

#### **Title**

rdpow — Power calculations for Regression Discontinuity designs using robust bias-corrected local polynomial inference.

## Syntax

rdpow depvar runvar [if] [in] [, c(#) tau(#) alpha(#) nsamples(# # # #) sampsi(#
 #) samph(# #) all plot graph\_range(# #) graph\_step(#) graph\_options(graph\_opt)
 bias(# #) variance(# #) covs(covars) covs\_drop(covsdropoption) deriv(#) p(#)
 q(#) h(# #) b(# #) rho(#) fuzzy(fuzzyvar [sharpbw]) kernel(kernelfn)
 bwselect(bwmethod) vce(vcetype [vceopt1 vceopt2]) weights(weightsvar)
 scalepar(#) scaleregul(#) masspoints(masspointsoption) bwcheck(#)
 bwrestrict(bwropt) stdvars(stdopt) ]

#### Description

rdpow provides power calculations in Regression Discontinuity designs using
 conventional and robust bias-corrected local polynomial methods. Companion
 command is: rdsampsi for sample size calculations.

A detailed introduction to this command is given in  $\underline{\text{Cattaneo, Titiunik and Vazquez-Bare (2019)}}$ .

Companion R functions are also available <u>here</u>.

This command employs the Stata (and R) package <u>rdrobust</u> for underlying calculations. See <u>Calonico</u>, <u>Cattaneo and Titiunik</u> (2014) and <u>Calonico</u>, <u>Cattaneo</u>, <u>Farrell and Titiunik</u> (2017) for more details.

Related Stata and R packages useful for inference in RD designs are described in the following website:

https://rdpackages.github.io/

# Options |

rdpow options

- c(#) specifies the RD cutoff for indepvar. Default is c(0).
- tau(#) specifies the treatment effect under the alternative at which the power function is evaluated. The default is half the standard deviation of the outcome for the untreated group.
- alpha(#) specifies the significance level for the power function. Default is alpha(.05).
- nsamples(# # # #) sets the total sample size to the left, sample size to the left
  inside the bandwidth, total sample size to the right and sample size to the
  right of the cutoff inside the bandwidth to calculate the variance when the
  running variable is not specified. When this option is not specified, the
  values are calculated using the running variable.
- sampsi(# #) sets the sample size at each side of the cutoff for power calculation.
   The first number is the sample size to the left of the cutoff and the second
   number is the sample size to the right. Default values are the sample sizes
   inside the chosen bandwidth.
- samph(# #) sets the bandwidths at each side of the cutoff for power calculation.
  The first number is the bandwidth to the left of the cutoff and the second
  number is the bandwidth to the right. Default values are the bandwidths used
  by rdrobust.

- all displays the power using the conventional variance estimator, in addition to the robust bias corrected one.
- plot plots the power function using the robust bias corrected standard error from rdrobust. If all is specified, the conventional power function is also plotted.
- graph\_range(# #) specifies the range of the plot when plot option is used.
   Default range is [-1.5\*tau]; 1.5\*tau].
- graph\_step(#) specifies the step increment of the plot when plot option is used.
   Default range is 0.2\*range.
- graph\_options(#) specifies the graph options (title, axes titles, etc) to be passed to the plot when plot option is used.
- bias(# #) allows the user to set bias to the left and right of the cutoff. If not specified, the biases are estimated using rdrobust.
- variance(# #) allows the user to set variance to the left and right of the cutoff.
  If not specified, the variances are estimated using rdrobust.

rdrobust options

The following options are passed directly to rdrobust:

- covs(covars) specifies additional covariates to be used for estimation and inference.
- covs\_drop(covsdropoption) specifies options to assess collinearity in covariates
   to be used for estimation and inference. Option on drops collinear additional
   covariates (default choice). Option off only checks collinear additional
   covariates but does not drop them.
- deriv(#) specifies the order of the derivative of the regression functions to be
   estimated. Default is deriv(0). Setting deriv(1) results in estimation of a
   Kink RD design (up to scale).
- p(#) specifies the order of the local polynomial used to construct the point estimator. Default is p(1) (local linear regression).
- $\mathbf{q}(\#)$  specifies the order of the local polynomial used to construct the bias correction. Default is  $\mathbf{q}(2)$  (local quadratic regression).
- h(##) specifies the main bandwidth (h) used to construct the RD point estimator. If not specified, bandwidth h is computed by the companion command  $\underline{rdbwselect}$ . If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.
- b(# #) specifies the bias bandwidth (b) used to construct the bias-correction
   estimator. If not specified, bandwidth b is computed by the companion command
   rdbwselect. If two bandwidths are specified, the first bandwidth is used for
   the data below the cutoff and the second bandwidth is used for the data above
   the cutoff.
- **rho**(#) specifies the value of rho, so that the bias bandwidth b equals b=h/rho. Default is rho(1) if h is specified but b is not.
- fuzzy(fuzzyvar [sharpbw]) specifies the treatment status variable used to
   implement fuzzy RD estimation (or Fuzzy Kink RD if deriv(1) is also
   specified). Default is Sharp RD design and hence this option is not used. If
   the option sharpbw is set, the fuzzy RD estimation is performed using a
   bandwidth selection procedure for the sharp RD model. This option is
   automatically selected if there is perfect compliance at either side of the
   threshold.
- kernel(kernelfn) specifies the kernel function used to construct the
   local-polynomial estimator(s). Options are: triangular, epanechnikov, and
   uniform. Default is kernel(triangular).

- **bwselect** (bwmethod) specifies the bandwidth selection procedure to be used. By default it computes both h and b, unless rho is specified, in which case it only computes h and sets b=h/rho. Options are:
  - mserd one common MSE-optimal bandwidth selector for the RD treatment effect
     estimator.
  - msetwo two different MSE-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
  - msesum one common MSE-optimal bandwidth selector for the sum of regression
     estimates (as opposed to difference thereof).
  - msecomb1 for min(mserd, msesum).
  - msecomb2 for median(msetwo,mserd,msesum), for each side of the cutoff
     separately.
  - ${\tt cerrd}$  one common CER-optimal bandwidth selector for the RD treatment effect estimator.
  - certwo two different CER-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
  - cersum one common CER-optimal bandwidth selector for the sum of regression
     estimates (as opposed to difference thereof).
  - cercomb1 for min(cerrd, cersum).
  - cercomb2 for median(certwo,cerrd,cersum), for each side of the cutoff
     separately.
  - Note: MSE = Mean Square Error; CER = Coverage Error Rate.
  - Default is **bwselect(mserd)**. For details on implementation, see <u>rdbwselect</u> and references therein.
- vce(vcetype [vceopt1 vceopt2]) specifies the procedure used to compute the variance-covariance matrix estimator. Options are:
  - vce(nn [nnmatch]) for heteroskedasticity-robust nearest neighbor variance
     estimator with nnmatch indicating the minimum number of neighbors to be
     used.
  - vce(hc0) for heteroskedasticity-robust plug-in residuals variance estimator without weights.
  - vce(hc1) for heteroskedasticity-robust plug-in residuals variance estimator with hc1 weights.
  - vce(hc2) for heteroskedasticity-robust plug-in residuals variance estimator with hc2 weights.
  - vce(hc3) for heteroskedasticity-robust plug-in residuals variance estimator with hc3 weights.
  - vce(nncluster clustervar [nnmatch]) for cluster-robust nearest neighbor
     variance estimation using with clustervar indicating the cluster ID
     variable and nnmatch matches indicating the minimum number of neighbors to
     be used.
  - vce(cluster clustervar) for cluster-robust plug-in residuals variance
     estimation with degrees-of-freedom weights and clustervar indicating the
     cluster ID variable.
  - Default is vce(nn 3).
- weights(weightsvar) is the variable used for optional weighting of the estimation
   procedure. The unit-specific weights multiply the kernel function.
- scalepar(#) specifies scaling factor for RD parameter of interest. This option is
   useful when the estimator of interest requires a known multiplicative factor
   rescaling (e.g., Sharp Kink RD). Default is scalepar(1) (no rescaling).
- scaleregul(#) specifies scaling factor for the regularization term added to the
   denominator of the bandwidth selectors. Setting scaleregul(0) removes the
   regularization term from the bandwidth selectors. Default is scaleregul(1).
- masspoints(masspointsoption) checks and controls for repeated observations in the
   running variable. Options are:
  - off ignores the presence of mass points.
  - check looks for and reports the number of unique observations at each side of the cutoff.
  - adjust controls that the preliminary bandwidths used in the calculations
     contain a minimal number of unique observations. By default it uses 10
     observations, but it can be manually adjusted with the option bwcheck.
    Default option is masspoints(adjust).
- bwcheck(bwcheck) if a positive integer is provided, the preliminary bandwidth used in the calculations is enlarged so that at least bwcheck unique observations are used.

