

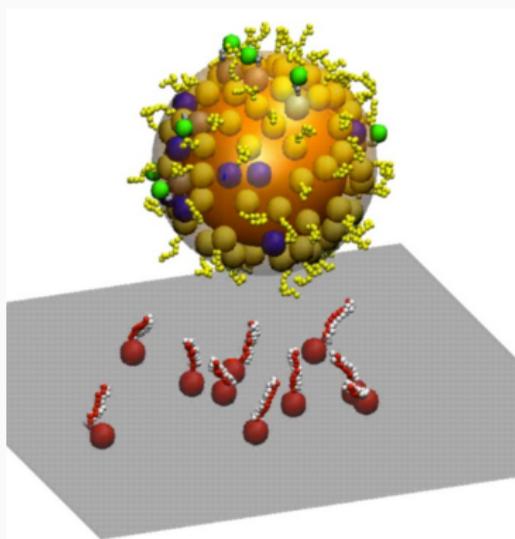
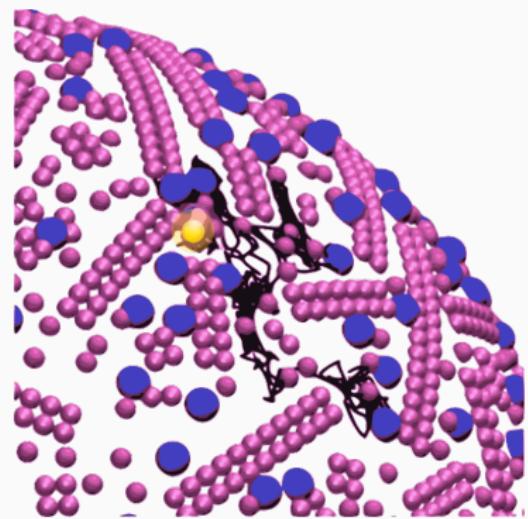


Reaction-diffusion simulations for signal transduction cascades

Christoph Fröhner, Moritz Hoffmann, Mohsen Sadeghi, Luigi Sbailò, Manuel Dibak, Mauricio Del Razo Sarmina, Frank Nöe

CMB Group, FU Berlin

Reaction-diffusion simulations



ReADDy software package



Content and goals

Content

- Motivation from biology
- Physics
- Molecular simulation
- Reaction-diffusion models → ReADDy model
- ReADDy implementation and neighborlists
- Membrane mechanics
- Lotka-Volterra models

Goal

- **why, where** reaction-diffusion methods are applied
- **how** to perform reaction-diffusion simulations

Organizational details

- everyone subscribed to participants list?
- bookmark this
 - https://readyy.github.io/readyy_documentation/workshop_info
- Linux, Bash, Python?

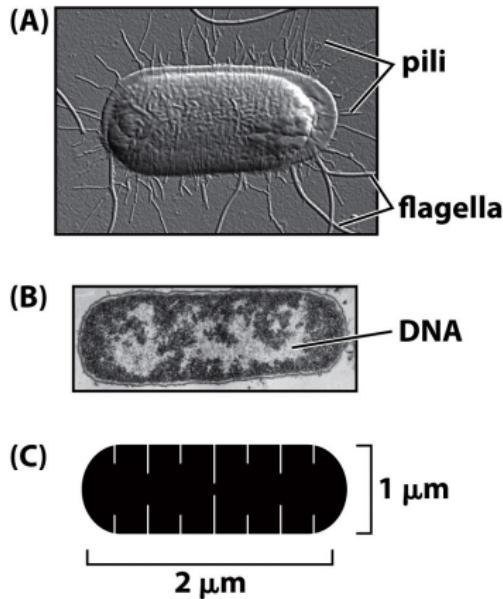
Biology by the numbers

Table of contents

1. How many proteins are in a cell?
2. Reaction-diffusion
3. Why is RD useful?

How many proteins are in a cell?

How many proteins are in a cell?



Number of proteins in *E. coli*

- 1 ?
- 1,000 ?
- 1,000,000 ?
- 1,000,000,000 ?
- 1,000,000,000,000 ?

