Image Captioning with RNNs

In this exercise you will implement a vanilla recurrent neural networks and use them it to train a model that can generate novel captions for images.

```
In [1]: # As usual, a bit of setup
        from __future__ import print_function
        import time, os, json
        import numpy as np
        import matplotlib.pyplot as plt
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
        from cs231n.rnn_layers import
        from cs231n.captioning_solver import CaptioningSolver
        from cs231n.classifiers.rnn import CaptioningRNN
        from cs231n.coco_utils import load_coco_data, sample_coco_minibatch, decode_captions
        from cs231n.image_utils import image_from_url
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
                returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(le-8, np.abs(x) + np.abs(y))))
```

Install h5py

The COCO dataset we will be using is stored in HDF5 format. To load HDF5 files, we will need to install the h5py Python package. From the command line, run:

pip install h5py

If you receive a permissions error, you may need to run the command as root:

sudo pip install h5py

You can also run commands directly from the Jupyter notebook by prefixing the command with the "!" character:

```
In [2]: | 1pip install h5py | Requirement already satisfied: h5py in /miniconda3/envs/cs4803/lib/python3.6/site-packages (2.10.0) | Requirement already satisfied: six in /miniconda3/envs/cs4803/lib/python3.6/site-packages (from h5py) (1.14.0) | Requirement already satisfied: numpy>=1.7 in /miniconda3/envs/cs4803/lib/python3.6/site-packages (from h5py) (1.18.1)
```

Microsoft COCO

For this exercise we will use the 2014 release of the Microsoft COCO dataset (http://mscoco.org/) which has become the standard testbed for image captioning. The dataset consists of 80,000 training images and 40,000 validation images, each annotated with 5 captions written by workers on Amazon Mechanical Turk.

You should have already downloaded the data by changing to the cs231n/datasets directory and running the script get_assignment3_data.sh . If you haven't yet done so, run that script now. Warning: the COCO data download is ~1GB.

We have preprocessed the data and extracted features for you already. For all images we have extracted features from the fc7 layer of the VGG-16 network pretrained on ImageNet; these features are stored in the files train2014_vgg16_fc7.h5 and val2014_vgg16_fc7.h5 respectively. To cut down on processing time and memory requirements, we have reduced the dimensionality of the features from 4096 to 512; these features can be found in the files train2014_vgg16_fc7_pca.h5 and val2014_vgg16_fc7_pca.h5.

The raw images take up a lot of space (nearly 20GB) so we have not included them in the download. However all images are taken from Flickr, and URLs of the training and validation images are stored in the files train2014_urls.txt and val2014_urls.txt respectively. This allows you to download images on the fly for visualization. Since images are downloaded on-the-fly, you must be connected to the internet to view images.

Dealing with strings is inefficient, so we will work with an encoded version of the captions. Each word is assigned an integer ID, allowing us to represent a caption by a sequence of integers. The mapping between integer IDs and words is in the file coco2014_vocab.json, and you can use the function decode_captions from the file cs231n/coco_utils.py to convert numpy arrays of integer IDs back into strings.

There are a couple special tokens that we add to the vocabulary. We prepend a special <START> token and append an <END> token to the beginning and end of each caption respectively. Rare words are replaced with a special <UNK> token (for "unknown"). In addition, since we want to train with minibatches containing captions of different lengths, we pad short captions with a special <NULL> token after the <END> token and don't compute loss or gradient for <NULL> tokens. Since they are a bit of a pain, we have taken care of all implementation details around special tokens for you.

You can load all of the MS-COCO data (captions, features, URLs, and vocabulary) using the load coco data function from the file cs231n/coco utils.py . Run the following cell to do so:

Look at the data

It is always a good idea to look at examples from the dataset before working with it.

train_urls <class 'numpy.ndarray'> (82783,) <U63
val_urls <class 'numpy.ndarray'> (40504,) <U63</pre>

You can use the sample_coco_minibatch function from the file cs231n/coco_utils.py to sample minibatches of data from the data structure returned from load_coco_data. Run the following to sample a small minibatch of training data and show the images and their captions. Running it multiple times and looking at the results helps you to get a sense of the dataset.

