

1ST Semester, 2nd Quarter
Performance Task
Calculus for Grade 12
SY 2016-2017

Name of Author:

Obee Principio

Title of Mobile Application:

LEON

Description of Mobile Application:

LEON is a learning tool that aims to teach Basic Calculus in an effective manner. Read easy to digest infographics. Practice and test your knowledge. Earn XP and unlock achievements.

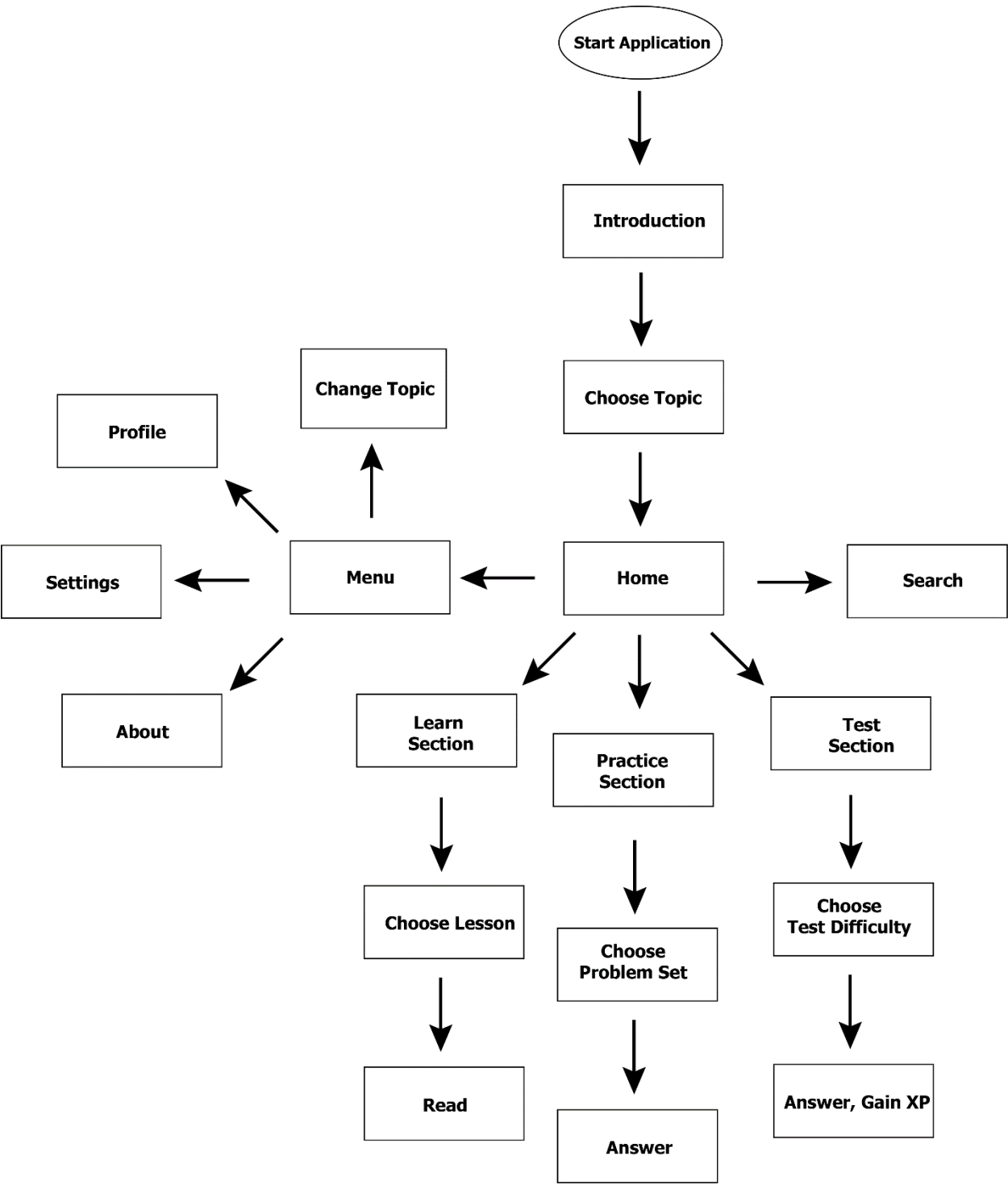
Functionalities:

- Learn – Easy to digest. Read more to learn more.
- Practice – No time limit, no stress. Practice makes perfect.
- Test – Battle the clock. Preserve your hearts. Test your capabilities.
- Profile – Earn XP. Unlock achievements.
- Search – Find what you're looking for. Easier navigation.

Logo



Flowchart/Diagram:

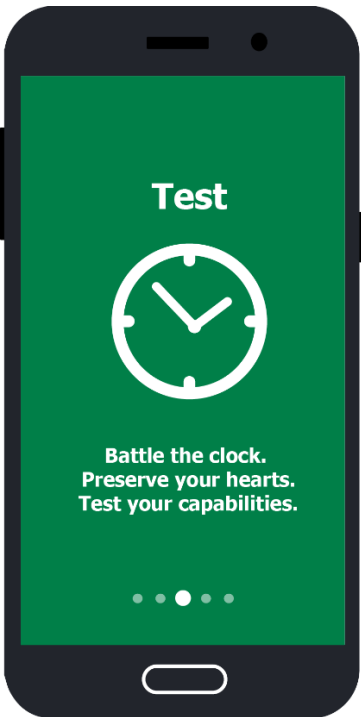
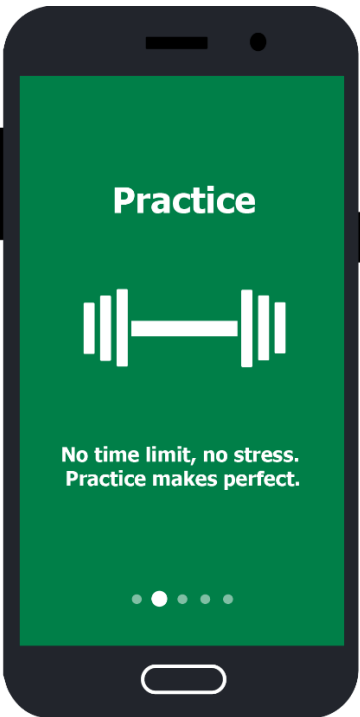
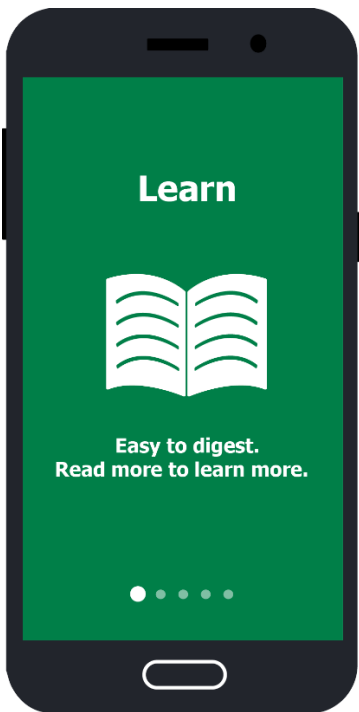