Figure 2.1 Physical Biology of the Cell (© Garland Science 2009)

Some numbers for E.coli

Table 1.1 Rules of thumb for biological estimates

	Quantity of interest	Symbol	Rule of thumb
<i>E. coli</i>	Cell volume	$V_{E. coli}$	$\approx 1 \mu\text{m}^3$
	Cell mass	$m_{E. coli}$	$\approx 1 \text{ pg}$
	Cell cycle time	$t_{E. coli}$	$\approx 3000 \text{ s}$
	Cell surface area	$A_{E. coli}$	$\approx 6 \mu\text{m}^2$
	Genome length	$N_{bp}^{E. coli}$	$\approx 5 \times 10^6 \text{ bp}$
	Swimming speed	$V_{E. coli}$	$\approx 20 \mu\text{m/s}$
Yeast	Volume of cell	V_{yeast}	$\approx 60 \mu\text{m}^3$
	Mass of cell	m_{yeast}	$\approx 60 \text{ pg}$
	Diameter of cell	d_{yeast}	$\approx 5 \mu\text{m}$
	Cell cycle time	t_{yeast}	$\approx 200 \text{ min}$
	Genome length	N_{bp}^{yeast}	$\approx 10^7 \text{ bp}$
Organelles	Diameter of nucleus	$d_{nucleus}$	$\approx 5 \mu\text{m}$
	Length of mitochondrion	l_{mito}	$\approx 2 \mu\text{m}$
	Diameter of transport vesicles	$d_{vesicle}$	$\approx 50 \text{ nm}$
Water	Volume of molecule	V_{H_2O}	$\approx 10^{-2} \text{ nm}^3$
	Density of water	ρ	1 g/cm^3
	Viscosity of water	η	$\approx 1 \text{ centipoise}$ $(10^{-2} \text{ g/(cm s)})$
	Hydrophobic embedding energy	$\approx E_{hydr}$	$25 \text{ cal}/(\text{mol } \text{\AA}^2)$
DNA	Length per base pair	l_{bp}	$\approx 1/3 \text{ nm}$
	Volume per base pair	V_{bp}	$\approx 1 \text{ nm}^3$
	Charge density	λ_{DNA}	$2 \text{ e}/0.34 \text{ nm}$
	Persistence length	ξ_p	50 nm
Amino acids and proteins	Radius of "average" protein	$r_{protein}$	$\approx 2 \text{ nm}$
	Volume of "average" protein	$V_{protein}$	$\approx 25 \text{ nm}^3$
	Mass of "average" amino acid	M_{aa}	$\approx 100 \text{ Da}$
	Mass of "average" protein	$M_{protein}$	$\approx 30,000 \text{ Da}$
	Protein concentration in cytoplasm	$c_{protein}$	$\approx 300 \text{ mg/mL}$
	Characteristic force of protein motor	F_{motor}	$\approx 5 \text{ pN}$
	Characteristic speed of protein motor	V_{motor}	$\approx 200 \text{ nm/s}$
Lipid bilayers	Diffusion constant of "average" protein	$D_{protein}$	$\approx 100 \mu\text{m}^2/\text{s}$
	Thickness of lipid bilayer	d	$\approx 5 \text{ nm}$
	Area per molecule	A_{lipid}	$\approx \frac{1}{2} \text{ nm}^2$
	Mass of lipid molecule	m_{lipid}	$\approx 800 \text{ Da}$

Table 1.1 Physical Biology of the Cell (© Garland Science 2009)

Number of proteins in E.coli

Typical Actin concentration

$$c = 0.5\text{mM} = \frac{n}{V}$$

leads to

$$n \approx 300,000$$

Number of proteins between 10^3 and 10^6

Relative numbers

Relative weight of macromolecules

Substance	% of total dry weight	Number of molecules	
Macromolecule			
Protein	55.0	2.4×10^6	
RNA	20.4		
23S RNA	10.6	19,000	
16S RNA	5.5	19,000	
5S RNA	0.4	19,000	
Transfer RNA (45)	2.9	200,000	
Messenger RNA	0.8	1,400	
Phospholipid	9.1	22×10^6	
Lipopolysaccharide	3.4	1.2×10^6	
DNA	3.1	2	
Murein	2.5	1	
Glycogen	2.5	4,360	
Total macromolecules	96.1		
Small molecules			
Metabolites, building blocks, etc.	2.9		
Inorganic ions	1.0		
Total small molecules	3.9		