Note that we decode the captions using the decode_captions function and that we download the images on-the-fly using their Flickr URL, so you must be connected to the internet to view images.

```
In [4]: # Sample a minibatch and show the images and captions
batch_size = 3

captions, features, urls = sample_coco_minibatch(data, batch_size=batch_size)
for i, (caption, url) in enumerate(zip(captions, urls)):
    plt.imshow(image_from_url(url))
    plt.axis('off')
    caption_str = decode_captions(caption, data['idx_to_word'])
    plt.title(caption_str)
    plt.show()
```

<START> a man wearing a <UNK> <UNK> looking a at a laptop <END>



<START> the dog <UNK> the frisbee in the event outside <END>



<START> a girl is standing on top of a bathroom counter <END>



Recurrent Neural Networks

As discussed in lecture, we will use recurrent neural network (RNN) language models for image captioning. The file cs231n/rnn_layers.py contains implementations of different layer types that are needed for recurrent neural networks, and the file cs231n/classifiers/rnn.py uses these layers to implement an image captioning model.

We will first implement different types of RNN layers in $cs231n/rnn_layers.py$.

Vanilla RNN: step forward

Open the file cs231n/rnn_layers.py . This file implements the forward and backward passes for different types of layers that are commonly used in recurrent neural networks.

First implement the function rnn step forward which implements the forward pass for a single timestep of a vanilla recurrent neural network. After doing so run the following to check your implementation. You should see errors less than 1e-8.

```
In [5]: N, D, H = 3, 10, 4
         x = np.linspace(-0.4, 0.7, num=N*D).reshape(N, D)
         prev_h = np.linspace(-0.2, 0.5, num=N*H).reshape(N, H)
         Wx = np.linspace(-0.1, 0.9, num=D*H).reshape(D, H)
         Wh = np.linspace(-0.3, 0.7, num=H*H).reshape(H, H)
         b = np.linspace(-0.2, 0.4, num=H)
         next_h, _ = rnn_step_forward(x, prev_h, Wx, Wh, b)
         expected_next_h = np.asarray([
           [-0.58172089, -0.50182032, -0.41232771, -0.31410098],
           [ 0.66854692, 0.79562378, 0.87755553, 0.92795967], [ 0.97934501, 0.99144213, 0.99646691, 0.99854353]])
        print('next_h error: ', rel_error(expected_next_h, next_h))
```

next h error: 6.292421426471037e-09

Vanilla RNN: step backward

In the file cs231n/rnn_layers.py implement the rnn_step_backward function. After doing so run the following to numerically gradient check your implementation. You should see errors less than 1e-8.

```
In [6]: from cs231n.rnn_layers import rnn_step_forward, rnn_step_backward
         np.random.seed(231)
        N, D, H = 4, 5, 6
         x = np.random.randn(N, D)
        h = np.random.randn(N, H)
         Wx = np.random.randn(D, H)
         Wh = np.random.randn(H, H)
        b = np.random.randn(H)
        out, cache = rnn_step_forward(x, h, Wx, Wh, b)
        dnext h = np.random.randn(*out.shape)
         fx = lambda x: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fh = lambda prev_h: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fWx = lambda Wx: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fWh = lambda Wh: rnn_step_forward(x, h, Wx, Wh, b)[0]
         fb = lambda b: rnn_step_forward(x, h, Wx, Wh, b)[0]
         dx_num = eval_numerical_gradient_array(fx, x, dnext_h)
         dprev_h_num = eval_numerical_gradient_array(fh, h, dnext_h)
         dWx_num = eval_numerical_gradient_array(fWx, Wx, dnext_h)
         dWh_num = eval_numerical_gradient_array(fWh, Wh, dnext_h)
        db_num = eval_numerical_gradient_array(fb, b, dnext_h)
        dx, dprev_h, dWx, dWh, db = rnn_step_backward(dnext_h, cache)
         print('dx error: ', rel_error(dx_num, dx))
         print('dprev_h error: ', rel_error(dprev_h_num, dprev_h))
        print('dwx error: ', rel_error(dwx_num, dwx))
print('dwh error: ', rel_error(dwh_num, dwh))
print('db error: ', rel_error(db_num, db))
        N 4, D 5, H 6
        dnext_h: (N, H) (4, 6)
        x: (N, D) (4, 5)
        prev_h: (N, H) (4, 6)
        Wx: (D, H) (5, 6)
        Wh: (H, H) (6, 6)
        dTanH: (N, H) (4, 6)
        dSum: (N, H) (4, 6)
```

