## **Image Captioning with RNNs**

In this exercise you will implement a vanilla recurrent neural networks and use them it to train a model that can generate novel captions for images.

```
In [1]: # As usual, a bit of setup
        from __future__ import print_function
        import time, os, json
        import numpy as np
        import matplotlib.pyplot as plt
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
        from cs231n.rnn_layers import
        from cs231n.captioning_solver import CaptioningSolver
        from cs231n.classifiers.rnn import CaptioningRNN
        from cs231n.coco_utils import load_coco_data, sample_coco_minibatch, decode_captions
        from cs231n.image utils import image from url
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
                returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(le-8, np.abs(x) + np.abs(y))))
```

### Install h5py

The COCO dataset we will be using is stored in HDF5 format. To load HDF5 files, we will need to install the h5py Python package. From the command line, run:

pip install h5py

If you receive a permissions error, you may need to run the command as root:

sudo pip install h5py

You can also run commands directly from the Jupyter notebook by prefixing the command with the "!" character:

```
In [2]: | !pip install h5py

Requirement already satisfied: h5py in /miniconda3/envs/cs4803/lib/python3.6/site-packages (2.10.0)

Requirement already satisfied: numpy>=1.7 in /miniconda3/envs/cs4803/lib/python3.6/site-packages (from h5py) (1.18.1)

Requirement already satisfied: six in /miniconda3/envs/cs4803/lib/python3.6/site-packages (from h5py) (1.14.0)
```

#### Microsoft COCO

For this exercise we will use the 2014 release of the Microsoft COCO dataset (http://mscoco.org/) which has become the standard testbed for image captioning. The dataset consists of 80,000 training images and 40,000 validation images, each annotated with 5 captions written by workers on Amazon Mechanical Turk.

You should have already downloaded the data by changing to the cs231n/datasets directory and running the script get\_assignment3\_data.sh . If you haven't yet done so, run that script now. Warning: the COCO data download is ~1GB.

We have preprocessed the data and extracted features for you already. For all images we have extracted features from the fc7 layer of the VGG-16 network pretrained on ImageNet; these features are stored in the files train2014\_vgg16\_fc7.h5 and val2014\_vgg16\_fc7.h5 respectively. To cut down on processing time and memory requirements, we have reduced the dimensionality of the features from 4096 to 512; these features can be found in the files train2014\_vgg16\_fc7\_pca.h5 and val2014\_vgg16\_fc7\_pca.h5.

The raw images take up a lot of space (nearly 20GB) so we have not included them in the download. However all images are taken from Flickr, and URLs of the training and validation images are stored in the files train2014\_urls.txt and val2014\_urls.txt respectively. This allows you to download images on the fly for visualization. Since images are downloaded on-the-fly, you must be connected to the internet to view images.

Dealing with strings is inefficient, so we will work with an encoded version of the captions. Each word is assigned an integer ID, allowing us to represent a caption by a sequence of integers. The mapping between integer IDs and words is in the file coco2014\_vocab.json, and you can use the function decode\_captions from the file cs231n/coco\_utils.py to convert numpy arrays of integer IDs back into strings.

There are a couple special tokens that we add to the vocabulary. We prepend a special <START> token and append an <END> token to the beginning and end of each caption respectively. Rare words are replaced with a special <UNK> token (for "unknown"). In addition, since we want to train with minibatches containing captions of different lengths, we pad short captions with a special <NULL> token after the <END> token and don't compute loss or gradient for <NULL> tokens. Since they are a bit of a pain, we have taken care of all implementation details around special tokens for you.

You can load all of the MS-COCO data (captions, features, URLs, and vocabulary) using the load coco data function from the file cs231n/coco utils.py . Run the following cell to do so:

## Look at the data

It is always a good idea to look at examples from the dataset before working with it.

train\_urls <class 'numpy.ndarray'> (82783,) <U63
val\_urls <class 'numpy.ndarray'> (40504,) <U63</pre>

You can use the sample\_coco\_minibatch function from the file cs231n/coco\_utils.py to sample minibatches of data from the data structure returned from load\_coco\_data. Run the following to sample a small minibatch of training data and show the images and their captions. Running it multiple times and looking at the results helps you to get a sense of the dataset.

Note that we decode the captions using the decode\_captions function and that we download the images on-the-fly using their Flickr URL, so you must be connected to the internet to view images.

```
In [4]: # Sample a minibatch and show the images and captions
batch_size = 3

captions, features, urls = sample_coco_minibatch(data, batch_size=batch_size)
for i, (caption, url) in enumerate(zip(captions, urls)):
    plt.imshow(image_from_url(url))
    plt.axis('off')
    caption_str = decode_captions(caption, data['idx_to_word'])
    plt.title(caption_str)
    plt.show()
```

<START> a small bathroom with a white toilet sitting next to a sink <END>



<START> a house with a two piece swinging door that is open <END>



<START> a woman and toddler sitting on a bench with <UNK> <END>



### **Recurrent Neural Networks**

As discussed in lecture, we will use recurrent neural network (RNN) language models for image captioning. The file cs23ln/rnn\_layers.py contains implementations of different layer types that are needed for recurrent neural networks, and the file cs23ln/classifiers/rnn.py uses these layers to implement an image captioning model.

### Vanilla RNN: step forward

Open the file cs231n/rnn\_layers.py . This file implements the forward and backward passes for different types of layers that are commonly used in recurrent neural networks.

First implement the function rnn step forward which implements the forward pass for a single timestep of a vanilla recurrent neural network. After doing so run the following to check your implementation. You should see errors less than 1e-8.

```
In [5]: N, D, H = 3, 10, 4
         x = np.linspace(-0.4, 0.7, num=N*D).reshape(N, D)
         prev_h = np.linspace(-0.2, 0.5, num=N*H).reshape(N, H)
         Wx = np.linspace(-0.1, 0.9, num=D*H).reshape(D, H)
         Wh = np.linspace(-0.3, 0.7, num=H*H).reshape(H, H)
         b = np.linspace(-0.2, 0.4, num=H)
         next_h, _ = rnn_step_forward(x, prev_h, Wx, Wh, b)
         expected_next_h = np.asarray([
           [-0.58172089, -0.50182032, -0.41232771, -0.31410098],
           [ 0.66854692, 0.79562378, 0.87755553, 0.92795967], [ 0.97934501, 0.99144213, 0.99646691, 0.99854353]])
        print('next_h error: ', rel_error(expected_next_h, next_h))
```