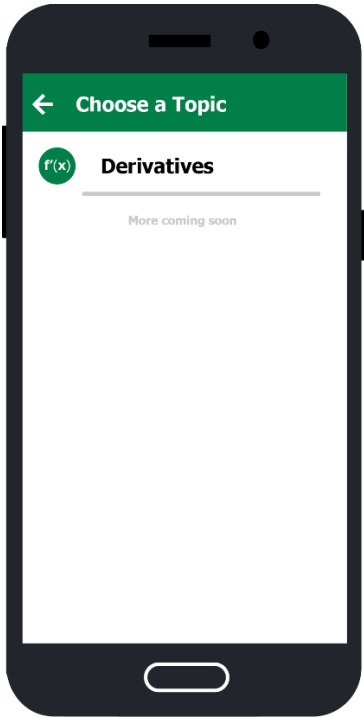
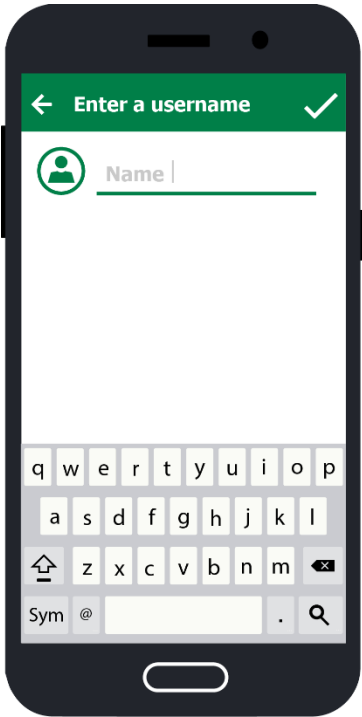
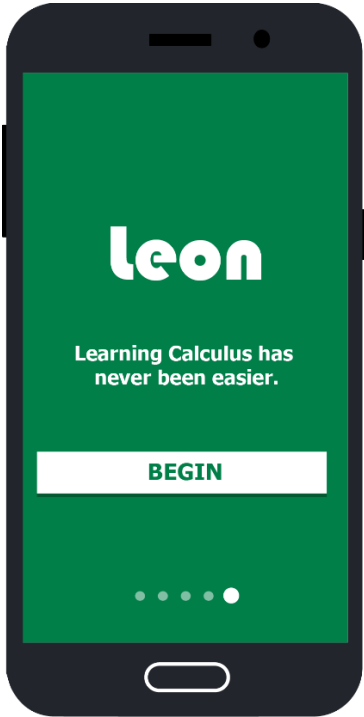
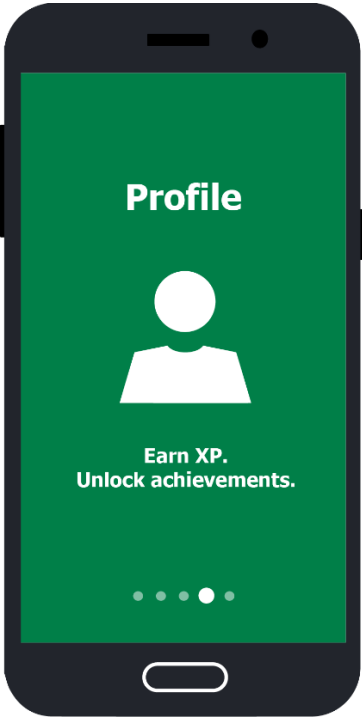
Sample Layout of Mobile:

Loading Screen

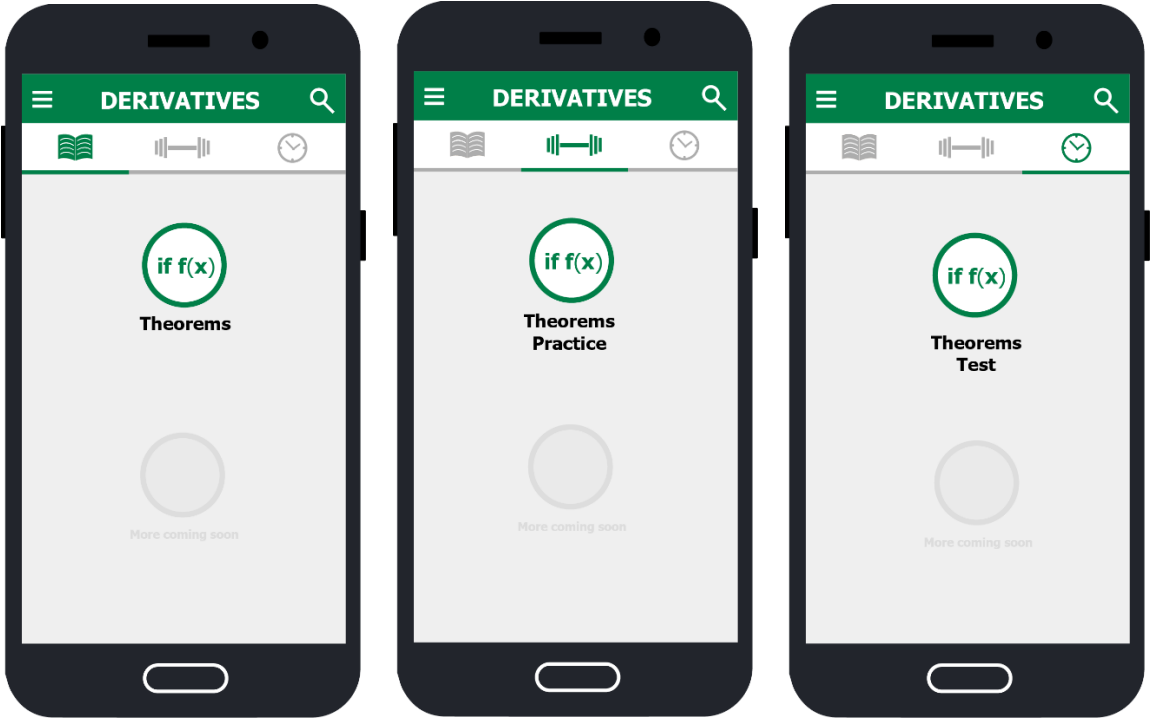


Introduction

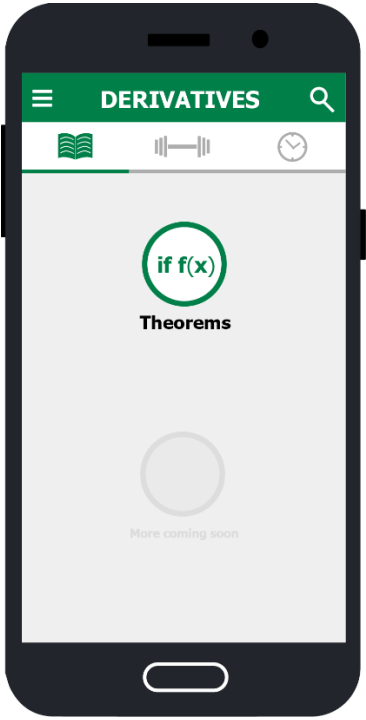


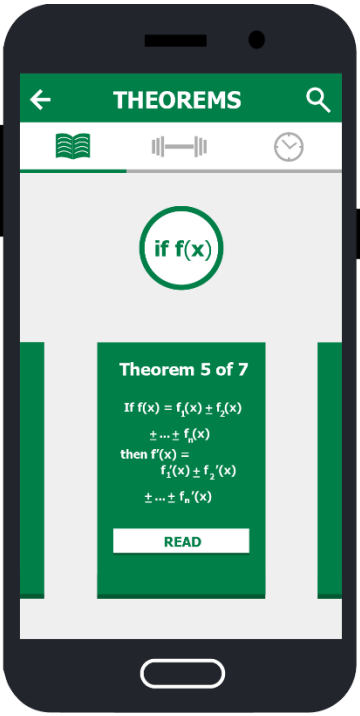
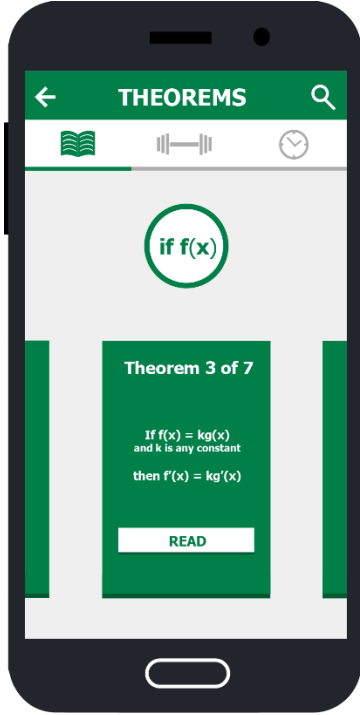
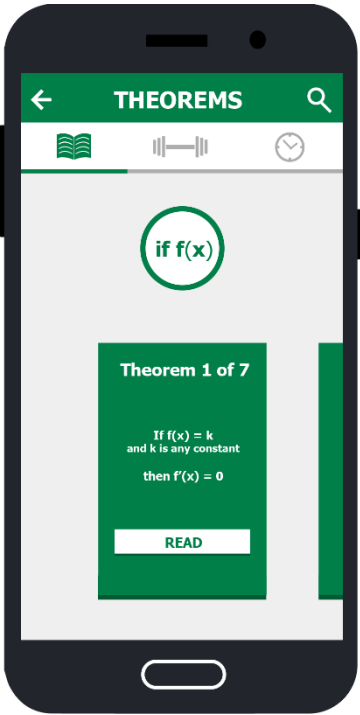


