

Unravelling the mechanisms for suppression of complete fusion in reactions of weakly bound nuclei



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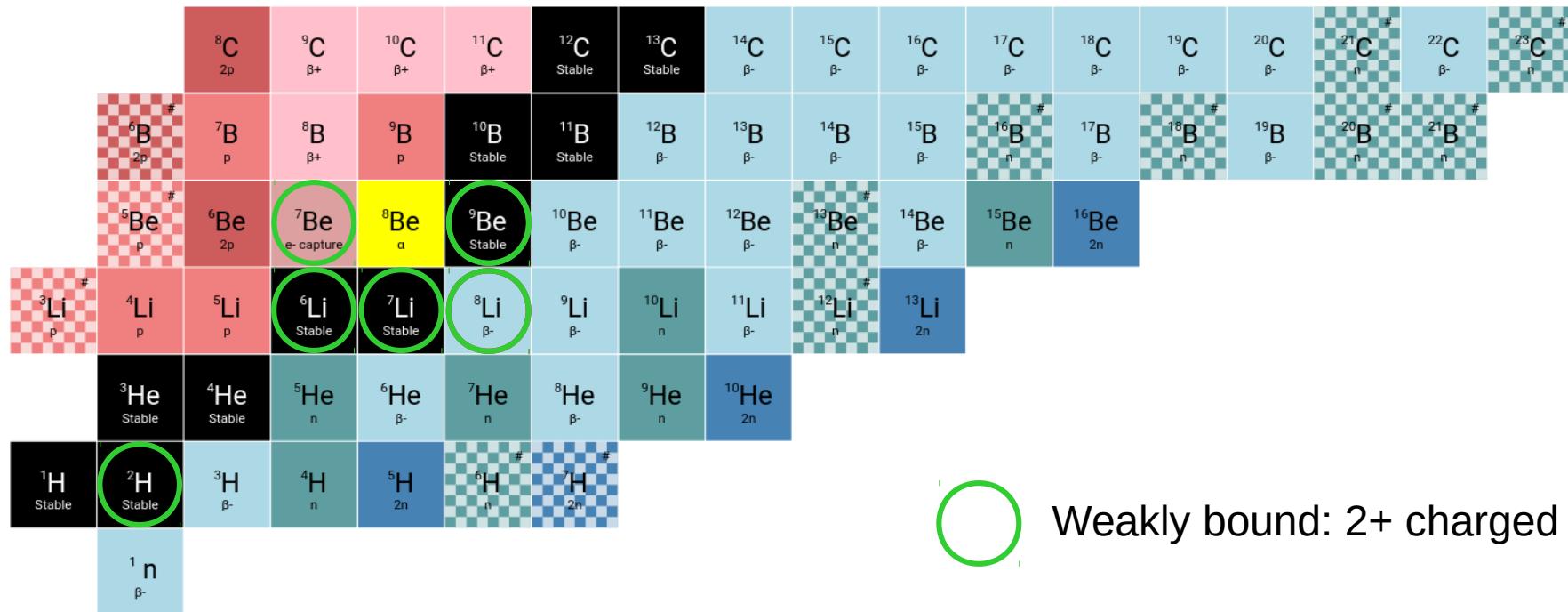
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Australian
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University



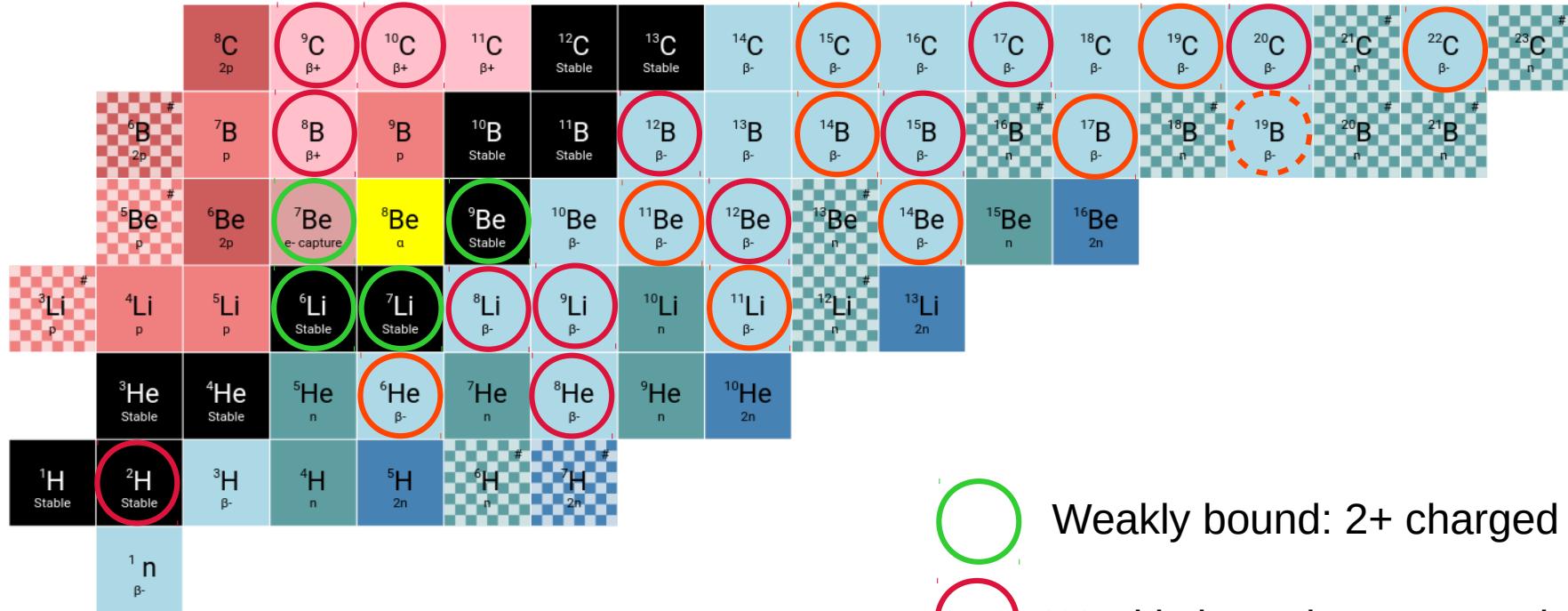
Weakly bound nuclei



Weakly bound: 2+ charged clusters

("weakly" is $\sim < 4$ MeV)

Weakly bound nuclei



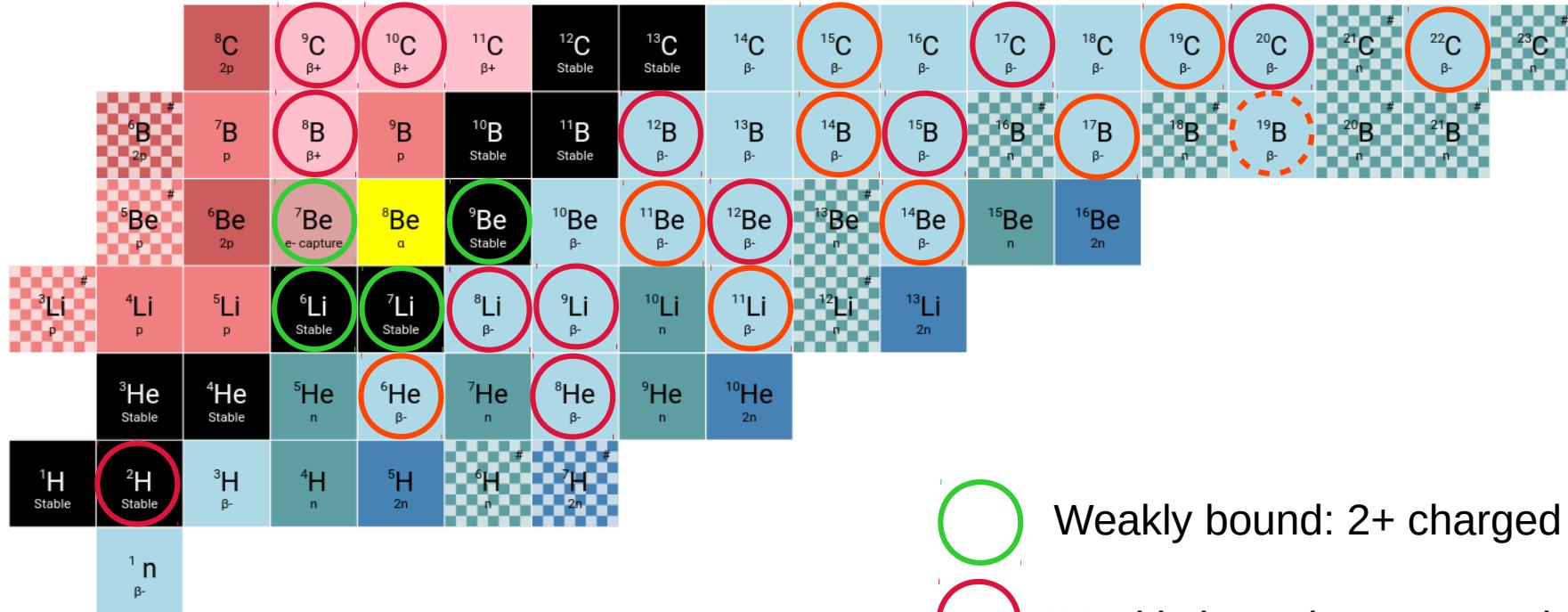
Weakly bound: 2+ charged clusters

Weakly bound: core + nucleon/s

Weakly bound: core + nucleon/s & halo

("weakly" is $\sim < 4 \text{ MeV}$)

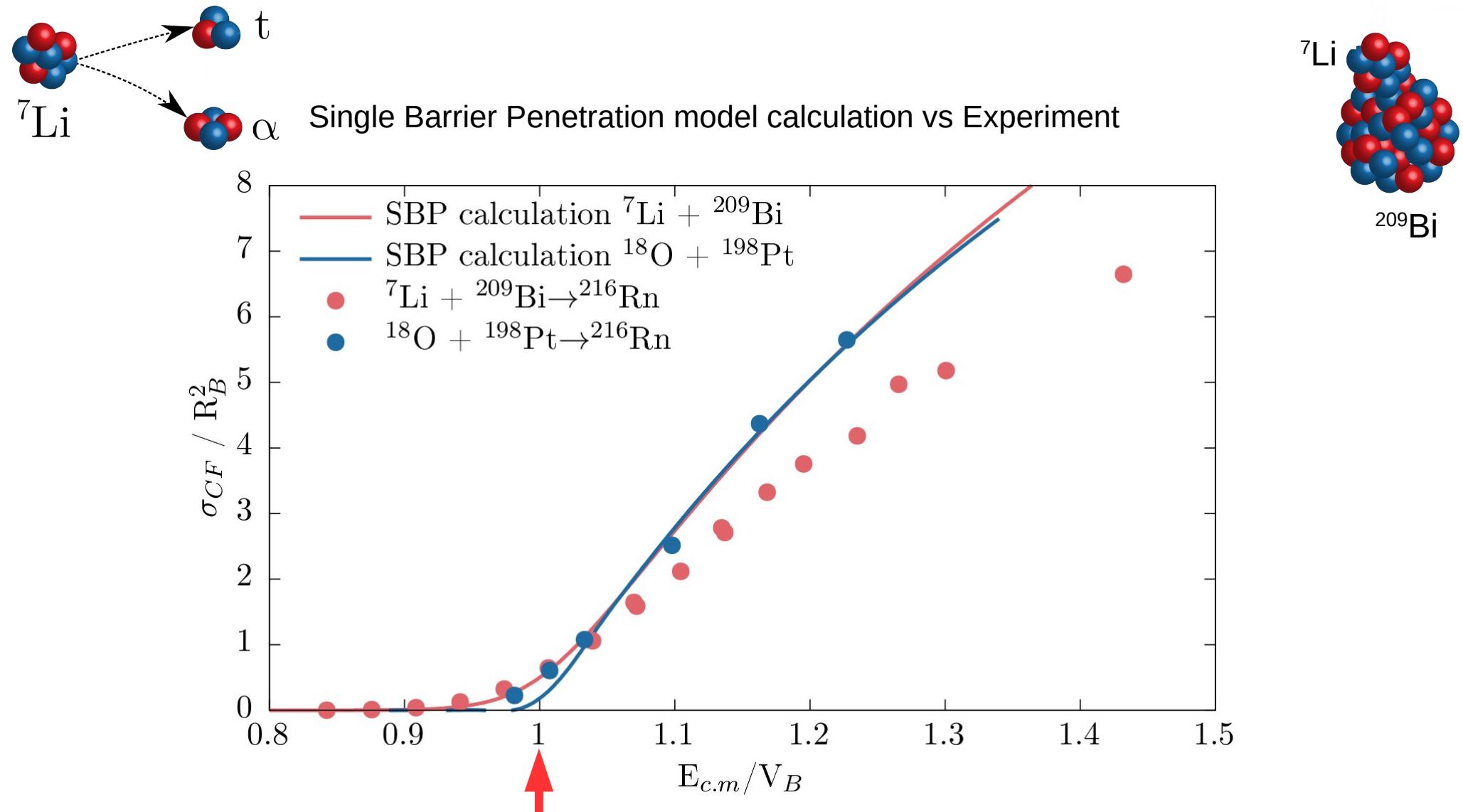
Weakly bound nuclei



What are the reaction dynamics of weakly bound nuclei?

("weakly" is $\sim < 4 \text{ MeV}$)

Above-barrier suppression of complete fusion



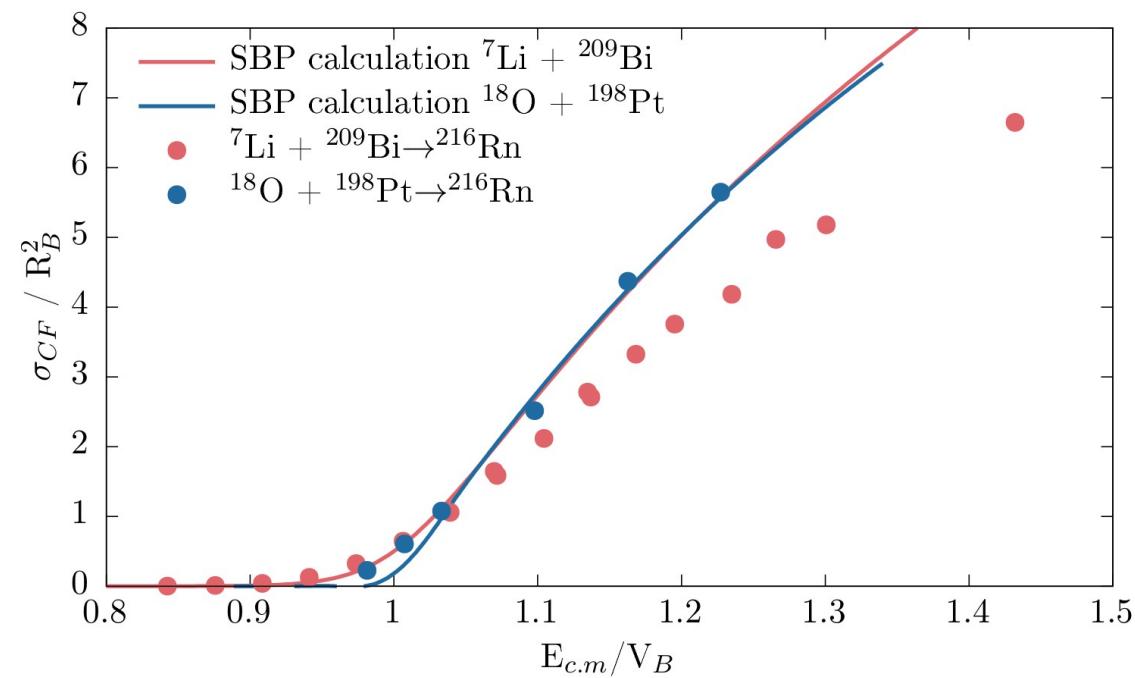
Precision measurements → Unambiguous determination of suppression

Dasgupta, PRC 70, 024606 (2004)

Above-barrier suppression of complete fusion

Well established phenomenon across stable weakly bound nuclei (${}^6, {}^7\text{Li}$, ${}^9\text{Be} \dots$)
e.g:

- Dasgupta, PRL **82** 1395 (1999)
Signorini, EPJA **5** 7 (1999)
Tripathi, PRL **88** 172701 (2002)
Dasgupta, PRC **70** 024606 (2004)
Signorini PTPS **154** 024606 (2004)
Wu, PRC **68** 044605 (2004)
Gomes, PRC **73** 064606 (2006)
Mukherjee, PLB **636** 91 (2006)
Aguilera PRC **80** 044605 (2009)
Rath, PRC **79** 051601 (2009)
Gasques, PRC **79** 034605 (2009)
Palshetkar, PRC **82** 044608 (2010)
Parkar, PRC **82** 054601 (2010)
Fang, PRC **87** 024604 (2013)
Shaikh, PRC **90** 024615 (2014)
Zhang, PRC **90** 024621 (2014) ...

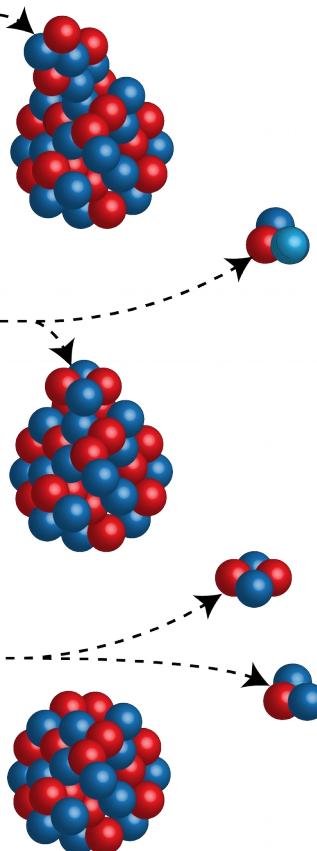


Recent review: Canto, Physics Reports 596 (2015)

Dasgupta, PRC **70**, 024606 (2004)

Hypothesis: breakup

Complete fusion



Breakup + capture

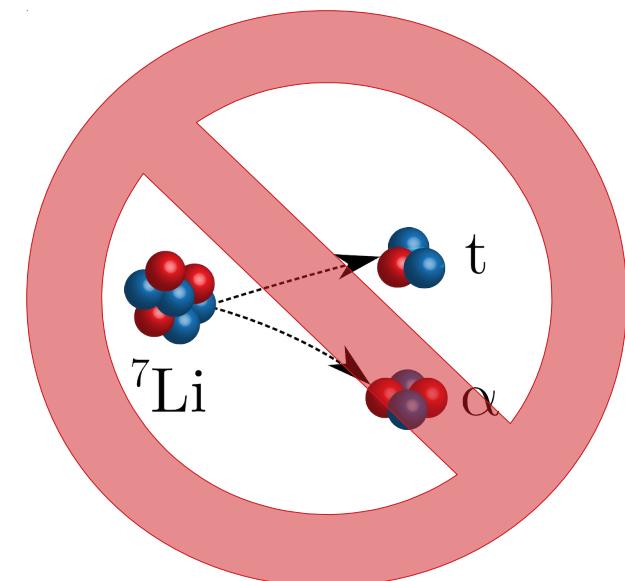
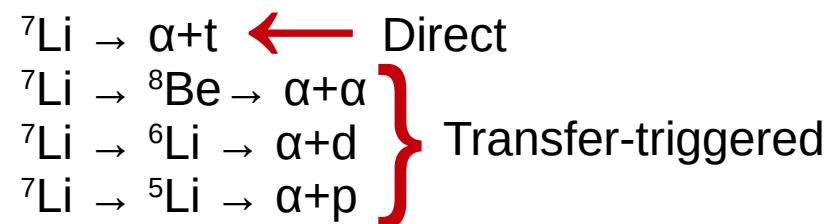
Breakup + no capture

- Breakup into charged clusters (e.g. ${}^7\text{Li} \rightarrow \alpha + t$) **reduces** complete charge capture (**complete fusion, CF**) and **increases** incomplete charge capture (**incomplete fusion, ICF**)
 - CF suppression $\propto \sigma(\text{ICF})$
- On less central trajectories, we observe breakup where no fragment is captured (**no capture breakup**)

Complications: breakup mechanisms

Not just direct breakup: Must consider the substantial amount of transfer to unbound states of neighbouring nuclei.