dx: (4, 5)dprev_h: (4, 6) dWx: (5, 6) dWh: (6, 6) db: (6,) dx error: 2.99311613693832e-10 dprev h error: 2.633205333189269e-10 dWx error: 9.684083573724284e-10 dWh error: 3.355162782632426e-10 db error: 1.5956895526227225e-11

Vanilla RNN: forward

Now that you have implemented the forward and backward passes for a single timestep of a vanilla RNN, you will combine these pieces to implement a RNN that process an entire sequence of data.

In the file cs231n/rnn layers.py, implement the function rnn_forward. This should be implemented using the rnn_step_forward function that you defined above. After doing so run the following to check your implementation. You should see errors less than 1e-7.

h error: 7.728466180186066e-08

Vanilla RNN: backward

In the file cs231n/rnn_layers.py, implement the backward pass for a vanilla RNN in the function rnn_backward. This should run back-propagation over the entire sequence, calling into the rnn_step_backward function that you defined above. You should see errors less than 5e-7.

```
In [8]: np.random.seed(231)
          N, D, T, H = 2, 3, 10, 5
          x = np.random.randn(N, T, D)
          h0 = np.random.randn(N, H)
          Wx = np.random.randn(D, H)
          Wh = np.random.randn(H, H)
         b = np.random.randn(H)
          out, cache = rnn_forward(x, h0, Wx, Wh, b)
          dout = np.random.randn(*out.shape)
          dx, dh0, dWx, dWh, db = rnn backward(dout, cache)
          fx = lambda x: rnn forward(x, h0, Wx, Wh, b)[0]
          fh0 = lambda \ h0: rnn_forward(x, h0, Wx, Wh, b)[0]
          fWx = lambda Wx: rnn_forward(x, h0, Wx, Wh, b)[0]
          fWh = lambda Wh: rnn_forward(x, h0, Wx, Wh, b)[0]
          fb = lambda b: rnn_forward(x, h0, Wx, Wh, b)[0]
          dx_num = eval_numerical_gradient_array(fx, x, dout)
          dh0_num = eval_numerical_gradient_array(fh0, h0, dout)
          dWx_num = eval_numerical_gradient_array(fWx, Wx, dout)
          dWh_num = eval_numerical_gradient_array(fWh, Wh, dout)
          db_num = eval_numerical_gradient_array(fb, b, dout)
          # print(f"correct dx: {dx num}")
          # print(f"reagans dx: {dx}")
         # print('rreagans ax: {ax; } ox; )
print('dx error: ', rel_error(dx_num, dx))
print('dh0 error: ', rel_error(dh0_num, dh0))
print('dWx error: ', rel_error(dWx_num, dWx))
print('dWh error: ', rel_error(dWh_num, dWh))
print('db error: ', rel_error(db_num, db))
         dx error: 2.3969112188524054e-09
         dh0 error: 3.3796875007867145e-09
          dWx error: 7.221000108504998e-09
         dWh error: 1.284586847530015e-07
```

Word embedding: forward

db error: 4.675767378424171e-10

In deep learning systems, we commonly represent words using vectors. Each word of the vocabulary will be associated with a vector, and these vectors will be learned jointly with the rest of the system.

In the file cs231n/rnn_layers.py, implement the function word_embedding_forward to convert words (represented by integers) into vectors. Run the following to check your implementation. You should see error around 1e-8.

out error: 1.000000094736443e-08

Word embedding: backward

Implement the backward pass for the word embedding function in the function word_embedding_backward. After doing so run the following to numerically gradient check your implementation. You should see errors less than 1e-11.

```
In [10]: np.random.seed(231)

N, T, V, D = 50, 3, 5, 6
    x = np.random.randint(V, size=(N, T))
    W = np.random.randn(V, D)

out, cache = word_embedding_forward(x, W)
    dout = np.random.randn(*out.shape)
    dW = word_embedding_backward(dout, cache)

f = lambda W: word_embedding_forward(x, W)[0]
    dW_num = eval_numerical_gradient_array(f, W, dout)

print('dW error: ', rel_error(dW, dW_num))

dW error: 3.2774595693100364e-12
```

