8

14

24 25

26 27 28

29 30 31

37

32

> 43 44 45

46

47 48

### SSA based global code motion of identical computations

ADITYA KUMAR. Samsung Austin R&D Center SEBASTIAN POP, Samsung Austin R&D Center

We present a global code motion compiler optimization which schedules identical computations across the program so as to save code size. Not only this code motion saves code size, it exposes redundancies in some cases, it exposes more instruction level parallelism in the basic block when the computations are hoisted, and it enables other passes like loop invariant motion to remove more redundancies. The cost model to drive the code motion is based on live range analysis on SSA representation such that the (virtual) register pressure does not increase.

We have implemented the pass in LLVM. It is based on Global Value Numbering infrastructure available in LLVM. The experimental results show an average of 2.5% savings in code size on SPEC Cpu 2006, although the code size also increases in many cases because it enables more inlining. We have also seen execution time improvements of approximately 5% in a couple of SPEC Cpu 2006 benchmarks viz. GCC and mcf, moreover, register spills reduced for almost all the SPEC Cpu 2006 bencmarks when compiled for X86\_64. This is an optimistic algorithm in the sense that it considers all identical computations in a function as potential candidates. We make an extra effort to hoist candidates by partitioning the potential candidates in a way to enable partial hoisting in case common hoisting points for all the candidates cannot be found. We also formalize how register pressure will reduce as a result of code-motion and why sorting the list of potential candidates w.r.t. their depth first numbers helps hoist more candidates with less compile time overhead.

CCS Concepts: •Software and its engineering → Compilers; Source code generation; •General and  $reference \rightarrow Performance;$ 

Additional Key Words and Phrases: Optimizing Compilers, GCC, LLVM, Code Generation, Global Scheduling

#### **ACM Reference format:**

Aditya Kumar and Sebastian Pop. 2017. SSA based global code motion of identical computations. PACM Progr. Lang. 1, 1, Article 1 (January 2017), 19 pages.

DOI: 10.1145/nnnnnn.nnnnnnn

#### 1 INTRODUCTION

Compiler techniques to remove redundant computations are composed of an analysis phase that detects identical computations in the program and a transformation phase that reduces the number of run-time computations. Classical scalar optimizations like CSE (Aho et al. 1986) work very well on single basic blocks but when it comes to detect redundancies across basic blocks these techniques fall short: more complex passes like GCSE and PRE have been designed to handle these cases based on dataflow analysis (Morel and Renvoise 1979). At first these techniques were described in the classical data-flow analysis framework, and later the use of the SSA representation lowered the cost in terms of compilation time (Briggs and Cooper 1994; Chow et al. 1997; Kennedy et al. 1999) and brought these techniques in the main stream: nowadays SSA based PRE is available in every industrial compiler.

This paper describes code-motion of congruent instructions (Briggs et al. 1997), a technique that uses the information computed for PRE to detect identical computations but has a transformation phase whose goal differs from PRE: it removes identical computations from different branches of execution. These

 identical computations in different branches of execution are not redundant computations at run-time and the number of run-time computations is not reduced. It is not a redundancy elimination pass, and thus it has different cost function and heuristics than PRE or CSE. It is more similar to global code scheduling (Aho et al. 1986; Click 1995) in the sense that it will only move computations. Code hoisting can reduce the critical path length of execution in out-of-order machines. As more instructions are available at the hoisting point, the hardware has more independent instructions to reorder. The following example illustrates how hoisting can improve performance by exposing more ILP.

In this program the computations of tmax and tmin are identical to the computations of tmin and tmax of sibling branch respectively. Both tmax and tmin depend on inv which depends on a division operation which is generally more expensive than the addition, subtraction, and multiplication operations. The total latency of computation across each branch is:  $C_{div} + 2(C_{sub} + C_{mul})$ . For an out-of-order processor with two add units and two multiply units, the total latency of computation is  $C_{div} + C_{sub} + C_{mul}$ .

Now if the computation of tmax and tmin are hoisted outside the conditionals, the C code version would look like this:

```
float fun(float d, float min, float max, float a) {
  float inv = 1.0f / d;
  float x = (min - a) * inv;
  float y = (max - a) * inv;
  float tmin = x, tmax = y;
  if (inv < 0) { tmin = y; tmax = x; }
  return tmax + tmin;
}</pre>
```

In this code the division operation can be executed in parallel with the two subtractions because there are no dependencies among them. So the total number of cycles will be  $max(C_{div}, C_{sub}) + C_{mul} = C_{div} + C_{mul}$ ; since  $C_{div}$  is usually much greater than  $C_{sub}$  (ARM 2014; Intel 2000).

In fact there are several advantages of code-motion of this kind:

- it helps reduce the code size of the program by replacing multiple instructions with one although the final code size may be higher because of improved inlining heuristics; functions become cheaper to inline when their code size decreases because the inliner heuristics depend on instruction count;
- it exposes more instruction level parallelism to the later compiler passes. By hoisting identical computations to be executed earlier, instruction schedulers can move heavy computations earlier in order to avoid pipeline bubbles;
- it reduces branch misprediction penalty on out-of-order processors with speculative execution of branches: by hoisting or sinking expressions out of branches, it can effectively reduce the amount of code to be speculatively executed and hence reduce the critical path;

- it reduces interference or register pressure with an appropriate cost-model: we have used a cost model in our implementation which only hoists or sinks when the register pressure is reduced;
- it reduces the total number of instructions to be executed for SIMD architectures which execute all code in branches based on masking or predication;
- it may improve loop vectorization by reducing a loop with control flow to a loop with a single BB, should all the instructions in a conditional get hoisted or sinked;
- it enables more loop invariant code motion (LICM): as LICM passes, in general, cannot effectively reason about instructions within conditional branches in the context of loops, code-hoisting is needed to move instructions out of conditional expressions and expose them to LICM.

There have been a lot of work both in industry and academia to hoist and sink code out of branches, and in general global scheduling (Click 1995). Some relate code-hoisting to code-size optimization (Rosen et al. 1988) and many (Barany and Krall 2013; Shobaki et al. 2013) use global scheduling to improve performance. Most of the recent work on global scheduling are done using ILP which results in prohibitively high compile time. To the best of our knowledge we have not found any reference which explored code-motion of identical computation in as much detail as we have done. A part of our implementation (aggressive code hoisting) is already merged in LLVM trunk, however, a general implementation of code-motion of congruent (non redundant) expressions is still missing from GCC and LLVM trunk. The main contributions of this paper are:

- a new optimistic algorithm to move congruent instruction out of branches;
- a cost model to reduce interference and hence, reduce spills;
- a technique to maximize hoisting in an optimistic approach by partitioning the list of potential candidates sorted by their DFS visit number;
- experimental evaluation of our implementation in LLVM which combines SSA based liveness
  analysis, and ranking of expressions to move very busy expressions in order to reduce code-size
  and improve performance in some cases.

