

CS 5173/4173 Computer Security

Topic 3.1 Secret Key Cryptography – Algorithms

Key Sizes

- A Key should be selected from a large potential set to prevent brute force attacks
 - If a key is of 3 bits, what are the possible keys?
 - 000, 001, 010, 011, 100, 101, 110, 111
 - Given a pair of (plaintext, ciphertext), an attacker can do a brute force search to find the key
 - If a key is of n bits, how many possible keys does a brute force attacker need to search?

Key Sizes (Cont'd)

- Secret key sizes
 - 40 bits were considered adequate in 70's
 - 56 bits used by DES were adequate in the 80's
 - 128 bits are adequate for now
- If computers increase in power by 40% per year, need roughly 5 more key bits per decade to stay “sufficiently” hard to break

Notation

Notation	Meaning
$X \oplus Y$	Bit-wise exclusive-or of X and Y
$X \mid Y$	Concatenation of X and Y
$K\{m\}$	Message m encrypted with secret key K

Two Principles for Cipher Design

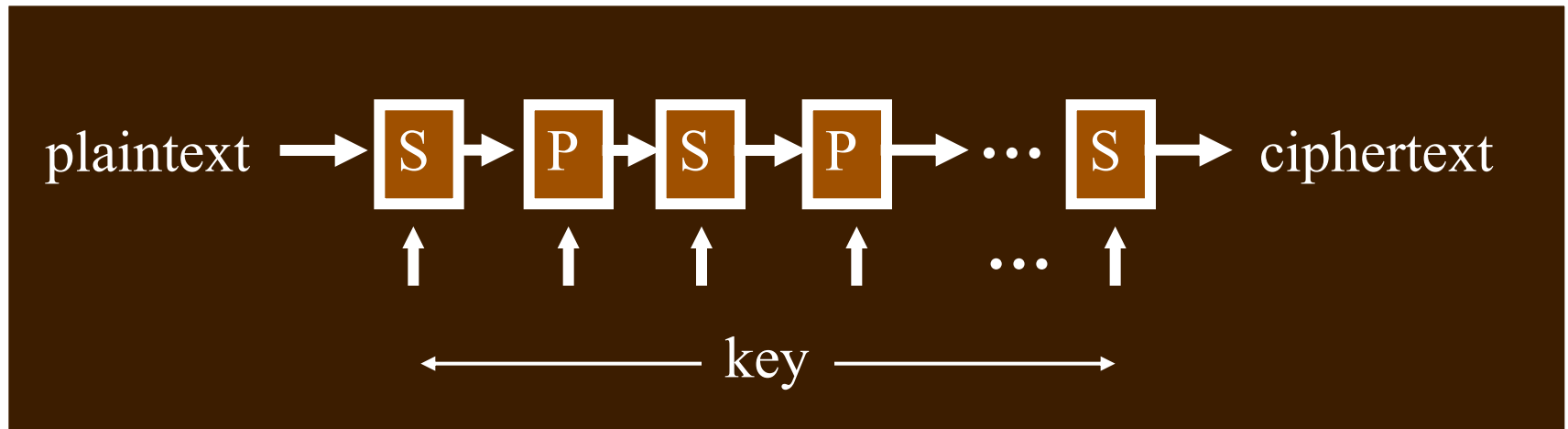
- **Confusion:**
 - Make the relationship between the <plaintext, key> input and the <ciphertext> output as complex (non-linear) as possible
- **Diffusion:**
 - Spread the influence of each input bit across many output bits

