## Argumentation and Answer Set Programming

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**Abstract.** Argumentation and answer set programming are two of the main knowledge representation paradigms that have emerged from logic programming for non-monotonic reasoning. This paper surveys recent work on using answer set programming as a mechanism for computing extensions in argumentation. The paper also indicates some possible directions for future work.

### 1 Introduction

Argumentation was developed, starting in the early '90s [9,16,8], as a computational framework to reconcile and understand common features and differences amongst most existing approaches to non-monotonic reasoning. These include various alternative treatments of negation as failure in logic programming [32,26,52,19], Theorist [43], default logic [45], autoepistemic logic [38], non-monotonic modal logic [37] and circumscription [36]. Argumentation relies upon

- the representation of knowledge in terms of an argumentation framework; defining *arguments* and a binary *attack* relation between the arguments;
- dialectical semantics for determining acceptable sets of arguments;
- a computational machinery for determining the acceptability of a given (set
  of) argument(s) or for computing all acceptable sets of arguments (also referred to as extensions), according to some dialectical semantics.

Answer set programming (ASP) [31] constitutes one of the main current trends in logic programming and non-monotonic reasoning. ASP relies upon

- the representation of knowledge in terms of (possibly disjunctive) logic programs with negation as failure (possibly including explicit negation, various forms of constraints, aggregates etc);
- the interpretation of these logic programs under the stable model/answer set semantics [32,33] and its extensions (to deal with explicit negation, constraints, aggregates etc);
- efficient computational mechanisms (ASP solvers) to compute answer sets for grounded logic programs, and efficient 'grounders' to transform non-ground logic programs into ground (variable-free) ones.

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Standard computational mechanisms for argumentation are defined using trees (e.g. [18]) or disputes (e.g. [20]) and only construct relevant parts of extensions. ASP can instead be used to support the full computation of extensions.

This paper provides a survey of recent work using ASP for computing extensions in abstract argumentation frameworks [16] and some other forms of argumentation. It also indicates possible directions for future work and cross-fertilisation between ASP and argumentation.

The paper is organised as follows. Section 2 gives some background on argumentation (focusing on abstract argumentation [16]) and ASP. Section 3 surveys existing approaches using ASP to compute extensions in argumentation (again focusing on abstract argumentation). Section 4 indicates some possible directions for future work. Section 5 concludes.

### 2 Background

### 2.1 Argumentation

An abstract argumentation (AA) framework [16] is a pair  $\langle Arg, att \rangle$  where Arg is a finite set, whose elements are referred to as arguments, and  $att \subseteq Arg \times Arg$  is a binary relation over Arg. Given  $\alpha, \beta \in Arg$ ,  $\alpha$  attacks  $\beta$  iff  $(\alpha, \beta) \in att$ . Given sets  $X, Y \subseteq Arg$  of arguments, X attacks Y iff there exists  $x \in X$  and  $y \in Y$  such that  $(x, y) \in att$ . A set of arguments is referred to as an extension. An extension  $X \subseteq Arg$  is

- conflict-free iff it does not attack itself;
- stable iff it is conflict-free and it attacks every argument it does not contain;
- acceptable wrt a set  $Y \subseteq Arg$  of arguments iff for each  $\beta$  that attacks an argument in X, there exists  $\alpha \in Y$  such that  $\alpha$  attacks  $\beta$ ;
- admissible iff X is conflict-free and X is acceptable wrt itself;
- preferred iff X is (subset) maximally admissible;
- complete iff X is admissible and X contains all arguments  $\alpha$  such that  $\{\alpha\}$  is acceptable wrt X;
- grounded iff X is (subset) minimally complete.

In addition, an extension  $X \subseteq Arg$  is

- ideal [18] iff X is admissible and it is contained in every preferred set of arguments;
- semi-stable [12] iff X is complete and  $X \cup X^+$  is (subset) maximal, where  $X^+ = \{\beta \mid (\alpha, \beta) \in att \text{ for some } \alpha \in X\}.$

These notions of extensions constitute different alternative dialectical semantics, giving different approaches for determining what makes arguments dialectically viable. Arguments can be deemed to hold *credulously* wrt a given dialectical semantics if they belong to an extension sanctioned by that semantics. Arguments can be deemed to hold *sceptically* wrt a given dialectical semantics if they

belong to all extensions sanctioned by that semantics. In some cases credulous and sceptical reasoning coincide, e.g. for grounded and ideal extensions, since these are unique.