next h error: 6.292421426471037e-09

# Vanilla RNN: step backward

In the file cs231n/rnn\_layers.py implement the rnn\_step\_backward function. After doing so run the following to numerically gradient check your implementation. You should see errors less than 1e-8.

```
In [6]: from cs231n.rnn_layers import rnn_step_forward, rnn_step_backward
         np.random.seed(231)
        N, D, H = 4, 5, 6
         x = np.random.randn(N, D)
        h = np.random.randn(N, H)
         Wx = np.random.randn(D, H)
         Wh = np.random.randn(H, H)
        b = np.random.randn(H)
        out, cache = rnn_step_forward(x, h, Wx, Wh, b)
        dnext h = np.random.randn(*out.shape)
         fx = lambda x: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fh = lambda prev_h: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fWx = lambda Wx: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fWh = lambda Wh: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fb = lambda b: rnn_step_forward(x, h, Wx, Wh, b)[0]
         dx_num = eval_numerical_gradient_array(fx, x, dnext_h)
         dprev_h_num = eval_numerical_gradient_array(fh, h, dnext_h)
         dWx_num = eval_numerical_gradient_array(fWx, Wx, dnext_h)
         dWh_num = eval_numerical_gradient_array(fWh, Wh, dnext_h)
        db_num = eval_numerical_gradient_array(fb, b, dnext_h)
        dx, dprev_h, dWx, dWh, db = rnn_step_backward(dnext_h, cache)
         print('dx error: ', rel_error(dx_num, dx))
         print('dprev_h error: ', rel_error(dprev_h_num, dprev_h))
        print('dwx error: ', rel_error(dwx_num, dwx))
print('dwh error: ', rel_error(dwh_num, dwh))
print('db error: ', rel_error(db_num, db))
        N 4, D 5, H 6
        dnext_h: (N, H) (4, 6)
        x: (N, D) (4, 5)
        prev_h: (N, H) (4, 6)
        Wx: (D, H) (5, 6)
        Wh: (H, H) (6, 6)
        dTanH: (N, H) (4, 6)
        dSum: (N, H) (4, 6)
```

dx: (4, 5)dprev\_h: (4, 6) dWx: (5, 6) dWh: (6, 6) db: (6,) dx error: 2.99311613693832e-10 dprev h error: 2.633205333189269e-10 dWx error: 9.684083573724284e-10 dWh error: 3.355162782632426e-10 db error: 1.5956895526227225e-11

### Vanilla RNN: forward

Now that you have implemented the forward and backward passes for a single timestep of a vanilla RNN, you will combine these pieces to implement a RNN that process an entire sequence of data.

In the file cs231n/rnn layers.py, implement the function rnn\_forward. This should be implemented using the rnn\_step\_forward function that you defined above. After doing so run the following to check your implementation. You should see errors less than 1e-7.

h error: 7.728466180186066e-08

#### Vanilla RNN: backward

In the file cs231n/rnn\_layers.py, implement the backward pass for a vanilla RNN in the function rnn\_backward. This should run back-propagation over the entire sequence, calling into the rnn\_step\_backward function that you defined above. You should see errors less than 5e-7.

```
In [8]: np.random.seed(231)
          N, D, T, H = 2, 3, 10, 5
          x = np.random.randn(N, T, D)
          h0 = np.random.randn(N, H)
          Wx = np.random.randn(D, H)
          Wh = np.random.randn(H, H)
         b = np.random.randn(H)
          out, cache = rnn_forward(x, h0, Wx, Wh, b)
          dout = np.random.randn(*out.shape)
          dx, dh0, dWx, dWh, db = rnn backward(dout, cache)
          fx = lambda x: rnn forward(x, h0, Wx, Wh, b)[0]
          fh0 = lambda \ h0: rnn_forward(x, h0, Wx, Wh, b)[0]
          fWx = lambda Wx: rnn_forward(x, h0, Wx, Wh, b)[0]
          fWh = lambda Wh: rnn_forward(x, h0, Wx, Wh, b)[0]
          fb = lambda b: rnn_forward(x, h0, Wx, Wh, b)[0]
          dx_num = eval_numerical_gradient_array(fx, x, dout)
          dh0_num = eval_numerical_gradient_array(fh0, h0, dout)
          dWx_num = eval_numerical_gradient_array(fWx, Wx, dout)
          dWh_num = eval_numerical_gradient_array(fWh, Wh, dout)
          db_num = eval_numerical_gradient_array(fb, b, dout)
          # print(f"correct dx: {dx num}")
          # print(f"reagans dx: {dx}")
         # print('rreagans ax: {ax; } ox; )
print('dx error: ', rel_error(dx_num, dx))
print('dh0 error: ', rel_error(dh0_num, dh0))
print('dWx error: ', rel_error(dWx_num, dWx))
print('dWh error: ', rel_error(dWh_num, dWh))
print('db error: ', rel_error(db_num, db))
         dx error: 2.3969112188524054e-09
         dh0 error: 3.3796875007867145e-09
          dWx error: 7.221000108504998e-09
         dWh error: 1.284586847530015e-07
```

# Word embedding: forward

db error: 4.675767378424171e-10

In deep learning systems, we commonly represent words using vectors. Each word of the vocabulary will be associated with a vector, and these vectors will be learned jointly with the rest of the system.

In the file cs231n/rnn\_layers.py, implement the function word\_embedding\_forward to convert words (represented by integers) into vectors. Run the following to check your implementation. You should see error around 1e-8.

out error: 1.000000094736443e-08

## Word embedding: backward

Implement the backward pass for the word embedding function in the function word\_embedding\_backward. After doing so run the following to numerically gradient check your implementation. You should see errors less than 1e-11.

```
In [10]: np.random.seed(231)

N, T, V, D = 50, 3, 5, 6
    x = np.random.randint(V, size=(N, T))
    W = np.random.randn(V, D)

out, cache = word_embedding_forward(x, W)
    dout = np.random.randn(*out.shape)
    dW = word_embedding_backward(dout, cache)

f = lambda W: word_embedding_forward(x, W)[0]
    dW_num = eval_numerical_gradient_array(f, W, dout)

print('dW error: ', rel_error(dW, dW_num))

dW error: 3.2774595693100364e-12
```

# **Temporal Affine layer**

At every timestep we use an affine function to transform the RNN hidden vector at that timestep into scores for each word in the vocabulary. Because this is very similar to the affine layer that you implemented in assignment 2, we have provided this function for you in the temporal\_affine\_forward and temporal\_affine\_backward functions in the file cs231n/rnn\_layers.py . Run the following to perform numeric gradient checking on the implementation. You should see errors less than 1e-9.

```
In [11]: np.random.seed(231)
           # Gradient check for temporal affine layer
           N, T, D, M = 2, 3, 4, 5
          x = np.random.randn(N, T, D)
           w = np.random.randn(D, M)
          b = np.random.randn(M)
           out, cache = temporal_affine_forward(x, w, b)
           dout = np.random.randn(*out.shape)
           fx = lambda x: temporal affine forward(x, w, b)[0]
           fw = lambda w: temporal_affine_forward(x, w, b)[0]
           fb = lambda b: temporal_affine_forward(x, w, b)[0]
           dx_num = eval_numerical_gradient_array(fx, x, dout)
           dw_num = eval_numerical_gradient_array(fw, w, dout)
           db_num = eval_numerical_gradient_array(fb, b, dout)
           dx, dw, db = temporal_affine_backward(dout, cache)
          print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
          dx error: 2.9215854231394017e-10
          dw error: 1.5772169135951167e-10
db error: 3.252200556967514e-11
```

# **Temporal Softmax loss**

In an RNN language model, at every timestep we produce a score for each word in the vocabulary. We know the ground-truth word at each timestep, so we use a softmax loss function to compute loss and gradient at each timestep. We sum the losses over time and average them over the minibatch.

