

# **Data Structures and Algorithms**

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## **1 Introduction**

These seminar notes contain my overview of the Data Structures and Algorithms course held at University of Bucharest. Because the course is based on heavy theoretic lectures, I tried a more practical approach to present some of the notions by discussing problems which arise natural from the main course.

Most of the problems come from a romanian website specialized on programming contests as well as codeforces or topcoder [1–3]. Of course, there are more interesting problems to tackle, but unfortunately I limit to the course material although sometimes I will talk about some ad-hoc problems.

## **2 Seminar I**

Synthesise first 2 courses:

- Basic notions of time and memory complexity.
- Stacks and Queues.

### **2.1 Sketch**

What is an algorithm? How can we measure the time complexity of a program? Examples (Choosing every pair of elements and eratosthene sieve). Introduction to stacks and queues. Details about their implementation and a short tutorial in STL. Can also talk about circular queues and double ended queues.

### **2.2 Checking if an expression has brackets in right order**

### **2.3 Emulate a queue using 2 stacks**

### **2.4 Editor [4]**

### **2.5 Alee [5]**

### **2.6 Trompeta [6]**

Given N digits, find the maximum number with K digits such that the digits preserve the initial order.

## 2.7 Tsunami [7]

Given a matrix  $N \times M$  with digits less than a value  $K (K \leq 10)$ . Find the number of cells with value less than a threshold  $T (T \leq K)$  such that when you start from 0 you always go up to digits  $\leq T$ .

## 2.8 Add or Multiply

Take a number  $X$ . You can add, subtract, multiply it by numbers in a set  $S$ . Find the shortest number of steps required to reach from  $X$  to  $Y$ .

## 2.9 Take-Out [8]

$N$  blocks, each black or white. You can remove at a time  $k$  white blocks and 1 black block such that there is no gap between the removed blocks.

## 2.10 Devices

You are given a row of  $n$  devices, each consuming some subset of  $k_i=8$  different resources when turned on, and producing some amount of energy when turned on. For each  $l$  from 1 to  $n$  you need to find the smallest  $r$  such that it's possible to turn on some devices from the segment  $[l;r]$  such that no two devices turned on consume the same resource, and that the total energy of the devices turned on is at least  $z$  [9].

# 3 Seminar II

- Divide and conquer, merge-sort, estimating complexity

## 3.1 Inv [10]

## 3.2 Stergeri [11]

## 3.3 Muzeu [12]

## 3.4 Binar [13]

# 4 Seminar III

Binary search. Fast exponentiation.  $K$ 'th element. Time complexity proofs (at least sketches).

#### 4.1 Classic Task [14]

#### 4.2 Nrtri [15]

#### 4.3 Sdo [16]

As a further challenge, consider that you can't store  $O(N)$  elements. Can you do dynamic medians?

#### 4.4 Loto [17]

### 5 Seminar IV

Heaps. Binary Heaps. Fibonacci Heaps.

Basic heap operations (Insert, Extract-Min, Merge).

Time, space complexity analysis. Heap reconstruction in  $O(N)$ .

#### 5.1 Sdo [16]

Can you find the median using heaps? Can you do this dynamically?

#### 5.2 Merge $K$ lists [18]

You have  $K$  sorted arrays. Can you merge them quickly?

#### 5.3 Sort using heaps

Classic sort algorithm, this time using heaps. Almost sorted list, can you sort it more efficiently than classic?

### 6 Seminar V

Stanford exercises. [19]

Wiki page about AVL. [20]

Get  $K$ 'th element from a BST. Construct BST from an array.

## 7 Seminar VI

### 7.1 Huffman Coding

#### General problem:

Given an alphabet  $\mathcal{A} = \{a_1, \dots, a_n\}$  and a set of weights  $\mathcal{W} = \{w_1, \dots, w_n\}$  compute a set of codewords  $\mathcal{C} = \{c_1, \dots, c_n\}$  such that  $\sum_{i=1}^n \text{length}(c_i) * w_i$  is minimum.

### 7.2 Additional Coding Methods

Other methods such as LZW and arithmetic encoding have a more improved encoding scheme [21, 22]. Unfortunately, these 2 schemes were patented and people should pay the owners to use them. Recently they went into public domain.

LZW is used for the GIF image format. Arithmetic encoding is currently used in WebP, an image format developed by Google [23].

LZW main idea is similar with an online hashing algorithm. Encode each character into a dictionary. Each time take the prefix string  $W$  which was already encoded. Concatenate  $W$  with the next character in the string and add it to dictionary of encoded strings.

Arithmetic encoding uses a probability model, encodings are values between  $[0, 1]$  on the real line [24].

## 8 Homework

- Editor [4]. Tsunami [7]. Trompeta [6].
- Muzeu [12]. Inv [10]. Binar [13]. Stergeri [11].
- Sdo [16]. ClassicTask [14] - optional. Nrtri [15]. Merge-K-Lists [18].
- SlidingWindow [25]
- Scandura [26]

### 8.1 Grading

Scoring at least 60 points on each problem will get you maximum grade (which means a bonus of 10% from your final grade). Each problem category values 0.3 only if you place in the first 5 people with successful submissions. An answer in class has an 0.15 score. You can get a maximum bonus of 1/10 points for the exam.

## 9 Back-up problems

9.1 Secv6 [27]

9.2 Dynamic GCD [28]

9.3 Matrice 2 [29]

9.4 Cabane [30]

9.5 Minim2 [31]

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