Exploiting the Principles

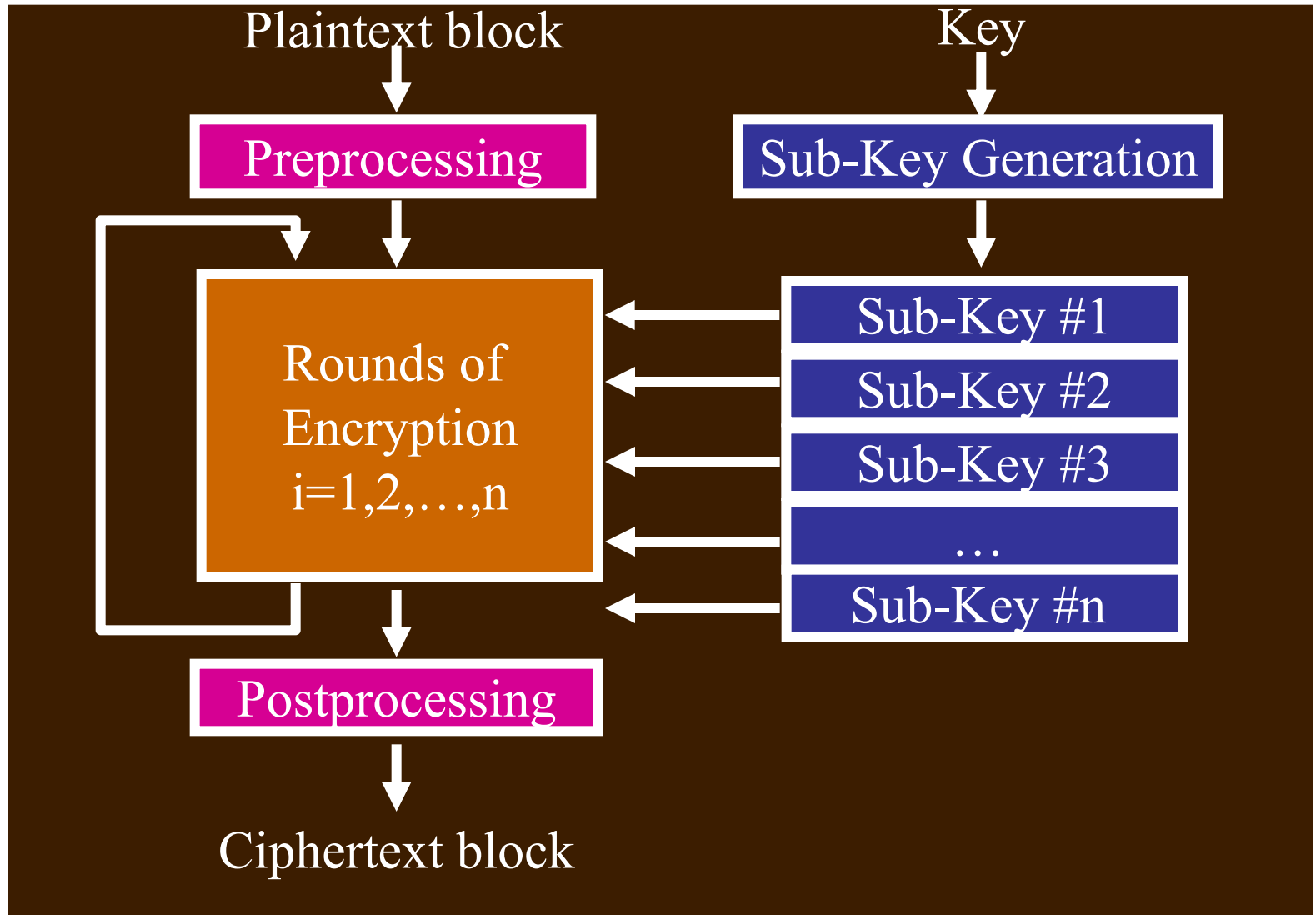
- Idea: use multiple, alternating permutations and substitutions, e.g.,
 - $S \rightarrow P \rightarrow S \rightarrow P \rightarrow S \rightarrow \dots$
 - $P \rightarrow S \rightarrow P \rightarrow S \rightarrow P \rightarrow \dots$
- Do they have to alternate? e.g....
 - $S \rightarrow S \rightarrow S \rightarrow P \rightarrow P \rightarrow P \rightarrow S \rightarrow S \rightarrow \dots?$
 - Consecutive Ps or Ss do not improve security
- Confusion is mainly accomplished by substitutions
- Diffusion is mainly accomplished by permutations