However there is one wrinkle: since we operate over minibatches and different captions may have different lengths, we append <NULL> tokens to the end of each caption so they all have the same length. We don't want these <NULL> tokens to count toward the loss or gradient, so in addition to scores and ground-truth labels our loss function also accepts a mask array that tells it which elements of the scores count towards the loss.

Since this is very similar to the softmax loss function you implemented in assignment 1, we have implemented this loss function for you; look at the temporal\_softmax\_loss function in the file cs231n/rnn layers.py.

Run the following cell to sanity check the loss and perform numeric gradient checking on the function. You should see an error for dx less than 1e-7.

```
In [12]: # Sanity check for temporal softmax loss
         from cs231n.rnn_layers import temporal_softmax_loss
          N, T, V = 100, 1, 10
          def check_loss(N, T, V, p):
              x = 0.001 * np.random.randn(N, T, V)
              y = np.random.randint(V, size=(N, T))
              mask = np.random.rand(N, T) <= p
              print(temporal_softmax_loss(x, y, mask)[0])
          check_loss(100, 1, 10, 1.0)  # Should be about 2.3
check_loss(100, 10, 10, 1.0)  # Should be about 23
          check_loss(5000, 10, 10, 0.1) # Should be about 2.3
          # Gradient check for temporal softmax loss
         N. T. V = 7.8.9
          x = np.random.randn(N, T, V)
          y = np.random.randint(V, size=(N, T))
          mask = (np.random.rand(N, T) > 0.5)
          loss, dx = temporal_softmax_loss(x, y, mask, verbose=False)
          dx_num = eval_numerical_gradient(lambda x: temporal_softmax_loss(x, y, mask)[0], x, verbose=False)
          print('dx error: ', rel error(dx, dx num))
         2.3027781774290146
         23.025985953127226
         2.2643611790293394
```

## **RNN** for image captioning

dx error: 2.583585303524283e-08

Now that you have implemented the necessary layers, you can combine them to build an image captioning model. Open the file cs231n/classifiers/rnn.py and look at the CaptioningRNN class.

Implement the forward and backward pass of the model in the loss function. For now you only need to implement the case where cell\_type='rnn' for vanialla RNNs; you will implement the LSTM case later. After doing so, run the following to check your forward pass using a small test case; you should see error less than le-l0.

```
In [13]: N, D, W, H = 10, 20, 30, 40
         word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
         V = len(word_to_idx)
         T = 13
         model = CaptioningRNN(word to idx,
                    input dim=D.
                    wordvec_dim=W,
                    hidden_dim=H,
                    cell_type='rnn'
                    dtype=np.float64)
          # Set all model parameters to fixed values
          for k, v in model.params.items():
             model.params[k] = np.linspace(-1.4, 1.3, num=v.size).reshape(*v.shape)
          features = np.linspace(-1.5, 0.3, num=(N * D)).reshape(N, D)
         captions = (np.arange(N * T) % V).reshape(N, T)
          loss. grads = model.loss(features. captions. verbose=False)
         expected_loss = 9.83235591003
         print('loss: ', loss)
         print('expected loss: ', expected_loss)
         print('difference: ', abs(loss - expected_loss))
         loss: 9.832355910027388
         expected loss: 9.83235591003
difference: 2.611244553918368e-12
```

Run the following cell to perform numeric gradient checking on the CaptioningRNN class; you should errors around 5e-6 or less.

```
In [14]: np.random.seed(231)
           batch_size = 2
           timesteps = 3
           input_dim = 4
           wordvec_dim = 5
           hidden_dim = 6
           word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
           vocab_size = len(word_to_idx)
           captions = np.random.randint(vocab_size, size=(batch_size, timesteps))
features = np.random.randn(batch_size, input_dim)
           model = CaptioningRNN(word_to_idx,
                       input_dim=input_dim,
                      wordvec_dim=wordvec_dim,
hidden_dim=hidden_dim,
                      cell_type='rnn',
                      dtype=np.float64,
           loss, grads = model.loss(features, captions)
           for param_name in sorted(grads):
                f = lambda _: model.loss(features, captions)[0]
                param_grad_num = eval_numerical_gradient(f, model.params[param_name], verbose=False, h=1e-6)
               e = rel_error(param_grad_num, grads[param_name])
print('%s relative error: %e' % (param_name, e))
           W embed relative error: 2.331072e-09
```

W\_embed relative error: 2.331072e-09
W\_proj relative error: 9.974424e-09
W\_vocab relative error: 4.274378e-09
Wh relative error: 5.954804e-09
Wx relative error: 8.455229e-07
b relative error: 9.727211e-10
b\_proj relative error: 1.991603e-08
b\_vocab relative error: 6.918525e-11

## Overfit small data

Similar to the Solver class that we used to train image classification models on the previous assignment, on this assignment we use a CaptioningSolver class to train image captioning models. Open the file cs231n/captioning\_solver.py and read through the CaptioningSolver class; it should look very familiar.

Once you have familiarized yourself with the API, run the following to make sure your model overfit a small sample of 100 training examples. You should see losses of less than 0.1.