bwrestrict(bwropt) if set on, computed bandwidths are restricted to lie within the range of runvar. Default is on.

stdvars(stdopt) if set on, depvar and runvar are standardized before computing the bandwidths. Default is off.

## Example: Cattaneo, Frandsen and Titiunik (2015) Incumbency Data

```
Setup
        . use rdpower_senate.dta
    Power calculation against an alternative hypothesis of tau = 5
        . rdpow demvoteshfor2 demmv, tau(5)
    Power calculation with covariates
        . rdpow demvoteshfor2 demmv, tau(5) covs(population dopen dmidterm)
    Power calculation with user-specified bandwidths
        . rdpow demvoteshfor2 demmv, tau(5) h(16 18) b(18 20)
    Power function plot with default options
        . rdpow demvoteshfor2 demmv, tau(5) plot
    Power function plot with user-specified range and step
        . rdpow demvoteshfor2 demmv, tau(5) plot graph_range(-9 9) graph_step(2)
    Power function plot with user-specified options
        . rdpow demvoteshfor2 demmv, tau(5) plot graph_range(-9 9) graph_step(2)
graph_options(title(Power function) xline(0, lcolor(black) lpattern(dash))
        xtitle(tau) ytitle(power) graphregion(fcolor(white)))
Saved results
    rdpow saves the following in r():
    Scalars
                           significance level used in power function
      r(alpha)
      r(tau)
                           treatment effect under alternative hypothesis
                           sample size in bandwidth to the left used to calculate
      r(N h 1)
                             variance
                           sample size in bandwidth to the right used to calculate
      r(N_h_r)
                             variance
      r(N 1)
                           sample size to the left used to calculate variance
      r(N_r)
                           sample size to the right used to calculate variance
      r(samph_1)
                           bandwidth to the left of the cutoff
                           bandwidth to the right of the cutoff
      r(samph_r)
      r(sampsi_1)
                           number of observations inside the window to the left of
                            the cutoff
      r(sampsi_r)
                           number of observations inside the window to the right of
                            the cutoff
                           robust bias corrected standard error
      r(se_rbc)
```

## References

r (power\_rbc)

r(power\_conv) r(Vl\_rb)

r(se\_conv)

r(Vr\_rb)

r(bias\_l) r(bias\_r)

Calonico, S., M. D. Cattaneo, M. H. Farrell, and R. Titiunik. 2017. <a href="mailto:rdrobust: software for Regression Discontinuity Designs">rdrobust: Software for Regression Discontinuity Designs</a>.

Stata Journal 17(2): 372-404.

conventional standard error

bias to the left of the cutoff bias to the left of the cutoff

error

power against tau using robust bias corrected standard

power against tau using conventional standard error

robust variance to the left of the cutoff

robust variance to the left of the cutoff

- Calonico, S., M. D. Cattaneo, and R. Titiunik. 2014. Robust Data-Driven Inference in the Regression-Discontinuity Design.

  Stata Journal 14(4): 909-946.
- Cattaneo, M. D., Frandsen, B., and R. Titiunik. 2015. <u>Randomization Inference in the Regression Discontinuity Design: An Application to Party Advantages in the U.S. Senate.</u>

  Journal of Causal Inference 3(1): 1-24.
- Cattaneo, M. D., R. Titiunik, and G. Vazquez-Bare. 2019. <u>Power Calculations for Regression Discontinuity Designs</u>.

  Stata Journal 19(1): 210-245.

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