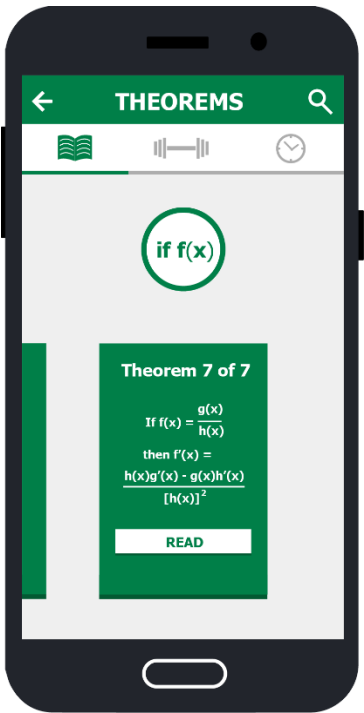
Home



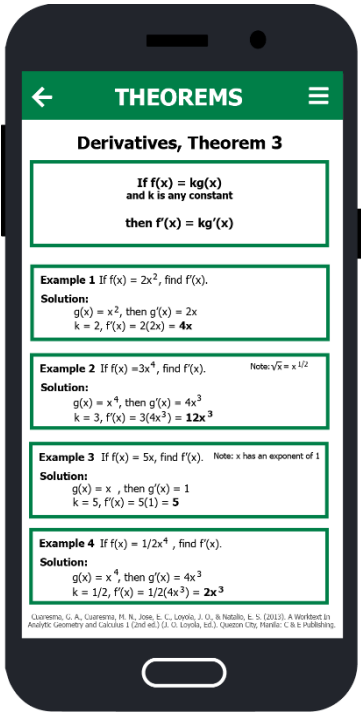
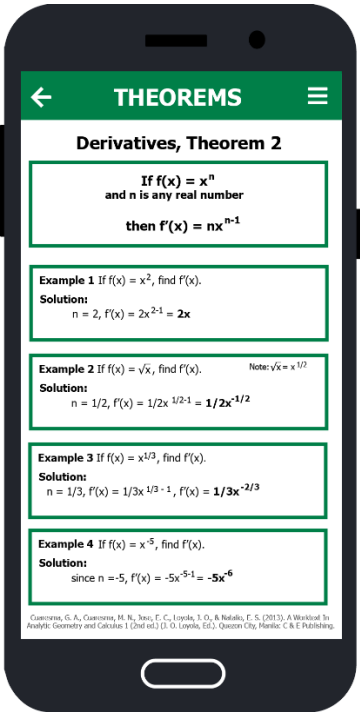
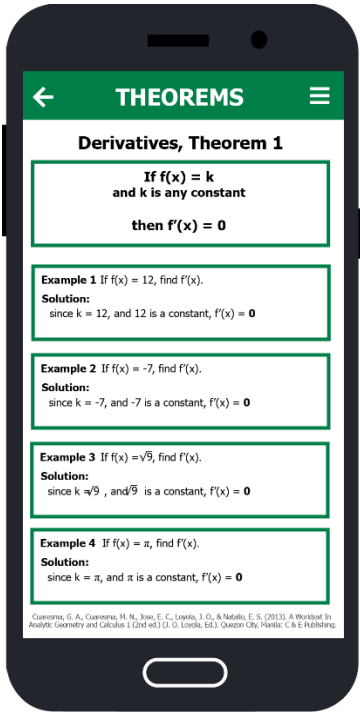
Learn Section

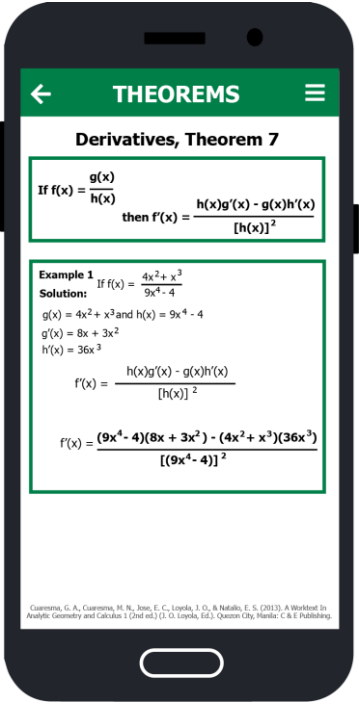
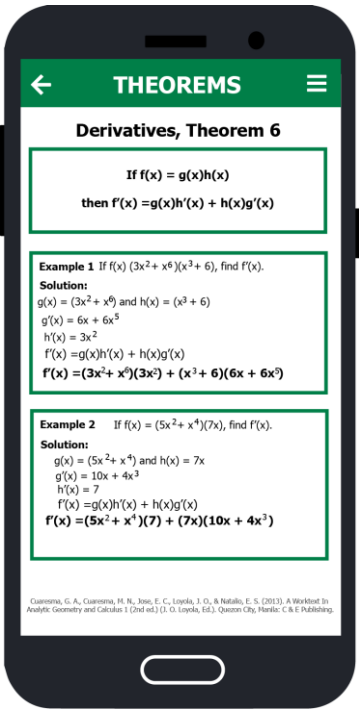
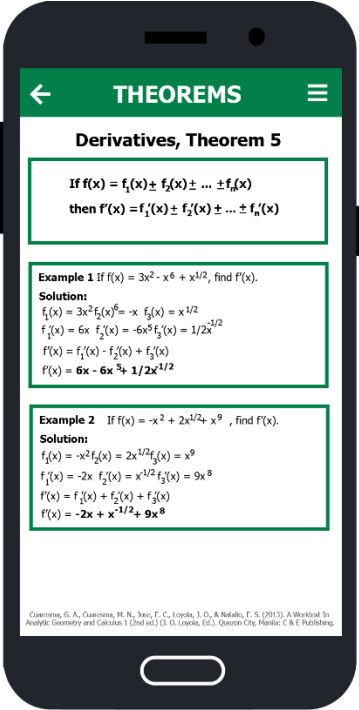
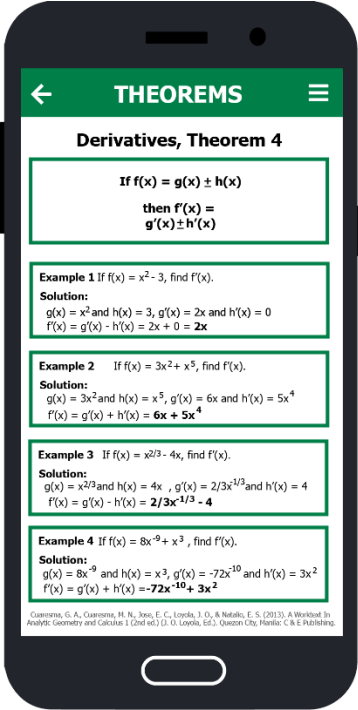