#### 2 RELATED WORK

There are a lot of bug reports in GCC and LLVM bugzillas (GCC 2016a; LLVM 2016), showing the interest in having a more powerful code hoist transform. The current LLVM implementation of code hoisting in SimplifyCFG.cpp is very limited to hoisting from identical basic blocks: the instructions of two sibling basic blocks are read at the same time, and all the instructions of the blocks are hoisted to the common parent block as long as the compiler is able to prove that the instructions are equivalent. This implementation does not allow for an easy extension: first in terms of compilation time overhead the implementation is quadratic in number of instructions to bisimulate and second, the equivalence of instructions is computed by comparing the operands which is neither general nor scalabale.

Dhamdhere (Dhamdhere 1988), Muchnick (Muchnick 1997) mention code hoisting in a data flow framework. A list of Very Busy Expressions (VBE) computed which are hoisted in a basic block where the expression is anticipable (all the operands are available). This algorithm would hoist as far as possible without regarding the impact on register pressure and as such a cost model will be required. Also the description of VBE is based on the classic dataflow model and an adaptation to a sparse SSA representation is required.

Rosen (Rosen et al. 1988) also briefly discuss hoisting computations with identical value numbers from immediate successors. Their algorithm iterates on computations of same rank and move the code with identical computations from the sibling branch to a common dominator if they are very busy

 (Muchnick 1997). The cost-model to mitigate register pressure is missing, also there is no mention of sinking congruent instructions.

GCC recently got code-hoisting (GCC 2016b) which is implemented as part of GVN-PRE: it uses the set of ANTIC\_IN and AVAIL\_OUT value expressions computed for PRE. ANTIC\_IN[B] contains very busy expressions at basic block B i.e., values computed on all paths from B to exit and AVAIL\_OUT[B] contains values which are already available. The algorithm hoists top down to a predecessor. It uses ANTIC\_IN[B] to know what expressions will be computed on every path from B to exit, and can be computed in B. It uses AVAIL\_OUT[B] to subtract out those values already being computed. The cost function is: for each hoist candidate, if all successors of B are dominated by B, then we know insertion into B will eliminate all the remaining computations. It then checks to see if at least one successor of B has the value available. This avoids hoisting it way up the chain to ANTIC\_IN[B]. It also checks to ensure that B has multiple successors, since hoisting in a straight line is pointless. The algorithm continues top down the dominator tree, working in tandem with PRE until no more hoisting is possible. One advantage of GCC implementation is that it works in sync with the GVN-PRE such that when new hoisting opportunities are created by GVN-PRE, code-hoisting will hoist them.

Click (Click 1995) describe aggressive global code motion to first schedule all the instructions as early as possible. This results in very long live ranges which is mitigated by again scheduling all the instructions as late as possible. They report speedup of as high as 23%.

Barany (Barany and Krall 2013) presented a global scheduler with integer linear programming (ILP) formulation with a goal to minimize register pressure. The results they got were not very promising. It may be because they only used the scheduler for smaller functions (< 1000 instructions); also, they compiled the benchmarks for ARM-Cortex which is more resilient to register pressure because it has more registers compared to X86, for example.

Shobaki (Shobaki et al. 2013) also recently presented a combinatorial global scheduler with reasonable performance improvements. It is possible that both Barany and Shobaki's implementation will have similar results when compiled for same target architecture. Also, both suffer from the same problem, although Shobaki not so much, of large compile times which is not feasible for industrial compilers like GCC and LLVM.

With the algorithm described in the next section, we got a reduction in register spills, a reduction in code-size and some performance improvements with very low compilation time overhead, on SPEC Cpu 2006 benchmarks.

#### 3 CODE MOTION

The algorithm for code motion uses several common representations of the program that we shortly describe below:

- Dominance (DOM) and Post-Dominance (PDOM) relations (Aho et al. 1986) on a Control Flow Graph (CFG);
- DJ-Graph (Sreedhar 1995) is a data structure that augments the dominator tree with join-edges to keep track of data-flow in a program. We use DJ-Graph to compute liveness of variables as illustrated in (Das et al. 2012);
- Static Single Assignment (SSA) (Cytron et al. 1989);
- Global Value Numbering (GVN) (Click 1995; Rosen et al. 1988): to identify similar computations compilers use GVN. Each expression is given a unique number and the expressions that the compiler can prove to be identical are given the same number;
- MemorySSA (Novillo 2007): it is a factored use-def chain of memory operations that the compiler is unable to prove independent. MemorySSA accelerates the access to the alias analysis information.

The code-motion pass can be broadly divided into the following steps that we will describe in the rest of this section:

- find candidates (congruent instructions) suitable for code-motion,
- compute a point in the program where it is both legal and profitable to move the code,
- move the code to hoist point or sink point, and
- update data structures to continue iterative code motion.