For  $AF = \langle Arg, att \rangle$ , the characteristic function  $\mathcal{F}_{AF}$  is such that  $\mathcal{F}_{AF}(X)$  is the set of all acceptable arguments wrt X. Then, a conflict-free  $X \subseteq Arg$  is

- an admissible extension iff  $X \subseteq \mathcal{F}_{AF}(X)$ ,
- a complete extension iff it is a fixpoint of  $\mathcal{F}_{AF}$ , and
- a grounded extension iff X is the least fixpoint of  $\mathcal{F}_{AF}$ .

Several other argumentation frameworks have been given in the literature, concretely specifying arguments and attacks, some instantiating abstract argumentation, e.g. assumption-based argumentation [9,8,17] and logic programming-based argumentation frameworks such as [44], some equipped with dialectical semantics other than the ones proposed for abstract argumentation, e.g. [7,30]. Moreover, extensions of abstract argumentation have been proposed, e,g, value-based argumentation [5].

### 2.2 Answer Set Programming (ASP)

A logic program is a set of clauses of the form

$$p_1 \vee \ldots \vee p_k \leftarrow q_1 \wedge \ldots \wedge q_m \wedge not \, q_{m+1} \wedge \ldots \wedge not \, q_{m+n}$$

for  $k \geq 0$ ,  $m \geq 0$ ,  $n \geq 0$ , k+m+n>0, where the  $p_i$  and  $q_j$  are literals, that is, of the form p or  $\neg p$  where p is an atom. not denotes negation as failure. Expressions of the form  $not\ q_j$  where  $q_j$  is a literal are called 'negation as failure literals', or nbf-literals for short. We will refer to  $\{p_1,\ldots,p_k\}$  as the head,  $\{q_1,\ldots,q_m,not\ q_{m+1},\ldots not\ q_{m+n}\}$  as the body and  $\{not\ q_{m+1},\ldots not\ q_{m+n}\}$  as the negative body of a clause. We will also refer to clauses with k=0 as denial clauses, clauses with k>1 as disjunctive clauses, and clauses with n=0 as positive clauses.

All variables in clauses in a logic program are implicitly universally quantified, with scope the individual clauses. A logic program stands for the set of all its ground instances over a given Herbrand universe. The semantics of logic programs is given for their grounded version over this Herbrand universe.

The answer sets of a (grounded) logic program are defined as follows [33].

Let X be a set of literals (that is, expressions p or  $\neg p$  where p is an atom). A literal is true in X if it belongs to X. A nbf-literal not p is true in X if the literal p does not belong to X. A clause is true in X if its head is true in X (there exists a literal in the head that is true in X) whenever its body is true in X (i.e., when all the literals and all the nbf-literals in that body are true in X). Thus, denial clauses are true in X if and only if their body is false in X (i.e., some literal in the body is not true in X). A set of literals X is closed under a set of clauses P if every clause in P is true in X. X is 'consistent' if it contains no pair of complementary literals p and  $\neg p$  for some atom p; X is logically closed if it is consistent or if it is the set of all literals otherwise.

If P is a set of positive clauses, that is, a set of clauses containing no occurrences of negation as failure not, then X is an answer set of P if it is a (subset) minimal set of literals that is logically closed and closed under the clauses in P.

If P is any set of clauses (not necessarily positive ones) the Gelfond-Lifschitz reduct  $P^X$  of P wrt to the set of literals X is obtained from P by deleting (1) all clauses in P containing a nbf-literal  $not \, p$  in the body where p is true in X, and (2) the negative body from all remaining clauses.  $P^X$  is a set of positive clauses. Then X is an  $answer\ set$  of P when X is an answer set of  $P^X$ .

None of the logic programs presented in section 3 of this paper contain occurrences of classical negation ( $\neg$ ): all of the literals in all of the clauses are atoms. For programs P of this type, the answer sets of P are also the *stable models* [32] of P.

Several very efficient ASP solvers are widely available and can be used to compute answer sets and/or perform query answering wrt answer sets. These solvers include Smodels<sup>1</sup>, DLV<sup>2</sup> and clasp<sup>3</sup>. These solvers incorporate, or are used in combination with, *grounders*, programs whose function is to generate, prior to computing answer sets, a finite ground logic program from a non-ground logic program (over a given, not necessarily finite Herbrand Universe).

## 3 ASP for Argumentation

Several approaches have been proposed for computing (several kinds of) extensions of abstract argumentation (AA) frameworks using ASP solvers [39,53,23,27]. All rely upon the mapping of an AA framework into a logic program whose answer sets are in one-to-one correspondence with the extensions of the original AA framework. All those summarised below use the DLV solver to compute these answer sets (and thus the extensions). The approaches differ in the kinds of extensions they focus on and in the mappings and correspondences they define, as we will see below. They fall into two groups: those which result in an AA framework-dependent logic program, and those which result in a logic program with an AA framework-dependent component and an AA framework-independent (meta-)logic program.