Table 2.1 Physical Biology of the Cell (© Garland Science 2009)

Relative volume of macromolecules
(proteins + other) $\approx 60\%$
Dense packing of spheres $\approx 70\%$



Overview of E.coli

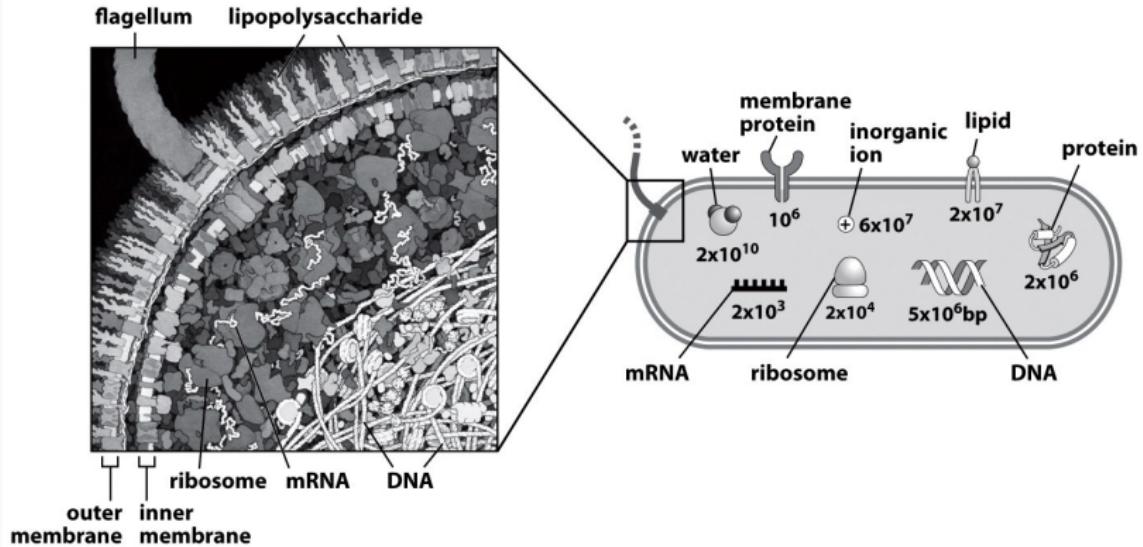
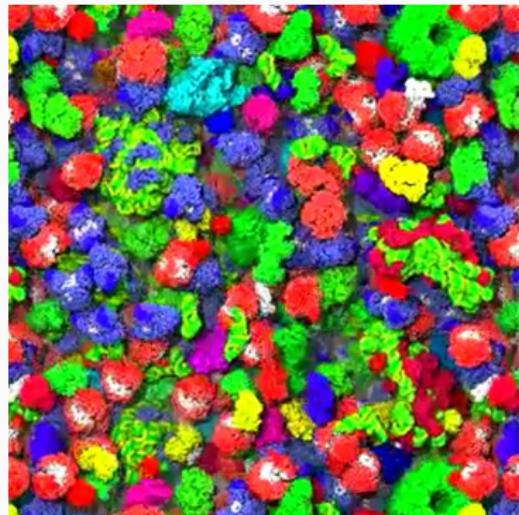
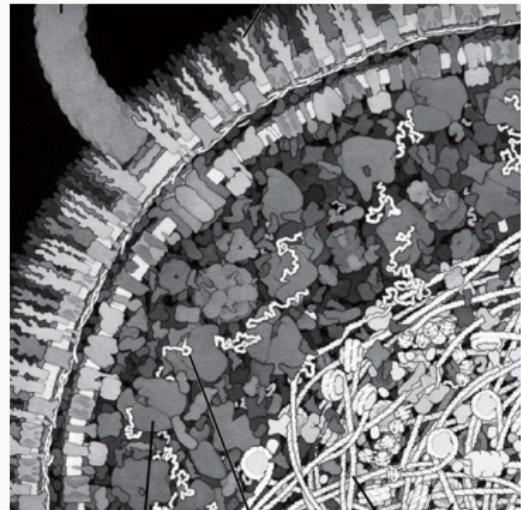