Temporal Affine layer

At every timestep we use an affine function to transform the RNN hidden vector at that timestep into scores for each word in the vocabulary. Because this is very similar to the affine layer that you implemented in assignment 2, we have provided this function for you in the temporal_affine_forward and temporal_affine_backward functions in the file cs231n/rnn_layers.py . Run the following to perform numeric gradient checking on the implementation. You should see errors less than 1e-9.

```
In [11]: np.random.seed(231)
           # Gradient check for temporal affine layer
           N, T, D, M = 2, 3, 4, 5
          x = np.random.randn(N, T, D)
           w = np.random.randn(D, M)
          b = np.random.randn(M)
           out, cache = temporal_affine_forward(x, w, b)
           dout = np.random.randn(*out.shape)
           fx = lambda x: temporal affine forward(x, w, b)[0]
           fw = lambda w: temporal_affine_forward(x, w, b)[0]
           fb = lambda b: temporal_affine_forward(x, w, b)[0]
           dx_num = eval_numerical_gradient_array(fx, x, dout)
           dw_num = eval_numerical_gradient_array(fw, w, dout)
           db_num = eval_numerical_gradient_array(fb, b, dout)
           dx, dw, db = temporal_affine_backward(dout, cache)
          print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
          dx error: 2.9215854231394017e-10
          dw error: 1.5772169135951167e-10
db error: 3.252200556967514e-11
```

Temporal Softmax loss

In an RNN language model, at every timestep we produce a score for each word in the vocabulary. We know the ground-truth word at each timestep, so we use a softmax loss function to compute loss and gradient at each timestep. We sum the losses over time and average them over the minibatch.

However there is one wrinkle: since we operate over minibatches and different captions may have different lengths, we append <NULL> tokens to the end of each caption so they all have the same length. We don't want these <NULL> tokens to count toward the loss or gradient, so in addition to scores and ground-truth labels our loss function also accepts a mask array that tells it which elements of the scores count towards the loss.

Since this is very similar to the softmax loss function you implemented in assignment 1, we have implemented this loss function for you; look at the temporal_softmax_loss function in the file cs231n/rnn layers.py.

Run the following cell to sanity check the loss and perform numeric gradient checking on the function. You should see an error for dx less than 1e-7.

```
In [12]: # Sanity check for temporal softmax loss
         from cs231n.rnn_layers import temporal_softmax_loss
          N, T, V = 100, 1, 10
          def check_loss(N, T, V, p):
              x = 0.001 * np.random.randn(N, T, V)
              y = np.random.randint(V, size=(N, T))
              mask = np.random.rand(N, T) <= p
              print(temporal_softmax_loss(x, y, mask)[0])
          check_loss(100, 1, 10, 1.0)  # Should be about 2.3
check_loss(100, 10, 10, 1.0)  # Should be about 23
          check_loss(5000, 10, 10, 0.1) # Should be about 2.3
          # Gradient check for temporal softmax loss
         N. T. V = 7.8.9
          x = np.random.randn(N, T, V)
          y = np.random.randint(V, size=(N, T))
          mask = (np.random.rand(N, T) > 0.5)
          loss, dx = temporal_softmax_loss(x, y, mask, verbose=False)
          dx_num = eval_numerical_gradient(lambda x: temporal_softmax_loss(x, y, mask)[0], x, verbose=False)
          print('dx error: ', rel error(dx, dx num))
         2.3027781774290146
         23.025985953127226
         2.2643611790293394
```

RNN for image captioning

dx error: 2.583585303524283e-08

Now that you have implemented the necessary layers, you can combine them to build an image captioning model. Open the file cs231n/classifiers/rnn.py and look at the CaptioningRNN class.