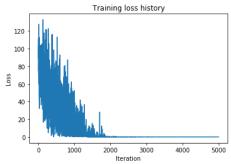
```
(Iteration 1 / 5000) loss: 89.538734
(Iteration 11 / 5000) loss: 89.436142
(Iteration 21 / 5000) loss: 41.782749
                5000)
(Iteration 31 /
                      loss: 97.063431
(Iteration 41 / 5000)
                      loss: 98.784393
(Iteration 51 / 5000)
                      loss: 103.743103
(Iteration 61 / 5000)
                      loss: 76.610619
(Iteration 71 / 5000)
                      loss: 46.232353
(Iteration 81 /
               5000)
                      loss: 47.529114
(Iteration 91 / 5000) loss: 51.454792
(Iteration 101 /
                 5000) loss: 41.202644
(Iteration 111 /
                 5000) loss: 103.156456
(Iteration 121 /
                 5000) loss: 63.173302
(Iteration 131 /
                 5000) loss: 37.913567
(Iteration 141 /
                 5000) loss: 99.907059
                 5000) loss: 85.212387
(Iteration 151
                 5000) loss: 57.529522
(Iteration 161
(Iteration 171
                       loss: 21.788654
                 5000)
(Iteration 181
                       loss: 27.034616
                 5000)
(Iteration 191
                 5000) loss: 29.954041
(Iteration 201
                 5000) loss: 20.125360
(Iteration 211
                 5000) loss: 42,703835
                 5000) loss: 50.779907
(Iteration 221
(Iteration 231
                 5000)
                       loss: 61.426395
(Iteration 241
                 5000)
                       loss: 64.845703
(Iteration 251
                 5000)
                       loss: 39.612869
(Iteration 261
                 5000) loss: 45.992516
(Iteration 271
                 5000) loss: 14.378930
(Iteration 281 /
                 5000) loss: 22.156929
(Iteration 291
                 5000) loss: 9.530903
(Iteration 301
                 5000) loss: 21.537636
(Iteration 311
                       loss: 28.899513
(Iteration 321
                 5000)
                       loss: 71.319817
(Iteration 331
                 5000) loss: 14.083916
(Iteration 341 /
                 5000) loss: 45.902863
(Iteration 351 /
                 5000) loss: 9.437120
(Iteration 361
                 5000) loss: 54.087708
(Iteration 371
                 5000) loss: 16.939861
(Iteration 381
                 5000) loss: 66.815460
(Iteration 391
                 5000) loss: 30.158628
(Iteration 401
                 5000) loss: 55.309616
(Iteration 411
                 5000) loss: 2.467841
                 5000) loss: 16.460686
(Iteration 421 /
(Iteration 431
                 5000) loss: 45.130829
(Iteration 441
                 5000) loss: 53.272102
                       loss: 51.743515
(Iteration 451
                 5000)
(Iteration 461
                 5000)
                       loss: 33.269196
(Iteration 471
                 5000) loss: 51.398998
(Iteration 481
                 5000) loss: 35.818146
(Iteration 491
                 5000) loss: 15.107388
                       loss: 54.070717
(Iteration 501
                 5000)
(Iteration 511
                 5000)
                       loss: 62.900036
(Iteration 521
                 5000) loss: 41.764988
(Iteration 531
                 5000)
                       loss: 12.469192
(Iteration 541
                 5000) loss: 60.341114
(Iteration 551
                 5000) loss: 25.075655
                 5000) loss: 6.382981
(Iteration 561
(Iteration 571
                 5000) loss: 2.519198
(Iteration 581
                 5000)
                       loss: 40.610477
(Iteration 591
                 5000) loss: 53.783371
(Iteration 601
                 5000) loss: 10.248645
(Iteration 611 /
                 5000) loss: 4.130352
(Iteration 621
                 5000) loss: 24.409468
(Iteration 631 /
                 5000) loss: 16.780783
(Iteration 641
                 5000) loss: 32.698448
(Iteration 651
                 5000)
                       loss: 8.323520
(Iteration 661 /
                 5000) loss: 48.345177
(Iteration 671
                 5000) loss: 55.929413
                 5000) loss: 37.345932
(Iteration 681
(Iteration 691
                 5000) loss: 47.278160
(Iteration 701
                 5000) loss: 9.752253
(Iteration 711
                 5000) loss: 17.875879
(Iteration 721
                       loss: 80.255623
                 5000)
(Iteration 731
                 5000) loss: 5.435860
(Iteration 741
                 5000) loss: 27.480110
(Iteration 751
                 5000) loss: 14.788023
(Iteration 761
                 5000) loss: 13.484448
(Iteration 771
                 5000) loss: 40.191666
                       loss: 28.038023
(Iteration 781
                 5000)
(Iteration 791
                 5000)
                       loss: 17.346283
(Iteration 801
                 5000) loss: 31.922714
(Iteration 811
                 5000) loss: 24.746355
(Iteration 821
                 5000) loss: 0.960066
(Iteration 831
                 5000) loss: 3.729098
(Iteration 841
                 5000) loss: 24.331656
(Iteration 851
                 5000) loss: 1.427623
(Iteration 861
                 5000)
                       loss: 4.385690
(Iteration 871
                 5000) loss: 19.940441
(Iteration 881 /
                 5000) loss: 47.771824
(Iteration 891
                 5000) loss: 7.549527
(Iteration 901
                 5000) loss: 34.210579
(Iteration 911
                 5000) loss: 7.658073
(Iteration 921
                 5000) loss: 4.147122
(Iteration 931
                 5000) loss: 7.015904
(Iteration 941 /
                 5000) loss: 0.634538
(Iteration 951 /
                 5000) loss: 2.414166
(Iteration 961 /
                 5000) loss: 3.767045
(Iteration 971
                 5000) loss: 9.693328
(Iteration 981
                       loss: 0.422882
                 5000)
(Iteration 991 /
                 5000) loss: 15.993933
(Iteration 1001 / 5000) loss: 3.902276
(Iteration 1011 / 5000) loss: 14.404881
(Iteration 1021 /
                  5000) loss: 1.892224
(Iteration 1031 / 5000) loss: 9.150167
```

```
(Iteration 1041 /
                  5000) loss: 1.529371
(Iteration 1051 /
                  5000) loss: 9.478404
(Iteration 1061
                  5000)
                        loss: 5.039266
(Iteration 1071
                  5000)
                        loss: 12.174468
(Iteration 1081
                        loss: 14.921804
                  5000)
(Iteration 1091
                  5000)
                        loss: 6.668529
(Iteration 1101 /
                  5000) loss: 3.538936
                  5000)
                        loss: 9.991777
(Iteration 1111
(Iteration 1121
                  5000)
                        loss: 5.878150
(Iteration 1131
                  5000)
                        loss: 0.295447
(Iteration 1141
                  5000)
                        loss: 2.295105
(Iteration 1151
                  5000)
                        loss: 0.180497
(Iteration 1161
                  5000)
                        loss: 19.845589
                  5000) loss: 3.390728
(Iteration 1171
(Iteration 1181
                  5000) loss: 5.576392
(Iteration 1191
                  5000)
                        loss: 6.027318
(Iteration 1201
                  5000)
                        loss: 1.031552
(Iteration 1211
                  5000)
                        loss: 0.574944
                  5000)
(Iteration 1221
                        loss: 0.266748
(Iteration 1231
                  5000)
                        loss: 0.517425
(Iteration 1241
                  5000) loss: 0.115634
(Iteration 1251
                  5000)
                        loss: 0.857323
(Iteration 1261
                  5000)
                        loss: 11.045198
(Iteration 1271
                        loss: 26.033632
(Iteration 1281
                  5000)
                        loss: 5.509893
(Iteration 1291
                  5000) loss: 5.609757
(Iteration 1301
                  5000)
                        loss: 7.111456
                  5000)
                        loss: 0.598661
(Iteration 1311
                        loss: 19.992622
(Iteration 1321
                  5000)
(Iteration 1331
                  5000)
                        loss: 2.082992
(Iteration 1341
                        loss: 4.956313
                  5000)
(Iteration 1351
                  5000)
                        loss: 0.214364
(Iteration 1361
                  5000)
                        loss: 0.750437
(Iteration 1371
                  5000)
                        loss: 0.400560
(Iteration 1381
                  5000) loss: 0.188203
(Iteration 1391
                  5000) loss: 0.574202
(Iteration 1401
                  5000)
                        loss: 0.292207
(Iteration 1411
                        loss: 0.089854
                  5000)
(Iteration 1421
                  5000)
                        loss: 0.568982
(Iteration 1431
                  5000) loss: 3.127827
(Iteration 1441
                  5000) loss: 0.206117
(Iteration 1451
                  5000) loss: 0.121819
(Iteration 1461
                  5000)
                        loss: 0.216600
(Iteration 1471
                  5000)
                        loss: 0.105744
(Iteration 1481
                  5000)
                        loss: 0.452972
(Iteration 1491
                  5000)
                        loss: 0.099933
(Iteration 1501
                  5000) loss: 0.253767
(Iteration 1511
                  5000)
                        loss: 0.397597
                  5000) loss: 0.262964
(Iteration 1521
(Iteration 1531
                  5000)
                        loss: 0.636551
(Iteration 1541
                  5000)
                        loss: 0.238412