^6B 2p	^7B p	^8B β^+	^9B p	^{10}B Stable	^{11}B Stable
^5Be p	^6Be 2p	^7Be e ⁻ capture	^8Be α	^9Be Stable	^{10}Be β^-
^3Li p	^4Li p	^5Li p	^6Li Stable	^7Li Stable	^8Li β^-
^3He Stable	^4He Stable	^5He n	^6He β^-	^7He n	^8He β^-
^1H Stable	^2H Stable	^3H β^-	^4H n	^5H 2n	^6H n
^1n β^-					



Shrivastava PLB 633 463 (2006)

Rafiei PRC 81 024601 (2010)

Luong PLB 695 105 (2011)

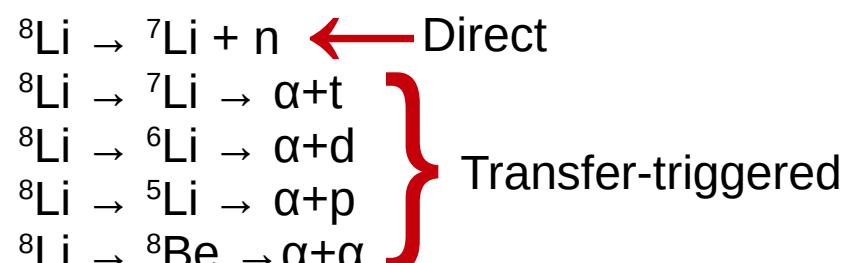
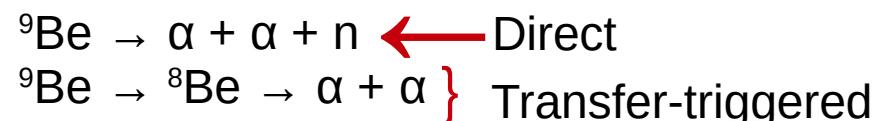
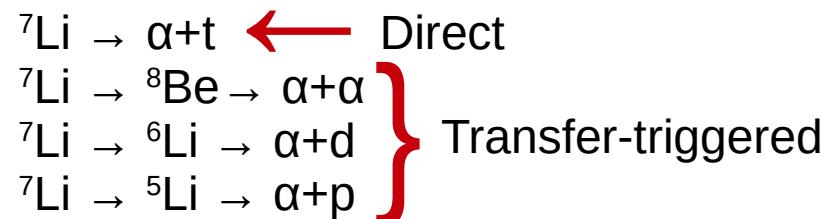
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Cook PRC 97 021601(R) (2018)

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	^1n β^-				^7H 2n



... Challenging theoretically!

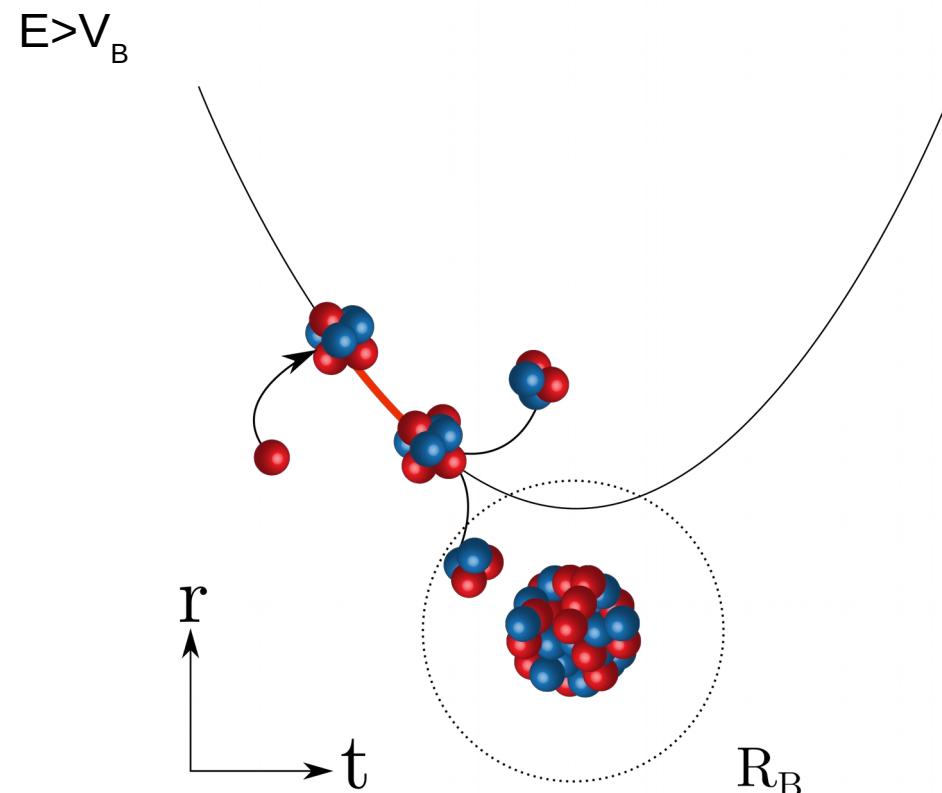
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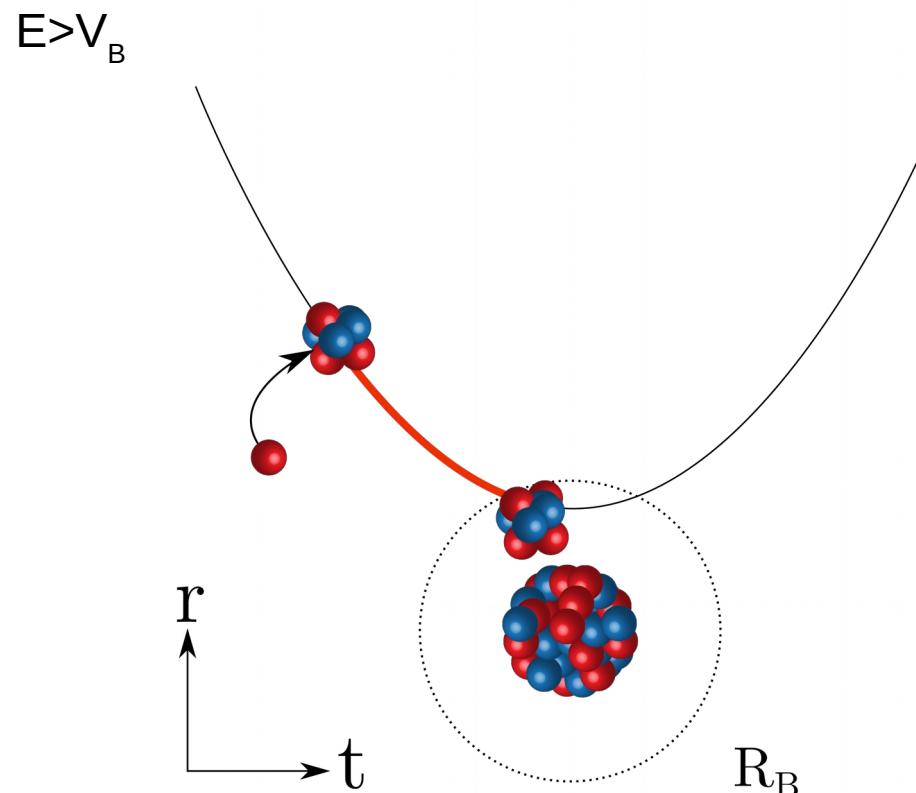
Complications: breakup timescales

Intermediate nucleus after transfer or direct excitation has a lifetime. \rightarrow Nuclei propagate for some time prior to breakup!



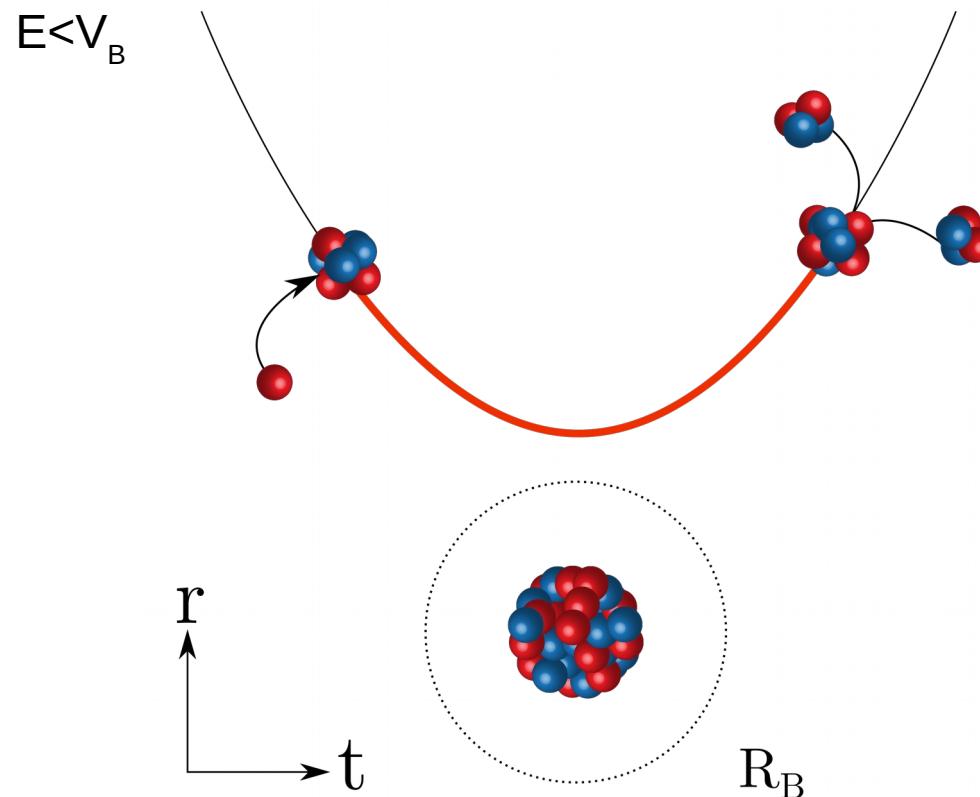
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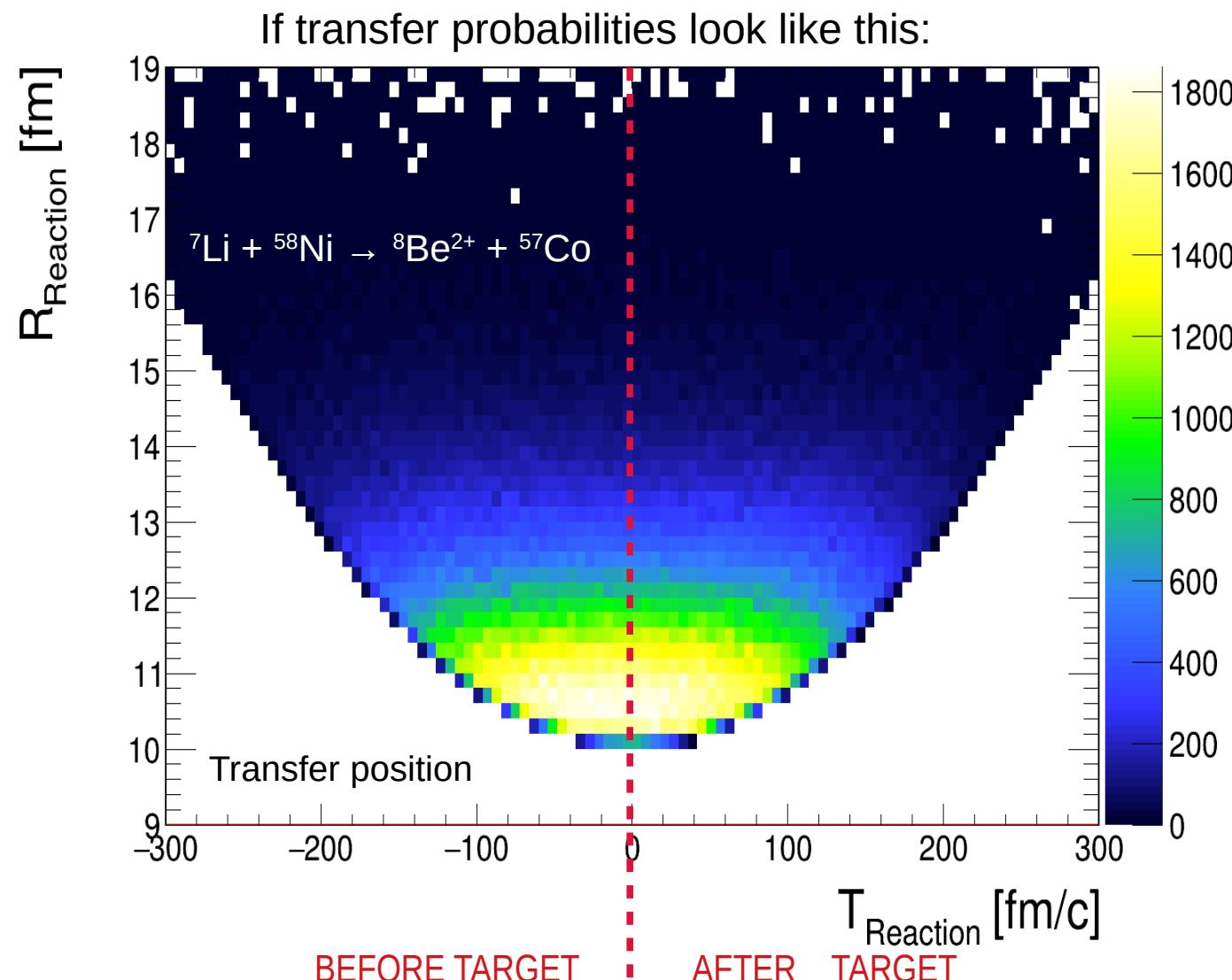
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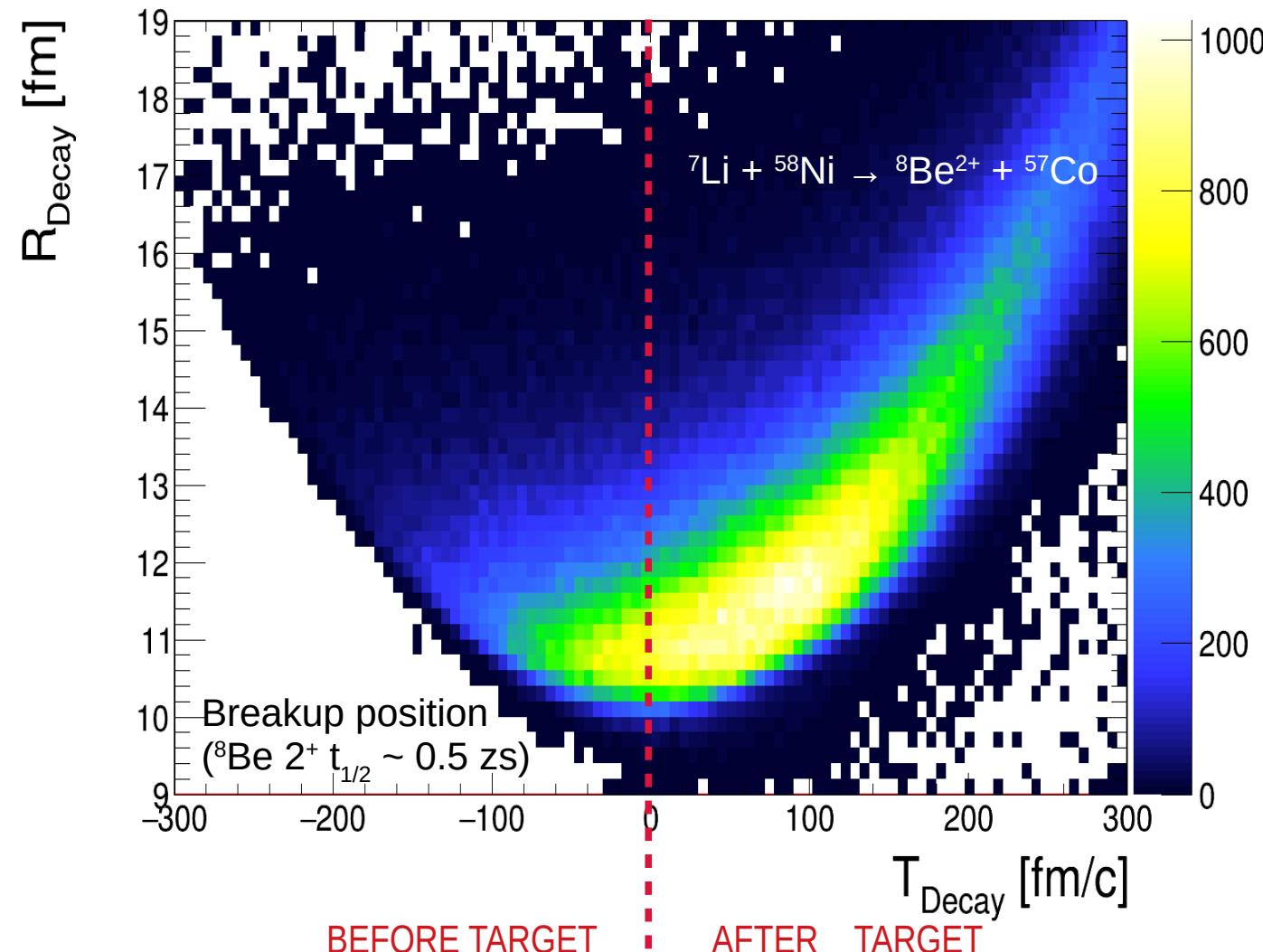


