad {
    let! a = 0k 2
    let! b = Some 10 ▷ Option.toResult
    return a + b
} // val v2 : Result<int,unit> = 0k 12
```

Specific monadic CE

<u>FsToolkit.ErrorHandling</u> library provides:

- CE option {} specific to type Option<'T> (example below)
- CE result {} specific to type Result<'0k, 'Err>
- Recommended as it is more explicit than monad CE.

```
#r "nuget: FSToolkit.ErrorHandling"
open FsToolkit.ErrorHandling

let addOptions x' y' = option {
    let! x = x'
    let! y = y'
    return x + y
}

let v1 = addOptions (Some 1) (Some 2) // Some 3
let v2 = addOptions (Some 1) None // None
```

Applicative (a.k.a Applicative Functor)

 \simeq Generic type M<'T> -- 3 styles:

Style A: Applicative with apply / <*> and pure / return

- X Not easy to understand
- · Not recommended by Don Syme in the Nov. 2020 note

Style B: Applications with mapN

· map2, map3... map5 combines 2 to 5 wrapped values

Style C: Applicatives with let! ... and! ... in a CE

- · Same principle: combine several wrapped values
- Available from F♯ 5 (announcement Nov. 2020)
- **Tip:** Styles B and C are equally recommended.

Applicative CE

Library <u>FsToolkit.ErrorHandling</u> offers:

- · CE validation {} supporting let! ... and! ... syntax.

Allows errors to be accumulated → Uses:

- Parsing external inputs
- · Smart constructor (Example code slide next...)

Applicative CE: example

```
#r "nuget: FSToolkit.ErrorHandling"
open FsToolkit.ErrorHandling
type [<Measure>] cm
type <u>Customer</u> = { Name: string; Height: int<cm> }
let validateHeight height =
    if height ≤ 0<cm>
    then Error "Height must me positive"
    else Ok height
let validateName name =
    if System.String.IsNullOrWhiteSpace name
    then Error "Name can't be empty"
    else Ok name
module Customer =
    let tryCreate name height : Result<Customer, string list> =
        validation {
            let! validName = validateName name
            and! validHeight = validateHeight height
            return { Name = validName; Height = validHeight }
let c1 = Customer.tryCreate "Bob" 180<cm> // Ok { Name = "Bob"; Height = 180 }
let c2 = Customer.tryCreate "Bob" 0<cm> // Error ["Height must me positive"]
let c3 = Customer.tryCreate "" 0<cm> // Error ["Name can't be empty"; "Height must me positive"]
```

Applicative vs Monad

The Result type is "monadic": on the 1st error, we "unplug".

There is another type called Validation that is "applicative": it allows to accumulate errors.

- → ≃ Result<'ok, 'error list>
- → Handy for validating user input and reporting all errors

Ressources

- → <u>FsToolkit.ErrorHandling</u>
- → Validation with F# 5 and FsToolkit

Applicative *vs* Monad (2)

Example: Validation.map2 to combine 2 results and get the list of their eventual errors.

```
module Validation =
    // f : 'T → 'U → Result<'V, 'Err list>
    // x': Result<'T, 'Err list>
    // y': Result<'U, 'Err list>
    // → Result<'V, 'Err list>
    let map2 f x' y' =
        match x', y' with
        | Ok x, Ok y → f x y
        | Ok _, Error errors | Error errors, Ok _ → Error errors
        | Error errors1, Error errors2 → Error (errors1 @ errors2) // → ②
```

Other CE

We've seen 2 libraries that extend F♯ and offer their CEs:

- → FSharpPlus → monad
- → FsToolkit.ErrorHandling → option, result, validation

Many libraries have their own DSL (Domain Specific Language.)
Some are based on CE:

- → Expecto: Testing library (test "..." { ... })
- → Farmer: Infra as code for Azure (storageAccount { ... })
- → <u>Saturn</u>: Web framework on top of ASP.NET Core (application { ... })

5 Wrap up



F♯ Training・Monadic Types

Union types: Option and Result

- → What they are used for:
 - → Model absence of value and business errors
 - → Partial operations made total tryXxx
 - → Smart constructor tryCreate
- → How to use them:
 - → Chaining: map, bind, filter → ROP
 - → Pattern matching
- → Their benefits:
 - → null free, Exception free → no guard clauses Cluttering the code
 - → Makes business logic and happy path more readable

Computation expression (CE)

- → Syntactic sugar: inner syntax standard or "banged" (let!)
- → Separation of Concerns: business logic vs "machinery"
- → Compiler is linked to builder
 - → Object storing a state
 - → Builds an output value of a specific type
- → Can be nested but not easy to combine!
- → Underlying theoretical concepts
 - → Monoid → seq (of composable elements and with a "zero")
 - → Monad → async, option, result
 - → Applicative → validation / Result<'T, 'Err list>
- → Libraries: FSharpPlus, FsToolkit, Expecto, Farmer, Saturn

Ô

Additional ressources

- → Compositional IT (Isaac Abraham)
 - → Writing more succinct C# in F#! (Part 2) · 2020
- → F# for Fun and Profit (Scott Wlaschin)
 - → The Option type · 2012
 - → <u>Making illegal states unrepresentable</u> · 2013
 - → The "Map and Bind and Apply, Oh my!" series · 2015
 - → The "Computation Expressions" series · 2013
- → Extending F# through Computation Expressions
 - → 🔓 Video
- → Computation Expressions Workshop
- → <u>Applicatives IRL</u> by Jeremie Chassaing

Thanks 🙏