### 3.1 Nieves, Cortés and Osorio [39]: Preferred Extensions

Nieves et al [39] focus on the computation of **preferred** extensions. Their mapping relies upon the method of [6] using propositional formulas to express conditions for sets of arguments to be extensions of AA frameworks. The mapping produces a disjunctive logic program defining a predicate def, where  $def(\alpha)$  can be read as 'argument  $\alpha$  is defeated'. Intuitively,

– each pair  $(\alpha, \beta)$  in the att component of an AA framework (Arg, att) is mapped to a disjunctive clause  $def(\alpha) \vee def(\beta) \leftarrow$ ;

<sup>1</sup> http://www.tcs.hut.fi/Software/smodels/

http://www.dbai.tuwien.ac.at/proj/dlv/

<sup>3</sup> http://potassco.sourceforge.net/

- for each pair  $(\beta, \alpha) \in att$ , a clause  $def(\alpha) \leftarrow def(\gamma_1) \wedge \ldots \wedge def(\gamma_k)$   $(k \geq 0)$  is introduced, where  $\gamma_1, \ldots, \gamma_k$  are all the 'defenders' of  $\alpha$  against  $\beta$  (that is, where  $(\gamma_1, \beta), \ldots, (\gamma_k, \beta) \in att$ , and there are no other attacks against  $\beta$  in att).

$$a \longrightarrow b \longrightarrow c$$

**Fig. 1.** Graph representation for the AA framework  $(\{a, b, c\}, \{(a, b), (b, c)\})$ 

For the AA framework of figure 1, the mapping returns

$$\begin{aligned} def(a) \lor def(b) \leftarrow \\ def(b) \lor def(c) \leftarrow \\ def(c) \leftarrow def(a) \\ def(b) \leftarrow \end{aligned}$$

The answer sets of the disjunctive logic program  $P_{NCO}^{pref}$  thus obtained are in one-to-one correspondence with the preferred extensions of the original AA framework  $\langle Arg, att \rangle$ , in that the complement

$$\mathcal{C}(AS) =_{\operatorname{def}} \{ \alpha \in Arg \mid def(\alpha) \not\in AS \}$$

of each answer set AS of  $P_{NCO}^{pref}$  is a preferred extension of  $\langle Arg, att \rangle$ .

In the example of the AA framework of figure 1 and the resulting  $P_{NCO}^{pref}$  given earlier, the only answer set is  $\{def(b)\}$ , corresponding to the only preferred extension  $\{a,c\} = \mathcal{C}(\{def(b)\})$  of the original AA framework.



**Fig. 2.** Graph representation for the AA framework  $(\{a\}, \{(a,a)\})$ 

In the example of figure 2,  $P_{NCO}^{pref}$  is

$$def(a) \lor def(a) \leftarrow$$
  
 $def(a) \leftarrow def(a)$ 

with answer set  $\{def(a)\}$  corresponding to the (only) preferred extension  $\{\}$  of the original AA framework. In the case of the AA framework of figure 3,  $P_{NCO}^{pref}$  is

$$def(a) \lor def(b) \leftarrow$$
$$def(a) \leftarrow def(a)$$
$$def(b) \leftarrow def(b)$$

with answer sets  $\{def(a)\}\$  and  $\{def(b)\}\$  corresponding to the preferred extensions  $\{b\}\$  and  $\{a\}\$  (respectively) of the original AA framework.

$$a \longleftrightarrow b$$

**Fig. 3.** Graph representation for the AA framework  $(\{a,b\},\{(a,b),(b,a)\})$ 

## 3.2 Wakaki and Nitta [53]: Complete, Stable, Preferred, Grounded, and Semi-stable Extensions

Wakaki and Nitta [53] focus on the computation of complete, stable, preferred, grounded, and semi-stable extensions. Their mappings rely upon Caminada's reinstatement labellings [11] and correspondences between various kinds of constraints on such labellings and various notions of extensions in abstract argumentation. Intuitively, a reinstatement labelling is a total function from arguments to labels  $\{in, out, undec\}$  such that (i) an argument is labelled out iff some argument attacking it is labelled in, and (ii) an argument is labelled in iff all arguments attacking it are labelled out.