Figure 2.2 Physical Biology of the Cell (© Garland Science 2009)

Reaction-diffusion

Cell is crowded

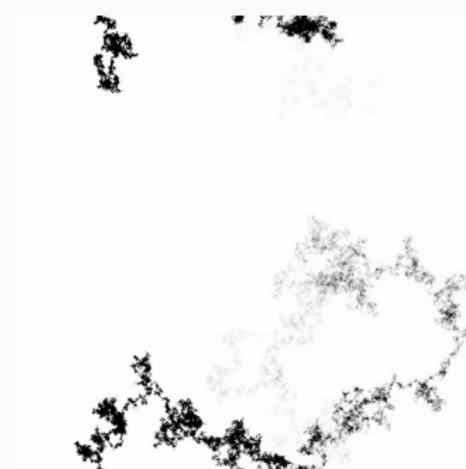


Transport via diffusion

Diffusion = dominant form of transport

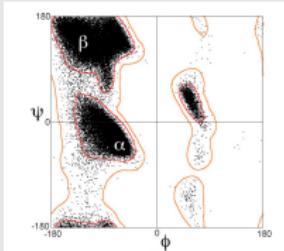
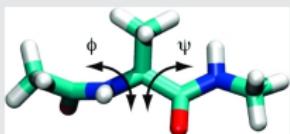
Diffusion

- stochastic/probabilistic motion
- systems at finite temperature
- ignore solvent - implicit solvent



Macro-molecules interact = Reactions

Conformational change



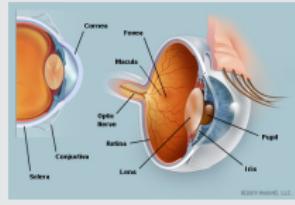
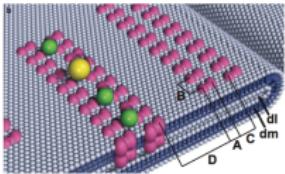
Protein-ligand interaction



Time evolution of systems

Reaction diffusion simulations generate realisations of **mesoscopic** systems

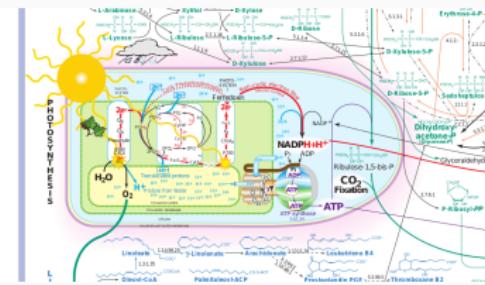
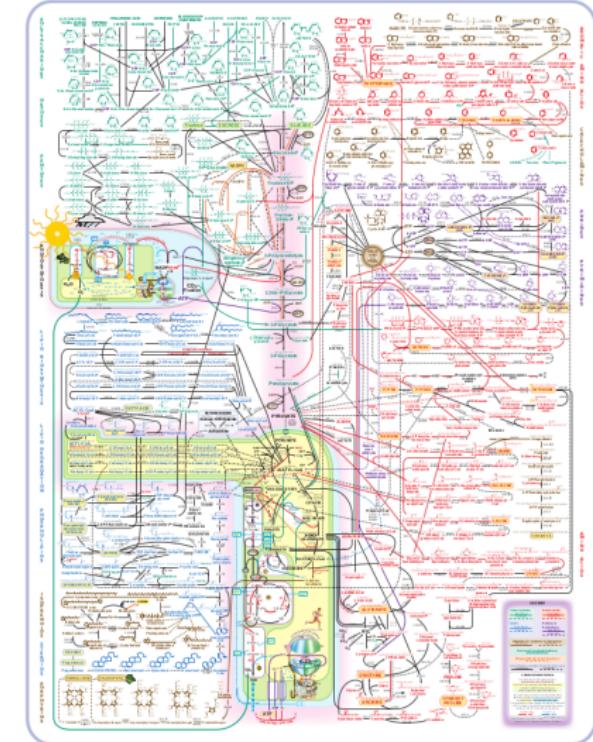
Different scales of visual signaling



Why is RD useful?

Metabolic processes

Metabolic Pathways



Experiments

- New techniques enable detailed images
- Proteins can be made fluorescent
- Reach sub- μm scale