Simpson, Cook et al.
EPJ WoC 163 2017

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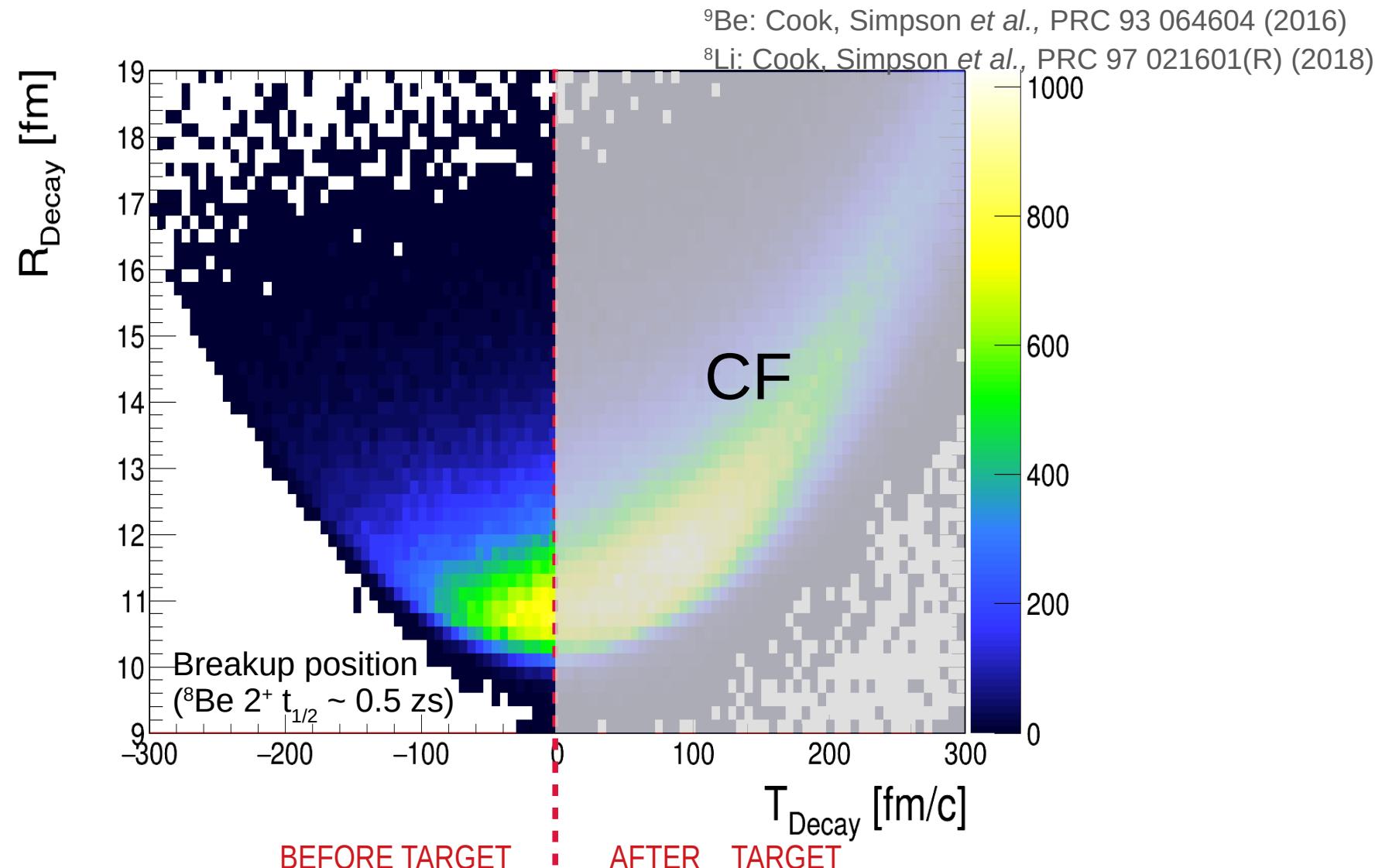
Intermediate nucleus after transfer or direct excitation has a lifetime. → Nuclei propagate for some time prior to breakup!

Breakup probabilities look like this:



Complications: breakup timescales

When lifetimes are included realistically in model calculations, breakup-capture cannot explain observed complete fusion suppression. Lifetimes must be included to explain the observed correlations in energy and angle between the breakup fragments.





- Measure no-capture breakup at below barrier energies.
- Infer breakup-capture above barrier with a model that includes lifetimes
- Compare to incomplete fusion cross-sections.

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$$F_{ICF} = \sigma_{ICF}/(\sigma_{ICF} + \sigma_{CF})$$

Experiments:

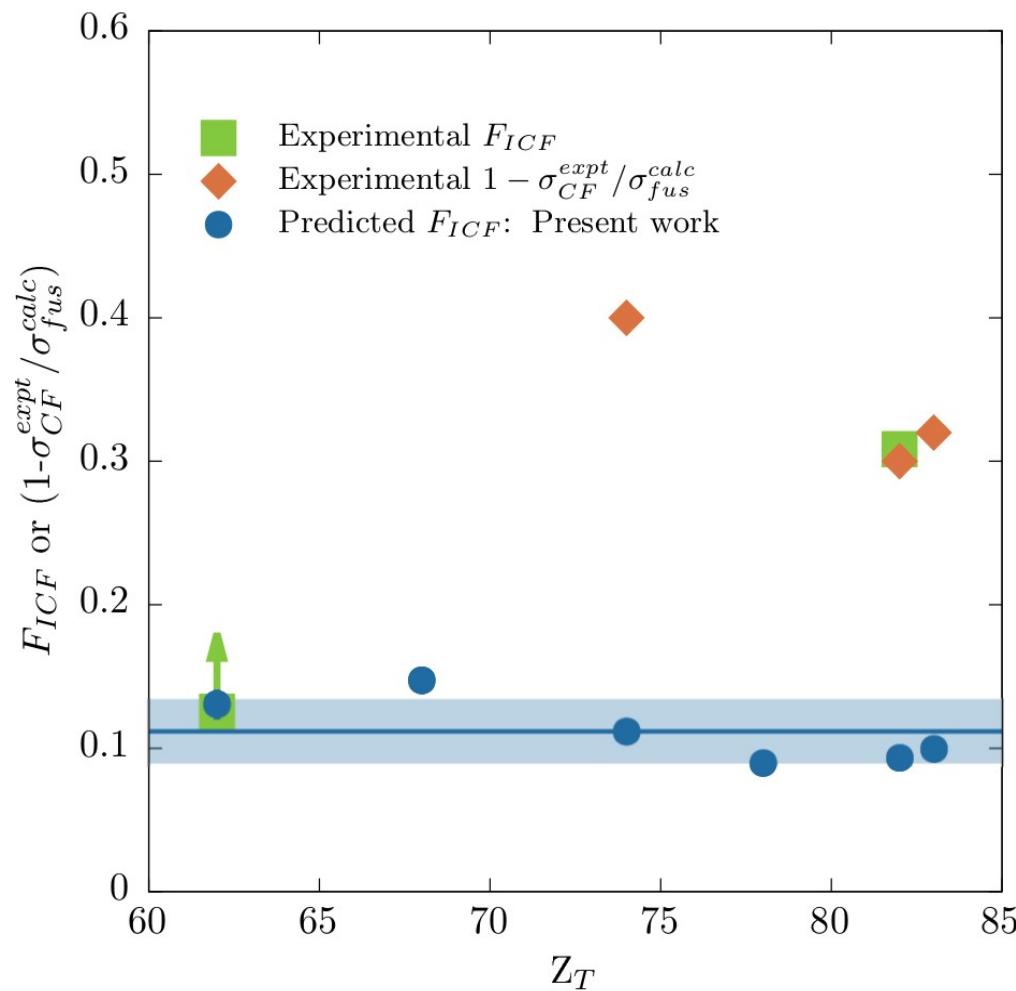
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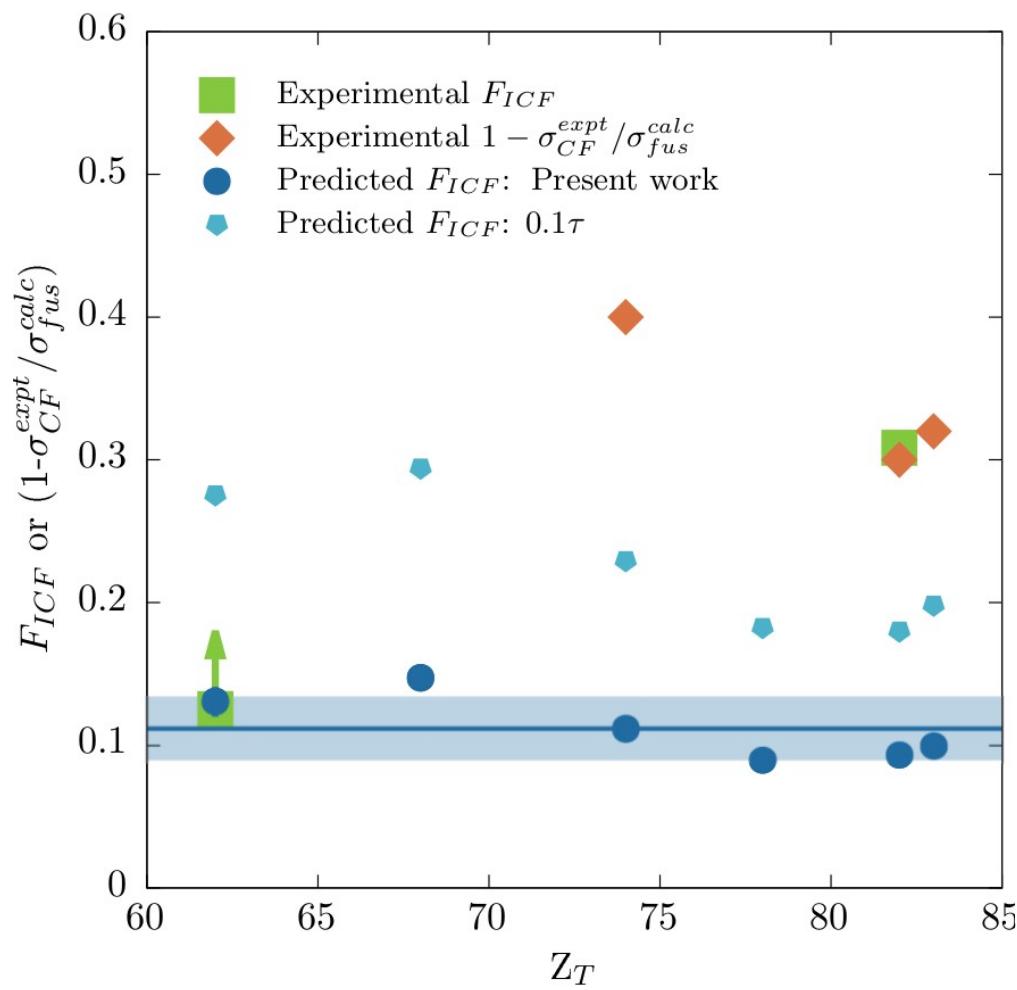
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Cook, Simpson et al., PRC 93 064604 (2016)

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Where do we go from here?

So, how can we understand the mechanism for complete fusion suppression?

Old strategy:

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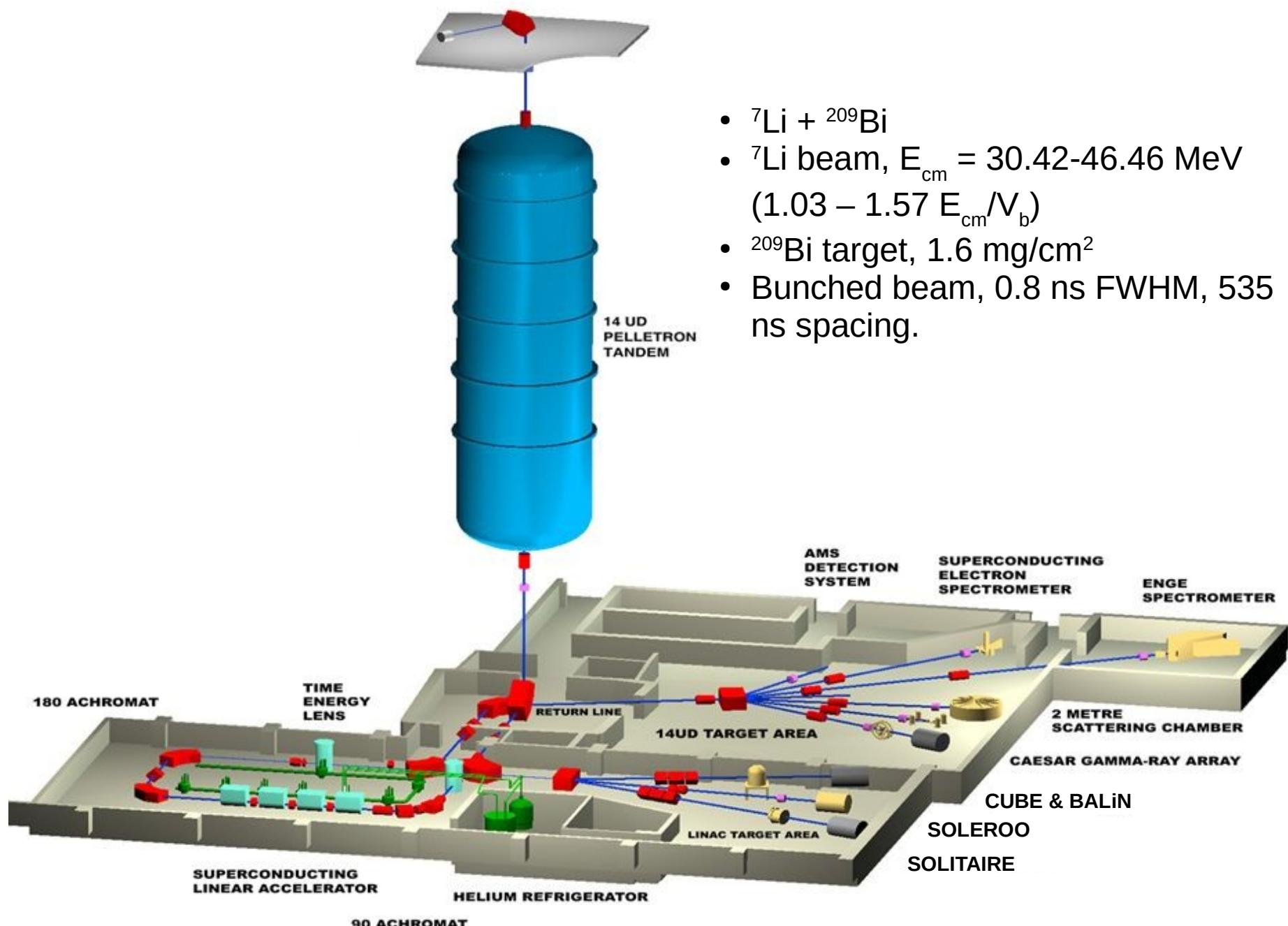
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An innovative experimental approach:

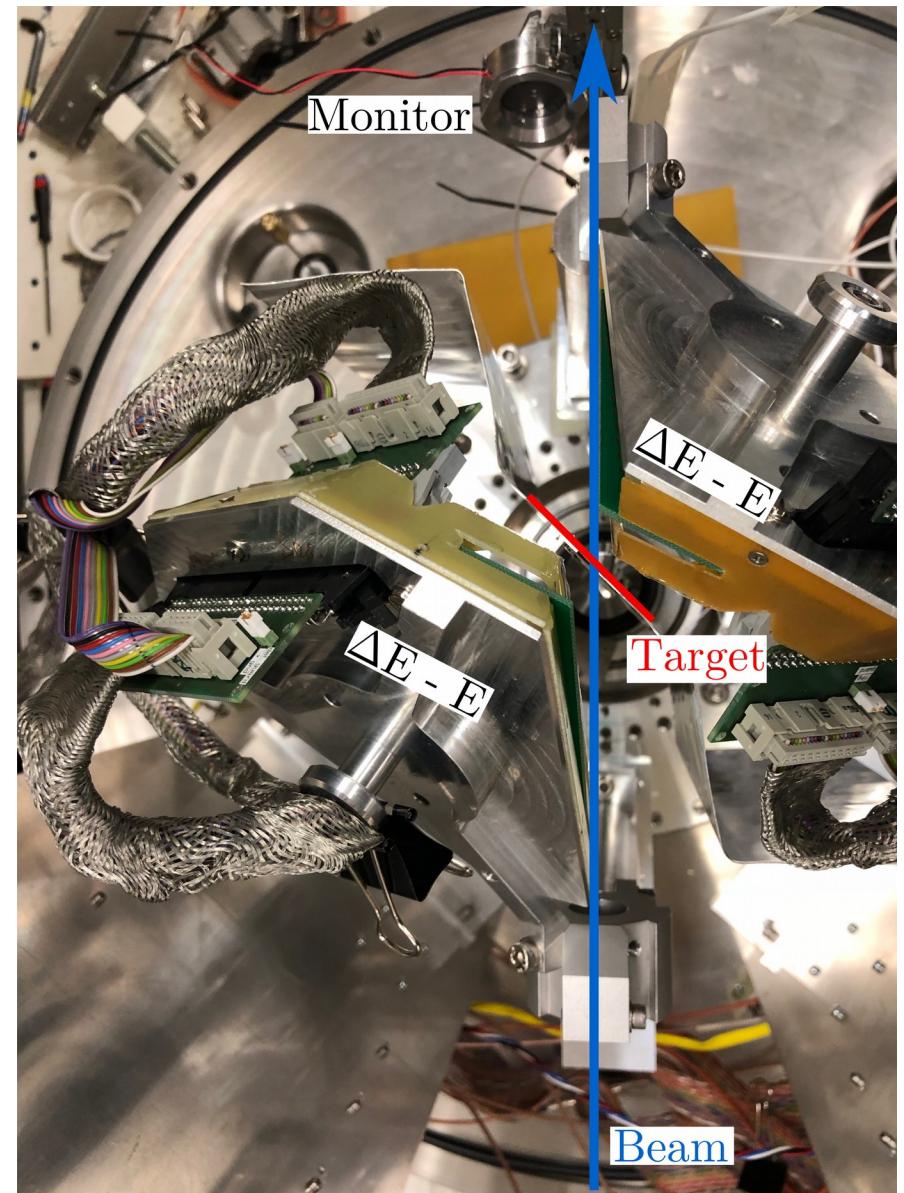
- Measure projectile-like particles left over after incomplete fusion (“unaccompanied particles”), and compare *directly* to no-capture breakup.