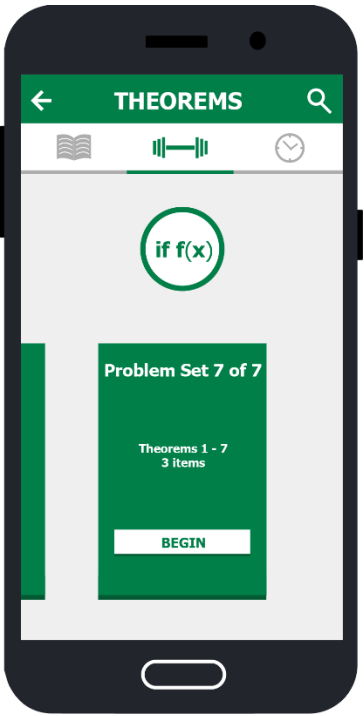
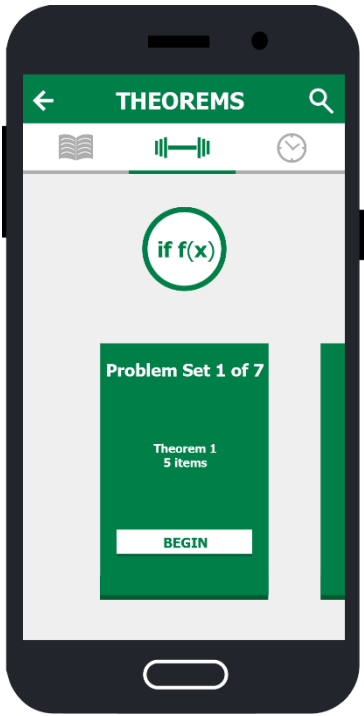
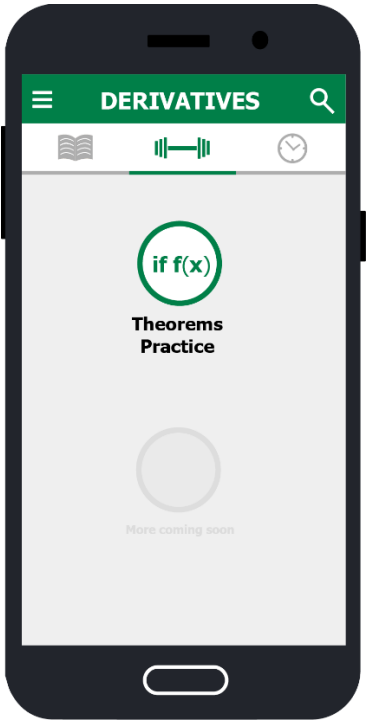


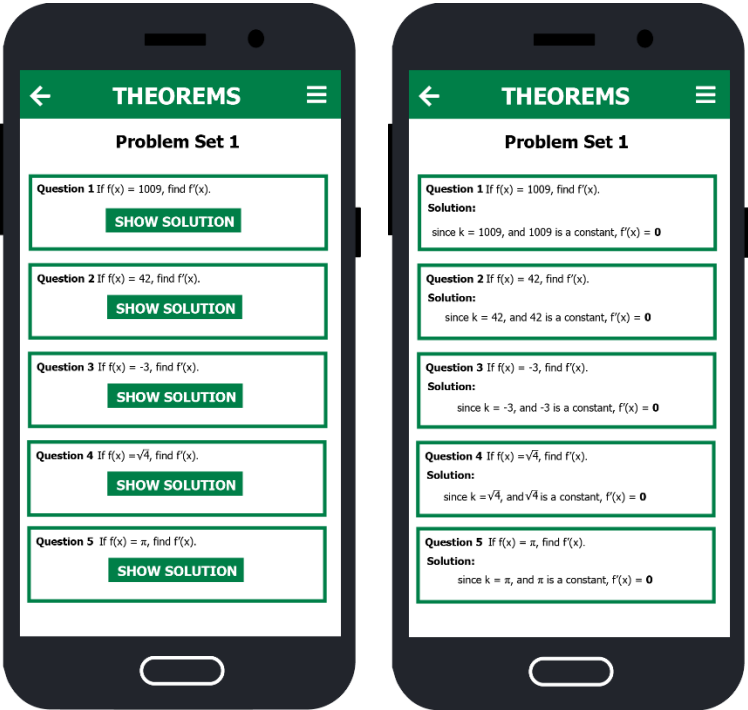
**Note: High resolution infographics are available at the end of the document*