## 8

10

11

12

13

14

15

16

17

18

19

47 48

1 2

3

4

6

#### 3.1 Liveness using DJ-graph

DJ-graph (Sreedhar 1995) is a data structure that augments the dominator tree with join-edges to keep track of data-flow in a program. We use DJ-graph and merge-sets to compute liveness of variables as illustrated in (Das et al. 2012). It is very efficient for computing liveness and does not require any bitvectors to be maintained for each basic block. The underlying simplicity of liveness computation is due to SSA form, where the the values only flow (from def to use) either through dominator edges or the join edges (where we insert a PHI). The DJ-graph contains both these edges which allows for computation of merge-sets for each basic block, i.e., a set of all basic blocks where the values can flow from a particular basic block. We have implemented the merge-set computation based on a DJ-graph as illustrated in (Das and Ramakrishna 2005). A simplified version of the merge-set that we implemented is presented here:

```
20
     // Return true if the merge-set of source node of a visited J-edge (incoming edge of
21
     // lnode) is not the subset of the merge-set of lnode.
22
     bool still_inconsistent(Node lnode, JEdges JE, Visited V, MergeSet Merge)
23
       for e in (all incoming edges to lnode)
24
         if (e is in JE && e in V)
25
           if (Merge(Source Node of e) is not a subset of Merge(lnode))
26
             return true
27
       return false
28
29
     // Compute a merge-set top-down in breadth first order.
30
     bool constructMergeSet_1(BFSList B, JEdges JE, DomLevel DL)
31
       repeat = false
32
       V = empty list of visited edges
33
       for n in B
34
         for e in (all incoming edges to n)
35
           if (e is in JE && e not in V)
36
             V(e) = true
37
             let tmp = Source Node of e
38
             let tnode = Target Node of e
39
             let lnode = NULL
40
             while (DL(tmp) >= DL(tnode))
41
               Merge(tmp) = Merge(tmp) U Merge(tnode) U {tnode}
42
               lnode = tmp
43
               tmp = dom-parent(tmp)
44
             repeat = still_inconsistent(lnode, JE, Merge)
45
       return repeat
46
```

```
// Construct merge-set of each node in Control-Flow-Graph G of a function.
2
     void constructMergeSet(CFG G) {
3
       B = Breadth First Order of G
4
       JE = JEdges of G
       DL = List of Path length (from root) of each node in G.
6
7
       do // Call until a fixed point is reached.
8
         Repeat = constructMergeSet_1(B, JE, DL)
9
       while (Repeat)
10
     }
11
       We compute merge sets of the control flow graph which remains the same through the code-motion
12
     transformation. For code-motion we only want to know if a use operand is a kill (to compute changes in
     register pressure.) For that we only need to know whether the use is also required later in the execution
13
14
     path. A variable is live out of a basic block B if it is used in the merge set of B. We compute the live-out
15
     relation on-demand when profitability of hoistable/sinkable candidates is to be evaluated. A simplified
16
     version of isLiveOutUsingMergeSet is presented here:
17
     // Return true if variable A is liveout from basic block N
18
     bool isLiveOutUsingMergeSet(Node N, Variable A)
19
        if (A is defined in N)
20
          if (A is used outside any basic block other than N)
21
            return true
22
         return false
23
24
       Ms(N) = null
       // Mergeset of N is the union of merge sets of its successors
26
       for W in successors(N)
27
         Ms(N) = Ms(N) U Mr(W)
28
29
       // Iterate over all the uses of A and see if any intersect with the merge-set of N.
30
       for T in users(A)
31
         B = basic_block(T)
32
         while (B != null and B != def_bb(A))
33
            if B in Ms(N) return true
34
            B = dom-parent(B)
35
       return false
36
37
     // Return true if op is the last use of the operand in I.
38
     bool isKill(Operand op, Instruction I)
39
        if (isLiveOutUsingMergeSet(op))
40
         return false
41
       B = basic_block(I)
42
       for each I1 after I in B
43
          if (I1 uses op)
44
            return false
45
       return true
46
47
48
```

PACM Progr. Lang., Vol. 1, No. 1, Article 1. Publication date: January 2017.

The original algorithm presented in (Das et al. 2012) has mismatched types in terms of uses and nodes because each node can have many instructions and hence many uses. Also, while iterating on the dominator of each user of a variable we may reach to the beginning of a function, in that case the inner while loop needs to terminate. These two cases were missing from the algorithm and we came across them during implementation. If a variable is not live-out of a basic block, it still may be used later in the basic block. To establish whether a use of a variable is a kill we iterate on all the subsequent instructions in a basic block checking for uses should is LiveOutUsingMergeSet return false.

#### 3.2 Finding candidates to move

 The first step is to find a set of congruent instructions (Briggs et al. 1997). This is performed by a linear scan of all instructions of the program and classifying them by their value numbers. We could compute available and anticipable sets as computed by GCC's code-hoisting but that would be a lot of data structures to maintain at each basic block level. For GCC it makes sense because their code-hoisting is integrated with GVN-PRE which already has those data structures available.

The current implementation of GVN in LLVM has some limitations when it comes to loads and stores so we compute the GVN of loads and stores separately. Our solution to value number loads is to hash the address from where the value is to be loaded. For stores, we value number the address as well as the value to be stored at that address. Another limitation of the current GVN implementation in LLVM is that the instructions dependent on the loads will not get numbered correctly, and so after hoisting all candidates we need to rerun the GVN analysis in order to discover new candidates now available after having hoisted load instructions. This limitation should be addressed in a new implementation of the GVN based on MemorySSA, that would better account for equivalent loads and their dependent instructions.

The process of computing GVN can be on-demand (as we come across an instruction) or, precomputed (computing GVN of all the instructions beforehand). Which process to choose is determined by the scope of code-hoisting we want to perform. In a pessimistic approach, we want to hoist a limited set of instructions from the sibling branches as we iterate the DFS tree bottom-up, it is sufficient to compute GVN values on-demand. Whereas, in the optimistic approach, as described in Section 4.1, we want to move as many instructions as possible, and it would require GVN values to be precomputed.

Once the instructions have been classified into congruence classes, we compute for each group of congruent instructions, a point in the program that is both legal and profitable for the instructions to be moved to.

#### 3.3 Legality check

Since the equality of candidates is purely based on the value numbers, we also need to establish if hoisting them to a common dominator or sinking them to a common post-dominator would be legal. Once a common dominator (post-dominator) is found, we check whether all the use-operands of the set of instructions are available at that position. It is possible reinstantiate (remateralize) the use-operands in some cases when the operands are not available and make it legal to move the instruction.

Subsequently, it is checked that the side-effects of the computations (if any) do not intersect with any side-effects between the instructions to be hoisted/sunk and their hoisting/sinking point. It is also necessary to check if there are indirect branch targets e.g., landing pad, case statements, goto labels etc., along the path because it becomes difficult to prove safety checks in those cases. In our current implementation we discard candidates on those paths.

- 9 10 11
- 13 14 15

- 16 17 18
- 19 20 21 22
- 23 24 25 26
- 27 28 29 30 31
- 32 33 34
- 35 36
- 37 38 39
- 41 42 43

40

48

- 3.3.1 Legality of hoisting scalars. Scalars are the easiest to hoist because we do not have to analyze them for aliasing memory references. As long as all the operands are available (or can be made available by rematerialization), the scalar computations can be hoisted.
- 3.3.2 Legality of hoisting loads. The availability of operand to the load (an address) is checked at the hoisting point. If that is not available we try to rematerialize the addresss if possible. Along the path, from current position of the load instruction backwards on the control flow to the hoisting point, we check whether there are writes to memory that may alias with the load, in which case the candidate is discarded. To iterate on the use-def chains for memory references the MemorySSA infrastructure of LLVM is used.
- 3.3.3 Legality of hoisting stores. For stores, we check the dependency requirements similar to the hoisting of loads using the MemorySSA of LLVM. We check that the operands of the store instruction are available at the hoisting point, and that there are no aliasing loads or store along the path from the current position to the hoisting point.
- 3.3.4 Legality of hoisting calls. Call instructions can be divided into three categories: those calls equivalent to purely scalar computations, calls reading from memory, and most of the time, without further information, calls have to be classified as writing to memory, that is the most restrictive form. Each category of call instructions is handled as described for scalar, load, and store instructions.

Hoisting loads/stores across calls also require precise analysis of all the memory addresses accessed by the call. The current implementation being an intraprocedural pass, cannot hoist aggressively across calls. In the presence of pure calls, loads can be hoisted but stores can't. Also, if a call throws exceptions, or if it may not return, nothing can be hoisted across that call.