(Iteration 1551
                  5000)
                        loss: 5.855202
(Iteration 1561
                  5000)
                        loss: 0.406963
(Iteration 1571
                  5000)
                        loss: 0.165135
(Iteration 1581
                  5000)
                        loss: 0.304915
(Iteration 1591
                  5000)
                        loss: 0.599466
(Iteration 1601
                  5000)
                        loss: 1.366495
(Iteration 1611
                  5000)
                        loss: 0.090246
(Iteration 1621
                  5000)
                        loss: 0.168135
(Iteration 1631
                  5000)
                        loss: 0.187476
(Iteration 1641
                  5000)
                        loss: 0.168081
(Iteration 1651
                  5000)
                        loss: 0.712782
(Iteration 1661
                  5000)
                        loss: 0.584735
(Iteration 1671
                        loss: 0.069395
(Iteration 1681
                        loss: 0.728173
                  5000)
(Iteration 1691
                  5000) loss: 0.069698
(Iteration 1701
                  5000)
                        loss: 0.063079
(Iteration 1711
                  5000) loss: 0.041461
(Iteration 1721
                  5000) loss: 0.562342
(Iteration 1731
                  5000)
                        loss: 0.072204
(Iteration 1741
                        loss: 0.548008
                  5000)
(Iteration 1751
                  5000)
                        loss: 0.038358
(Iteration 1761
                  5000) loss: 0.676519
(Iteration 1771
                  5000) loss: 0.033160
(Iteration 1781
                  5000) loss: 0.168352
(Iteration 1791
                  5000) loss: 0.272866
(Iteration 1801
                  5000)
                        loss: 0.644750
(Iteration 1811
                        loss: 0.466863
(Iteration 1821
                  5000)
                        loss: 0.331481
(Iteration 1831
                  5000) loss: 0.051933
(Iteration 1841
                  5000)
                        loss: 0.252053
(Iteration 1851
                  5000)
                        loss: 0.093088
                        loss: 0.265629
(Iteration 1861
                  5000)
(Iteration 1871
                  5000)
                        loss: 0.222783
(Iteration 1881
                  5000)
                        loss: 0.141227
(Iteration 1891
                  5000)
                        loss: 0.115807
(Iteration 1901
                  5000)
                        loss: 0.104958
(Iteration 1911
                  5000)
                        loss: 0.066892
                  5000)
(Iteration 1921
                        loss: 0.075094
(Iteration 1931
                  5000)
                        loss: 0.064218
(Iteration 1941
                  5000)
                        loss: 0.094453
(Iteration 1951
                  5000)
                        loss: 0.270463
(Iteration 1961
                  5000)
                        loss: 0.100966
(Iteration 1971
                  5000) loss: 0.096354
(Iteration 1981
                  5000)
                        loss: 0.107349
(Iteration 1991
                  5000)
                        loss: 0.160119
(Iteration 2001
                  5000)
                        loss: 0.054516
(Iteration 2011
                  5000)
                        loss: 0.125294
(Iteration 2021
                  5000) loss: 0.325757
(Iteration 2031
                  5000) loss: 0.077539
(Iteration 2041 /
                  5000) loss: 0.125360
(Iteration 2051 /
                  5000) loss: 0.080237
(Iteration 2061 /
                  5000) loss: 0.068496
(Iteration 2071 /
                  5000) loss: 0.072739
(Iteration 2081 /
                  5000) loss: 0.113197
```

```
(Iteration 2091 /
                  5000) loss: 0.080975
(Iteration 2101
                  5000) loss: 0.096208
(Iteration 2111
                  5000)
                        loss: 0.059108
(Iteration 2121
                  5000)
                        loss: 0.034324
(Iteration 2131
                        loss: 0.032771
                  5000)
(Iteration 2141
                  5000)
                        loss: 0.050986
(Iteration 2151
                  5000)
                        loss: 0.033320
(Iteration 2161
                  5000)
                        loss: 0.059138
(Iteration 2171
                  5000)
                        loss: 0.049778
(Iteration 2181
                  5000)
                        loss: 0.134106
(Iteration 2191
                  5000)
                        loss: 0.132563
(Iteration 2201
                  5000)
                        loss: 0.054139
(Iteration 2211
                  5000)
                        loss: 0.102579
(Iteration 2221
                  5000) loss: 0.044399
(Iteration 2231
                  5000) loss: 0.027050
(Iteration 2241
                  5000)
                        loss: 0.083712
(Iteration 2251
                  5000)
                        loss: 0.048737
(Iteration 2261
                  5000)
                        loss: 0.087930
                  5000)
(Iteration 2271
                        loss: 0.065641
(Iteration 2281
                  5000)
                        loss: 0.066378
(Iteration 2291
                  5000)
                        loss: 0.134018
(Iteration 2301
                  5000)
                        loss: 0.063139
(Iteration 2311
                  5000)
                        loss: 0.049333
(Iteration 2321
                         loss: 0.046218
(Iteration 2331
                  5000)
                        loss: 0.062667
                  5000)
(Iteration 2341
                        loss: 0.155200
(Iteration 2351
                  5000)
                        loss: 0.077619
(Iteration 2361
                  5000)
                        loss: 0.073163
(Iteration 2371
                        loss: 0.038135
                  5000)
(Iteration 2381
                  5000)
                        loss: 0.045802
(Iteration 2391
                        loss: 0.179533
                  5000)
(Iteration 2401
                  5000)
                        loss: 0.045145
(Iteration 2411
                  5000)
                        loss: 0.046927
(Iteration 2421
                  5000)
                        loss: 0.063020
(Iteration 2431
                  5000)
                        loss: 0.040154
(Iteration 2441
                        loss: 0.029081
                  5000)
(Iteration 2451
                  5000)
                        loss: 0.092092
(Iteration 2461
                        loss: 0.024319
                  5000)
(Iteration 2471
                  5000)
                        loss: 0.052775
(Iteration 2481
                  5000) loss: 0.051961
(Iteration 2491
                  5000)
                        loss: 0.043971
(Iteration 2501
                  5000)
                        loss: 0.074047
(Iteration 2511
                  5000)
                        loss: 0.037329
(Iteration 2521
                  5000)
                        loss: 0.069169
(Iteration 2531
                  5000)
                        loss: 0.049513
(Iteration 2541
                  5000)
                        loss: 0.041850
(Iteration 2551
                  5000) loss: 0.429351
(Iteration 2561
                  5000)
                        loss: 0.045865
                  5000)
(Iteration 2571
                        loss: 0.051164
(Iteration 2581
                        loss: 0.037816
                  5000)
(Iteration 2591
                  5000)
                        loss: 0.028778
(Iteration 2601
                  5000)
                        loss: 0.048968
(Iteration 2611
                  5000)
                        loss: 0.060120
(Iteration 2621
                  5000)
                        loss: 0.077502
(Iteration 2631
                  5000)
                        loss: 0.068717
(Iteration 2641
                  5000)
                        loss: 0.034594
(Iteration 2651
                  5000)
                         loss: 0.185056
(Iteration 2661
                  5000)
                        loss: 0.039449
(Iteration 2671
                  5000)
                        loss: 0.063915
(Iteration 2681
                  5000)
                        loss: 0.086589
(Iteration 2691
                  5000)
                        loss: 0.153010
(Iteration 2701
                  5000)
                        loss: 0.108605
                        loss: 0.043920
(Iteration 2711
                  5000)
(Iteration 2721
                        loss: 0.054018
(Iteration 2731
                        loss: 0.036808
                  5000)
                  5000)
(Iteration 2741
                        loss: 0.064860
(Iteration 2751
                  5000)
                        loss: 0.032127
(Iteration 2761
                  5000)
                        loss: 0.030468
(Iteration 2771
                  5000)
                        loss: 0.037008
(Iteration 2781
                  5000)
                        loss: 0.054076
(Iteration 2791
                  5000)
                        loss: 0.034199
(Iteration 2801
                  5000)
                        loss: 0.036159
(Iteration 2811
                  5000) loss: 0.030899
(Iteration 2821
                  5000)
                        loss: 0.070932
(Iteration 2831
                  5000)
                        loss: 0.024053
(Iteration 2841
                  5000)
                        loss: 0.035270
(Iteration 2851
                  5000)
                        loss: 0.025898
(Iteration 2861