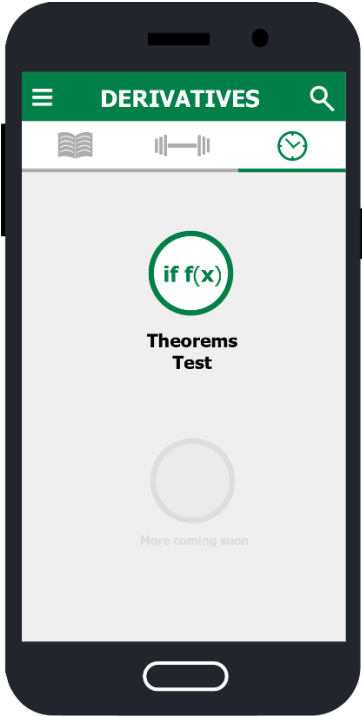


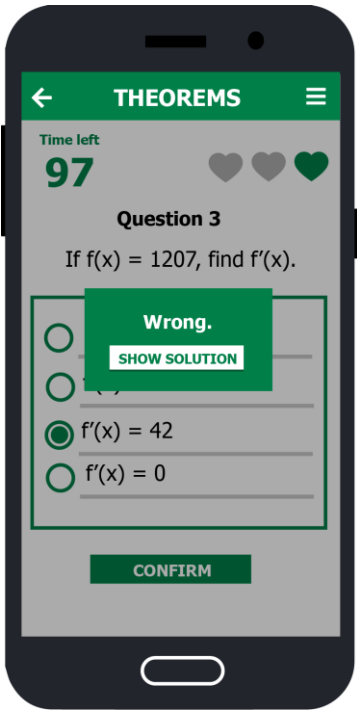
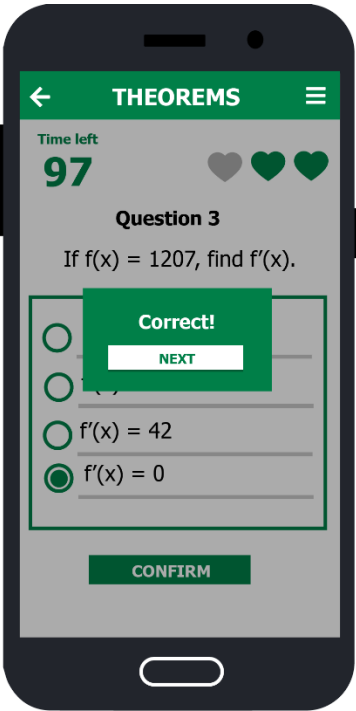
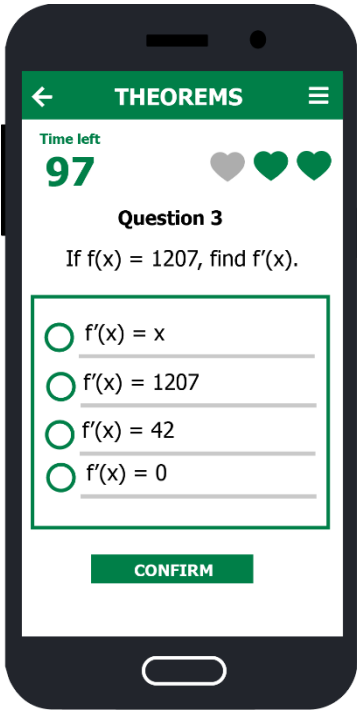
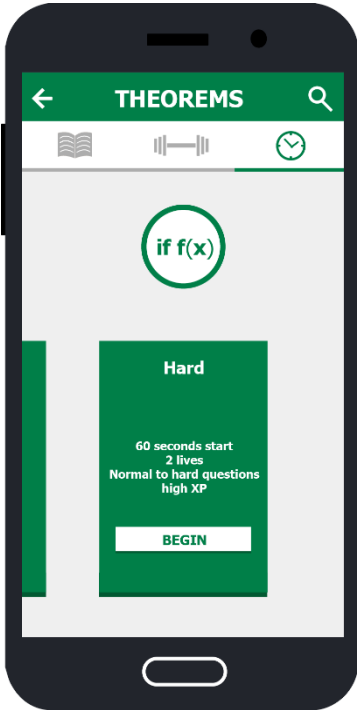
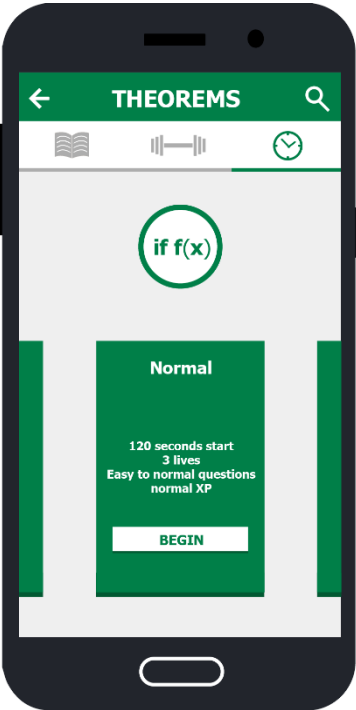
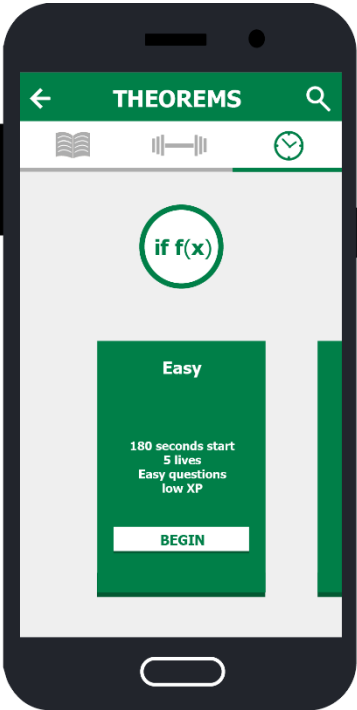
Practice Section