Secret Key... (Cont'd)

- Basic technique used in secret key ciphers: multiple applications of alternating substitutions and permutations



Basic Form of Modern Block Ciphers



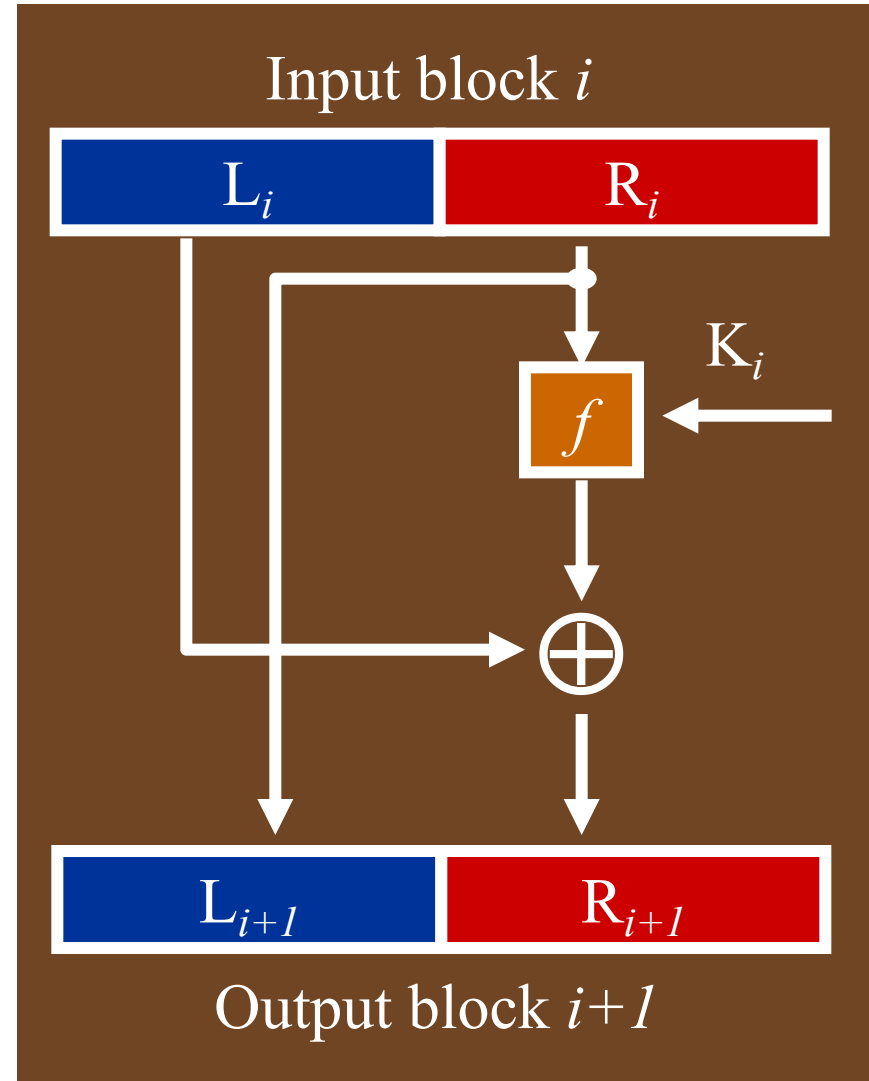
Feistel Ciphers

Feistel Ciphers

- Feistel Cipher has been a very influential “template” for designing a block cipher
- Major benefit: Encryption and decryption take the same time
 - they can be performed on the same hardware
- Examples: DES, RC5