3.3.5 Legality of sinking expressions. Sometimes, hoisting is not upward-safe?? e.g., if the expressions are in a landing pad etc., in that case sinking of those expressions may reduce code size. Sinking may also reduce the register pressure in some cases e.g., when the use operands are not kills. For sinking, higher ranked expressions would be sunk first. And it would be illegal to sink higher ranked identical expressions if they are not anticipable in the common post-dominator. For example:

```
B0: i0 = load B
B1: i1 = load A
    c1 = i1 + 10
    d1 = i0 + 20
    goto B3
B2: i2 = load A
    c2 = i2 + 10
    d2 = i0 + 20
    goto B3
```

B3: phi(c1, c2)

```
phi(d1, d2)
  In this example (c1, c2) or (d1, d2) are potential sinkable candidates. Since (c1, c2) depend on i1
and i2 respectively which are also in their original basic blocks, c1 and c2 are not anticipable in B3. So
without knowing the sinkability of 'i1' and 'i2' it would be illegal to sink (c1, c2) to B3. On the other
```

hand (d1, d2) can safely be sunk because their operands are readily available at the sink point i.e., B3. It should also be noted that, just because the expressions are identical and operands are available, it still requires a unique post-dominating PHI to use the exact same values to be legally sinkable.

A general global scheduling algorithm also requires checks for undefinedness when introducing a new computation along a path. Since only very busy expressions are moved in the current implementation, there is no need to check for undefinedness resulting due to movement of instructions. This simplifies the implementation.

#### 3.4 Profitability check (Cost models)

 $\frac{44}{45}$ 

 After the legality checks have passed, we check if a code-motion is profitable. That takes into account the impact code-motion would have on various parameters that might affect runtime performance e.g., impact on live-range, gain in the code size. Since this is mostly a code-size optimization pass, the goal is to not regress in performance across popular benchmarks at the same time reduce code size as much as possible. Following are the cost models which are implemented:

3.4.1 Reduce register pressure. Hoisting upwards will decrease the live-range of its use, if it is a last use (a kill), but increase the live-range of its definition. Conversely, sinking will decrease the live-range of the defined register but increase the live-range for killed operands. If the live-range after code-motion is less than before it will be moved. Essentially, as long as there is one killed operand, code hoisting will either decrease or preserve the register pressure. Similarly, code-sinking will either decrease or preserve the register pressure as long as there is one operand killed at most. Following example explains how code motion of identical computations can reduce the register pressure. Consider the following example where the labels prefixed with 'P' represent the position of instruction in a basic block (names prefixed with 'B').

```
b = m
c = n

B0: if c is true then goto B3 else goto B4

B1: a0 = b<kill> + c<kill>

B2: a1 = b<kill> + c<kill>
```

After hoisting a0 and a1 are removed and a copy of a0 as a01 is placed in B0 just before the branch.

In this case, since 'b' and 'c' are killed in 'a0' and 'a1', hoisting them will reduce the register pressure in B3 and B4 because two registers will be freed.

Ideally, it should be okay to hoist all the instructions and a later a live-range-splitting (Cooper and Simpson 1998) pass should make the right decision of rematerializing the instruction should it be beneficial to do so. But the current live-range splitting pass of LLVM is not making the optimial decision and we have found regressions while hoisting aggressively.

Moreover, LLVM has a 'getelementptr' instruction which computes the address where a load or a store would happen. It is a scalar computation and gets hoisted frequently even if the corresponding loads/stores would not get hoisted. In order to reduce register pressure while hoisting loads, we have restricted hoisting of address computations away from their corresponding loads and stores when the loads and stores cannot be moved. This restriction is only to mitigate the limitations of LLVM's register allocator and may be lifted in the future, when the register allocation rematerialization pass has been improved to catch these regressions.

3.4.2 Hoisting an expression across a call. Even hoisting scalars across calls is tricky because it can increase the number of spills. During the frame lowering of calls, the argument registers also known as

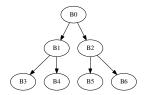


Fig. 1. CFG to illustrate partitioning

the caller saved registers are saved because they might be modified by the callee and after the call they are restored. So before the call, the register pressure is high because the number of available registers are reduced by the number of caller saved registers. In that situation a computation that increases register pressure is not profitable to hoist.

3.4.3 Partitioning the list of hoistable candidates to maximize hoisting. In the approach, described in Section 4.1, it is possible that a common hoisting point for all the instructions does not satisfy legality or profitability checks. In these cases, it is still possible to 'partially' hoist a subset of instructions by splitting the set of candidates and finding a closer hoisting point for each subset.

In order to hoist a subset of identical instructions, we partition the list of all candidates in a way to maximize the total number of hoistings. By sorting the list of all the candidates in the increasing order of their depth first search discovery time stamp (Cormen et al. 2001) (DFSIn numbers), we make sure that candidates closer in the list have their common dominator nearby. In Figure-1, if B3, B4, B5, and B6 have identical computations and if for some reason, they cannot be hoisted at B0, then we partition the set of hoistable candidates in their DFSIn order. In this case the DFSIn ordering would be B3, B4, B5, B6 which will allow the instructions in B3, B4 to be hoisted at B1 and those in B5, B6 to be hoisted at B2. Even if (B3, B4) could not be hoisted, for some reason, to B1, (B5, B6) can still be hoisted – if legal and profitable – to B2.

In our current implementation we keep as many candidates in one set as possible (greedy approach). We split the list at a point where the legality checks fail to hoist subset of candidates which are legal to hoist and then start finding new hoisting point for the remaining ones.

There is a special case for hoisting load instructions when the hoist-point is the predecessor basic block for all the loads. Even if the register pressure would increase, we prefer to hoist loads in this case. The reason being, that would make the loaded value available by the time it is used. Also, because stores and calls are hoisted the least ??, the performance does not change much whether they are hoisted or not.

#### 3.5 Code generation

Once all the legality and profitability checks are satisfied for a set of congruent instructions, they are suitable candidates for hoisting. A copy of the computation is inserted at the hoisting point along with any instructions which needed to be rematerialized. Thereafter, all the computations made redundant by the new copy are removed, and the SSA form is restored by updating the intermediate representation (IR) to reflect the changes. At the same time MemorySSA is also updated to get up-to-date information about memory references.

After one iteration of algorithm runs through the entire function, it creates more oppportunities for higher ranked computations (Rosen et al. 1988). Currently, this is a limitation of the GVN analysis pass, and so we rerun the code-hoisting algorithm until there are no more instructions left to be hoisted. Obviously, this is not the most optimal approach and can be improved by ranking the computations (Rosen et al. 1988), or by improving the GVN analysis to correctly populate congruence classes.

Finally after the transformation is done, we verify a set of post-conditions to establish that program invariants are maintained: e.g., consistency of use-defs, and SSA semantics.