Implement the forward and backward pass of the model in the loss function. For now you only need to implement the case where cell_type='rnn' for vanialla RNNs; you will implement the LSTM case later. After doing so, run the following to check your forward pass using a small test case; you should see error less than le-l0.

```
In [13]: N, D, W, H = 10, 20, 30, 40
         word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
         V = len(word_to_idx)
         T = 13
         model = CaptioningRNN(word to idx,
                    input dim=D.
                    wordvec_dim=W,
                    hidden_dim=H,
                    cell_type='rnn'
                    dtype=np.float64)
          # Set all model parameters to fixed values
          for k, v in model.params.items():
             model.params[k] = np.linspace(-1.4, 1.3, num=v.size).reshape(*v.shape)
          features = np.linspace(-1.5, 0.3, num=(N * D)).reshape(N, D)
         captions = (np.arange(N * T) % V).reshape(N, T)
          loss. grads = model.loss(features. captions. verbose=False)
         expected_loss = 9.83235591003
         print('loss: ', loss)
         print('expected loss: ', expected_loss)
         print('difference: ', abs(loss - expected_loss))
         loss: 9.832355910027388
         expected loss: 9.83235591003
difference: 2.611244553918368e-12
```

Run the following cell to perform numeric gradient checking on the CaptioningRNN class; you should errors around 5e-6 or less.

```
In [14]: np.random.seed(231)
           batch_size = 2
           timesteps = 3
           input_dim = 4
           wordvec_dim = 5
           hidden_dim = 6
           word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
           vocab_size = len(word_to_idx)
           captions = np.random.randint(vocab_size, size=(batch_size, timesteps))
features = np.random.randn(batch_size, input_dim)
           model = CaptioningRNN(word_to_idx,
                       input_dim=input_dim,
                      wordvec_dim=wordvec_dim,
hidden_dim=hidden_dim,
                      cell_type='rnn',
                      dtype=np.float64,
           loss, grads = model.loss(features, captions)
           for param_name in sorted(grads):
                f = lambda _: model.loss(features, captions)[0]
                param_grad_num = eval_numerical_gradient(f, model.params[param_name], verbose=False, h=1e-6)
               e = rel_error(param_grad_num, grads[param_name])
print('%s relative error: %e' % (param_name, e))
           W embed relative error: 2.331072e-09
```

W_embed relative error: 2.331072e-09
W_proj relative error: 9.974424e-09
W_vocab relative error: 4.274378e-09
Wh relative error: 5.954804e-09
Wx relative error: 8.455229e-07
b relative error: 9.727211e-10
b_proj relative error: 1.991603e-08
b_vocab relative error: 6.918525e-11

Overfit small data

Similar to the Solver class that we used to train image classification models on the previous assignment, on this assignment we use a CaptioningSolver class to train image captioning models. Open the file cs231n/captioning_solver.py and read through the CaptioningSolver class; it should look very familiar.

Once you have familiarized yourself with the API, run the following to make sure your model overfit a small sample of 100 training examples. You should see losses of less than 0.1.