                         loss: 0.088055
(Iteration 2871
                  5000)
                        loss: 0.058870
                  5000)
(Iteration 2881
                        loss: 0.102871
(Iteration 2891
                  5000)
                        loss: 0.020145
(Iteration 2901
                  5000)
                        loss: 0.076126
(Iteration 2911
                  5000)
                        loss: 0.084456
(Iteration 2921
                  5000)
                        loss: 0.058761
(Iteration 2931
                  5000)
                        loss: 0.040017
(Iteration 2941
                  5000)
                        loss: 0.051068
(Iteration 2951
                  5000)
                        loss: 0.042650
(Iteration 2961
                  5000)
                        loss: 0.059668
(Iteration 2971
                  5000)
                        loss: 0.039594
(Iteration 2981
                  5000)
                        loss: 0.074025
(Iteration 2991
                  5000)
                         loss: 0.059274
(Iteration 3001
                  5000)
                        loss: 0.053715
(Iteration 3011
                  5000)
                        loss: 0.033955
(Iteration 3021
                  5000) loss: 0.027305
(Iteration 3031
                        loss: 0.036434
                  5000)
(Iteration 3041
                  5000)
                        loss: 0.037711
(Iteration 3051
                  5000)
                        loss: 0.024567
(Iteration 3061
                  5000)
                        loss: 0.019330
(Iteration 3071
                  5000) loss: 0.056741
(Iteration 3081
                  5000)
                        loss: 0.033976
(Iteration 3091 /
                  5000) loss: 0.037970
(Iteration 3101 /
                  5000) loss: 0.041788
(Iteration 3111 /
                  5000) loss: 0.041199
(Iteration 3121 /
                  5000) loss: 0.042894
(Iteration 3131 /
                  5000) loss: 0.045536
```

```
(Iteration 3141 /
                  5000) loss: 0.024420
(Iteration 3151
                  5000) loss: 0.070113
(Iteration 3161
                  5000)
                        loss: 0.084537
(Iteration 3171
                  5000)
                        loss: 0.039280
(Iteration 3181
                        loss: 0.062656
                  5000)
(Iteration 3191
                  5000)
                        loss: 0.031054
(Iteration 3201 /
                  5000) loss: 0.018972
(Iteration 3211
                  5000)
                        loss: 0.066831
(Iteration 3221
                  5000)
                        loss: 0.050220
(Iteration 3231
                  5000)
                        loss: 0.040032
(Iteration 3241
                  5000)
                        loss: 0.054585
(Iteration 3251
                  5000)
                        loss: 0.039107
                  5000)
(Iteration 3261
                        loss: 0.036374
(Iteration 3271
                  5000) loss: 0.048054
(Iteration 3281
                  5000) loss: 0.031696
(Iteration 3291
                  5000)
                        loss: 0.074086
(Iteration 3301
                  5000)
                        loss: 0.049917
(Iteration 3311
                  5000)
                        loss: 0.052601
                  5000)
(Iteration 3321
                        loss: 0.037278
(Iteration 3331
                  5000)
                        loss: 0.028118
(Iteration 3341
                  5000)
                        loss: 0.016693
(Iteration 3351
                  5000)
                        loss: 0.058237
(Iteration 3361
                  5000)
                        loss: 0.023223
(Iteration 3371
                        loss: 0.034234
(Iteration 3381
                  5000)
                        loss: 0.023802
(Iteration 3391
                  5000)
                        loss: 0.024292
(Iteration 3401
                  5000)
                        loss: 0.041935
(Iteration 3411
                  5000)
                        loss: 0.028851
(Iteration 3421
                        loss: 0.016171
                  5000)
(Iteration 3431
                  5000)
                        loss: 0.035037
(Iteration 3441
                        loss: 0.045557
                  5000)
(Iteration 3451
                  5000)
                        loss: 0.026993
(Iteration 3461
                  5000)
                        loss: 0.034992
(Iteration 3471
                  5000)
                        loss: 0.034399
(Iteration 3481
                  5000) loss: 0.031287
(Iteration 3491
                  5000) loss: 0.049543
(Iteration 3501
                  5000)
                        loss: 0.041938
(Iteration 3511
                        loss: 0.026432
                  5000)
(Iteration 3521
                  5000)
                        loss: 0.014573
(Iteration 3531
                  5000) loss: 0.043989
(Iteration 3541
                  5000) loss: 0.034629
(Iteration 3551
                  5000) loss: 0.047457
(Iteration 3561
                  5000)
                        loss: 0.032869
(Iteration 3571
                        loss: 0.030975
                  5000)
(Iteration 3581
                  5000)
                        loss: 0.034374
(Iteration 3591
                  5000)
                        loss: 0.029360
(Iteration 3601
                  5000) loss: 0.034517
(Iteration 3611
                  5000)
                        loss: 0.032150
(Iteration 3621
                  5000)
                        loss: 0.074807
(Iteration 3631
                        loss: 0.045313
                  5000)
(Iteration 3641
                  5000)
                        loss: 0.035010
(Iteration 3651
                  5000)
                        loss: 0.047982
(Iteration 3661
                  5000)
                        loss: 0.030952
(Iteration 3671
                  5000)
                        loss: 0.021259
(Iteration 3681
                  5000)
                        loss: 0.053226
(Iteration 3691
                  5000)
                        loss: 0.064203
(Iteration 3701
                  5000)
                        loss: 0.024083
(Iteration 3711
                  5000)
                        loss: 0.021322
(Iteration 3721
                  5000)
                        loss: 0.041338
(Iteration 3731
                  5000)
                        loss: 0.023299
(Iteration 3741
                  5000)
                        loss: 0.014141
(Iteration 3751
                  5000)
                        loss: 0.028998
(Iteration 3761
                  5000)
                        loss: 0.030180
(Iteration 3771
                        loss: 0.024464
(Iteration 3781
                        loss: 0.021665
                  5000)
                  5000)
(Iteration 3791
                        loss: 0.029613
(Iteration 3801 /
                  5000)
                        loss: 0.022322
(Iteration 3811 /
                  5000) loss: 0.024273
(Iteration 3821
                  5000) loss: 0.011466
(Iteration 3831
                  5000)
                        loss: 0.039700
(Iteration 3841
                  5000)
                        loss: 0.038757
(Iteration 3851
                  5000)
                        loss: 0.037643
(Iteration 3861
                  5000) loss: 0.035864
(Iteration 3871
                  5000)
                        loss: 0.023433
(Iteration 3881
                  5000)
                        loss: 0.038423
(Iteration 3891
                  5000)
                        loss: 0.015724
(Iteration 3901
                  5000)
                        loss: 0.028129
(Iteration 3911
                        loss: 0.026116
(Iteration 3921
                  5000)
                        loss: 0.057014
(Iteration 3931
                  5000)
                        loss: 0.043385
(Iteration 3941
                  5000)
                        loss: 0.015868
(Iteration 3951
                  5000)
                        loss: 0.021217
(Iteration 3961
                        loss: 0.040107
                  5000)
(Iteration 3971
                  5000)
                        loss: 0.027008
(Iteration 3981
                  5000)
                        loss: 0.015068
(Iteration 3991
                  5000)
                        loss: 0.021460
(Iteration 4001
                  5000)
                        loss: 0.026698
(Iteration 4011
                  5000)
                        loss: 0.023678
(Iteration 4021
                  5000)
                        loss: 0.040953
(Iteration 4031
                  5000)
                        loss: 0.044832
(Iteration 4041
                  5000)
                        loss: 0.014249
(Iteration 4051
                  5000)
                        loss: 0.019687
(Iteration 4061
                  5000)
                        loss: 0.032964
(Iteration 4071
                  5000) loss: 0.029726
(Iteration 4081
                  5000)
                        loss: 0.029178
(Iteration 4091
                  5000)
                        loss: 0.033962
(Iteration 4101
                  5000)
                        loss: 0.024902
(Iteration 4111
                  5000)
                        loss: 0.010078
(Iteration 4121
                  5000) loss: 0.039600
(Iteration 4131
                  5000) loss: 0.015251
(Iteration 4141 /
                  5000) loss: 0.037625
(Iteration 4151 /
                  5000) loss: 0.026909
(Iteration 4161 /
                  5000) loss: 0.039265
(Iteration 4171 /
                  5000) loss: 0.067568
(Iteration 4181 /
                  5000) loss: 0.050671
```