#### 4 SSA BASED GLOBAL CODE MOTION OF IDENTICAL COMPUTATIONS

In this section we will present an overview of the algorithm we implemented in LLVM. The amount of hoisting depends on whether we collect GVN of instructions before finding candidates (optimistic) or, on-demand (pessimistic). It also depends on the generality of the GVN algorithm as mentioned earlier in Section 3.2. We have implemented a optimistic global code motion of congruent instructions which uses the liveness analysis as illustrated in Das (Das et al. 2012) and ranking expressions explained in Rosen (Rosen et al. 1988).

Code-motion basically consists of two parts i.e., hoisting and sinking. This implementation only moves congruent instructions. An immediate guarantee of this approach is gain in code size (the final executable may be of larger size because of more inlining). The algorithm prefers hoisting to sinking. If the dependency of a hoistable candidate is in the same basic block as the candidate, then the dependency must also be hoistable otherwise hoisting will be illegal or would require a complicated code generation to make it legal. The current algorithm discards cases if the dependency is neither hoistable nor rematerializable.

#### 4.1 Optimistic code motion algorithm

 $\frac{4}{5}$ 

 We collect the GVN of all the instructions in the function and iterate on the list of instructions having identical GVNs. The algorithm prefers hoisting to sinking. So first we find the common dominator dominating all such identical computations and perform legality checks, as described in Section 3.3. Often times it is not possible to hoist all the instructions to one common dominator, due to legality constraints, e.g., intersecting side-effects, or profitability constraints, e.g., increasing register pressure; in those cases, this algorithm would partition (Section 3.4.3) the list of identical instructions into subsets which can be partially hoisted to their respective common dominators. However, it should be noted that we only hoist very busy expressions to avoid checking for undefined behaviors resulting because of introducing extra computation in an execution path.

Barriers are based on the concept of pinned instructions (Click 1995) but extended to adapt to LLVM IR. Since a basic block in LLVM IR is actually an extended basic block because there might be calls in the middle of a basic block which might not return. So barriers can be present in the middle of a basic block. Essentially, any instruction that cannot not guarantee progress is marked as a barrier. In the absense of context (as in our current implementation), some instructions which might be safe are still classified a barrier e.g., volatile loads/stores, calls with missing attributes.

computing barriers:

```
for each basic block B in a function:
  barrier_found = false
  for each instruction I in B:
    if I does not guarantee progress:
       mark I as a barrier instruction
      barrier_found = true
      break;

// Find the last barrier below which instructions can be sunk.
// If there was no barrier in B, any instruction satisfying
// other legality checks can be sunk.
if barrier_found:
```

#### 1:12 • Aditya Kumar and Sebastian Pop

```
for each instruction I in B in reverse order:
           if I does not guarantee progress:
             mark I as a sink barrier
4
             break
     computing downward-safety of hoistable instructions at hoist-point
6
     Worklist = list of all basic blocks of hoistable instructions
     for each basic block B in the dominator tree starting at hoist-point:
8
       if Worklist is empty
         return false // Path exists! not downward safe
9
10
       if B is in Worklist:
11
         remove B from worklist
12
         remove subtree with root at B // Available at B => downward safe from B
13
       if B is a leaf basic block:
14
         return false // Path exists! not downward safe
15
       if B dominates hoist-point:
16
         return false // Back edge
17
18
     Analyses available: Dominator Tree, DFS Numbering, Memory SSA,
19
20
     Compute GVN of each expression in the function
21
     Compute DJ-graph of function and compute mergeset based on that
22
23
     For each value number VN with 2 or more instructions:
24
       sort the instructions according to DFSIn numbers
25
       if first two I1, I2 are hoistable:
26
         if they are downward-safe at hoist-point:
27
           if they are profitable to be hoisted at hoist-point:
28
             proceed to check hoistability of subsequent instruction with same VN
29
           else
30
             proceed to check if I2 and I3 (if available) is hoistable
31
32
     For each hoistable VN:
33
       move the first one I1 to the hoist-point
34
       update the use of all other candidates to refer to I1
35
       remove all others.
36
       if I1 has memory references (a load, store etc.)
37
         update MemorySSA of I1 and others to point to the MemorySSA reference of I1
38
         remove MemorySSA reference of all others which were deleted
39
       update statistics
40
41
     If any of candidates were hoisted then repeat hoisting
42
     Once no more candidates are hoistable proceed to sinking
43
     Analyses available: Dominator Tree, DFS Numbering, Memory SSA, Mergeset
44
     Compute GVN of each expression in the function
45
46
47
48
```

```
1
     For each value number VN with 2 or more instructions:
2
       if there are two instructions with same immediate successor as post-dominator
3
         if both are only used in the same PHI-node of the successor
4
           if both have dependencies that are available or can be made available at the sink point
              mark VN as sinkable
6
7
     For each pair I1, I2 of sinkable instructions:
8
       Move the first one I1 to the sink point which is just after all the PHI-nodes
9
       in the post-dominator
10
       update the use of PHI with I1
11
       Remove I2 and PHI
       if I1 is a memory reference:
12
         update MemorySSA of I1 and others to point to the MemorySSA reference of I1
13
         remove MemorySSA reference of all others which were deleted
14
15
       update statistics
16
```

Code hoisting opens new opportunities for other hoistable candidates which were of higher rank (depended on candidates which got hoisted). Ideally we could iterate on lower ranking expressions first and then proceed to higher ranking expressions in the same iteration but LLVM's GVN infrastructure does not compute equivalence classes in a effective way. We found it simpler to just recompute the value numbers and start finding hoistable candidates again.

#### 4.2 Time complexity of algorithm

 The complexity of code hoisting is linear in number of instructions that are candidates for code-motion, matching the complexity of PRE on SSA form. The analyses computed for this pass are Global Value Numbering, Computation of DJ-graph and merge-sets, Marking Barriers, all are linear in number of instructions in a function. Liveness analysis expensive but only performed on-demand for hoistable candidates so it does not affect the overall compile time by much. Other analyses like Alias Analysis, MemorySSA and Dominator Tree are already available in the LLVM pass pipeline. Although we recompute GVN, and Barriers for each iteration of the code-motion, we have not seen significant increase in the compilation times. We have also provided appropriate compiler flags to expedite code-motion by bailing out with fewer iterations, or skip the liveness based profitability analysis to aggressively move the code as long as they are legal (Section 5).

The analysis is followed by a simple code generation that adds the identified instruction in the destination point and removes all instructions rendered redundant as a result of code-motion.

#### 5 EXPERIMENTAL EVALUATION

We ran SPEC Cpu 2006 with the patch. All the experiments were conducted on x86\_64 Ubuntu-Linux machine and at -Ofast optimization level. The results for code-hoisting are listed in Table 5. The table lists the number of scalars, loads, stores and calls hoisted as well as removed. For each category, the number of instructions removed is greater or equal to the number of instructions hoisted because each hoisting is performed only when at least one identical computation is found.