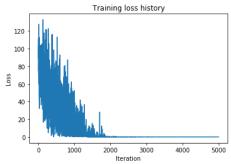
```
(Iteration 1 / 5000) loss: 89.538734
(Iteration 11 / 5000) loss: 89.436142
(Iteration 21 / 5000) loss: 41.782749
                5000)
(Iteration 31 /
                      loss: 97.063431
(Iteration 41 / 5000)
                      loss: 98.784393
(Iteration 51 / 5000)
                      loss: 103.743103
(Iteration 61 / 5000)
                      loss: 76.610619
(Iteration 71 / 5000)
                      loss: 46.232353
(Iteration 81 /
               5000)
                      loss: 47.529114
(Iteration 91 / 5000) loss: 51.454792
(Iteration 101 /
                 5000) loss: 41.202644
(Iteration 111 /
                 5000) loss: 103.156456
(Iteration 121 /
                 5000) loss: 63.173302
(Iteration 131 /
                 5000) loss: 37.913567
(Iteration 141 /
                 5000) loss: 99.907059
                 5000) loss: 85.212387
(Iteration 151
                 5000) loss: 57.529522
(Iteration 161
(Iteration 171
                       loss: 21.788654
                 5000)
(Iteration 181
                       loss: 27.034616
                 5000)
(Iteration 191
                 5000) loss: 29.954041
(Iteration 201
                 5000) loss: 20.125360
(Iteration 211
                 5000) loss: 42,703835
                 5000) loss: 50.779907
(Iteration 221
(Iteration 231
                 5000)
                       loss: 61.426395
(Iteration 241
                 5000)
                       loss: 64.845703
(Iteration 251
                 5000)
                       loss: 39.612869
(Iteration 261
                 5000) loss: 45.992516
(Iteration 271
                 5000) loss: 14.378930
(Iteration 281 /
                 5000) loss: 22.156929
(Iteration 291
                 5000) loss: 9.530903
(Iteration 301
                 5000) loss: 21.537636
(Iteration 311
                       loss: 28.899513
(Iteration 321
                 5000)
                       loss: 71.319817
(Iteration 331
                 5000) loss: 14.083916
(Iteration 341 /
                 5000) loss: 45.902863
(Iteration 351 /
                 5000) loss: 9.437120
(Iteration 361
                 5000) loss: 54.087708
(Iteration 371
                 5000) loss: 16.939861
(Iteration 381
                 5000) loss: 66.815460
(Iteration 391
                 5000) loss: 30.158628
(Iteration 401
                 5000) loss: 55.309616
(Iteration 411
                 5000) loss: 2.467841
                 5000) loss: 16.460686
(Iteration 421 /
(Iteration 431
                 5000) loss: 45.130829
(Iteration 441
                 5000) loss: 53.272102
                       loss: 51.743515
(Iteration 451
                 5000)
(Iteration 461
                 5000)
                       loss: 33.269196
(Iteration 471
                 5000) loss: 51.398998
(Iteration 481
                 5000) loss: 35.818146
(Iteration 491
                 5000) loss: 15.107388
                       loss: 54.070717
(Iteration 501
                 5000)
(Iteration 511
                 5000)
                       loss: 62.900036
(Iteration 521
                 5000) loss: 41.764988
(Iteration 531
                 5000)
                       loss: 12.469192
(Iteration 541
                 5000) loss: 60.341114
(Iteration 551
                 5000) loss: 25.075655
                 5000) loss: 6.382981
(Iteration 561
(Iteration 571
                 5000) loss: 2.519198
(Iteration 581
                 5000)
                       loss: 40.610477
(Iteration 591
                 5000) loss: 53.783371
(Iteration 601
                 5000) loss: 10.248645
(Iteration 611 /
                 5000) loss: 4.130352
(Iteration 621
                 5000) loss: 24.409468
(Iteration 631 /
                 5000) loss: 16.780783
(Iteration 641
                 5000) loss: 32.698448
(Iteration 651
                 5000)
                       loss: 8.323520
(Iteration 661 /
                 5000) loss: 48.345177
(Iteration 671
                 5000) loss: 55.929413
                 5000) loss: 37.345932
(Iteration 681
(Iteration 691
                 5000) loss: 47.278160
(Iteration 701
                 5000) loss: 9.752253
(Iteration 711
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(Iteration 721
                       loss: 80.255623
                 5000)
(Iteration 731
                 5000) loss: 5.435860
(Iteration 741
                 5000) loss: 27.480110
(Iteration 751
                 5000) loss: 14.788023
(Iteration 761
                 5000) loss: 13.484448
(Iteration 771
                 5000) loss: 40.191666
                       loss: 28.038023
(Iteration 781
                 5000)
(Iteration 791
                 5000)
                       loss: 17.346283
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(Iteration 831
                 5000) loss: 3.729098
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(Iteration 851
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(Iteration 861
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                       loss: 4.385690
(Iteration 871
                 5000) loss: 19.940441
(Iteration 881 /
                 5000) loss: 47.771824
(Iteration 891
                 5000) loss: 7.549527
(Iteration 901
                 5000) loss: 34.210579
(Iteration 911
                 5000) loss: 7.658073
(Iteration 921
                 5000) loss: 4.147122
(Iteration 931
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(Iteration 961 /
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(Iteration 971
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(Iteration 981
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                 5000)
(Iteration 991 /
                 5000) loss: 15.993933
(Iteration 1001 / 5000) loss: 3.902276
(Iteration 1011 / 5000) loss: 14.404881
(Iteration 1021 /
                  5000) loss: 1.892224
(Iteration 1031 / 5000) loss: 9.150167
```

```
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(Iteration 1051 /
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(Iteration 1061
                  5000)
                        loss: 5.039266
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(Iteration 1081
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                  5000)
(Iteration 1091
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                        loss: 6.668529
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                  5000)
                        loss: 9.991777
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(Iteration 1181
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                        loss: 6.027318
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(Iteration 1421
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(Iteration 1491
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                  5000)
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(Iteration 1791
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(Iteration 1821
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(Iteration 1871
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(Iteration 1891
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                        loss: 0.115807
(Iteration 1901
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                        loss: 0.104958
(Iteration 1911
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                        loss: 0.066892
                  5000)
(Iteration 1921
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(Iteration 1931
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                        loss: 0.064218
(Iteration 1941
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                        loss: 0.094453
(Iteration 1951
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                        loss: 0.270463
(Iteration 1961
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                        loss: 0.100966
(Iteration 1971
                  5000) loss: 0.096354
(Iteration 1981
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                        loss: 0.107349
(Iteration 1991
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                        loss: 0.160119
(Iteration 2001
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                        loss: 0.054516
(Iteration 2011
                  5000)
                        loss: 0.125294
(Iteration 2021
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(Iteration 2031
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(Iteration 2041 /
                  5000) loss: 0.125360
(Iteration 2051 /
                  5000) loss: 0.080237
(Iteration 2061 /
                  5000) loss: 0.068496
(Iteration 2071 /
                  5000) loss: 0.072739
(Iteration 2081 /
                  5000) loss: 0.113197
```

```
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                  5000) loss: 0.096208
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                  5000)
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                        loss: 0.034324
(Iteration 2131
                        loss: 0.032771
                  5000)
(Iteration 2141
                  5000)
                        loss: 0.050986
(Iteration 2151
                  5000)
                        loss: 0.033320
(Iteration 2161
                  5000)
                        loss: 0.059138
(Iteration 2171
                  5000)
                        loss: 0.049778
(Iteration 2181
                  5000)
                        loss: 0.134106
(Iteration 2191
                  5000)
                        loss: 0.132563
(Iteration 2201
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                        loss: 0.054139
(Iteration 2211
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                        loss: 0.102579
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                  5000) loss: 0.044399
(Iteration 2231
                  5000) loss: 0.027050
(Iteration 2241
                  5000)
                        loss: 0.083712
(Iteration 2251
                  5000)
                        loss: 0.048737
(Iteration 2261
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                        loss: 0.087930
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(Iteration 2301
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(Iteration 2311
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(Iteration 2321
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(Iteration 2331
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(Iteration 2561
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                        loss: 0.045865
                  5000)
(Iteration 2571
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(Iteration 2581
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                        loss: 0.035270
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                        loss: 0.084456
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                         loss: 0.059274
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                        loss: 0.053715
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(Iteration 3091 /
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(Iteration 3101 /
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(Iteration 3111 /
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(Iteration 3131 /
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```

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(Iteration 3141 /
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(Iteration 3171
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                        loss: 0.039280
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                  5000)
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(Iteration 3251
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(Iteration 4161 /
                  5000) loss: 0.039265
(Iteration 4171 /
                  5000) loss: 0.067568
(Iteration 4181 /
                  5000) loss: 0.050671
```