The experiment: ANU Heavy Ion Accelerator Facility



The experiment: BALiN

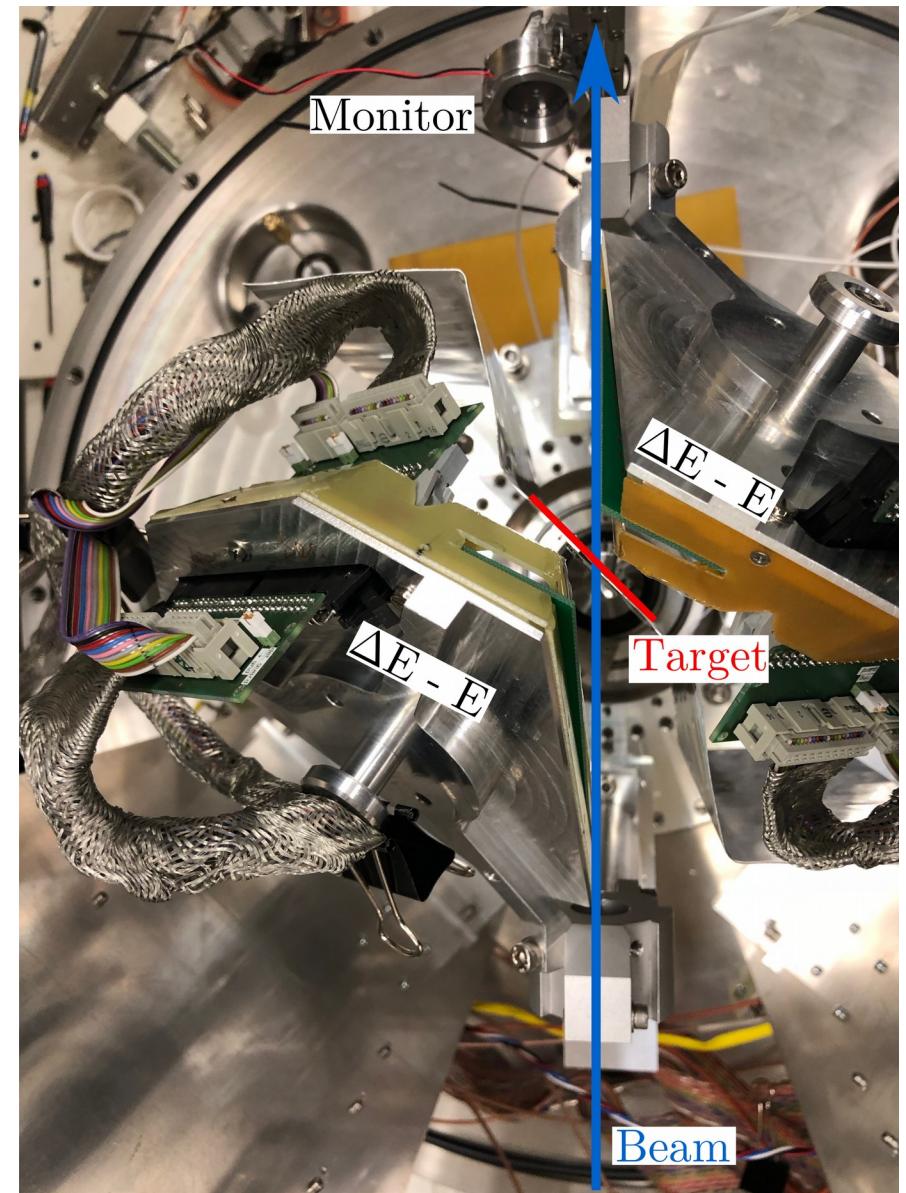
- Two DSSD ΔE -E telescopes
 - Particle ID via ΔE -E & ToF
 - θ ($29^\circ < \theta_{\text{lab}} < 89^\circ$ and $94^\circ < \theta_{\text{lab}} < 157^\circ$)
 - $-107^\circ < \varphi < 176^\circ$ and $185^\circ < \varphi < 254^\circ$



Cook, Simpson et al. PRL 122 102501 (2019)

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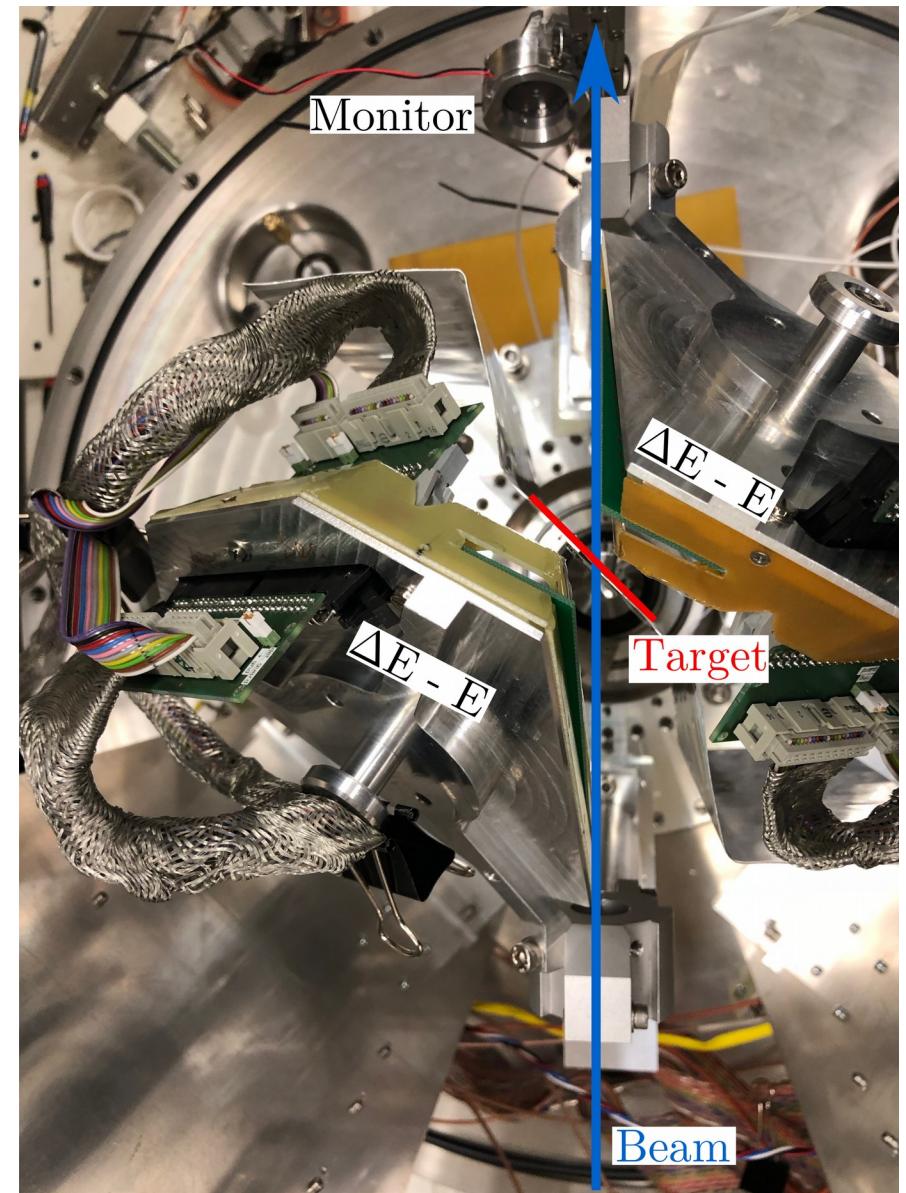
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- Extracted:
 - Elastic scattering
 - Inclusive α
 - Coincidences between beam-associated charged particles (no-capture breakup)
 - Coincidences between decay α and beam-associated α for short-lived ^{212}Po



Cook, Simpson et al. PRL 122 102501 (2019)

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 - Coincidences between decay α and beam-associated α for short-lived ^{212}Po
- Detector efficiency for no-capture breakup determined using classical dynamical model simulation (Cook PRC 2016, Simpson EPJ Web. Conf. 2017)



Cook, Simpson et al. PRL 122 102501 (2019)

No Capture Breakup

At $E_{\text{cm}} = 38.72 \text{ MeV}$, $\sigma_{\text{NCBU}} = 36 \pm 1 \text{ mb}$

Modes:

Direct breakup: $\sigma_{\alpha t} = 9.6 \pm 0.6 \text{ mb}$

1p pickup: $\sigma_{\alpha\alpha} = 7.3 \pm 0.4 \text{ mb}$

1n stripping: $\sigma_{\alpha d} = 10.8 \pm 0.5 \text{ mb}$

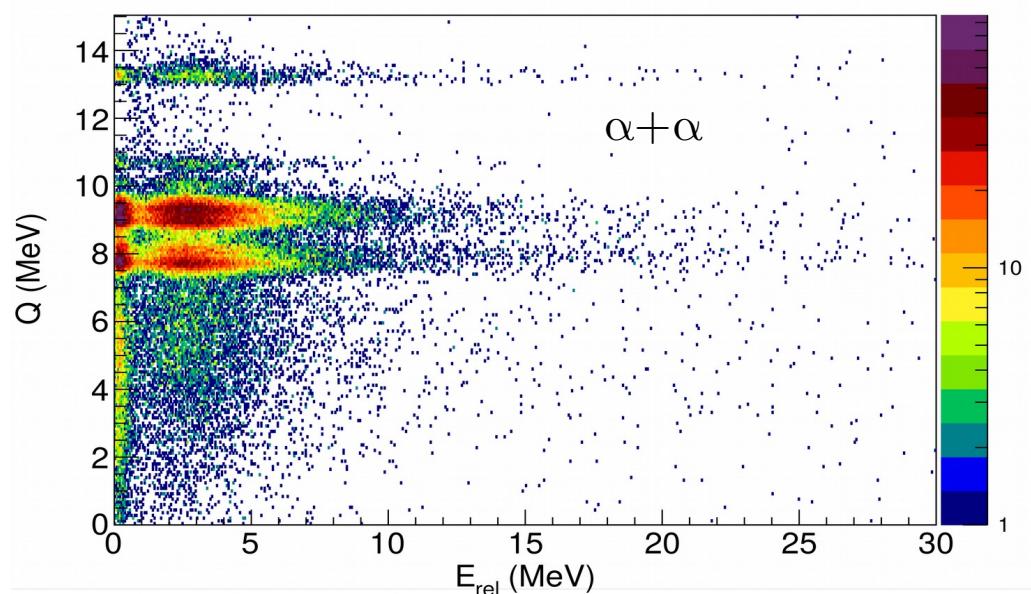
2n stripping: $\sigma_{\alpha p} = 8.6 \pm 0.5 \text{ mb}$

Lifetimes (determined from E_{rel}):

~16 mb of the breakup occurs via long-lived resonant states ($\geq 10^{-20} \text{ s}$)

Of the remaining 20mb, only a small fraction occurs fast enough to suppress CF ($\leq 10^{-21} \text{ s}$)

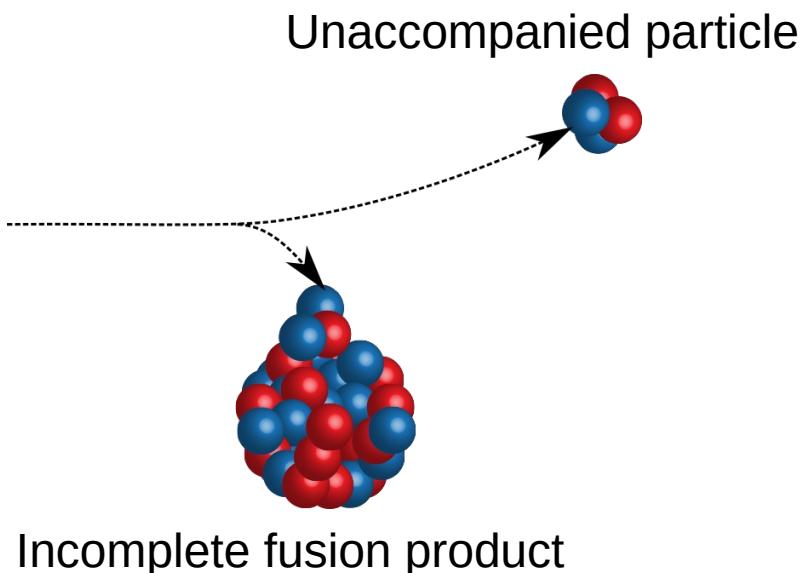
Consistent with previous studies: no-capture breakup shows that breakup-capture cannot significantly contribute to incomplete fusion.



New insight: unaccompanied α



(negligible charged particle evaporation!)



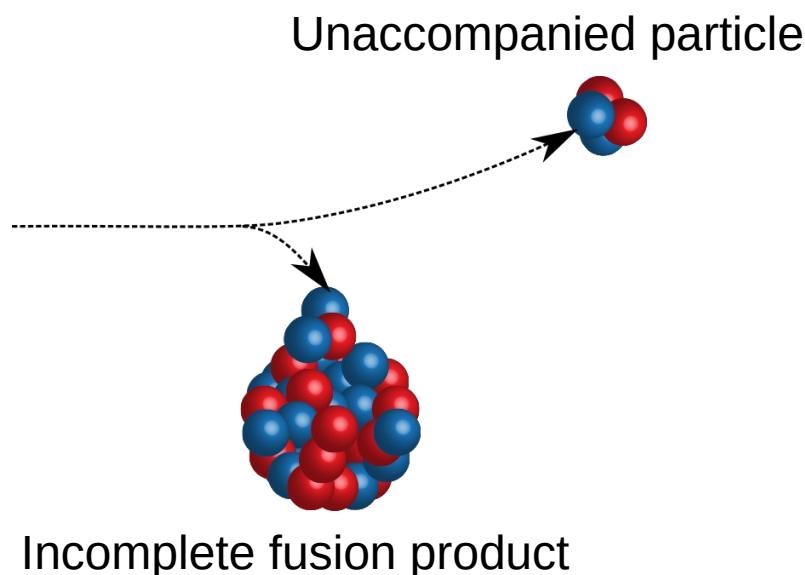
- Polonium incomplete fusion products must be associated with a Z=2 particle that is unaccompanied by any other charged fragment: “unaccompanied α ”

Cook, Carter *et al.* PRC 97 021601(R) (2018)
Cook, Simpson *et al.* PRL 122 102501 (2019)

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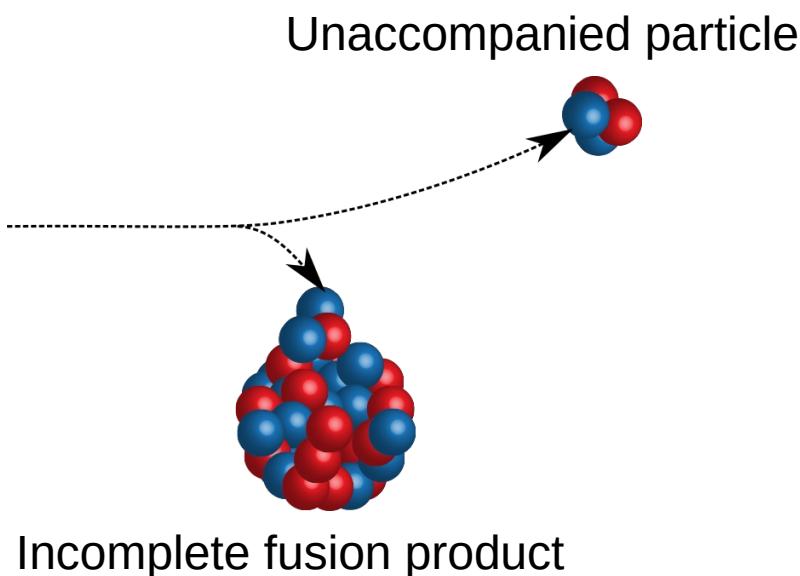
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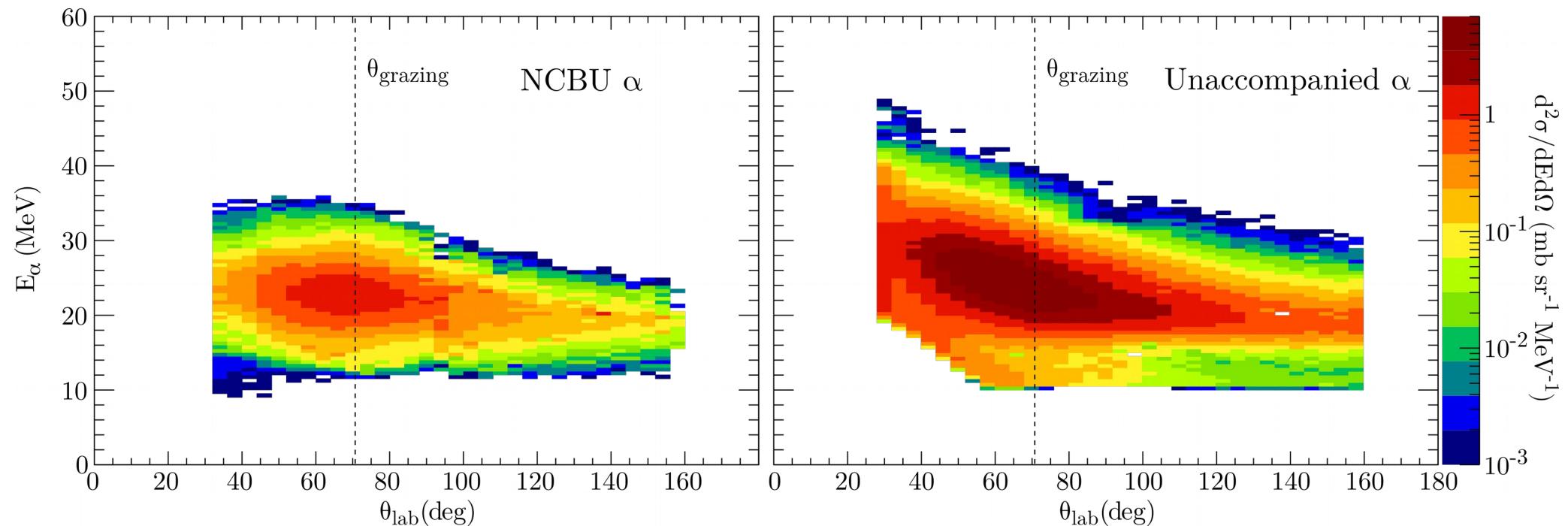
- Polonium incomplete fusion products must be associated with a Z=2 particle that is unaccompanied by any other charged fragment: “unaccompanied α ”
- The same reaction mechanism that produces incomplete fusion products (and CF supp) produces unaccompanied particles!
- Experimentally:
$$\sigma(\text{Unaccompanied } \alpha) = \sigma(\text{Inclusive } \alpha) - \sigma(\text{NCBU } \alpha)$$

Easy-ish

Hard!