Loads are hoisted the most followed by scalars, stores and calls in decreasing order. This was the common trend in all our experiments. One reason why loads are hoisted the most is the early execution of this pass (before mem2reg) in the LLVM pass pipeline. Passes like mem2reg, instcombine might actually remove those loads so this order may change should this pass be scheduled later. The number of

 instructions sunk is very less because LLVM has a code sinking pass inside SimplifyCFG which is run before the global code-motion and sinks some instructions. Another reason is that instructions for which dependencies are not directly available in the successor is not sunk for now. Sinking those instructions would require a look ahead on the sinkability of the dependencies. We plan to implement this in near future.

Other static metrics are listed in Table 4 and in Table 5. Here we can see that except for rematerializing defs for splitting, which has an overhead of 2%, all other parameters have less than 1% overhead. This is to explain why the performance does not go down with our implementation (and cost-model) of code hoisting pass.

| Number of spills | base(-Ofast) | code-motion(-Ofast) | %change |
|------------------|--------------|---------------------|---------|
| 400.perlbench    | 2539         | 2493                | 0.98    |
| 401.bzip2        | 718          | 707                 | 0.98    |
| 403.gcc          | 5782         | 5722                | 0.99    |
| 429.mcf          | 14           | 17                  | 1.21    |
| 433.milc         | 635          | 642                 | 1.01    |
| 444.namd         | 3223         | 3274                | 1.01    |
| 445.gobmk        | 2166         | 2173                | 1.00    |
| 447.dealII       | 11074        | 10234               | 0.92    |
| 450.soplex       | 1122         | 1125                | 1.00    |
| 453.povray       | 4701         | 4692                | 1.09    |
| 456.hmmer        | 1197         | 1274                | 1.06    |
| 458.sjeng        | 168          | 176                 | 1.05    |
| 462.libquantum   | 118          | 118                 | 1.00    |
| 464.h264ref      | 3379         | 3454                | 1.02    |
| 470.lbm          | 33           | 33                  | 1.00    |
| 471.omnetpp      | 524          | 527                 | 1.00    |
| 473.astar        | 180          | 201                 | 1.12    |
| 482.sphinx3      | 674          | 670                 | 0.99    |
| 483.xalancbmk    | 5102         | 4965                | 0.97    |
| Grand Total      | 43349        | 42497               | 0.98    |

Table 1. Number of spills on before and after code-motion on SPEC2006 at -Ofast

Spills are listed in Table (?). Spills were reduced by an average of 2% on the SPEC Cpu 2006 benchmark suite. This is a result of cost-model which limits the code-motion to those candidates which do not increase the register pressure (except for loads Section (?), overall spills still decreases.

Code size remained almost the same as a result of code-motion as shown in Table (?). The code size listed here is the text size (from linux size command) of the final executables for each benchmark. Some bencmarks like 473 astar increased in code size by almost 2%. This is because once the code-size of a function decreases it becomes cheaper to inline. As we can see in Table-(?), four more functions got inlined in 473 astar. Except for 447 dealII, 450 soplex, 482 sphinx3 and 483 xalancbmk all other benchmarks got more functions inlined.

The compilation time actually reduced for most of the benchmarks as a result of code motion. This is because as code-motion removes (congruent) instructions, the number of instructions to be processed by

| -  |
|----|
| 2  |
| 3  |
| 4  |
| 5  |
| 6  |
| 7  |
| 8  |
| 9  |
| 10 |
| 11 |
| 12 |
| 13 |
| 14 |
| 15 |
| 16 |
| 17 |
| 18 |
| 19 |
| 20 |
| 21 |
| 22 |

| Code size      | % age increase in codesize |
|----------------|----------------------------|
| 400.perlbench  | 1.00                       |
| 401.bzip2      | 1.00                       |
| 403.gcc        | 1.01                       |
| 429.mcf        | 1.00                       |
| 433.milc       | 1.00                       |
| 444.namd       | 1.01                       |
| 445.gobmk      | 1.01                       |
| 447.dealII     | 1.01                       |
| 450.soplex     | 0.99                       |
| 453.povray     | 1.00                       |
| 456.hmmer      | 1.00                       |
| 458.sjeng      | 1.00                       |
| 462.libquantum | 1.00                       |
| 464.h264ref    | 1.00                       |
| 470.lbm        | 1.00                       |
| 471.omnetpp    | 0.99                       |
| 473.astar      | 1.02                       |
| 482.sphinx3    | 1.00                       |
| 483.xalancbmk  | 0.99                       |
| Grand total    | 1.00                       |

Table 2. Change in code size with and without code-motion on SPEC2006 at -Ofast

later compilation passes also reduces. The compilation time listed here is the total instruction count as outputted from valgrind (-tool=cachegrind).

Some useful statc metric are presented in Table (?), which shows how code-motion impacted important compiler optimizations like inlining and LICM. LICM removes loop invariant code out of the loop. It may hoist the code to the loop's preheader or sink the code to loop's post-dominator (Muchnick 1997). As we can see number of instructions hoisted increased significantly in several benchmarks, although number of instructions sunk did not change by much. Number of inlined functions also improved for most benchmarks. In general when more functions were inlined, more functions were deleted as in 400.perlbench, 445.gobmk.

While benchmarking SPEC Cpu 2006 we see both increase as well as decrease in the codesizes of the final binaries. Since the pass runs early, it affects many optimizations which rely on the number of instructions, lenth of the use-def chain, and other metrics. For instance, the inliner is impacted by a decrease in the number of instructions in the caller and callee, as its heuristics estimate the size of functions to be inlined. Various code-size metrics are shown in Table 2. All but one benchmark varied between -5.32% and 5.43%. In one benchmark FreeBench/distray/distray.test, the codesize increased by 35.38%. In this benchmark 3 more functions got inlined (15 as compared to 12) and because of that 10 more vector instructions got generated (81 vs. 71), 3 calls got hoisted/sunk as (compared to 0), one loop got unswitched (compared to 0), 6 high latency machine instructions got hoisted out of loop, 59 (compared to 30) machine instructions got hoisted out of loop, 70 (compared to 39) machine instructions were sunk.

