

## Assignment 3 -- Programming Project

### Design and Analysis of Algorithms (CS 4071) – Spring 2018

#### Diameter and Connected Components of a Network

*Electronic copy of source code due Thursday, March 22 at 12:00 midnight. Hard copy due at beginning of class on Friday, March 23. Include your group number and members of the group as a comment at the beginning of the program and submit only ONE hard copy and ONE electronic copy (have ONE group member upload electronic copy).*

**Topics covered:** *Graphs, BFS, BFT, diameter, connected components.*

The topology of a network is modeled with a graph. Write a C++ program that inputs a graph  $G$  by first inputting the number of vertices  $n$  followed by a sequence of pairs  $i\ j$  where  $i$  and  $j$  are integers between 0 and  $n$ , inclusive, representing the edges of the graph, and ending with a negative integer sentinel to indicate the end of the input. For example,

5   0   1   1   4   2   3   1   3   3   4   -1

represents the graph  $G = (V, E)$  given by:

$$V = \{0, 1, 2, 3, 4\}$$

$$E = \{\{0, 1\}, \{1, 4\}, \{2, 3\}, \{1, 3\}, \{3, 4\}\}.$$

Your program will compute the **diameter** of  $G$  in the case when  $G$  is connected and the **connected components** of  $G$ , otherwise.

You can proceed as follows:

- Implement the graph  $G$  with its **adjacency matrix**
- Implement the function  $\text{BFS}(G, v)$  for performing a **breadth-first search** where the visit operation involves computing the distance from  $v$  to the vertex being visited. This will require a queue, which you can get from the Standard Template Library (STL).
- Implement a function  $\text{Diameter}(G)$  that returns the **diameter** of  $G$  if  $G$  is connected and -1, otherwise.
- Implement a function  $\text{Components}(G)$  for computing the vertex sets of the connected components of  $G$ .  $\text{Components}()$  will employ a BFT (Breadth-First Traversal), which involves calling  $\text{BFS}(G, v)$ ,  $v = 0, 1, \dots, n - 1$ , as discussed in class.

Store the entire source code for your program in a **single** file. Your program should run using Visual C++.

Have your program output the adjacency matrix of the graph as well as the diameter in the case when  $G$  is connected and the connected components, otherwise. Output the connected components by outputting the vertex set of each connected component.

Your program should be **user-friendly**, **well-commented**, with the output **well-documented**.

Submit the source code for your program on-line by uploading to Blackboard (have ONE member of your group upload. Make sure to include a comment in your program with your Group Number and Group Members). Also submit a **hard copy** of your program with output for **two** sample runs, one with a connected graph  $G$  and one with a disconnected graph  $G$  (ONE hard copy per group submitted at the beginning of class on the due date).