All mappings given by Wakaki and Nitta result in a logic program that contains, for a given AA framework  $\langle Arg, att \rangle$ ), a set  $P_{\langle Arg, att \rangle}$  of clauses  $arg(\alpha) \leftarrow$  for all arguments  $\alpha \in Arg$  and clauses  $att(\alpha, \beta) \leftarrow$  for all pairs  $(\alpha, \beta) \in att$ . For example, in the case of the AA framework of figure 1, one obtains:

$$arg(a) \leftarrow$$
 $arg(b) \leftarrow$ 
 $arg(c) \leftarrow$ 
 $att(a,b) \leftarrow$ 
 $att(b,c) \leftarrow$ 

In the case of **complete** extensions, the logic program  $P_{WN}^{compl}$  resulting from the mapping includes in addition to  $P_{\langle Arg, att \rangle}$  the following (AA framework-independent) clauses (directly corresponding to the notion of reinstatement labelling):

$$\begin{split} ∈(X) \leftarrow arg(X) \wedge not \, ng(X) \\ &ng(X) \leftarrow in(Y) \wedge att(Y,X) \\ &ng(X) \leftarrow undec(Y) \wedge att(Y,X) \\ &out(X) \leftarrow in(Y) \wedge att(Y,X) \\ &undec(X) \leftarrow arg(X) \wedge not \, in(X) \wedge not \, out(X) \end{split}$$

The answer sets of  $P_{WN}^{compl}$  thus obtained are in one-to-one correspondence with the original AA framework  $\langle Arg, att \rangle$ , in that the *in* arguments

$$\mathcal{I}(AS) =_{\mathsf{def}} \{\alpha \in Arg \mid in(\alpha) \in AS\}$$

of each answer set AS of  $P_{WN}^{compl}$  is a complete extension of  $\langle Arg, att \rangle$ .

In the example AA framework of figure 1, there is just one answer set of  $P_{WN}^{compl}$ :  $\{in(a), in(c), out(b)\}$ , corresponding to the only complete extension  $\{a,c\} = \mathcal{I}(\{in(a), in(c), out(b)\})$  of the original AA framework. In the example

AA framework of figure 2, there is just one answer set of  $P_{WN}^{compl}$ :  $\{undec(a)\}$ , corresponding to the only complete extension  $\{\} = \mathcal{I}(\{undec(a)\})$  of the original AA framework. In the example AA framework of figure 3, there are three answer sets of  $P_{WN}^{compl}$ :  $\{in(a), out(b)\}$ ,  $\{in(b), out(a)\}$ , and  $\{undec(a), undec(b)\}$ , corresponding to the three complete extensions  $\{a\}$ ,  $\{b\}$  and  $\{\}$ , respectively, of the original AA framework.

In the case of **stable** extensions, the logic program defined by Wakaki and Nitta is  $P_{WN}^{stable}$  obtained by extending  $P_{WN}^{compl}$  with the clause

$$\leftarrow undec(X)$$

which imposes the further requirement that reinstatement labellings have an empty undec component. Thus, in the case of the AA framework of figure 3, there are only two answer sets of  $P_{WN}^{stable}$ , since  $\{undec(a), undec(b)\}$  is not an answer set in this case. In the case of the AA framework of figure 2, there is also no answer set of  $P_{WN}^{stable}$ , since  $\{undec(a)\}$  is no longer an answer set. The answer sets of  $P_{WN}^{stable}$  are in one-to-one correspondence with the original AA framework  $\langle Arg, att \rangle$ , in that the in arguments  $\mathcal{I}(AS)$  of each answer set AS of  $P_{WN}^{stable}$  is a stable extension of  $\langle Arg, att \rangle$ , similarly to complete extensions.

Caminada [11] has proven that reinstatement labellings with a minimal in component, a maximal in component, and a minimal undec component correspond, respectively, to grounded, preferred and semi-stable extensions. In order to impose these maximality/minimality conditions and obtain logic programs with answer sets corresponding to grounded, preferred and semi-stable extensions, Wakaki and Nitta extend  $P_{WN}^{compl}$  to include meta-logic programs to be used to check answer sets of  $P_{WN}^{compl}$  (and thus reinstatement labellings). Such answer sets are determined in a 'guess & check' fashion [25]. The meta-logic programs are different for the three notions of extensions, but include a common core  $MP_{WN}$  consisting of the following (meta-)clauses

$$m_1(in_t(X)) \leftarrow in(X) \wedge arg(X)$$
  
 $m_1(undec_t(X)) \leftarrow undec(X) \wedge arg(X)$ 

where  $in_t(\alpha)$  and  $undec_t(\alpha)$  are terms corresponding to atoms  $in(\alpha)$  and  $undec(\alpha)$  in  $P_{WN}^{compl}$  and  $m_1$  is a meta-predicate expressing the candidate reinstatement labelling to be checked, as well as (meta-)clauses, for all answer sets AS of  $P_{WN}^{compl}$ :

$$m_2(in_t(X), \psi(AS)) \leftarrow in(X) \in AS$$
  
 $m_2(undec_t(X), \psi(AS)) \leftarrow undec(X) \in AS$ 

 $\psi$  is a function assigning a unique natural number to every answer set of  $P_{WN}^{compl}$  and  $m_2$  is a meta-predicate expressing alternative reinstatement labellings to be compared with the candidate reinstatement labelling being checked.