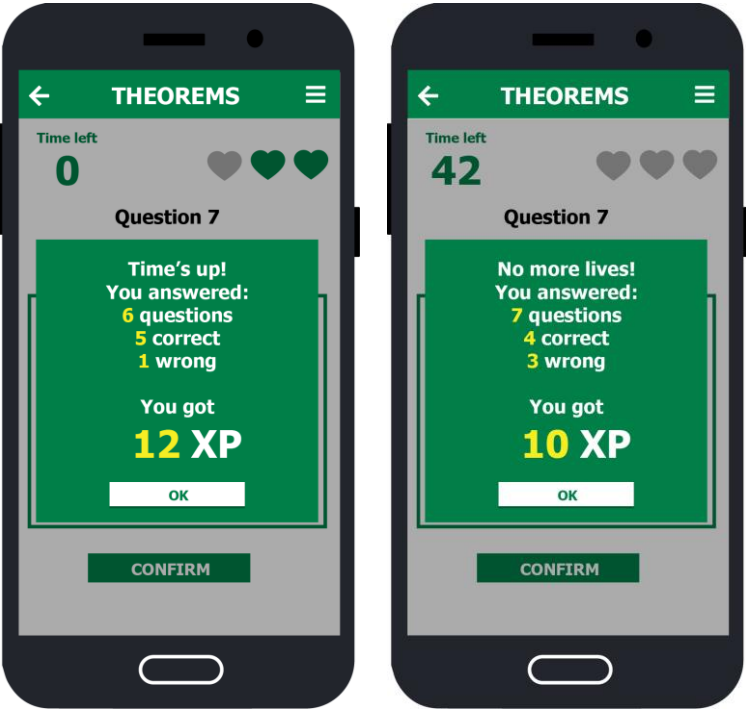




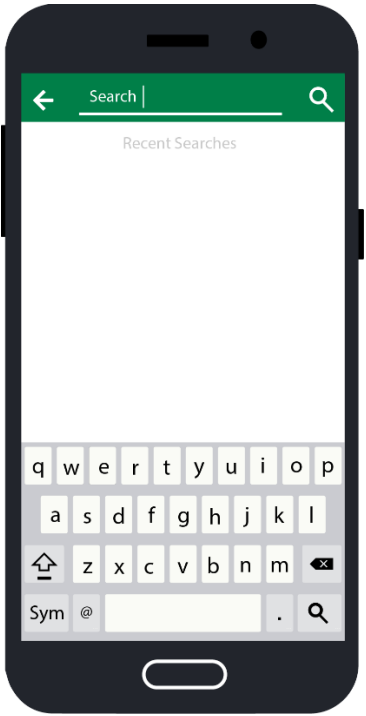
Test Section



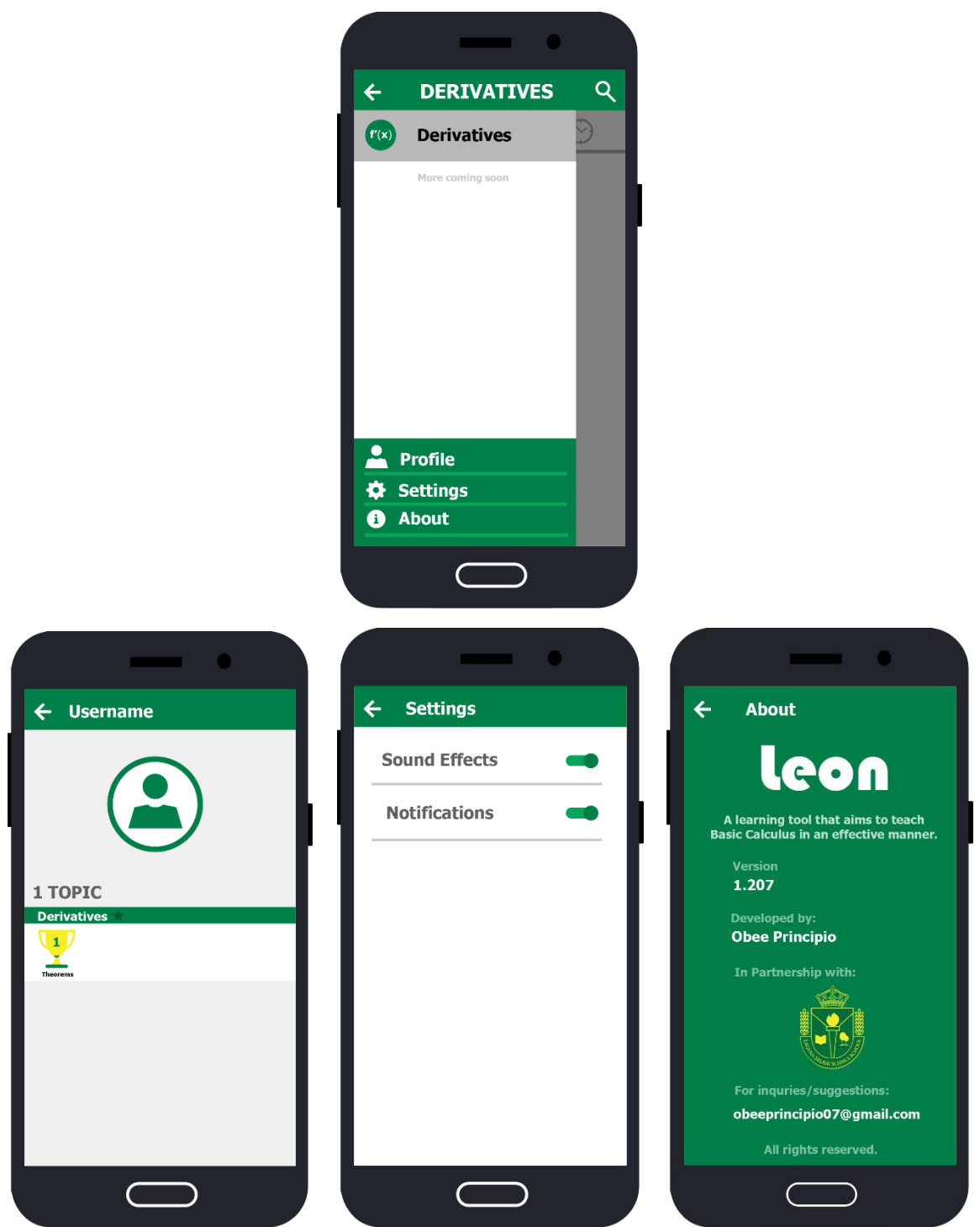




Search



Menu



**Fun fact: The app name "Leon" came from two words, Leibniz and Newton, the two who independently developed Calculus.*

High Resolution Infographics below

THEOREMS

Derivatives, Theorem 1

**If $f(x) = k$
and k is any constant**

then $f'(x) = 0$

Example 1 If $f(x) = 12$, find $f'(x)$.

Solution:

since $k = 12$, and 12 is a constant, $f'(x) = 0$

Example 2 If $f(x) = -7$, find $f'(x)$.

Solution:

since $k = -7$, and -7 is a constant, $f'(x) = 0$

Example 3 If $f(x) = \sqrt{9}$, find $f'(x)$.

Solution:

since $k = \sqrt{9}$, and $\sqrt{9}$ is a constant, $f'(x) = 0$

Example 4 If $f(x) = \pi$, find $f'(x)$.

Solution:

since $k = \pi$, and π is a constant, $f'(x) = 0$

THEOREMS

Derivatives, Theorem 2

**If $f(x) = x^n$
and n is any real number**

then $f'(x) = nx^{n-1}$

Example 1 If $f(x) = x^2$, find $f'(x)$.

Solution:

$$n = 2, f'(x) = 2x^{2-1} = \mathbf{2x}$$

Example 2 If $f(x) = \sqrt{x}$, find $f'(x)$.

Note: $\sqrt{x} = x^{1/2}$

Solution:

$$n = 1/2, f'(x) = 1/2x^{1/2-1} = \mathbf{1/2x^{-1/2}}$$

Example 3 If $f(x) = x^{1/3}$, find $f'(x)$.

Solution:

$$n = 1/3, f'(x) = 1/3x^{1/3-1}, f'(x) = \mathbf{1/3x^{-2/3}}$$

Example 4 If $f(x) = x^{-5}$, find $f'(x)$.

Solution:

$$\text{since } n = -5, f'(x) = -5x^{-5-1} = \mathbf{-5x^{-6}}$$

THEOREMS

Derivatives, Theorem 3

**If $f(x) = kg(x)$
and k is any constant**

then $f'(x) = kg'(x)$

Example 1 If $f(x) = 2x^2$, find $f'(x)$.

