# Assignment 4 - CS 4071 - Spring 2018

Due: 2018-02-19

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## 1. Exercise 6.5

**Problem**: Solve the following instance of the knapsack problem for capacity C=30.

i	0	1	2	3	4	5	6	7
$v_i$	60	50	40	30	20	10	5	1
$w_i$	30	100	10	10	8	8	1	1

To solve this knapsack problem, we want to greedily select objects of decreasing densities, i.e. the ratio of value to weight,  $v_i/w_i$ , until the knapsack is full. So first we compute the densities for each object.

	i	0	1	2	3	4	5	6	7
$f_i$	$=v_i/w_i$	2	0.5	4	3	2.5	1.25	5	1

Then we repeatedly select the next available object with the highest density until the knapsack is full (or we run out of items).

- 0. Starting capacity: 30
- 1. Select: 6 (d=5, w=1), fraction: 1, remaining capacity: 29
- 2. Select: 2 (d=4, w=10), fraction: 1, remaining capacity: 19
- 3. Select: 3 (d=3, w=10), fraction: 1, remaining capacity: 9
- 4. Select: 4 (d=2.5, w=8), fraction: 1, remaining capacity: 1
- 5. Select: 0 (d=2, w=30), fraction: 1/30, remaining capacity: 0

The fractions,  $f_i$ , of each item that yield the optimal value for the knapsack are provided in the table below.

i	0	1	2	3	4	5	6	7	Total
$f_i$	1/30	0	1	1	1	0	1	0	
$f_i v_i$	2	0	40	30	20	0	5	0	97
$f_iw_i$	1	0	10	10	8	0	1	0	30

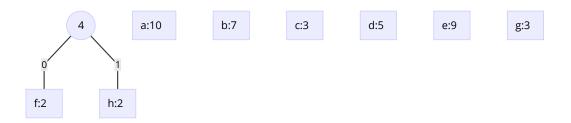
## 2. Exercise 6.9

**Problem**: Trace the action of *HuffmanCode* for the letters *a*, *b*, *c*, *d*, *e*, *f*, *g*, *h* occurring with frequencies 10, 7, 3, 5, 9, 2, 3, 2.

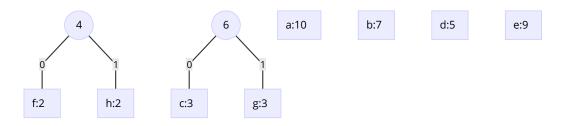
#### 0. Initial forest



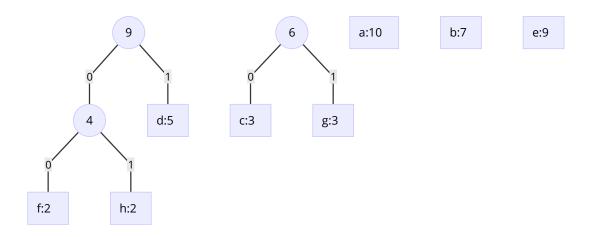
#### 1. Stage 1



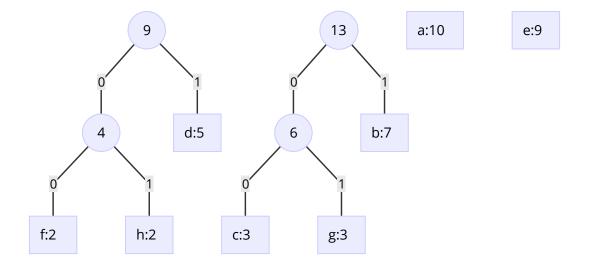
#### 2. Stage 2



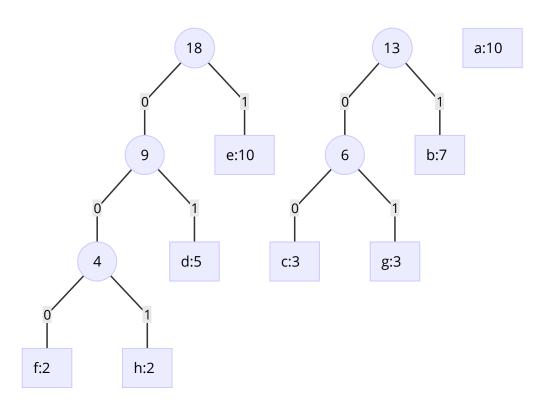
#### 3. Stage 3



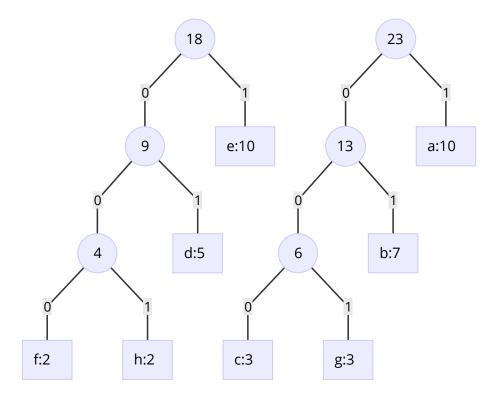
#### 4. Stage 4



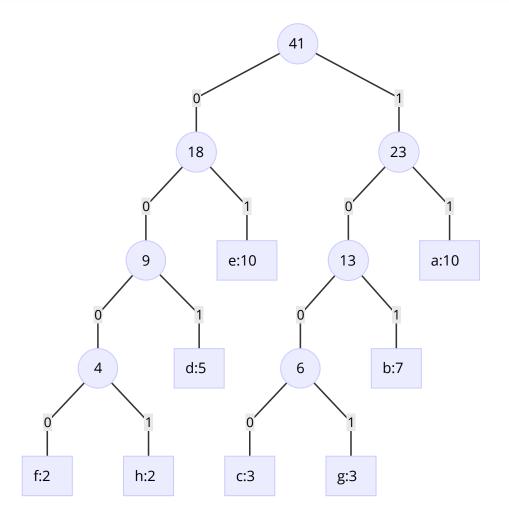
## 5. Stage 5



## 6. Stage 6



7. Stage 7: Huffman Tree



letter	frequency	encoding
а	10	11
b	7	101
С	3	1000
d	5	001
е	9	01
f	2	0000
g	3	1001
h	2	0001

## **3. Exercise 6.10**

**Problem**: Given the Huffman Code Tree in Figure 6.6, decode the string 100111100001101111001

Figure 6.6

letter	frequency	encoding
а	9	01
Ь	8	00
С	5	101
d	3	1001
е	15	11
f	2	1000

We read binary characters from the encoded string one at a time. Because the Huffman Code is a prefix code, when the binary substring we've read matches one of the letter encodings from Figure 6.6 we can unambiguously determine which letter is decoded.

Reading the string from the front:

1. 
$$1001 = d$$

3. 
$$1000 = f$$

4. 
$$01 = a$$

7. 
$$1001 = d$$

Then 10011111000011011111001 decoded is "defaced".