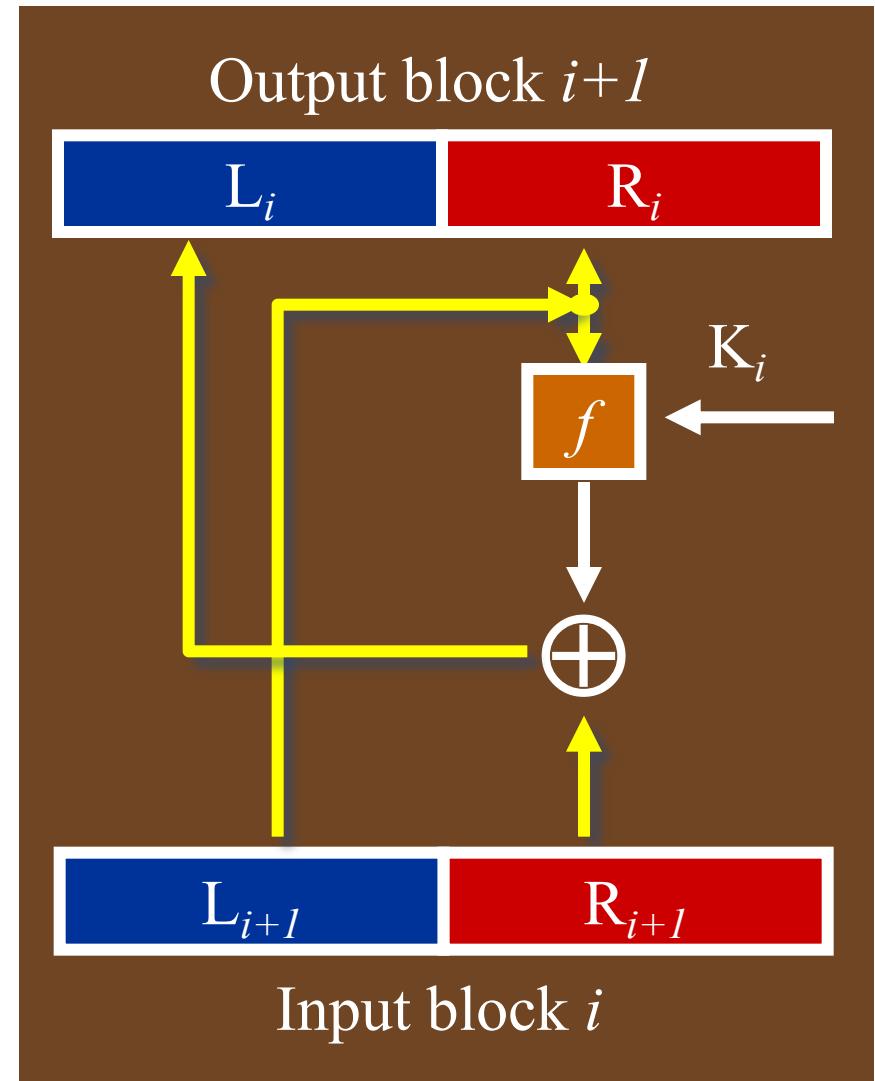
One “Round” of Feistel Encryption

1. Break input block i into left and right halves L_i and R_i
2. Copy R_i to create output half block L_{i+1}
3. Half block R_i and key K_i are “scrambled” by function f
4. XOR result with input half-block L_i to create output half-block R_{i+1}



One “Round” of Feistel Decryption

- Just reverse the arrows!
- Why?