Then,  $P_{WN}^{pref}$  is  $P_{WN}^{compl} \cup MP_{WN}$  extended with

$$\leftarrow d(Z) \wedge not \ c(Z)$$

$$d(\psi(AS)) \leftarrow m_2(in_t(X), \psi(AS)) \wedge not \ m_1(in_t(X))$$

$$c(\psi(AS)) \leftarrow m_1(in_t(X)) \wedge not \ m_2(in_t(X), \psi(AS))$$

 $P_{WN}^{grounded}$  is  $P_{WN}^{compl} \cup MP_{WN}$  extended with

$$\leftarrow c(Z) \wedge not \, d(Z)$$

$$d(\psi(AS)) \leftarrow m_2(in_t(X), \psi(AS)) \wedge not \, m_1(in_t(X))$$

$$c(\psi(AS)) \leftarrow m_1(in_t(X)) \wedge not \, m_2(in_t(X), \psi(AS))$$

Finally,  $P_{WN}^{semi}$  is  $P_{WN}^{compl} \cup MP_{WN}$  extended with

$$\leftarrow d(Z) \wedge not \ c(Z)$$

$$d(\psi(AS)) \leftarrow m_2(undec_t(X), \psi(AS)) \wedge not \ m_1(undec_t(X))$$

$$c(\psi(AS)) \leftarrow m_1(undec_t(X)) \wedge not \ m_2(undec_t(X), \psi(AS))$$

As in the case of complete and stable extensions, preferred, grounded and semistable extensions correspond to the in arguments  $\mathcal{I}(AS)$  of answer sets AS of the respective logic programs.

# 3.3 Egly, Gaggl and Woltran [23,24]: Conflict-Free, Admissible, Preferred, Stable, Semi-stable, Complete, Grounded Extensions

Egly et al [23] deal with the computation of conflict-free, admissible, preferred, stable, complete, and grounded extensions. Like Wakaki and Nitta [53] summarised in the previous section, an AA framework  $\langle Arg, att \rangle$  is first mapped to a set of clauses  $P_{\langle Arg, att \rangle}$  to be included in logic programs defined for computing the various notions of extension.

For conflict-free extensions, the logic program  $P_{EGW}^{cf}$  consists of  $P_{\langle Arg, att \rangle}$  together with<sup>4</sup>

$$\leftarrow in(X) \wedge in(Y) \wedge att(X, Y)$$
$$in(X) \leftarrow not \ out(X) \wedge arg(X)$$
$$out(X) \leftarrow not \ in(X) \wedge arg(X)$$

The answer sets of  $P_{EGW}^{cf}$  are in one-to-one correspondence with the conflict-free extensions of the AA framework  $\langle Arg, att \rangle$  mapped onto the  $P_{\langle Arg, att \rangle}$  component of  $P_{EGW}^{cf}$ , in the same sense as in [53] (namely that the in arguments  $\mathcal{I}(AS)$  of the answer sets AS correspond to conflict-free extensions).

A similar correspondence exists for the other kinds of extensions and the answer sets of the logic programs given below.

For **stable** extensions, the logic program  $P_{EGW}^{stable}$  consists of  $P_{EGW}^{cf}$  and

$$\leftarrow out(X) \land not \ defeated(X)$$
  
  $defeated(X) \leftarrow in(Y) \land att(Y, X)$ 

<sup>&</sup>lt;sup>4</sup> Note that predicates *in* and *out* here are different from those used in [53] and, in particular, do not refer to the reinstatement labelling of [11].

For admissible extensions, the logic program  $P_{EGW}^{adm}$  consists of  $P_{EGW}^{cf}$  and

$$\leftarrow in(X) \land not\_defended(X)$$
  
 $not\_defended(X) \leftarrow att(Y, X) \land not\ defeated(Y)$   
 $defeated(X) \leftarrow in(Y) \land att(Y, X)$ 

For **complete** extensions, the logic program  $P_{EGW}^{compl}$  consists of  $P_{EGW}^{adm}$  and

$$\leftarrow out(X) \land not not\_defended(X)$$

For **grounded** extensions, the logic program  $P_{EGW}^{grounded}$  is obtained by mirroring the characteristic function presentation of this semantics (see section 2.1). The program makes use of an arbitrary ordering < over arguments assumed to be given a priori. The program consists of three components. The first component  $P_{EGW}^{<}$  uses the given ordering < over arguments to define notions of infimum inf, supremum sup and successor succ over arguments, as follows:

$$succ(X,Y) \leftarrow lt(X,Y) \land not \, nsucc(X,Y)$$

$$nsucc(X,Z) \leftarrow lt(X,Y) \land lt(Y,Z)$$

$$lt(X,Y) \leftarrow arg(X) \land arg(Y) \land X < Y$$

$$inf(X) \leftarrow arg(X) \land not \, ninf(X)$$

$$ninf(Y) \leftarrow lt(X,Y)$$

$$sup(X) \leftarrow arg(X) \land not \, nsup(X)$$

$$nsup(X) \leftarrow lt(X,Y)$$

The second component computes all arguments defended (by all arguments currently in) in the layers obtained using inf, sup and succ, as follows:

$$\begin{split} defended(X) \leftarrow sup(Y) \wedge defended\_up\_to(X,Y) \\ defended\_up\_to(X,Y) \leftarrow inf(Y) \wedge arg(X) \wedge not \ att(Y,X) \\ defended\_up\_to(X,Y) \leftarrow inf(Y) \wedge in(Z) \wedge att(Z,Y) \wedge att(Y,X) \\ defended\_up\_to(X,Y) \leftarrow succ(Z,Y) \wedge defended\_up\_to(X,Z) \wedge not \ att(Y,X) \\ defended\_up\_to(X,Y) \leftarrow succ(Z,Y) \wedge defended\_up\_to(X,Z) \wedge in(V) \wedge \\ att(V,Y) \wedge att(Y,X) \end{split}$$

The third component of  $P_{EGW}^{grounded}$  simply imposes that all defended arguments should be in:

$$in(X) \leftarrow defended(X)$$

Further, for **preferred** extensions,  $P_{EGW}^{pref}$  is  $P_{EGW}^{adm} \cup P_{EGW}^{<}$  extended with a further component incorporating a maximality check on the in arguments. This is done by guessing a larger extension with more in arguments than the current extension, and checking that this is not admissible, again in a 'guess & check'

fashion [25]. Membership in the guessed larger extension is defined using a new predicate inN (and corresponding new predicate outN). This additional component in  $P_{EGW}^{pref}$  is:

```
\leftarrow not \, spoil
spoil \leftarrow eq
eq \leftarrow sup(Y) \land eq\_up\_to(Y)
eq\_up\_to(Y) \leftarrow inf(Y) \wedge in(Y) \wedge inN(Y)
eq\_up\_to(Y) \leftarrow inf(Y) \land out(Y) \land outN(Y)
eq\_up\_to(Y) \leftarrow succ(Z,Y) \wedge in(Y) \wedge inN(Y) \wedge eq\_up\_to(Z)
eq\_up\_to(Y) \leftarrow succ(Z,Y) \land out(Y) \land outN(Y) \land eq\_up\_to(Z)
spoil \leftarrow inN(X) \wedge inN(Y) \wedge att(X, Y)
spoil \leftarrow inN(X) \land outN(Y) \land att(Y,X) \land undefeated(Y)
undefeated(X) \leftarrow sup(Y) \land undefeated\_up\_to(X, Y)
undefeated\_up\_to(X,Y) \leftarrow inf(Y) \wedge outN(X) \wedge outN(Y)
undefeated\_up\_to(X,Y) \leftarrow inf(Y) \wedge outN(X) \wedge not \ att(Y,X)
undefeated\_up\_to(X,Y) \leftarrow succ(Z,Y) \land undefeated\_up\_to(X,Z) \land outN(Y)
undefeated\_up\_to(X,Y) \leftarrow succ(Z,Y) \land undefeated\_up\_to(X,Z) \land not\ att(Y,X)
inN(X) \leftarrow spoil \wedge arg(X)
outN(X) \leftarrow spoil \land arg(X)
```

Finally, for **semi-stable** extensions, Egly et al define  $P_{EGW}^{semi}$  as a variant of  $P_{EGW}^{pref}$  (see [24] for details).

#### 3.4 Faber and Woltran [27]: Ideal Extensions

Faber and Woltran present an encoding of the computation of ideal extensions into so-called manifold answer set programs [27]. These programs allow various forms of meta-reasoning to be implemented within ASP, including credulous and sceptical reasoning. The manifold answer set program used for computing ideal extensions follows the algorithm of [21], which works as follows.

- Let adm be the set of all the admissible extensions of a given argumentation framework  $\langle Arg, att \rangle$ .
- Let  $X^- = Arg \setminus \bigcup_{S \in adm} S$ . Let  $X^+ = \{ \alpha \in Arg \mid \forall \beta, \gamma \in Arg : (\beta, \alpha), (\alpha, \gamma) \in att \Rightarrow \beta, \gamma \in X^- \} \setminus X^-$ .
- Let  $\langle Arg^*, att^* \rangle$  be the argumentation framework with  $Arg^* = X^+ \cup X^$ and  $att^* = att \cap \{(\alpha, \beta), (\beta, \alpha) \mid \alpha \in X^+, \beta \in X^-\}.$
- Let  $adm^*$  be the set of all admissible extensions of  $\langle Arg^*, att^* \rangle$ .

