

# Cryptography 2/19

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## Polynomial Ring over Finite Field ( $\mathbb{F}_2$ in particular)

	$\mathbb{Z}$	$\mathbb{F}_p[x]$
Cardinality	Infinite primes $\frac{\mathbb{Z}}{p} \approx \mathbb{F}_p$ XCGD, CRT	Infinite irreducibles $\frac{\mathbb{F}_2[x]}{(f(x))} \approx \mathbb{F}_p n$ XGCD, CRT
Factorization	Hard Security	Easy Error-correcting code

## AES

- Bytes  $\iff \frac{\mathbb{F}_2[x]}{x^8+x^4+x^3+x+1}$
- Most of the lecture has been him doing stuff on Sage, tbh I have no idea what's happening and haven't had an idea of what's happening since Friday of last week
  - I'm totally lost. Someone help

## Don't know what this is pertaining to...oops

- For every prime  $p$  and every  $n \in \mathbb{Z}^+$ , there is a field of  $p^n$  elements and it is unique
- For every finite field  $GF(p^n)$ , there exists a multiplicative generator
- $p =$  characteristic of the field
  - If you add elements  $p$  times, you'll get 0 (or at least 1? I couldn't tell what he said)