		-			
(Iteration	4191	/	5000)	loss:	0.026822
(Iteration	4201	/	5000)	loss:	0.016860
(Iteration	4211	/	5000)	loss:	0.013854
(Iteration	4221	/	5000)	loss:	0.034788
(Iteration	4231	/	5000)	loss:	0.027025
(Iteration	4241	/	5000)	loss:	0.042791
(Iteration	4251	/	5000)	loss:	0.023338
(Iteration	4261	/	5000)	loss:	0.023062
(Iteration	4271	/	5000)	loss:	0.021530
(Iteration	4281	/	5000)	loss:	0.029499
(Iteration	4291	/	5000)	loss:	0.014466
(Iteration	4301	/	5000)	loss:	0.034534
(Iteration	4311	/	5000)	loss:	0.020793
(Iteration	4321	/	5000)	loss:	0.036590
(Iteration	4331		5000)	loss:	0.021338
•		/			0.021336
(Iteration	4341		5000)	loss:	
(Iteration	4351	1	5000)	loss:	0.021757
(Iteration	4361	/	5000)	loss:	0.015433
(Iteration	4371	/	5000)	loss:	0.035592
(Iteration	4381	/	5000)	loss:	0.012812
(Iteration	4391	/	5000)	loss:	0.020061
(Iteration	4401	/	5000)	loss:	0.016843
(Iteration	4411	/	5000)	loss:	0.047522
(Iteration	4421	/	5000)	loss:	0.020902
(Iteration	4431	/	5000)	loss:	0.021699
(Iteration	4441	/	5000)	loss:	0.027268
(Iteration	4451	/	5000)	loss:	0.036473
(Iteration	4461	/	5000)	loss:	0.019258
(Iteration	4471	/	5000)	loss:	0.032144
(Iteration	4481	/	5000)	loss:	0.021610
(Iteration	4491	/	5000)	loss:	0.040519
(Iteration	4501	/	5000)	loss:	0.020248
	4511				0.020246
(Iteration		/,	5000)	loss:	
(Iteration	4521	1	5000)	loss:	0.026689
(Iteration	4531	1	5000)	loss:	0.035013
(Iteration	4541	/	5000)	loss:	0.038092
(Iteration	4551	/	5000)	loss:	0.021795
(Iteration	4561	/	5000)	loss:	0.017306
(Iteration	4571	/	5000)	loss:	0.024408
(Iteration	4581	/	5000)	loss:	0.039591
(Iteration	4591	/	5000)	loss:	0.038009
(Iteration	4601	/	5000)	loss:	0.019653
(Iteration	4611	/	5000)	loss:	0.030744
(Iteration	4621	/	5000)	loss:	0.021717
(Iteration	4631	/	5000)	loss:	0.035041
(Iteration	4641	/	5000)	loss:	0.034605
(Iteration	4651	/	5000)	loss:	0.030661
(Iteration	4661	/	5000)	loss:	0.028397
(Iteration	4671	/	5000)	loss:	0.023510
(Iteration	4681	/	5000)	loss:	0.009300
(Iteration	4691	/	5000)	loss:	0.016868
(I CEL a CIOII					
•	4701	/			
(Iteration	4701	/,	5000)	loss:	0.018807
(Iteration (Iteration	4711	/	5000) 5000)	loss:	0.018807 0.038027
(Iteration (Iteration (Iteration	4711 4721	/	5000) 5000) 5000)	loss: loss: loss:	0.018807 0.038027 0.029547
(Iteration (Iteration (Iteration (Iteration	4711 4721 4731	//	5000) 5000) 5000) 5000)	loss: loss: loss:	0.018807 0.038027 0.029547 0.027049
(Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741	////	5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751	/////	5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761	//////	5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771	///////	5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781	/////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821 4831	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821 4831 4841	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.015210 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4821 4831 4841 4851	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4821 4831 4841 4851 4861	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4831 4841 4851 4861 4871	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.035850
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4821 4831 4851 4851 4871 4881	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01898 0.028656 0.011859 0.024290 0.024290 0.026768 0.035850 0.035850
(Iteration	4711 4721 4731 4741 4751 4771 4771 4781 4801 4821 4831 4841 4851 4851 4871 4881 4891	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.015210 0.016371 0.021306 0.01898 0.028656 0.011859 0.024290 0.026768 0.035850 0.035850 0.034955 0.024955 0.024955 0.029178
(Iteration	4711 4721 4731 4741 4751 4751 4771 4781 4891 4821 4821 4841 4851 4861 4871 4881 4891 4891	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.029920 0.019818 0.013648 0.034945 0.015210 0.01637 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.024955 0.027959 0.027959 0.029178
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4821 4831 4841 4851 4851 4851 4851 4851 4861 4871 4891 4901 4911	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027949 0.019818 0.013648 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.024955 0.024955 0.027959 0.029178 0.036602 0.036602
(Iteration	4711 4721 4731 4741 4761 4761 4771 4781 4891 4811 4851 4851 4871 4881 4891 4901 4901 4921 4931	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027949 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01859 0.024290 0.024290 0.024768 0.035850 0.035850 0.035850 0.024955 0.024955 0.024955 0.029178 0.03602 0.026819 0.019062
(Iteration	4711 4721 4731 4741 4751 4761 4771 4801 4801 4811 4841 4851 4861 4871 4891 4901 4921 4921 4931	111111111111111111111111111111111111111	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.015210 0.016371 0.021306 0.01898 0.028656 0.011859 0.024290 0.026768 0.035850 0.035850 0.024955 0.027959 0.027959 0.026819 0.03602 0.019062 0.019062
(Iteration	4711 4721 4731 4751 4761 4771 4781 4781 4801 4811 4821 4851 4851 4861 4871 4891 4991 4991 4991 4991	11111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.02495 0.027959 0.027959 0.026819 0.026819 0.026819 0.026819
(Iteration	4711 4721 4731 4741 4751 4761 4771 4801 4821 4831 4841 4851 4851 4871 4881 4891 4991 4931 4941 4941 4951	1111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.024955 0.024955 0.029178 0.026819 0.026819 0.026819 0.025788
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4821 4831 4861 4871 4861 4901 4911 4921 4931 4951 4951 4971	11111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01859 0.024290 0.024290 0.024768 0.035850 0.035850 0.034955 0.024955 0.024955 0.024955 0.029178 0.03602 0.025788 0.034722 0.042984 0.014903
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4781 4881 4881 4881 4861 4871 4901 4901 4911 4921 4941 4951 4961 4961 4981	11111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.027959 0.0249178 0.026819 0.026819 0.025788 0.035850 0.037959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.025788 0.034722 0.042984 0.042984 0.042984 0.042984 0.042983 0.033723
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4821 4831 4861 4871 4861 4901 4911 4921 4931 4951 4951 4971	11111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01859 0.024290 0.024290 0.024768 0.035850 0.035850 0.034955 0.024955 0.024955 0.024955 0.029178 0.03602 0.025788 0.034722 0.042984 0.014903