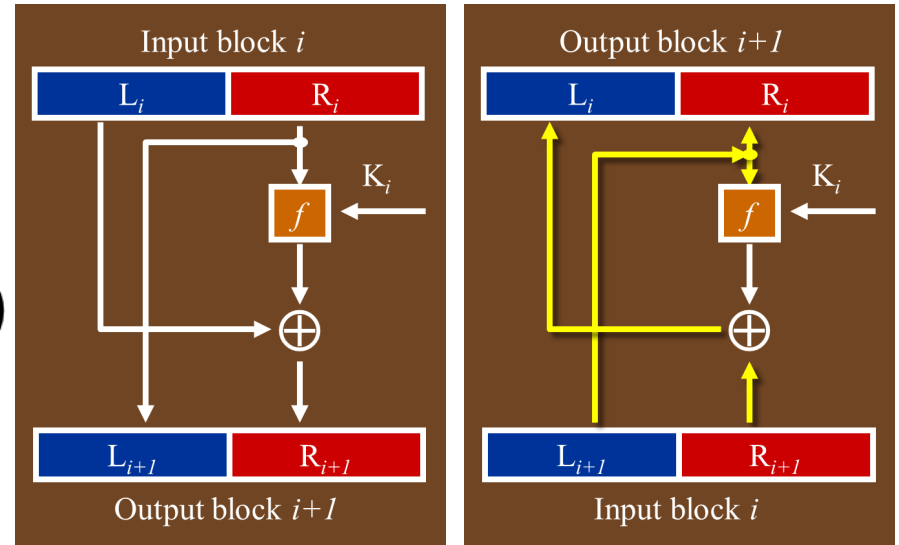
Feistel Cipher: Decryption (cont'd)

- Encryption

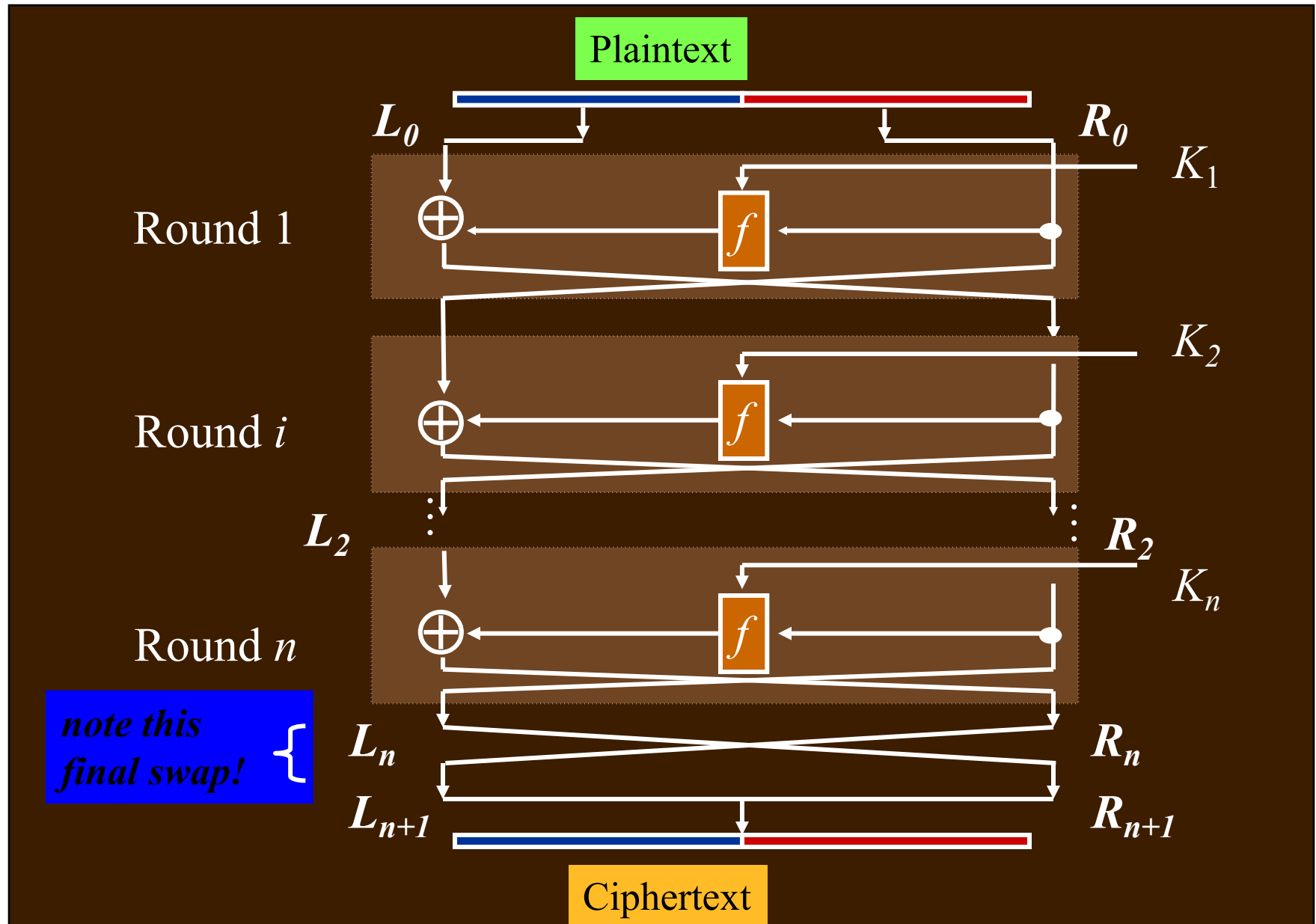
- $L_{i+1} = R_i$
- $R_{i+1} = L_i \oplus f(R_i, K_i)$