Cook, Carter *et al.* PRC 97 021601(R) (2018)
Cook, Simpson *et al.* PRL 122 102501 (2019)

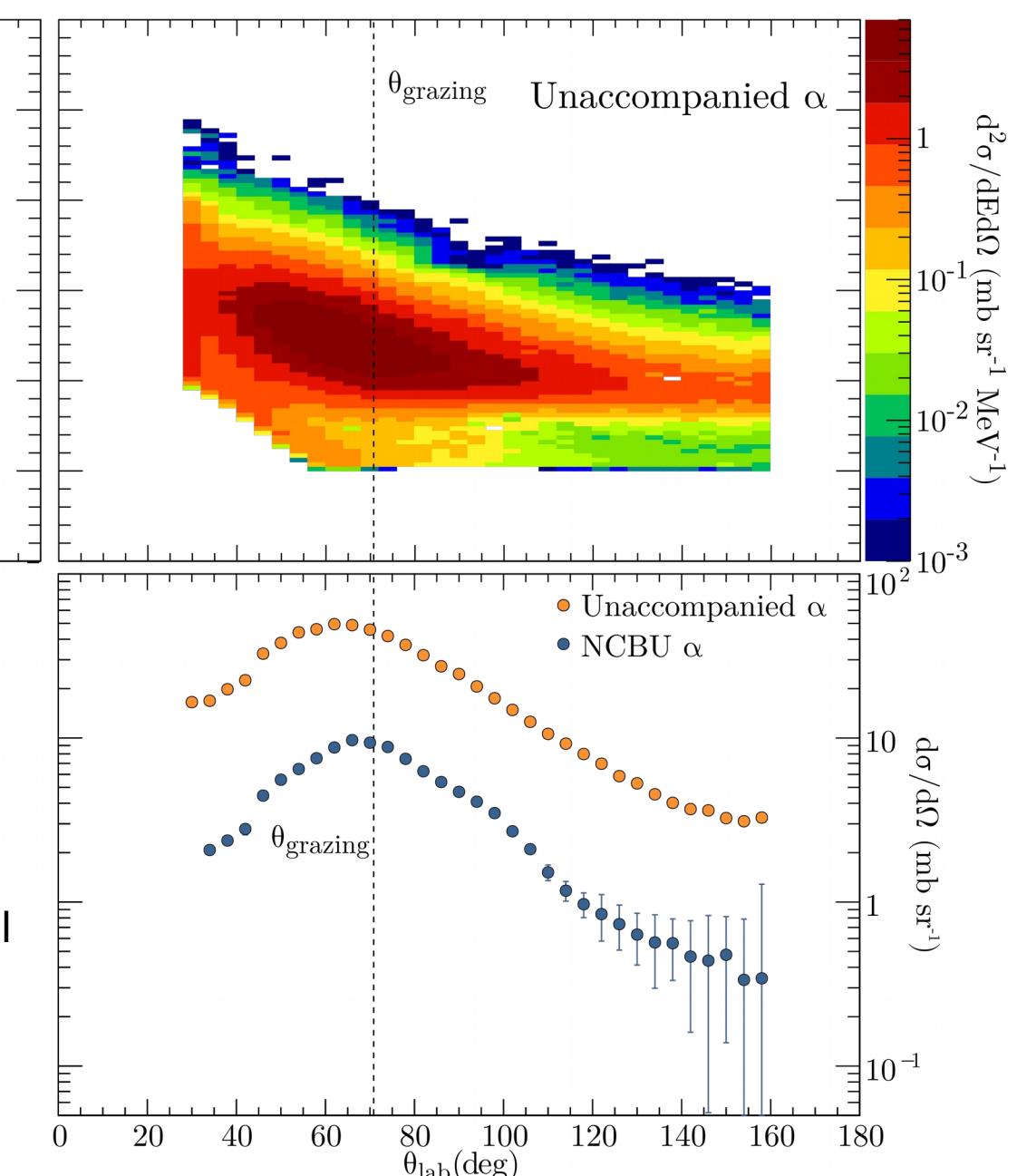
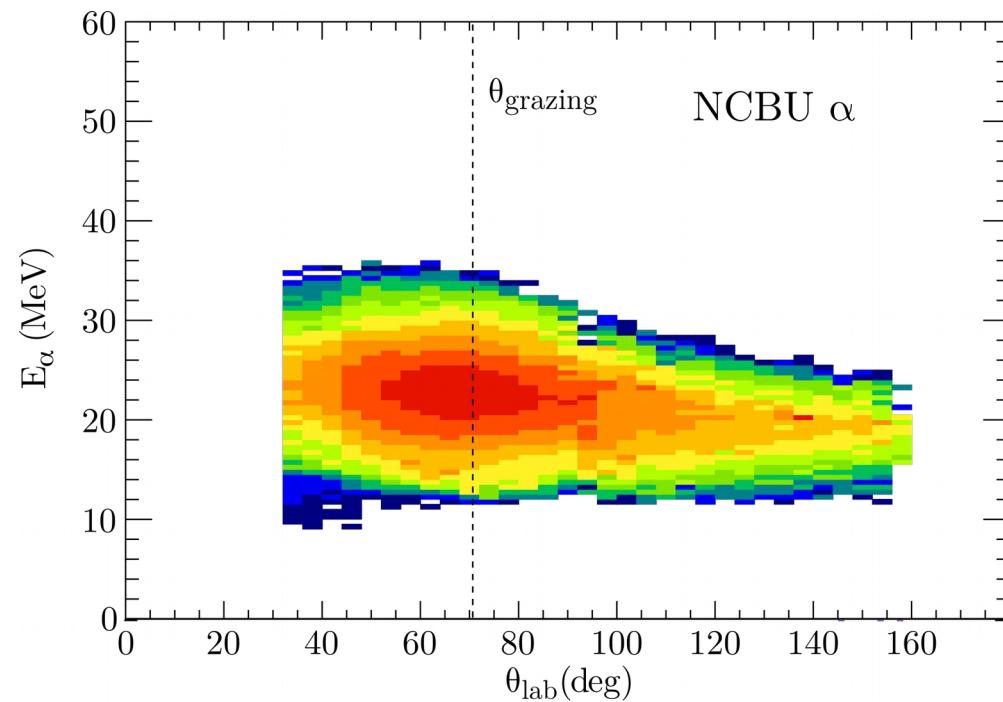
Unaccompanied α vs BU



The unaccompanied α particles:

- Extend to much higher energies
- Exhibit a very different correlation in E_α and θ
- Have a much higher cross section at all angles
- Peak at a more forward angle

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Classical dynamical model calculations

Can the unaccompanied α and the no-capture breakup be explained by the same reaction mechanism?

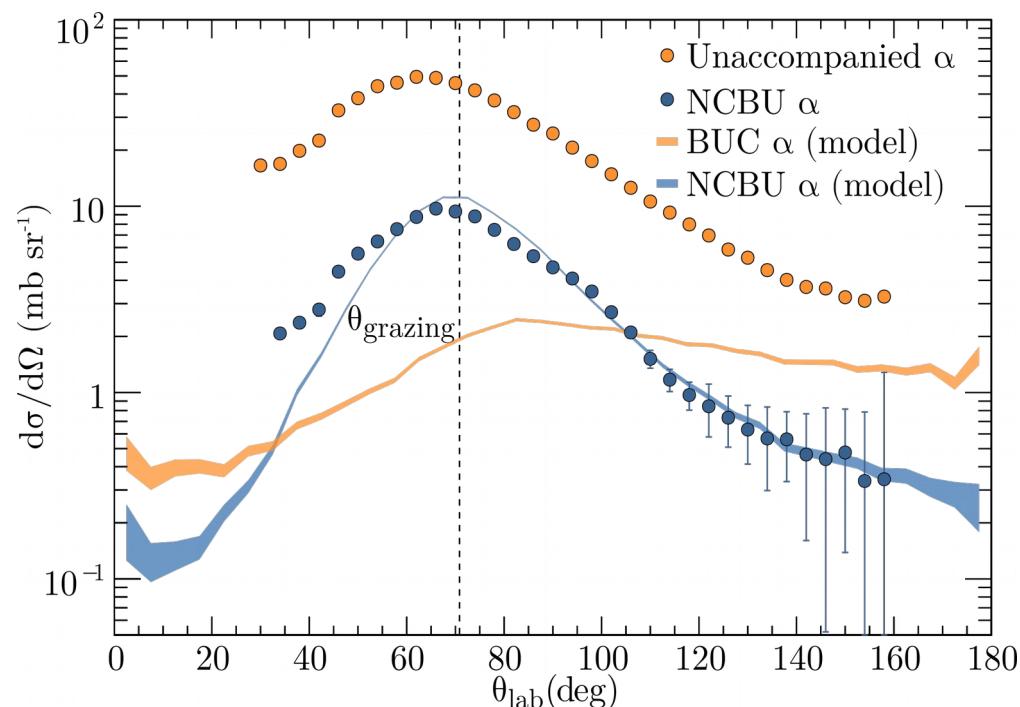
- Classical dynamical simulation of breakup
- Constrained to individual no-capture breakup cross-sections & relative energy distributions

Model information:
Simpson, Cook *et al* EPJ WoC 163 2017

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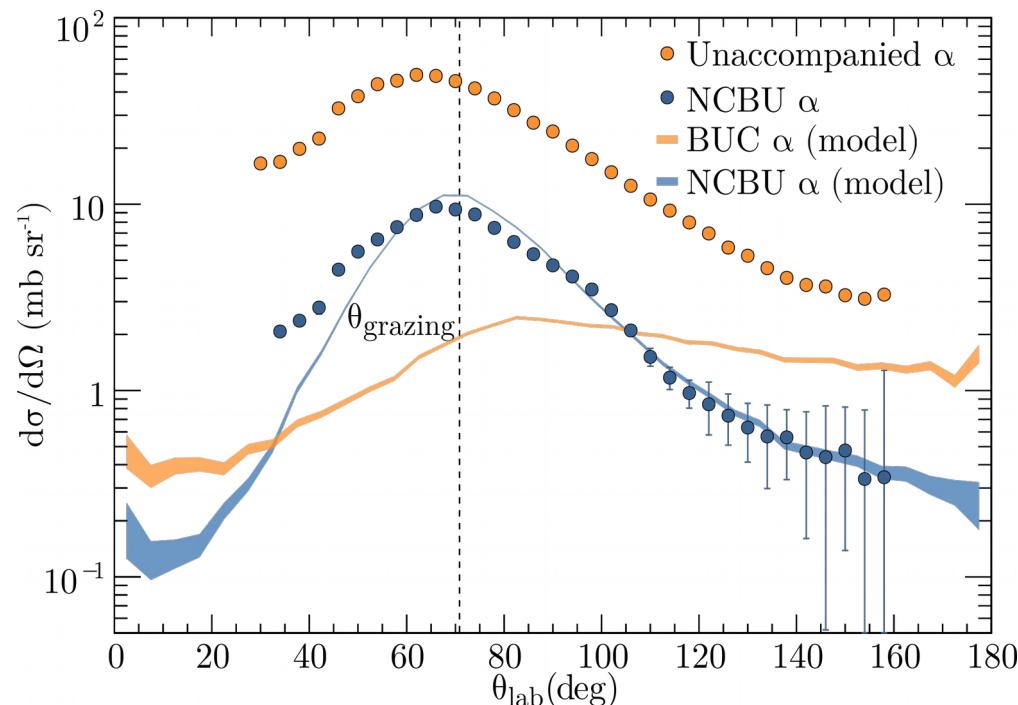


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- Breakup-capture peaks backward of no-capture breakup.
- Breakup-capture does not explain unaccompanied α yields.

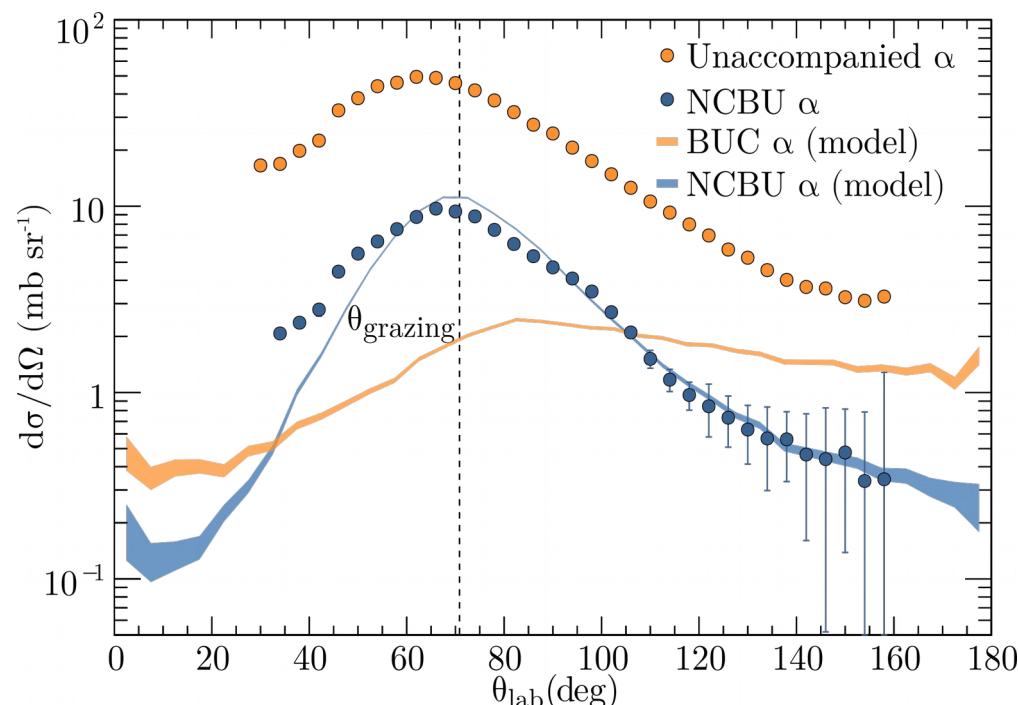


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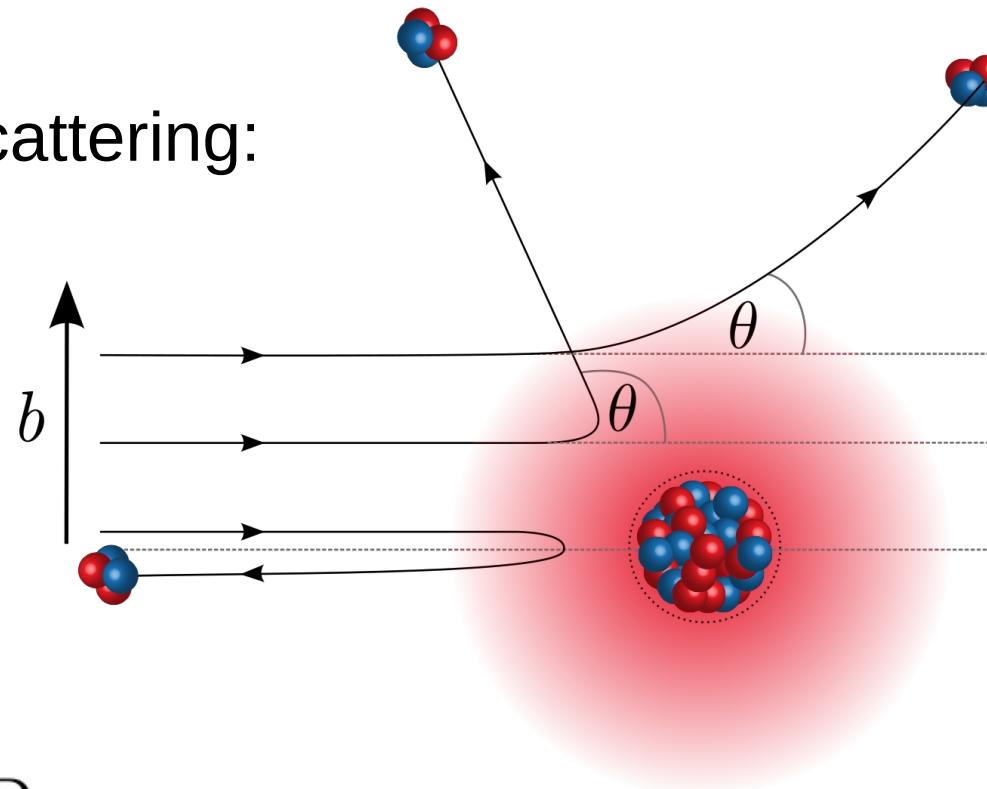


But maybe we don't need a model...

Model information:
Simpson, Cook et al EPJ WoC 163 2017

Can the unaccompanied α be explained by BU?

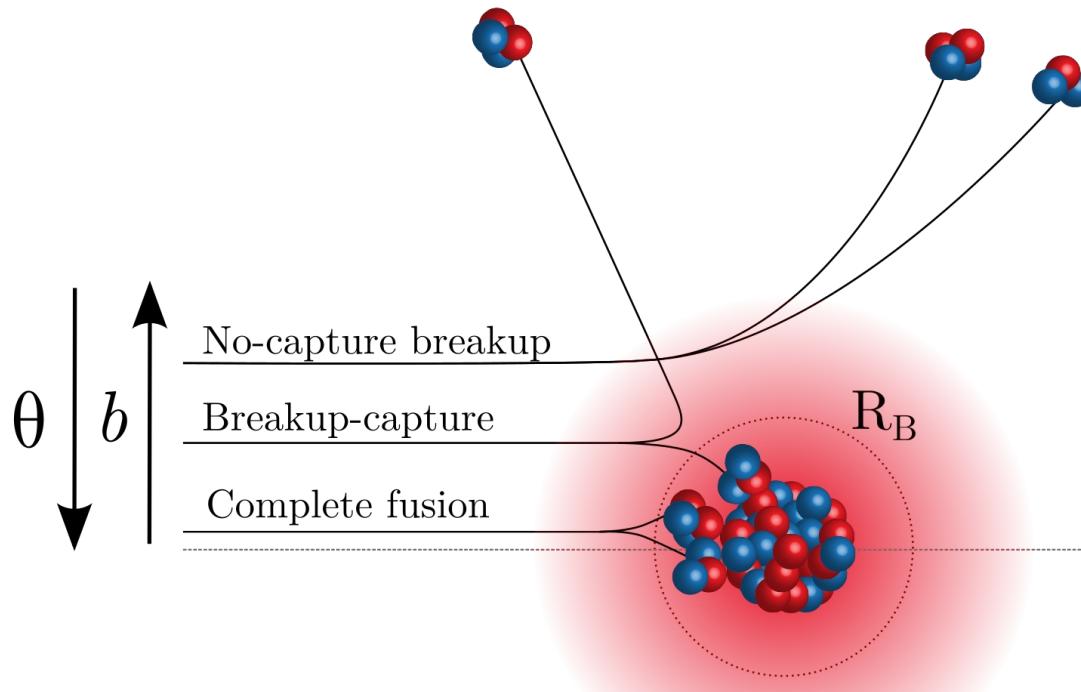
Rutherford scattering:



$$\tan \frac{\theta}{2} = \frac{D}{2b}$$
$$D = \frac{Z_1 Z_2 e^2}{4\pi \epsilon_0 E}$$

$b \uparrow \quad \theta \downarrow$
More central trajectories \rightarrow scattering to more backward angles

Can the unaccompanied α be explained by BU?