Then, the ideal extension of  $\langle Arg, att \rangle$  is  $\bigcup_{S \in adm^*} S \cap X^+$ .

The admissible extensions of  $(Arg^*, att^*)$  can be computed using a fixpoint iteration (which can be done in polynomial time since this argumentation framework is bipartite [21]). At the first iteration,  $X_1$  is generated by eliminating all arguments in  $Arg^*$  that are attacked by unattacked arguments. At the second iteration,  $X_2$  is  $X_1$  minus all arguments that are attacked by arguments unattacked by  $X_1$ , and so on, until no more arguments can be eliminated (after at most  $|X^+|$  iterations).

The logic program whose answer sets correspond to ideal extensions is obtained by using the manifold for credulous reasoning of the logic program for admissible extensions given by [23], further extended to identify  $(Arg^*, att^*)$  and to simulate the fixpoint algorithm outlined above. Details of this logic program can be found in [27].

### 3.5 DLV for ASP for Abstract Argumentation

All approaches described above have been implemented using the DLV ASP solver.

For the method of [39] (section 3.1) DLV can be used to perform credulous and sceptical reasoning under preferred extensions as follows. Given the logic program  $P_{NCO}^{pref}$  for an AA framework (Arg, att) and the query  $\alpha$ ? for an argument  $\alpha \in Arg$ , DLV used in -brave mode determines whether  $\alpha$  belongs to a preferred extension of (Arg, att), and in -cautious mode whether  $\alpha$  belongs to all preferred extensions of (Arg, att).

DLV is employed in a system<sup>5</sup> that can perform credulous and sceptical reasoning under the various semantics considered by [53] (section 3.2 above). DLV is also the core of the ASPARTIX system<sup>6</sup> [23,22]. This system supports the computation of admissible, stable, complete, grounded, preferred and ideal extensions, following the work of [23,27] (see section 3.3 above), as well as semi-stable extensions [12] and cf2 extensions [3] (see section 3.6 below) following encodings given in [24].

### 3.6 ASP for Other Forms of Argumentation

ASP has been used as a computational tool for abstract argumentation under other semantics, notably the cf2 extensions semantics [3], as well as for forms of argumentation other than abstract argumentation. In particular:

- Thimm and Kern-Isberner [48] present mappings of the DeLP argumentation framework [30] onto ASP.
- Egly et al [23] define mappings for value-based argumentation [5], a form preference-based abstract argumentation [1] and bipolar argumentation [2].
- Wakaki and Nitta [54] use ASP for computing extensions of a form of abductive argumentation they define.
- Devred et al [15] use ASP to compute extensions of abstract argumentation frameworks extended with constraints in the form of propositional formulas. Their mapping of constrained argumentation onto ASP uses lists and, as

<sup>5</sup> http://www.ailab.se.shibaura-it.ac.jp/compARG.html

<sup>6</sup> http://rull.dbai.tuwien.ac.at:8080/ASPARTIX/

a consequence, only ASP solvers capable of dealing with lists can be used with the outcome of this mapping. These include DLV-complex<sup>7</sup> [10] and ASPerIX<sup>8</sup> [35].

- Gaggl and Woltran [29] and Egly et al [24] propose encodings for abstract argumentation under the cf2 extensions semantics [3]. These are incorporated within the ASPARTIX system (see section 3.5).
- Osorio et al [40] propose an alternative mapping for abstract argumentation under the cf2 extensions semantics and use the DLV system to compute these extensions under the given mapping.

### 4 Some Future Directions

The approaches presented in section 3 employ the DLV system as the underlying ASP solver of choice. The approach of [39] (section 3.1) makes use of the capability of DLV to deal with disjunctive clauses and deploy the brave and cautious modes of DLV. The approach of [23,24] (section 3.3) makes use of the < ordering that is built into DLV. The approach of [53] (section 3.2) uses the brave and cautious modes of DLV. It would be interesting to see whether other ASP solvers, e.g. the clasp and claspD (for disjunctive clauses)<sup>9</sup> solvers, could be beneficially used to support the computation of extensions and query answering in abstract argumentation. It would also be interesting to perform a comparative performance analysis of the methods presented in section 3 to identify the most efficient method to support various kinds of applications.