- Decryption

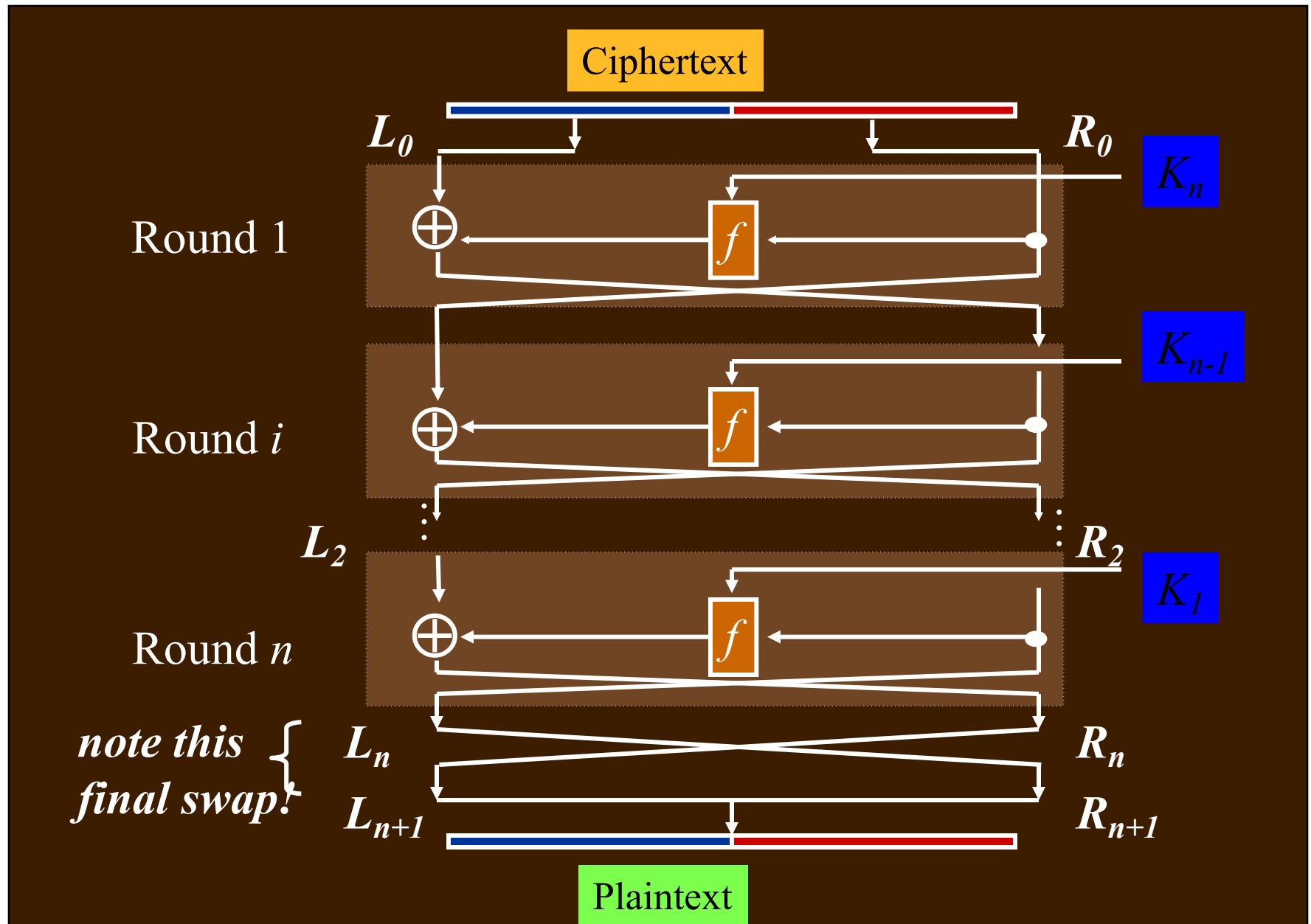
- $R_i = L_{i+1}$
- $L_i = R_{i+1} \oplus f(R_i, K_i)$
 $= L_i \oplus f(R_i, K_i) \oplus f(R_i, K_i) = L_i$