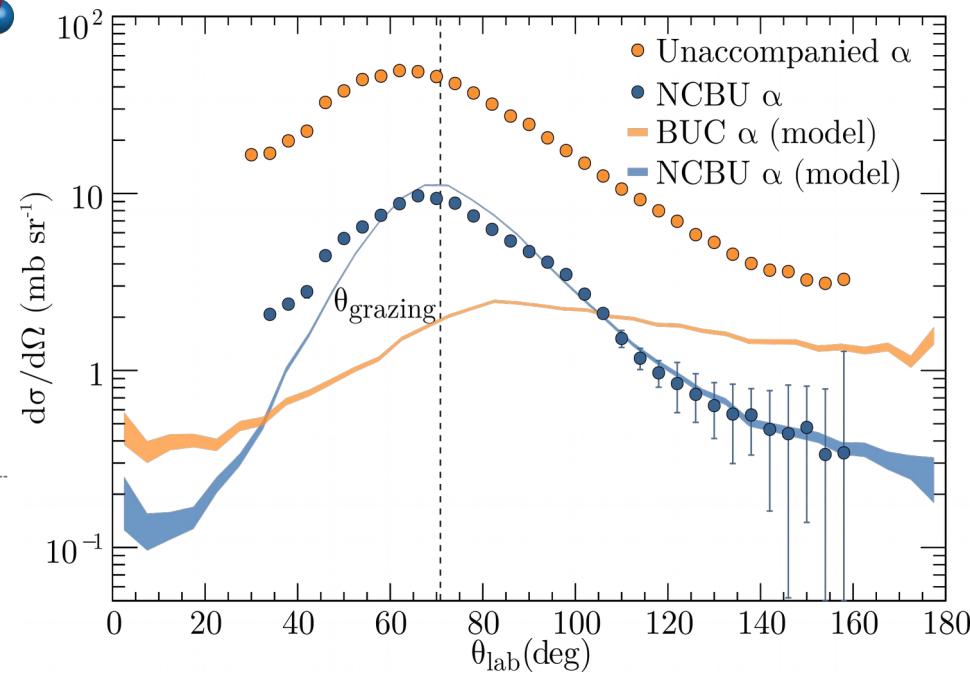
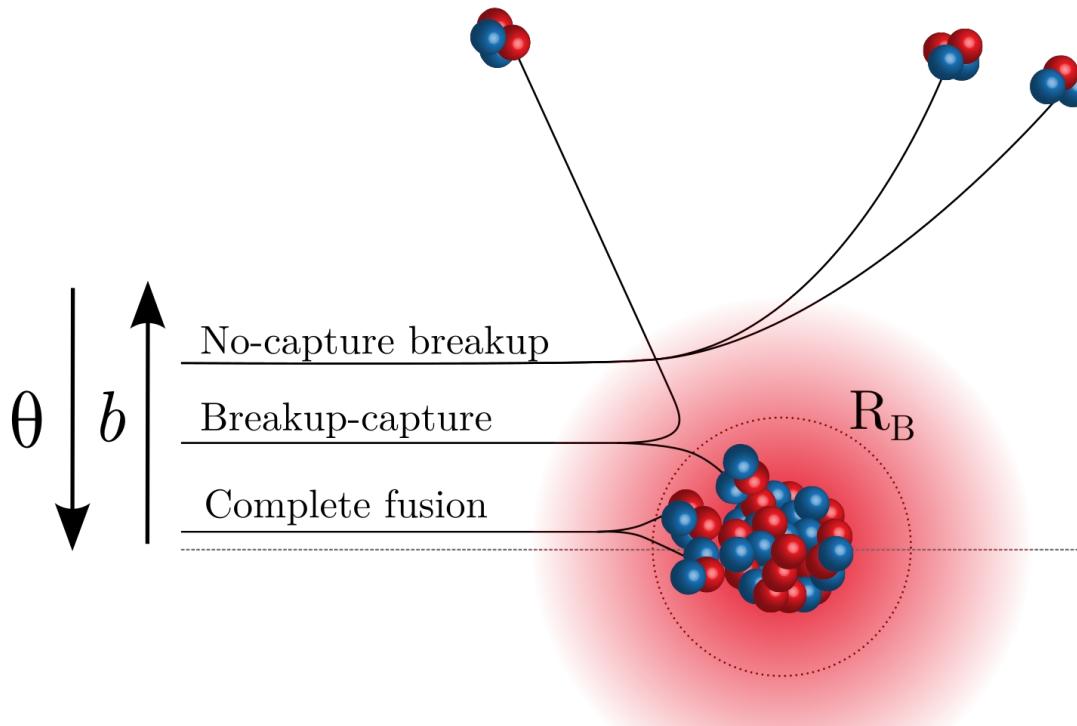
Breakup followed by capture of one fragment (breakup-capture) leading to incomplete fusion products will occur on more central trajectories than no-capture breakup:

$$b(\text{breakup-capture}) < b(\text{no-capture breakup})$$



$$\theta(\text{breakup-capture}) > \theta(\text{no-capture breakup})$$

Can the unaccompanied α be explained by BU?



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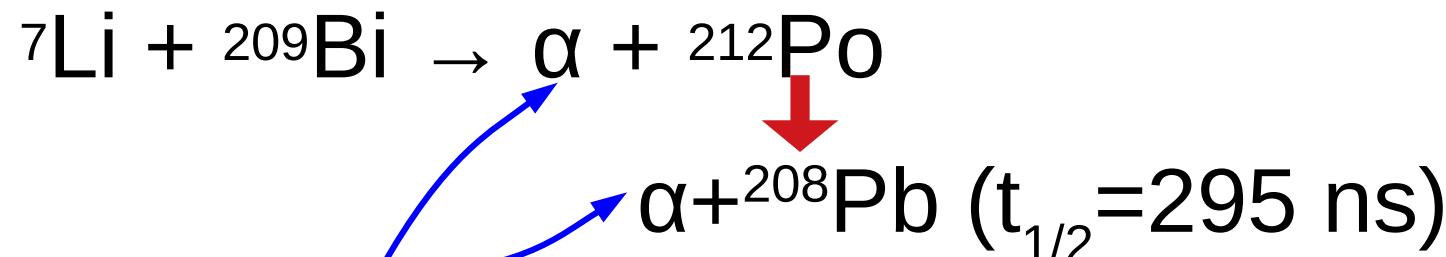
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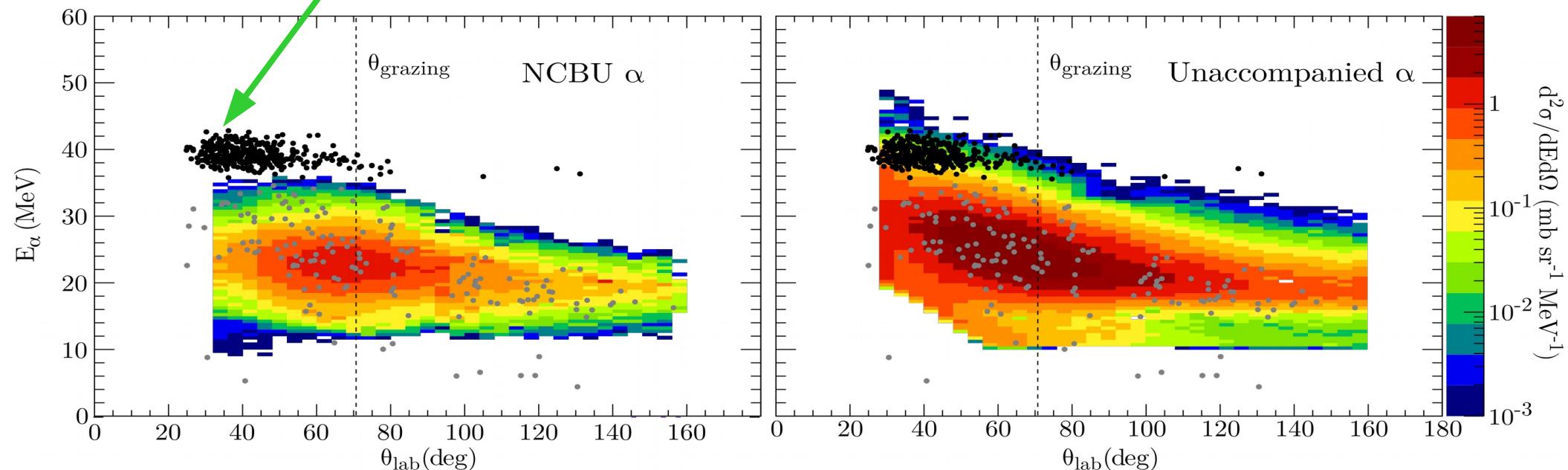
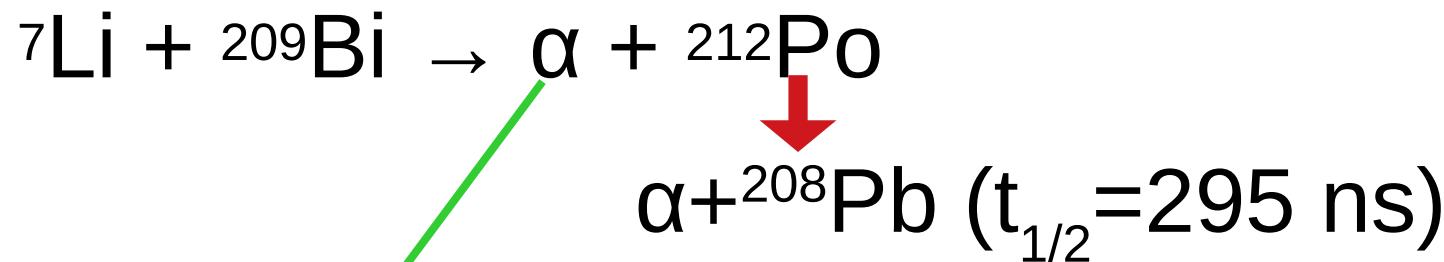
... But the unaccompanied α peak *forward* of the no-capture breakup.
So, what is the mechanism? Cluster transfer is the only mechanism left!

Clues: Coincidences with decay alphas



Tag the prompt α with the decay α

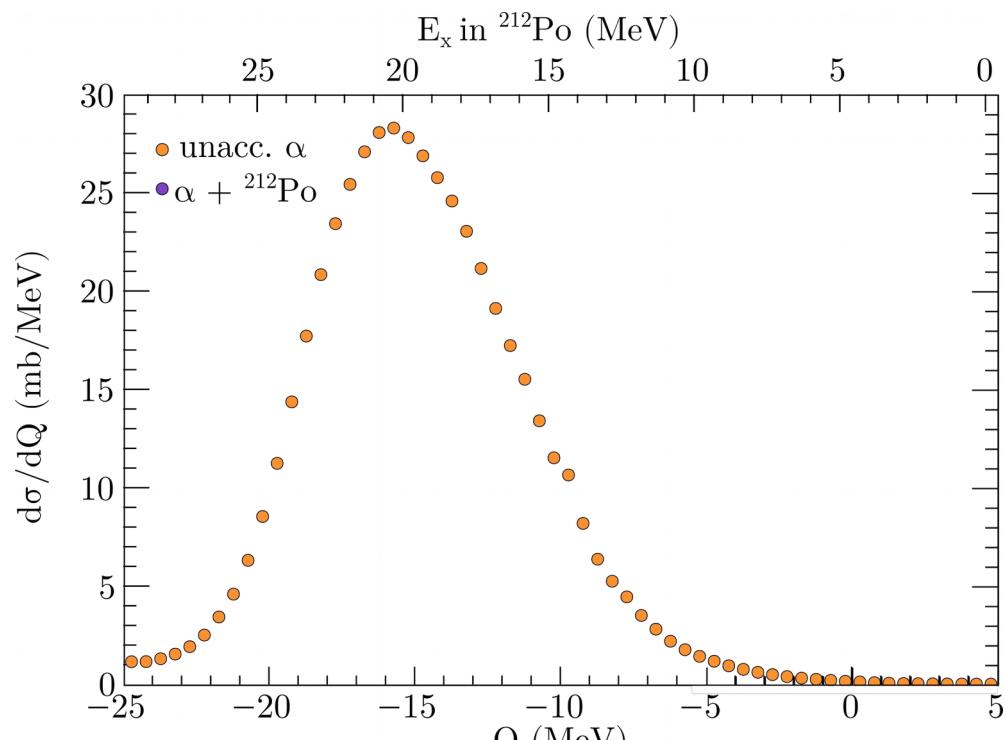
Clues: Coincidences with decay alphas



These α fall totally outside range of NCBU α and are in the high energy, forward angle tail of unaccompanied α

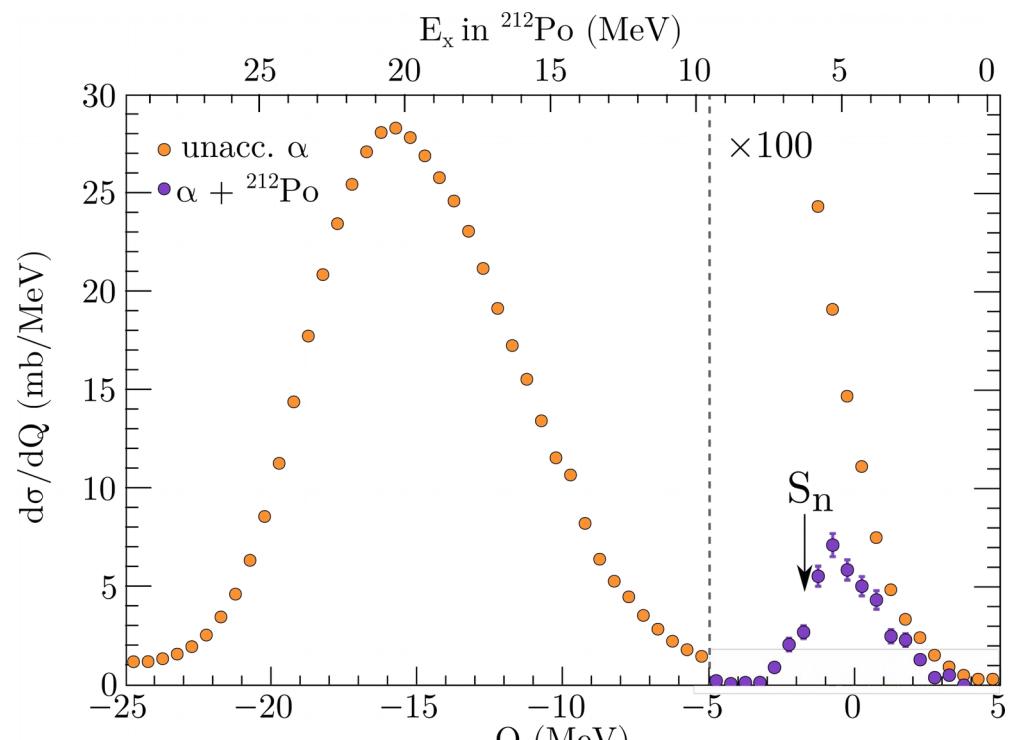
Cook, Simpson et al. PRL 122 102501 (2019)

Evidence for cluster transfer



Q-value spectrum reconstructed from $d\sigma/dE\theta$

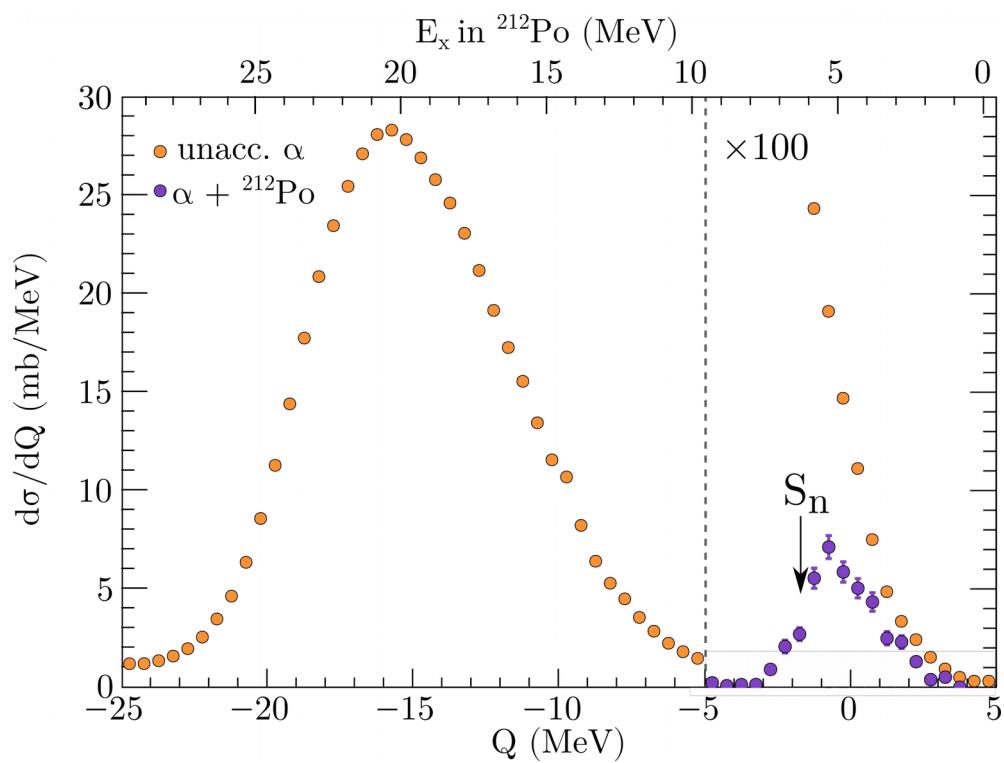
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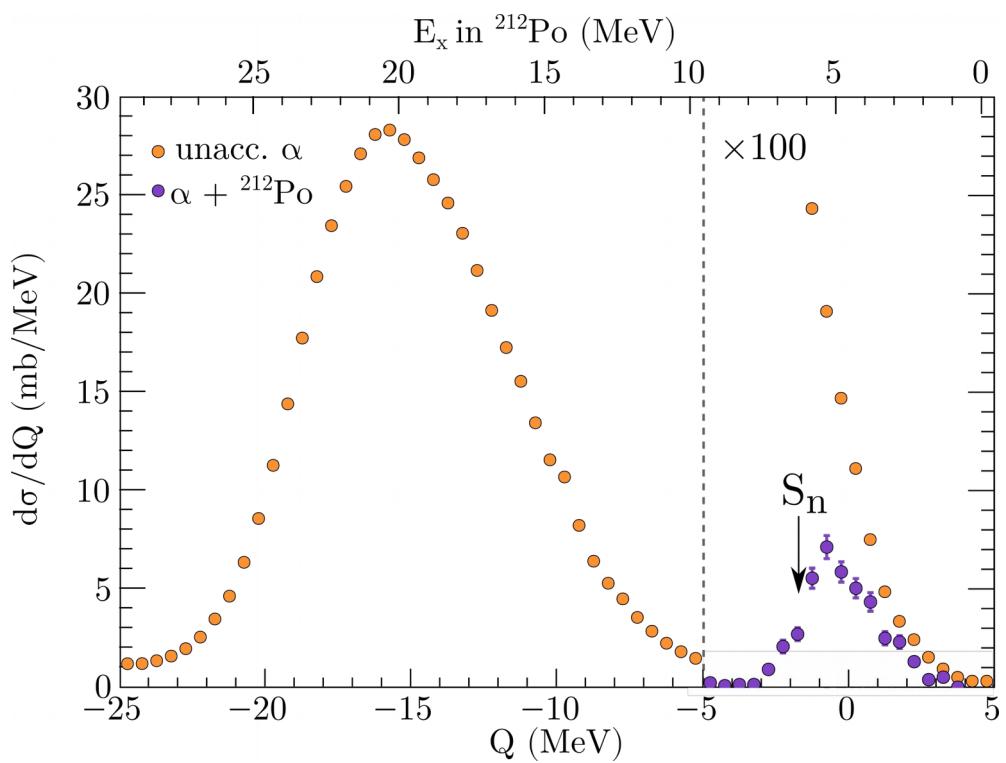
Evidence for cluster transfer

- Coincidence α associated with production of ^{212}Po at low excitation energy, E_x , below $S_n = 6.01 \text{ MeV}$.