		-			
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(Iteration	4331		5000)	loss:	0.021338
•		/			0.021336
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	4511				0.020246
(Iteration		/,	5000)	loss:	
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(Iteration	4591	/	5000)	loss:	0.038009
(Iteration	4601	/	5000)	loss:	0.019653
(Iteration	4611	/	5000)	loss:	0.030744
(Iteration	4621	/	5000)	loss:	0.021717
(Iteration	4631	/	5000)	loss:	0.035041
(Iteration	4641	/	5000)	loss:	0.034605
(Iteration	4651	/	5000)	loss:	0.030661
(Iteration	4661	/	5000)	loss:	0.028397
(Iteration	4671	/	5000)	loss:	0.023510
(Iteration	4681	/	5000)	loss:	0.009300
(Iteration	4691	/	5000)	loss:	0.016868
(I CEL a CIOII					
•	4701	/			
(Iteration	4701	/,	5000)	loss:	0.018807
(Iteration (Iteration	4711	/	5000) 5000)	loss:	0.018807 0.038027
(Iteration (Iteration (Iteration	4711 4721	/	5000) 5000) 5000)	loss: loss: loss:	0.018807 0.038027 0.029547
(Iteration (Iteration (Iteration (Iteration	4711 4721 4731	//	5000) 5000) 5000) 5000)	loss: loss: loss:	0.018807 0.038027 0.029547 0.027049
(Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741	////	5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751	/////	5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761	//////	5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771	///////	5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781	/////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988
(Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821 4831	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4791 4801 4811 4821 4831 4841	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.015210 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290
(Iteration (Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4821 4831 4841 4851	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768
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(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4831 4841 4851 4861 4871	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.035850
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4811 4821 4831 4851 4851 4871 4881	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01898 0.028656 0.011859 0.024290 0.024290 0.026768 0.035850 0.035850
(Iteration	4711 4721 4731 4741 4751 4771 4771 4781 4801 4821 4831 4841 4851 4851 4871 4881 4891	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.027049 0.019818 0.013648 0.015210 0.016371 0.021306 0.01898 0.028656 0.011859 0.024290 0.026768 0.035850 0.035850 0.034955 0.024955 0.024955 0.029178
(Iteration	4711 4721 4731 4741 4751 4751 4771 4781 4891 4821 4821 4841 4851 4861 4871 4881 4891 4891	///////////////////////////////////////	5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.029920 0.019818 0.013648 0.034945 0.015210 0.01637 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.024955 0.027959 0.027959 0.029178
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(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4801 4821 4831 4861 4871 4861 4901 4911 4921 4931 4951 4951 4971	11111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.027049 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.01859 0.024290 0.024290 0.024768 0.035850 0.035850 0.034955 0.024955 0.024955 0.024955 0.029178 0.03602 0.025788 0.034722 0.042984 0.014903
(Iteration	4711 4721 4731 4741 4751 4761 4771 4781 4781 4881 4881 4881 4861 4871 4901 4901 4911 4921 4941 4951 4961 4961 4981	11111111111111111111111111111111	5000) 5000)	loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss: loss:	0.018807 0.038027 0.029547 0.029920 0.019818 0.013648 0.034945 0.015210 0.016371 0.021306 0.018988 0.028656 0.011859 0.024290 0.026768 0.035850 0.031955 0.027959 0.0249178 0.026819 0.026819 0.025788 0.035850 0.037959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.027959 0.025788 0.034722 0.042984 0.042984 0.042984 0.042984 0.042983 0.033723
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Test-time sampling