With the exception of a few works (see section 3.6) ASP has been deployed to support abstract argumentation. However, the majority of applications of argumentation, e.g. medical decision making [28] and legal reasoning [4], require concrete argumentation frameworks, where arguments and attacks are built from knowledge bases of rules and facts and are constructed on demand, that is to say, as determined by the needs of a given query/claim to be argued for or against. In particular, there are a number of approaches to argumentation based on logic programming (e.g. [44,47,42]), extending logic programming (e.g. assumption-based argumentation [9,8,17]), or based upon classical logic (e.g. [7]). It would be useful to see whether these other forms of argumentation could be fruitfully computed using ASP.

Evidently this can always be done in the sense that these concrete forms of argumentation are (usually) also instances of abstract argumentation frameworks: having generated the relevant arguments and attacks, one could compute the extensions of the resulting abstract argumentation framework using any of the methods described in previous sections. What we have in mind however is rather different. What we would really like is a mapping from the rule base R used to construct arguments and attacks to a logic program P used to compute extensions, but one which retains some well defined correspondence between the argument-generating rules in R and (some of) the clauses in P.

<sup>7</sup> http://www.mat.unical.it/dlv-complex

<sup>8</sup> http://www.info.univ-angers.fr/pub/claire/asperix/

<sup>9</sup> http://potassco.sourceforge.net/

As has often been remarked, ASP computations are oriented primarily towards the generation of models (answer sets) rather than to proofs or chains of reasoning as in other forms of logic programming. In several of the existing applications of argumentation, however, it is precisely the explanation/justification of answers to queries, in the form of arguments for and against a particular claim, that matters more than the answers themselves. This is an essential feature, for example, when argumentation is used in a collaborative setting, e.g. as in [46,13], where arguments are constructed and evaluated across agents with possibly different knowledge bases, and explanations serve to inform and share information. In applications concerned with the (internal) resolution of dilemmas, conflicts between defeasible rules of conduct, decisions about vague or uncertain outcomes, it is often the explanations/justifications that are of primary interest. In an argumentation setting, explanations/justifications take the form of a dialectical structure which presents the relevant arguments, identifies the attacks between them, possibly classifying them into different types, and provides some representation of how arguments are defended against attacks. The specific details vary according to the concrete form of argumentation employed and the chosen dialectical semantics.

It would be extremely valuable to investigate to what extent dialectical explanations could be meaningfully extracted from extensions computed by means of ASP. A step in this direction has been made with the ASPARTIX system (see section 3.5) which includes a graphical interface labelling nodes of argumentation graphs to provide a visualisation of abstract argumentation frameworks. In general, however, and especially when the graph is large, only relevant parts of the graph should be presented (as the presentation of full extensions tends to obscure matters).

The survey presented in this paper was motivated in part by an interest in how argumentation frameworks could be extended with priorities (also referred to as 'preferences' in the literature). We are interested in how priorities (relative strengths of rules and arguments) could be used in the resolution of conflicts between defeasible rules of belief, and between defeasible rules of conduct in practical reasoning. There is reason to think that these forms of reasoning, though similar, might nevertheless be different in some important respects. See, for example, the recent discussion in [41] (though that is not presented in argumentation terms). There is some existing work on incorporating forms of priority/preference in (non-abstract) argumentation. See for example [44,34,49,51,50]. It is fair to say that it is still fragmented, however, certainly when compared to the long standing investigations of priorities/preferences in nonmonotonic reasoning. See [14] for a survey and classification of approaches, including the computation of answer sets. As observed in [14], a major difficulty in adding a treatment of priority into a (rule-based) argumentation framework lies in defining a suitable ordering on the strength of arguments based on a priority ordering of the rules from which they are constructed. It may be that it is better to approach the problem by ordering the strengths of attacks instead of the strengths of arguments, or some combination of the two. These questions

remain to be investigated, as well as possible relationships to existing work on priorities/preferences in ASP. There is then the further issue, essential for the kind of applications we have in mind, of finding some way of extracting dialectical explanations from the computed extensions.

### 5 Conclusions

Argumentation and answer set programming are two of the main knowledge representation paradigms that have emerged from logic programming for nonmonotonic reasoning.

We have surveyed a number of existing approaches to using ASP for computing extensions in argumentation. The majority of these approaches focus on abstract argumentation, and rely upon mapping abstract argumentation frameworks onto logic programs whose answer sets correspond to (various kinds of) extensions for abstract argumentation. We have seen that approaches exist for computing the majority of existing notions of extensions (including conflict-free, admissible, stable, preferred, complete, semi-stable, and ideal extensions). All presented approaches have been implemented in DLV.

We have also indicated some possible directions for future research on using ASP for argumentation, including: (i) deploying ASP solvers other than DLV, e.g. claspD, (ii) considering concrete (rather than abstract) argumentation frameworks in support of applications, and (iii) developing methods for explaining answers to queries (claims) in dialectical terms, drawing from relevant parts of answer sets corresponding to extensions where the claims hold true.

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