

We are given three points $A = (x_1, y_1)$, $B = (x_2, y_2)$, and $C = (x_3, y_3)$, which belong to the certain curve: $y = ax^2 + bx + s$, we want to find the secret s , where a , b , and s are unknown constants.

Step 1: Substitute the coordinates of each point into the quadratic equation

$$y_1 = a(x_1^2) + b(x_1) + s$$

$$y_2 = a(x_2^2) + b(x_2) + s$$

$$y_3 = a(x_3^2) + b(x_3) + s$$

Step 2: Eliminate s by subtracting the equations:

Subtract equation (2) from (1):

$$(y_1 - y_2) = a(x_1^2 - x_2^2) + b(x_1 - x_2)$$

Subtract equation (3) from (2):

$$(y_2 - y_3) = a(x_2^2 - x_3^2) + b(x_2 - x_3)$$

Step 3: We now have two linear equations with two unknowns, a and b :

$$(1) (y_1 - y_2) = a(x_1^2 - x_2^2) + b(x_1 - x_2)$$

$$(2) (y_2 - y_3) = a(x_2^2 - x_3^2) + b(x_2 - x_3)$$

Step 4) Solve for a and b :

Rearrange equation (1) to keep a by itself and in terms of b :

$$(y_1 - y_2) = a(x_1^2 - x_2^2) + b(x_1 - x_2)$$

$$a(x_1^2 - x_2^2) = (y_1 - y_2) - b(x_1 - x_2)$$

$$(3) a = [(y_1 - y_2) - b(x_1 - x_2)] / (x_1^2 - x_2^2)$$

Substitute equation (3) into (2):

$$(y_2 - y_3) = \{[(y_1 - y_2) - b(x_1 - x_2)] / (x_1^2 - x_2^2)\} * (x_2^2 - x_3^2) + b(x_2 - x_3)$$

Simplify and solve for b .

Step 5) When b is found, substitute it back into equation (3) to solve for a :

$$a = [(y_1 - y_2) - b(x_1 - x_2)] / (x_1^2 - x_2^2)$$

Step 6) solve for s :

Use the equation $y_1 = a(x_1^2) + b(x_1) + s$ to solve for s :

$$s = y_1 - a(x_1^2) - b(x_1)$$

Substitute the values of a and b into this equation to find s .