Q-value spectrum reconstructed from $d\sigma/dE\theta$

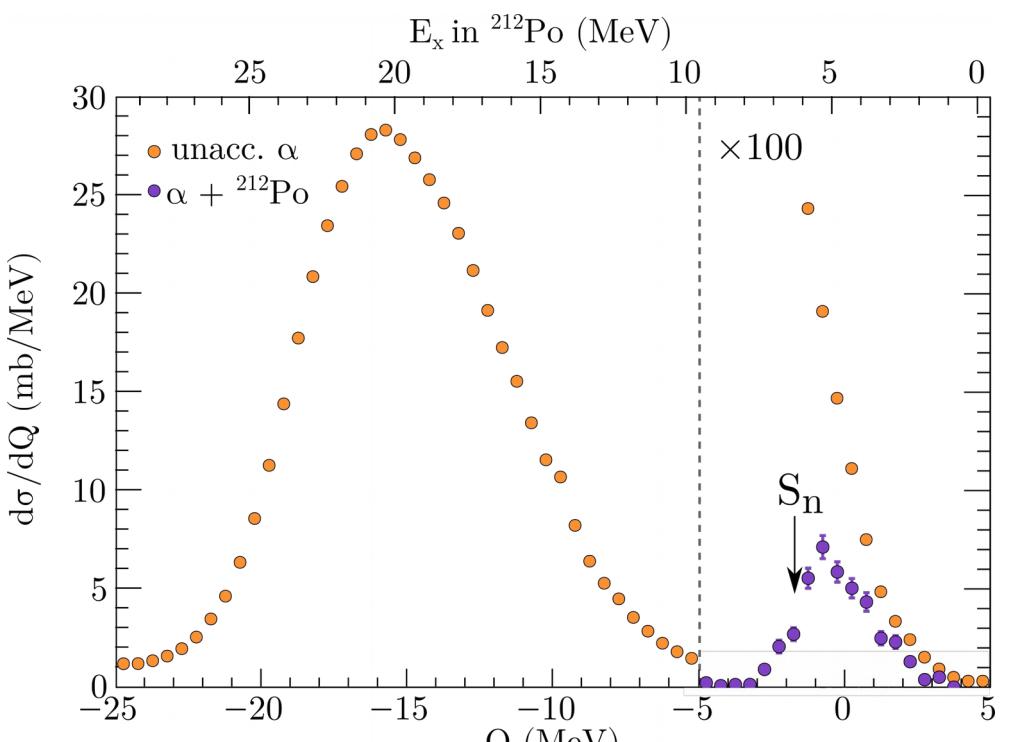
Evidence for cluster transfer



Q-value spectrum reconstructed from $d\sigma/dE\theta$

- Coincidence α associated with production of ${}^{212}\text{Po}$ at low excitation energy, E_x , below $S_n = 6.01$ MeV.
- E_x from triton capture after breakup > 7.061 MeV (Q-value for triton capture).

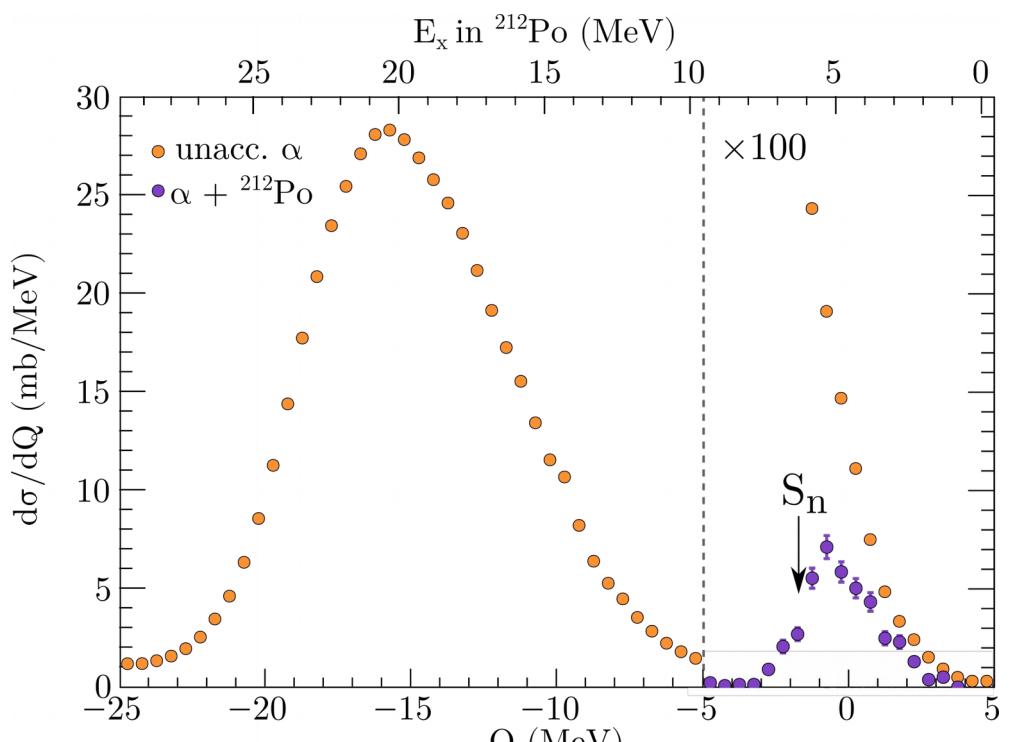
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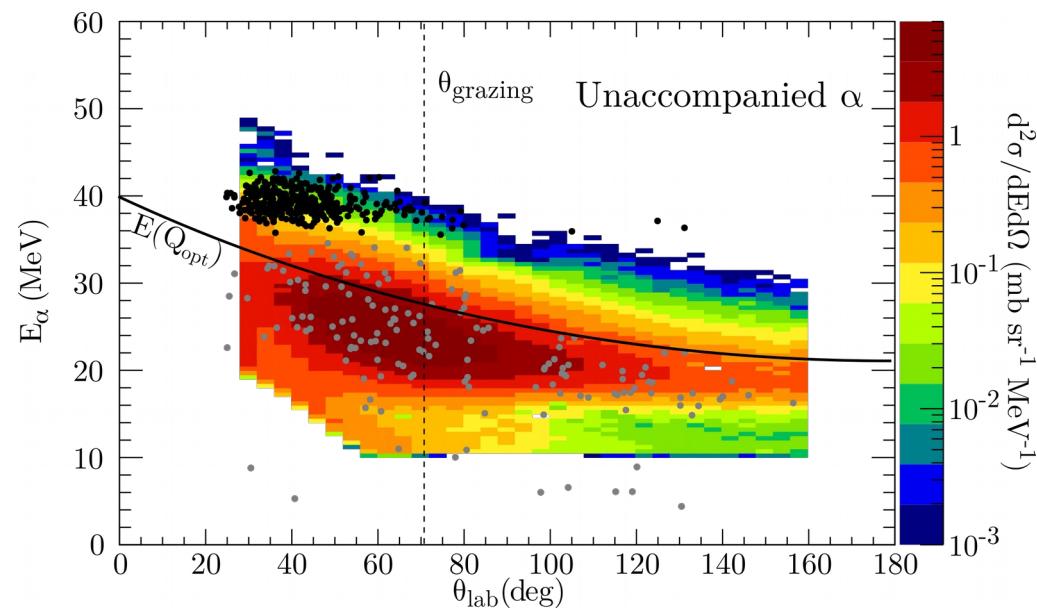
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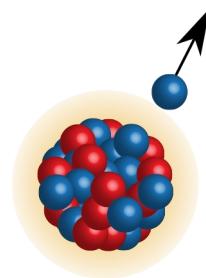
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- The ${}^{212}\text{Po}$ events form the tail of the much broader unaccompanied α Q-value distribution.

Evidence for cluster transfer

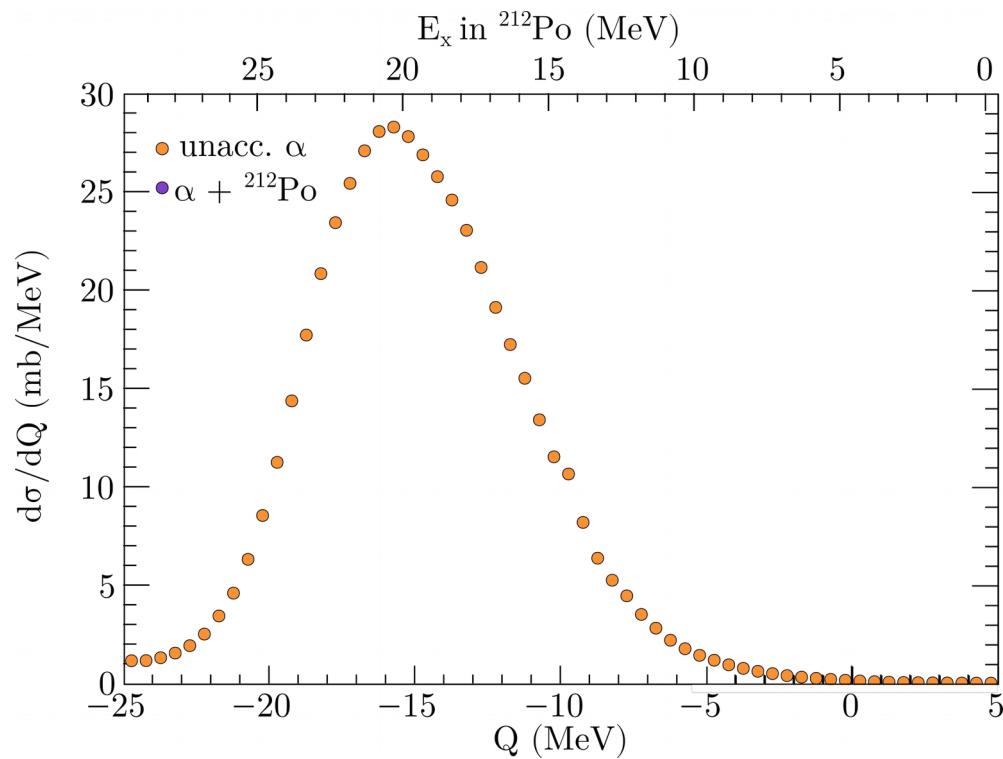


- Unaccompanied α E vs $\theta \rightarrow$ consistent α produced at the Optimum Q-value (Q_{opt}) [Schiffer PLB 44 (1973)]. (Excitation energy with highest cross-section, expected from a transfer reaction)
- The total unaccompanied α distribution is therefore broadly consistent with production of ^{212}Po up to $E_x \sim 28$ MeV via triton cluster transfer.

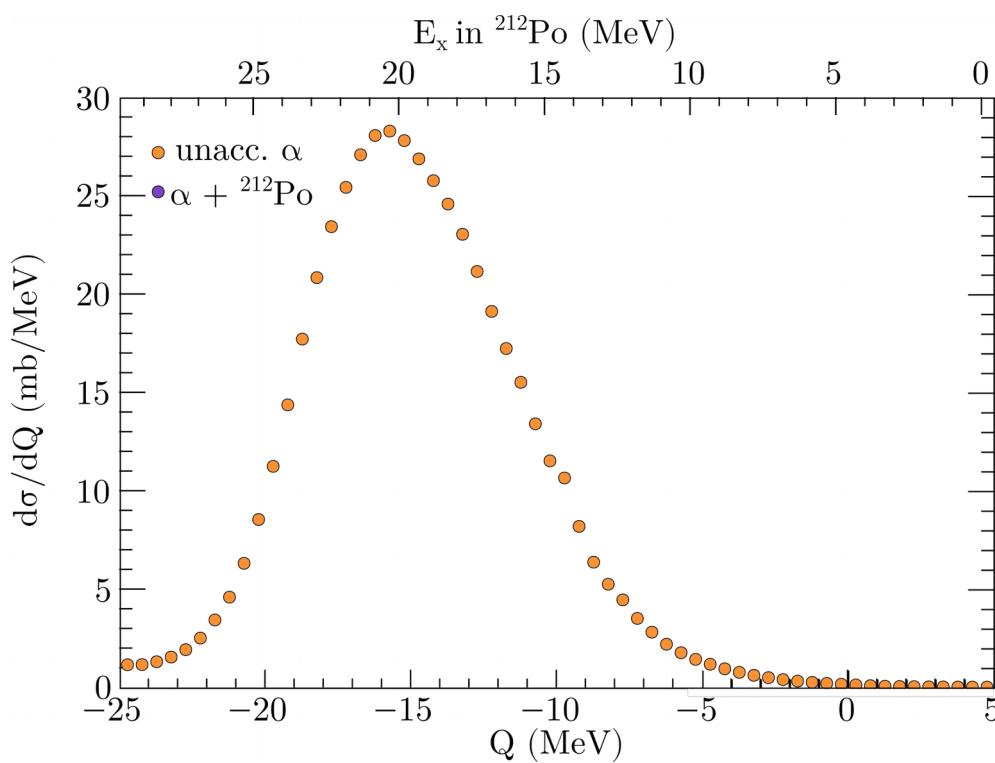
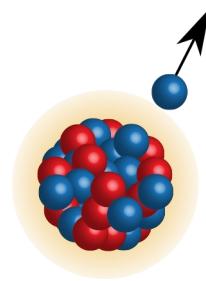
Excitation energy + n evaporation



- ^{212}Po produced at high $E_x \rightarrow$ neutron evaporation. This is the mechanism producing lighter Po.

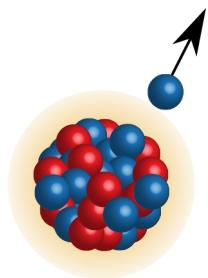


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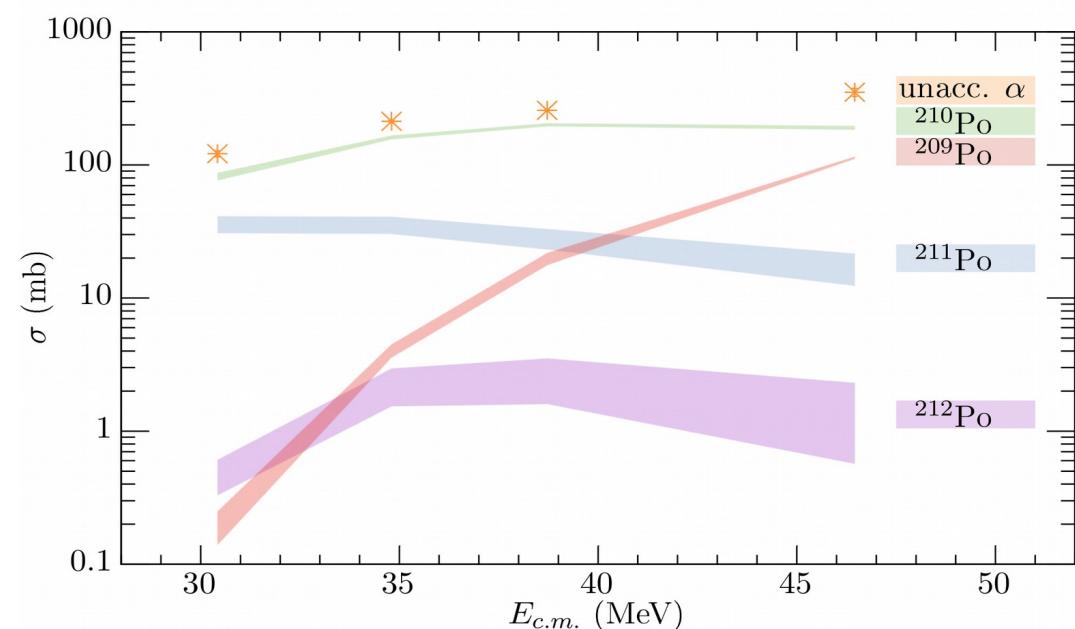