| Benchmark      | Baseline       | GCM            | %Incrase |
|----------------|----------------|----------------|----------|
| 400.perlbench  | 186,829,426    | 184,690,006    | 0.99     |
| 401.bzip2      | 76,337,033     | 75,942,641     | 0.99     |
| 403.gcc        | 1,079,625,231  | 1,073,158,220  | 0.99     |
| 429.mcf        | 78,336,298     | 77,859,513     | 0.99     |
| 433.milc       | 272,525,306    | 269,684,876    | 0.99     |
| 444.namd       | 78,354,313     | 77,875,603     | 0.99     |
| 445.gobmk      | 261,229,078    | 258,459,798    | 0.99     |
| 447.dealII     | 643,457,797    | 638,628,331    | 0.99     |
| 450.soplex     | 245,442,755    | 242,811,500    | 0.99     |
| 453.povray     | 499,034,715    | 494,785,035    | 0.99     |
| 456.hmmer      | 214,425,324    | 211,984,389    | 0.99     |
| 458.sjeng      | 89,612,524     | 88,803,166     | 0.99     |
| 462.libquantum | 84,762,158     | 84,077,905     | 0.99     |
| 464.h264ref    | 151,049,588    | 149,284,624    | 0.99     |
| 470.lbm        | 71,878,726     | 71,775,405     | 1.00     |
| 471.omnetpp    | 382,661,268    | 379,123,833    | 0.99     |
| 473.astar      | 78,351,117     | 77,872,820     | 0.99     |
| 482.sphinx3    | 158,434,290    | 156,586,406    | 0.99     |
| 483.xalancbmk  | 22,485,708,759 | 22,455,060,569 | 1.00     |

Table 3. Change in compilation time with and without code-motion on SPEC2006 at -Ofast

The code shown in Section 1 is a reduced example that appears in a hot loop of a proprietary benchmark. When the expressions are hoisted from the conditional clauses, the overall performance of that benchmark improves by 15% on an out-of-order processor due to increased instruction level parallelism, and better scheduling of the instructions, accommodating for the long latency of the division operation.

#### 6 CONCLUSION AND FUTURE WORK

We have presented the GVN based code hoisting algorithm. The primary goal is to reduce the code size but it benefits performance in some cases as well. To preserve performance and not hoist too much we have implemented several cost models described in Section 3.4. Since those cost models depend on a set of thresholds, it requires tuning, as such, we used representative benchmarks to tune them.

In general it is a good idea to start with lower ranked expression first such that maximum hoisting can happen in one iteration, however, current implementation does not rank the expressions and iteratively finds a fixed point when no more candidates are available. Even this implementation converges quickly and no significant compile time regression have been observed because of code hoisting pass. This is not the most optimal approach and results in multiple data structures to be recomputed. This can be improved by ranking the computations (Rosen et al. 1988). Also GVN-hoist runs very early in the pass pipeline, it will be good to evaluate the codesize/performance impact when it is run in sync with GVN-PRE just like GCC does.

With the implementation of code-hoisting in LLVM, the passes which rely on the code-size/instruction-count to make optimization decisions needs to be revisited. The first candidate would be the inliner. We

| 1  |
|----|
| 2  |
| 3  |
| 4  |
| 5  |
| 6  |
| 7  |
| 8  |
| 9  |
| 10 |
| 11 |
| 12 |
| 13 |
| 14 |
| 15 |
| 16 |
| 17 |
| 18 |
| 19 |
| 20 |
| 21 |

2324252627

28

29 30

31

32

33 34

35

36

37

38

39

40

41

42

43

44

45

46

47 48

|                | Hoisted by LICM |       | Sunk by LICM |     | Functions Inlined |        | Functions Deleted |       |
|----------------|-----------------|-------|--------------|-----|-------------------|--------|-------------------|-------|
| Benchmark      | trunk           | GCM   | trunk        | GCM | trunk             | GCM    | trunk             | GCM   |
| 400.perlbench  | 2428            | 2480  | 36           | 35  | 1562              | 1565   | 232               | 234   |
| 401.bzip2      | 721             | 825   | 3            | 3   | 172               | 180    | 32                | 33    |
| 403.gcc        | 8867            | 10079 | 143          | 182 | 5034              | 5080   | 1303              | 130   |
| 429.mcf        | 55              | 51    | 1            | 1   | 4                 | 4      | 0                 | 0     |
| 433.milc       | 2537            | 2795  | 3            | 3   | 75                | 81     | 0                 | 0     |
| 444.namd       | 2204            | 2206  | 240          | 240 | 387               | 390    | 57                | 55    |
| 445.gobmk      | 3090            | 3107  | 18           | 19  | 735               | 775    | 230               | 234   |
| 447.dealII     | 59114           | 95884 | 60           | 8   | 100891            | 100692 | 30219             | 29966 |
| 450.soplex     | 4668            | 4848  | 18           | 17  | 9801              | 9784   | 3125              | 3112  |
| 453.povray     | 9533            | 9079  | 23           | 32  | 5522              | 5532   | 1202              | 1201  |
| 456.hmmer      | 3200            | 3232  | 3            | 8   | 562               | 562    | 103               | 101   |
| 458.sjeng      | 400             | 446   | 0            | 0   | 127               | 135    | 18                | 18    |
| 462.libquantum | 362             | 386   | 0            | 0   | 87                | 87     | 21                | 21    |
| 464.h264ref    | 17075           | 17153 | 4            | 4   | 338               | 382    | 72                | 72    |
| 470.lbm        | 39              | 39    | 0            | 0   | 13                | 13     | 4                 | 4     |
| 471.omnetpp    | 565             | 661   | 32           | 30  | 4790              | 4843   | 1321              | 1316  |
| 473.astar      | 691             | 754   | 0            | 0   | 359               | 363    | 113               | 113   |
| 482.sphinx3    | 1599            | 1693  | 11           | 9   | 198               | 194    | 53                | 53    |
| 483.xalancbmk  | 9997            | 11453 | 56           | 54  | 69534             | 68839  | 29875             | 29519 |

Table 4. Static metrics before and after code-hoisting on SPEC2006 at -Ofast

have seen different inlining decisions in Table 2, before and after code-hoisting was enabled. Since inliner

has several magic numbers tuned for the previous pass layout, it would need some improvement.

#### **ACKNOWLEDGMENTS**

We would like to thank Daniel Berlin for his code reviews and for his feedback on earlier versions of this paper and Brian Grayson for motivating examples that started this work.

#### REFERENCES

- Alfred V Aho, Ravi Sethi, and Jeffrey D Ullman. 1986. Compilers, Principles, Techniques. Addison Wesley.
- ARM. 2014. ARM Cortex-A57 Software Optimization Guide. (2014). http://infocenter.arm.com/help/topic/com.arm.doc.uan0015b/Cortex\_A57\_Software\_Optimization\_Guide\_external.pdf
- Gergö Barany and Andreas Krall. 2013. Optimal and heuristic global code motion for minimal spilling. In *International Conference on Compiler Construction*. Springer, 21–40.
- Preston Briggs and Keith D Cooper. 1994. Effective partial redundancy elimination. In ACM SIGPLAN Notices, Vol. 29. ACM, 159–170.
- Preston Briggs, Keith D Cooper, and L Taylor Simpson. 1997. Value numbering. Software Practice & Experience 27, 6 (1997), 701–724.
- Fred Chow, Sun Chan, Robert Kennedy, Shin-Ming Liu, Raymond Lo, and Peng Tu. 1997. A new algorithm for partial redundancy elimination based on SSA form. In *ACM SIGPLAN Notices*, Vol. 32. ACM, 273–286.
- Cliff Click. 1995. Global code motion/global value numbering. In ACM SIGPLAN Notices, Vol. 30. ACM, 246-257.
- Keith D Cooper and L Taylor Simpson. 1998. Live range splitting in a graph coloring register allocator. In *International Conference on Compiler Construction*. Springer, 174–187.