## **Test-time sampling**

Unlike classification models, image captioning models behave very differently at training time and at test time. At training time, we have access to the ground-truth caption, so we feed ground-truth words as input to the RNN at each timestep. At test time, we sample from the distribution over the vocabulary at each timestep, and feed the sample as input to the RNN at the next timestep.

In the file cs231n/classifiers/rnn.py, implement the sample method for test-time sampling. After doing so, run the following to sample from your overfitted model on both training and validation data. The samples on training data should be very good; the samples on validation data probably won't make sense.

Note: Some of the URLs are missing and will throw an error; re-run this cell until the output is at least 2 good caption samples.

```
In [17]: for split in ['train', 'val']:
    minibatch = sample_coco_minibatch(small_data, split=split, batch_size=2)
    gt_captions, features, urls = minibatch
    gt_captions = decode_captions(gt_captions, data['idx_to_word'])

sample_captions = small_rnn_model.sample(features)
    sample_captions = decode_captions(sample_captions, data['idx_to_word'])

for gt_caption, sample_caption, url in zip(gt_captions, sample_captions, urls):
    plt.imshow(image_from_url(url))
    plt.title('%s\n%s\nGT:%s' % (split, sample_caption, gt_caption))
    plt.axis('off')
    plt.show()
```

train

GT:<START> a woman is kneeling near some large <UNK> of food <END>



train

GT:<START> a group of men riding in a boat across a lake <END>



val

GT:<START> the man in the helmet is jumping while wearing <UNK> <UNK> <END>



va

GT:<START> a little boy sitting on the stairs with a racquet <END>