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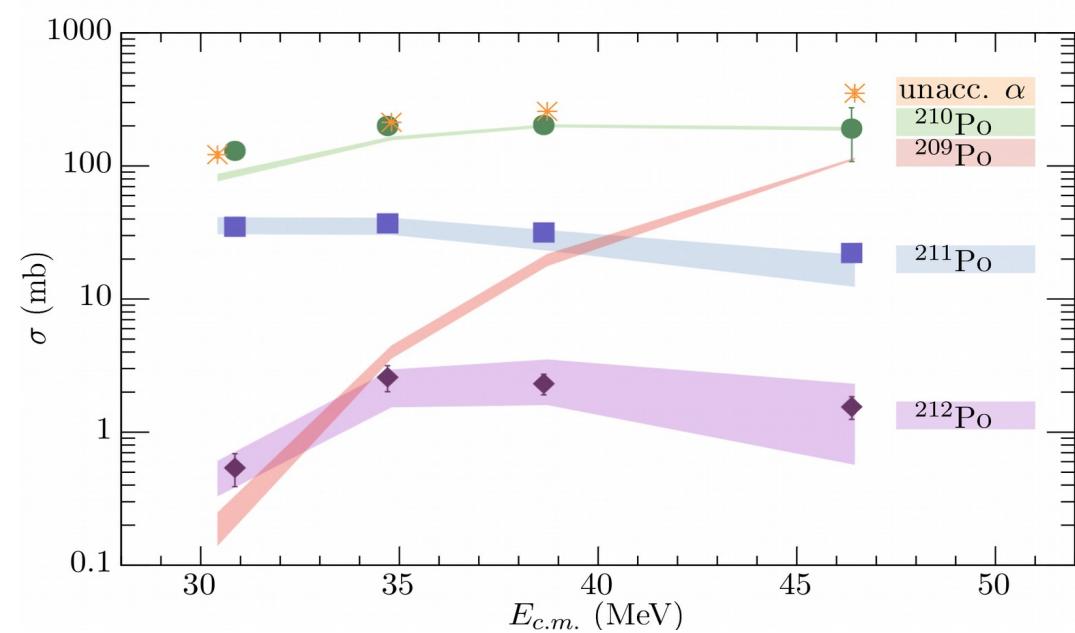
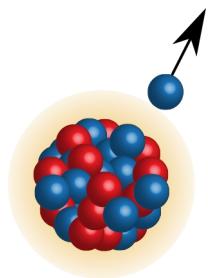
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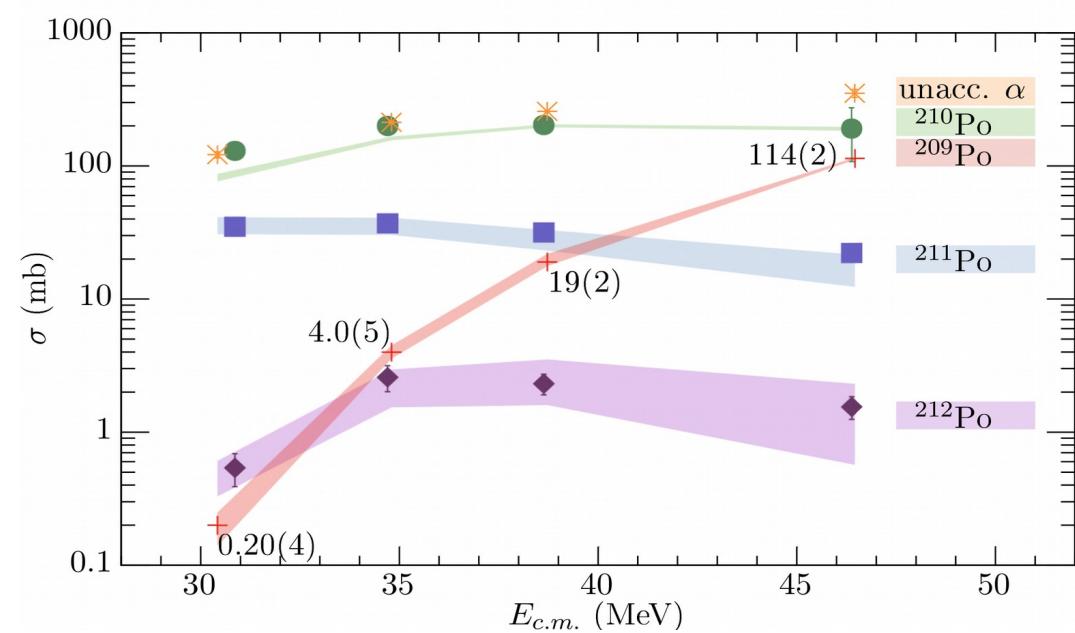
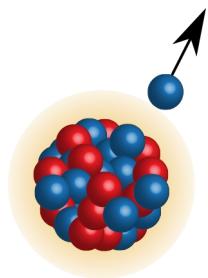


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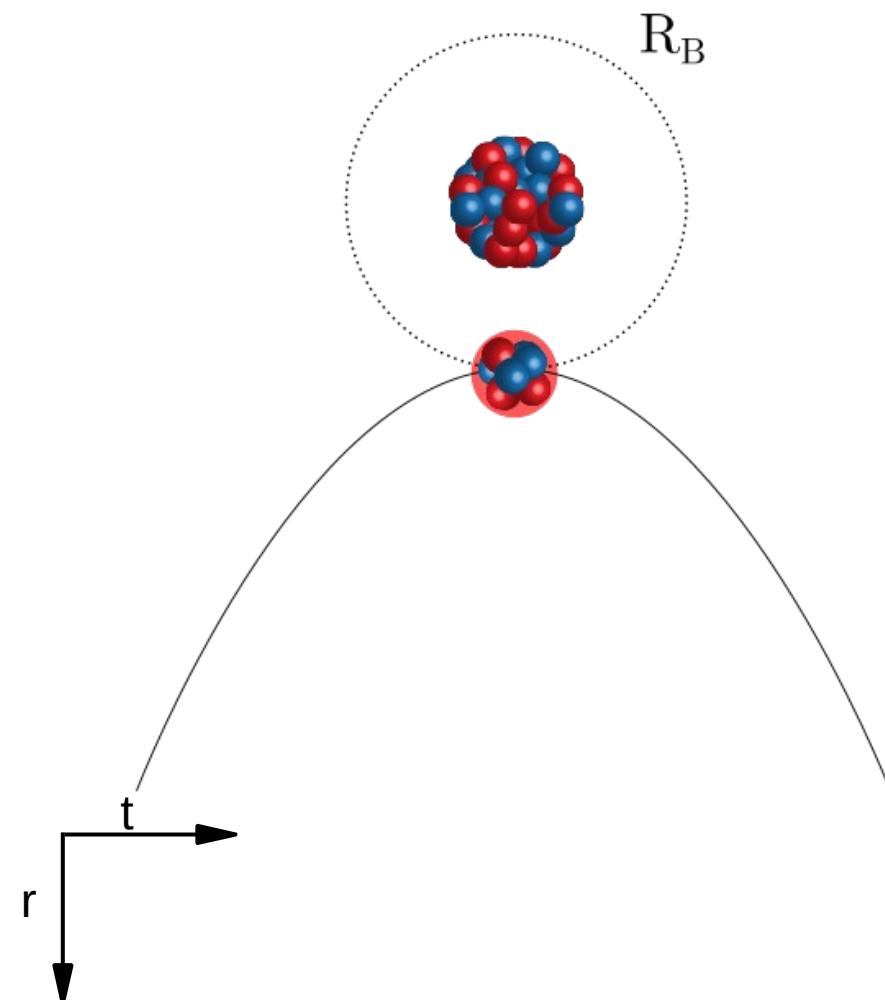
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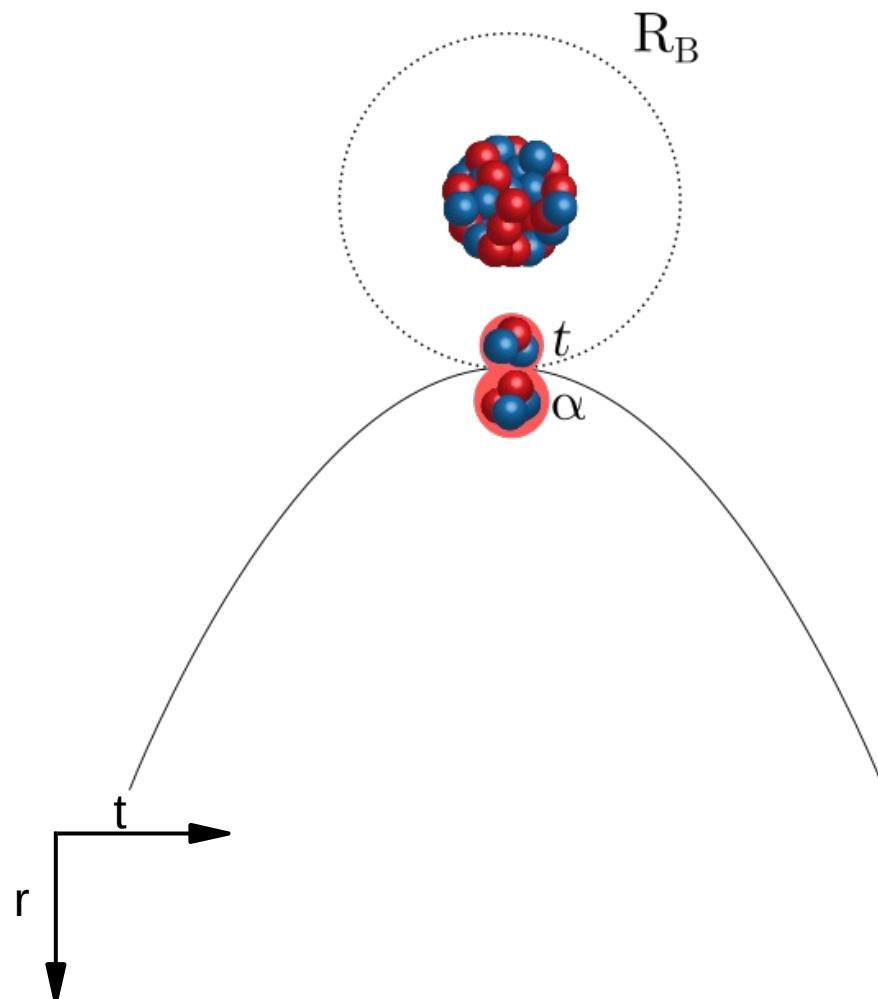
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- Prediction for ^{209}Po ($t_{1/2} = 124$ years)

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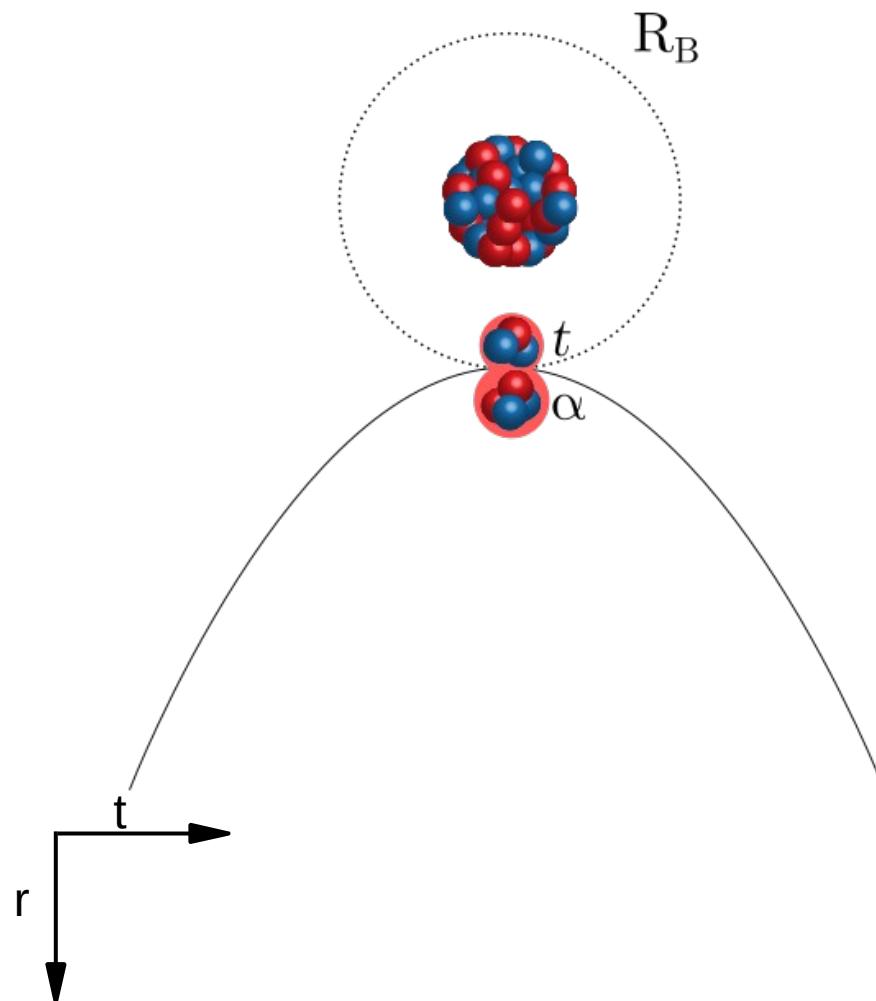
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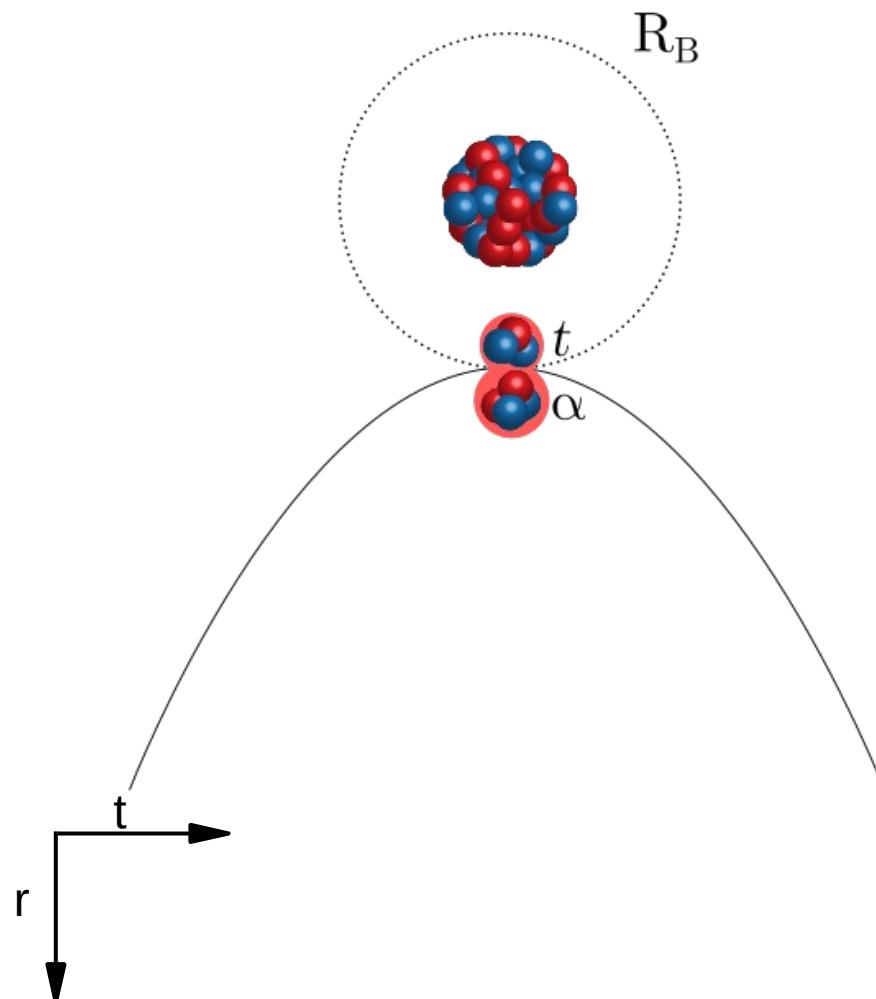
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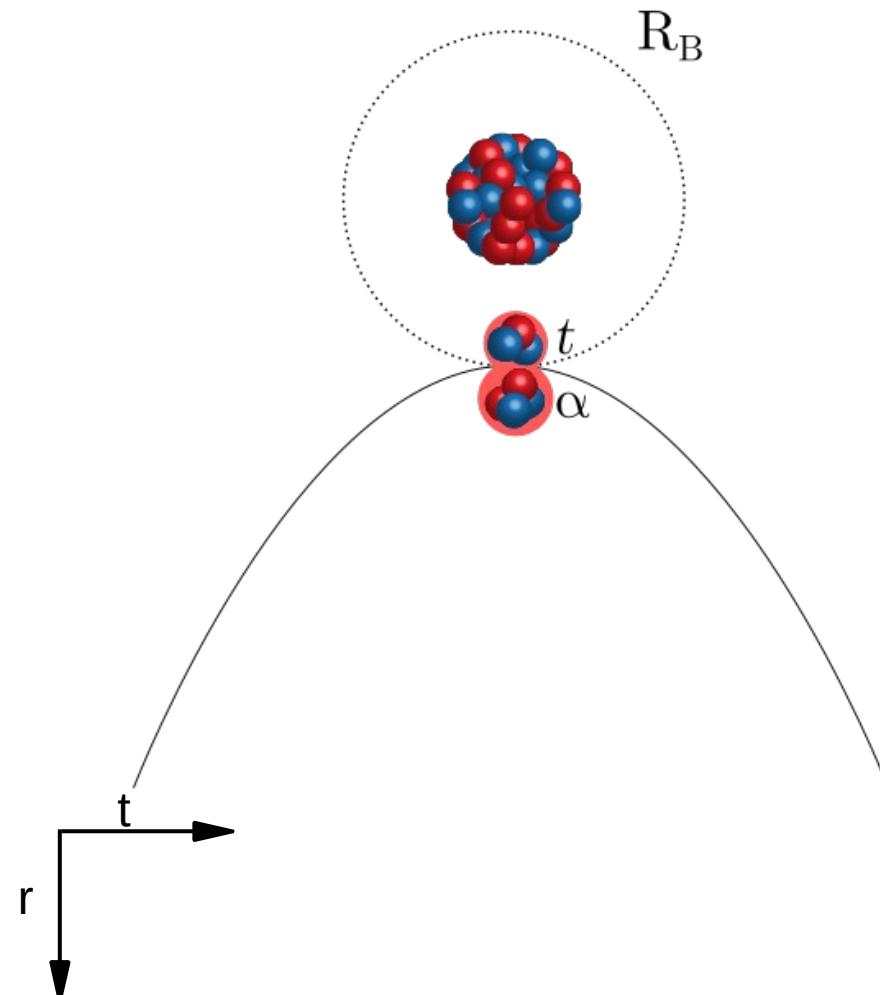
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- Numerical support from Lei & Moro PRL 122 042503 (2019) using the Ichimura, Austern, and Vincent (IAV) spectator-participant inclusive breakup model. They associate it with a “Trojan Horse” mechanism.



This should be true wherever nuclei are strongly clustered!

- Breakup followed by capture cannot produce most of the incomplete fusion products in ${}^7\text{Li} + {}^{209}\text{Bi}$ reactions.
- ${}^{212}\text{Po}$ is produced by direct triton cluster transfer.
- Unaccompanied α particles (all Po isotopes) are consistent with production via triton transfer.
- Clustering of the projectile nucleus → explains both incomplete fusion products and the suppression of complete fusion.

- **New technique:** Measurements of unaccompanied particle spectra offer a new and widely applicable approach to understand near-barrier fusion dynamics of weakly bound nuclei.
- **New interpretation:** The idea that cluster transfer rather than breakup is responsible for complete fusion suppression should be valid for any nuclides that exhibit strong clustering.
- **Need new measurements:**
 - How does this picture evolve at the limits of weak binding? The cross sections for complete and incomplete fusion products in reactions of exotic nuclei, such as ${}^6\text{He}$, ${}^8\text{Li}$, and ${}^{7,10,11}\text{Be}$, ${}^8\text{B}$, will provide very interesting insights into near-barrier reaction dynamics.



Physics is a team sport

Ed Simpson

Ian Carter

Sunil Kalkal

Nanda Dasgupta

David Hinde

Lauren Bezzina

Chandrima Sengupta

Cedric Simenel

Kaushik Banerjee

Ben Swinton-Bland

Kirsten Vo-Phouc

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