| 44 |  |
|----|--|
| 45 |  |
|    |  |
| 46 |  |

| code-motion                                      | Total In | structions | Sca     | alars   | Lo      | oads    | Stores          | Calls   | Instructions |
|--|----------|------------|---------|---------|---------|---------|-----------------|---------|--------------|
| metric   | hoisted  | removed    | hoisted | removed | hoisted | removed | hoisted=removed | hoisted | sunk         |
| 400.perlbench                                    | 2387     | 2456       | 855     | 857     | 1493    | 1560    | 38              | 1       | 4            |
| 401.bzip2  | 176      | 300        | 27      | 27      | 149     | 273     | 0               | 0       | 0            |
| 403.gcc  | 5670     | 5761       | 2558    | 2567    | 3109    | 3191    | 3               | 0       | 1            |
| 429.mcf  | 42       | 43         | 5       | 5       | 37      | 38      | 0               | 0       | 0            |
| 433.milc   | 128      | 130        | 10      | 10      | 117     | 119     | 0               | 1       | 0            |
| 444.namd   | 262      | 264        | 113     | 113     | 148     | 150     | 0               | 1       | 0            |
| 445.gobmk  | 1021     | 1052       | 312     | 314     | 705     | 734     | 3               | 1       | 1            |
| 447.dealII                                       | 10455    | 12325      | 4009    | 4063    | 6394    | 8210    | 20              | 32      | 0            |
| 450.soplex                                       | 2389     | 2731       | 927     | 1004    | 1437    | 1702    | 14              | 11      | 0            |
| 453.povray                                       | 1967     | 2269       | 560     | 590     | 1389    | 1661    | 4               | 14      | 0            |
| 456.hmmer  | 408      | 427        | 82      | 82      | 319     | 338     | 1               | 6       | 0            |
| 458.sjeng  | 372      | 399        | 128     | 138     | 234     | 251     | 1               | 9       | 1            |
| 462.libquantum                                   | 49       | 49         | 17      | 17      | 32      | 32      | 0               | 0       | 0            |
| 464.h264ref                                      | 2953     | 3438       | 712     | 779     | 2238    | 2656    | 2               | 1       | 1            |
| 470.lbm  | 23       | 23         | 4       | 4       | 19      | 19      | 0               | 0       | 0            |
| 471.omnetpp                                      | 391      | 408        | 92      | 92      | 297     | 314     | 0               | 2       | 0            |
| 473.astar  | 202      | 222        | 62      | 64      | 140     | 158     | 0               | 0       | 0            |
| 482.sphinx3                                      | 168      | 172        | 32      | 32      | 136     | 140     | 0               | 0       | 0            |
| 483.xalancbmk                                    | 5894     | 6162       | 2586    | 2660    | 3301    | 3495    | 4               | 3       | 2            |
| Grand total                                      | 34957    | 38631      | 13091   | 13418   | 21694   | 25041   | 90              | 82      | 10           |
| Table 5. Code motion stats on SPEC2006 at -Ofast |          |            |         |         |         |         |                 |         |              |

Table 5. Code motion stats on SPEC2006 at -Ofast

Thomas H.. Cormen, Charles Eric Leiserson, Ronald L Rivest, and Clifford Stein. 2001. *Introduction to algorithms*. Vol. 6. MIT press Cambridge.

Ron Cytron, Jeanne Ferrante, Barry K Rosen, Mark N Wegman, and F Kenneth Zadeck. 1989. An efficient method of computing static single assignment form. In *Proceedings of the 16th ACM SIGPLAN-SIGACT symposium on Principles of programming languages*. ACM, 25–35.

Dibyendu Das, B Dupont De Dinechin, and Ramakrishna Upadrasta. 2012. Efficient liveness computation using merge sets and dj-graphs. ACM Transactions on Architecture and Code Optimization (TACO) 8, 4 (2012), 27.

Dibyendu Das and U Ramakrishna. 2005. A practical and fast iterative algorithm for  $\varphi$ -function computation using DJ graphs. ACM Transactions on Programming Languages and Systems (TOPLAS) 27, 3 (2005), 426–440.

Dhananjay M Dhamdhere. 1988. A fast algorithm for code movement optimisation. ACM SIGPLAN Notices 23, 10 (1988), 172–180

GCC. 2016a. GCC bugs related to code hoisting. Bug IDs: 5738, 11820, 11832, 21485, 23286, 29144, 32590, 33315, 35303, 38204, 43159, 52256. (2016). https://gcc.gnu.org/bugzilla

GCC. 2016b. GCC code hoisting implementation. (2016). https://gcc.gnu.org/viewcvs/gcc?view=revision&revision=238242 Intel. 2000. Intel IA-64 Architecture Software Developer's Manual. (2000). http://www.intel.com/content/dam/doc/manual/64-ia-32-architectures-optimization-manual.pdf

Robert Kennedy, Sun Chan, Shin-Ming Liu, Raymond Lo, Peng Tu, and Fred Chow. 1999. Partial redundancy elimination in SSA form. ACM Transactions on Programming Languages and Systems (TOPLAS) 21, 3 (1999), 627–676.

LLVM. 2016. LLVM bugs related to code hoisting. Bug IDs: 12754, 20242, 22005. (2016). https://llvm.org/bugs

Etienne Morel and Claude Renvoise. 1979. Global optimization by suppression of partial redundancies. Commun. ACM 22, 2 (1979), 96–103.

Steven S. Muchnick. 1997. Advanced compiler design implementation. Morgan Kaufmann.

PACM Progr. Lang., Vol. 1, No. 1, Article 1. Publication date: January 2017.

Diego Novillo. 2007. Memory SSA – a unified approach for sparsely representing memory operations. In Proc of the GCC
 Developers' Summit.

- Barry K Rosen, Mark N Wegman, and F Kenneth Zadeck. 1988. Global value numbers and redundant computations. In Proceedings of the 15th ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages. ACM, 12–27.
- Ghassan Shobaki, Maxim Shawabkeh, and Najm Eldeen Abu Rmaileh. 2013. Preallocation instruction scheduling with register pressure minimization using a combinatorial optimization approach. ACM Transactions on Architecture and Code Optimization (TACO) 10, 3 (2013), 14.
- Vugranam C. Sreedhar. 1995. Efficient Program Analysis Using DJ Graphs. Ph.D. Dissertation. Montreal, Que., Canada, Canada. UMI Order No. GAXNN-08158.