Unlike classification models, image captioning models behave very differently at training time and at test time. At training time, we have access to the ground-truth caption, so we feed ground-truth words as input to the RNN at each timestep. At test time, we sample from the distribution over the vocabulary at each timestep, and feed the sample as input to the RNN at the next timestep.

In the file cs231n/classifiers/rnn.py, implement the sample method for test-time sampling. After doing so, run the following to sample from your overfitted model on both training and validation data. The samples on training data should be very good; the samples on validation data probably won't make sense.

Note: Some of the URLs are missing and will throw an error; re-run this cell until the output is at least 2 good caption samples.

```
In [17]: for split in ['train', 'val']:
    minibatch = sample_coco_minibatch(small_data, split=split, batch_size=2)
    gt_captions, features, urls = minibatch
    gt_captions = decode_captions(gt_captions, data['idx_to_word'])

sample_captions = small_rnn_model.sample(features)
    sample_captions = decode_captions(sample_captions, data['idx_to_word'])

for gt_caption, sample_caption, url in zip(gt_captions, sample_captions, urls):
    plt.imshow(image_from_url(url))
    plt.title('%s\n%s\nGT:%s' % (split, sample_caption, gt_caption))
    plt.axis('off')
    plt.show()
```

train

GT:<START> a woman is kneeling near some large <UNK> of food <END>



train

GT:<START> a group of men riding in a boat across a lake <END>



val

GT:<START> the man in the helmet is jumping while wearing <UNK> <UNK> <END>



va

GT:<START> a little boy sitting on the stairs with a racquet <END>