Solution:

$$g(x) = x^2, \text{ then } g'(x) = 2x$$

$$k = 2, f'(x) = 2(2x) = \mathbf{4x}$$

Example 2 If $f(x) = 3x^4$, find $f'(x)$.

Note: $\sqrt{x} = x^{1/2}$

Solution:

$$g(x) = x^4, \text{ then } g'(x) = 4x^3$$

$$k = 3, f'(x) = 3(4x^3) = \mathbf{12x^3}$$

Example 3 If $f(x) = 5x$, find $f'(x)$. Note: x has an exponent of 1

Solution:

$$g(x) = x, \text{ then } g'(x) = 1$$

$$k = 5, f'(x) = 5(1) = \mathbf{5}$$

Example 4 If $f(x) = 1/2x^4$, find $f'(x)$.

Solution:

$$g(x) = x^4, \text{ then } g'(x) = 4x^3$$

$$k = 1/2, f'(x) = 1/2(4x^3) = \mathbf{2x^3}$$

THEOREMS

Derivatives, Theorem 4

If $f(x) = g(x) \pm h(x)$

**then $f'(x) =$
 $g'(x) \pm h'(x)$**

Example 1 If $f(x) = x^2 - 3$, find $f'(x)$.

Solution:

$$g(x) = x^2 \text{ and } h(x) = 3, g'(x) = 2x \text{ and } h'(x) = 0$$

$$f'(x) = g'(x) - h'(x) = 2x + 0 = \mathbf{2x}$$

Example 2 If $f(x) = 3x^2 + x^5$, find $f'(x)$.

Solution:

$$g(x) = 3x^2 \text{ and } h(x) = x^5, g'(x) = 6x \text{ and } h'(x) = 5x^4$$

$$f'(x) = g'(x) + h'(x) = \mathbf{6x + 5x^4}$$

Example 3 If $f(x) = x^{2/3} - 4x$, find $f'(x)$.

Solution:

$$g(x) = x^{2/3} \text{ and } h(x) = 4x, g'(x) = \frac{2}{3}x^{-1/3} \text{ and } h'(x) = 4$$

$$f'(x) = g'(x) - h'(x) = \mathbf{\frac{2}{3}x^{-1/3} - 4}$$

Example 4 If $f(x) = 8x^{-9} + x^3$, find $f'(x)$.

Solution:

$$g(x) = 8x^{-9} \text{ and } h(x) = x^3, g'(x) = -72x^{-10} \text{ and } h'(x) = 3x^2$$

$$f'(x) = g'(x) + h'(x) = \mathbf{-72x^{-10} + 3x^2}$$

THEOREMS

Derivatives, Theorem 5

If $f(x) = f_1(x) \pm f_2(x) \pm \dots \pm f_n(x)$

then $f'(x) = f_1'(x) \pm f_2'(x) \pm \dots \pm f_n'(x)$

Example 1 If $f(x) = 3x^2 - x^6 + x^{1/2}$, find $f'(x)$.

Solution:

$$f_1(x) = 3x^2 \quad f_2(x) = -x^6 \quad f_3(x) = x^{1/2}$$

$$f_1'(x) = 6x \quad f_2'(x) = -6x^5 \quad f_3'(x) = \frac{1}{2}x^{-1/2}$$

$$f'(x) = f_1'(x) - f_2'(x) + f_3'(x)$$

$$f'(x) = 6x - 6x^5 + \frac{1}{2}x^{-1/2}$$

Example 2 If $f(x) = -x^2 + 2x^{1/2} + x^9$, find $f'(x)$.

Solution:

$$f_1(x) = -x^2 \quad f_2(x) = 2x^{1/2} \quad f_3(x) = x^9$$

$$f_1'(x) = -2x \quad f_2'(x) = x^{-1/2} \quad f_3'(x) = 9x^8$$

$$f'(x) = f_1'(x) + f_2'(x) + f_3'(x)$$

$$f'(x) = -2x + x^{-1/2} + 9x^8$$

THEOREMS

Derivatives, Theorem 6

If $f(x) = g(x)h(x)$

then $f'(x) = g(x)h'(x) + h(x)g'(x)$

Example 1 If $f(x) = (3x^2 + x^6)(x^3 + 6)$, find $f'(x)$.

Solution:

$$g(x) = (3x^2 + x^6) \text{ and } h(x) = (x^3 + 6)$$

$$g'(x) = 6x + 6x^5$$

$$h'(x) = 3x^2$$

$$f'(x) = g(x)h'(x) + h(x)g'(x)$$

$$\mathbf{f'(x) = (3x^2 + x^6)(3x^2) + (x^3 + 6)(6x + 6x^5)}$$

Example 2 If $f(x) = (5x^2 + x^4)(7x)$, find $f'(x)$.

Solution:

$$g(x) = (5x^2 + x^4) \text{ and } h(x) = 7x$$

$$g'(x) = 10x + 4x^3$$

$$h'(x) = 7$$

$$f'(x) = g(x)h'(x) + h(x)g'(x)$$

$$\mathbf{f'(x) = (5x^2 + x^4)(7) + (7x)(10x + 4x^3)}$$

THEOREMS

Derivatives, Theorem 7

$$\text{If } f(x) = \frac{g(x)}{h(x)} \quad \text{then } f'(x) = \frac{h(x)g'(x) - g(x)h'(x)}{[h(x)]^2}$$

Example 1 If $f(x) = \frac{4x^2 + x^3}{9x^4 - 4}$

Solution:

$$g(x) = 4x^2 + x^3 \text{ and } h(x) = 9x^4 - 4$$

$$g'(x) = 8x + 3x^2$$

$$h'(x) = 36x^3$$

$$f'(x) = \frac{h(x)g'(x) - g(x)h'(x)}{[h(x)]^2}$$

$$f'(x) = \frac{(9x^4 - 4)(8x + 3x^2) - (4x^2 + x^3)(36x^3)}{[(9x^4 - 4)]^2}$$