Complete Feistel Cipher: Encryption

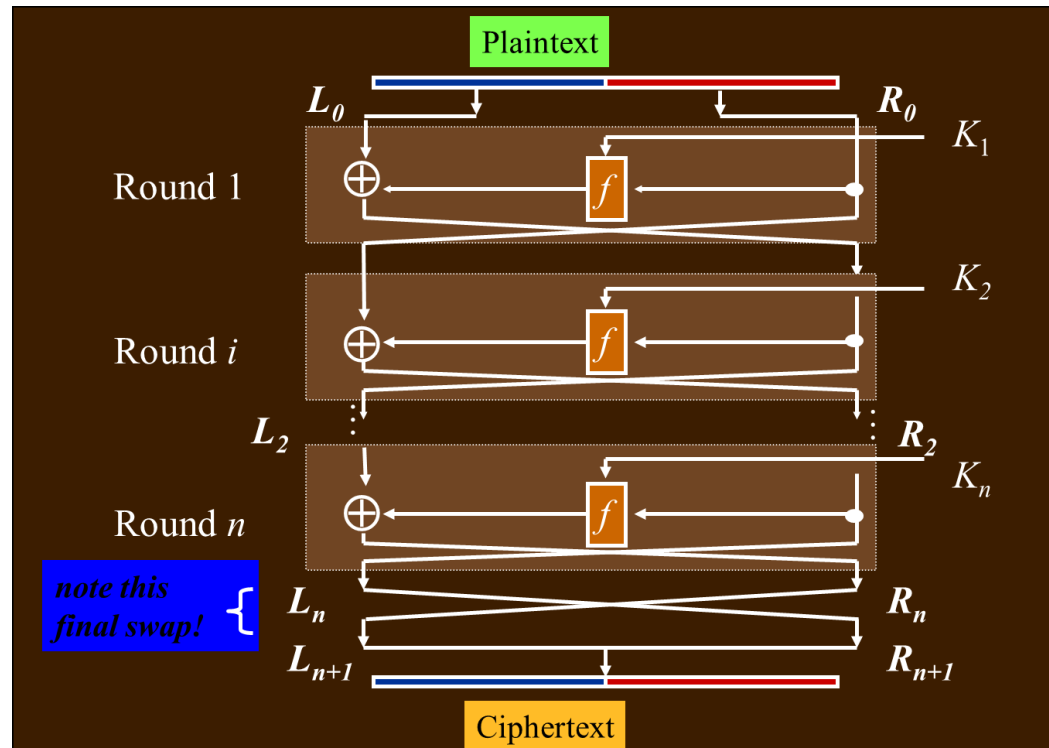


Feistel Cipher: Decryption

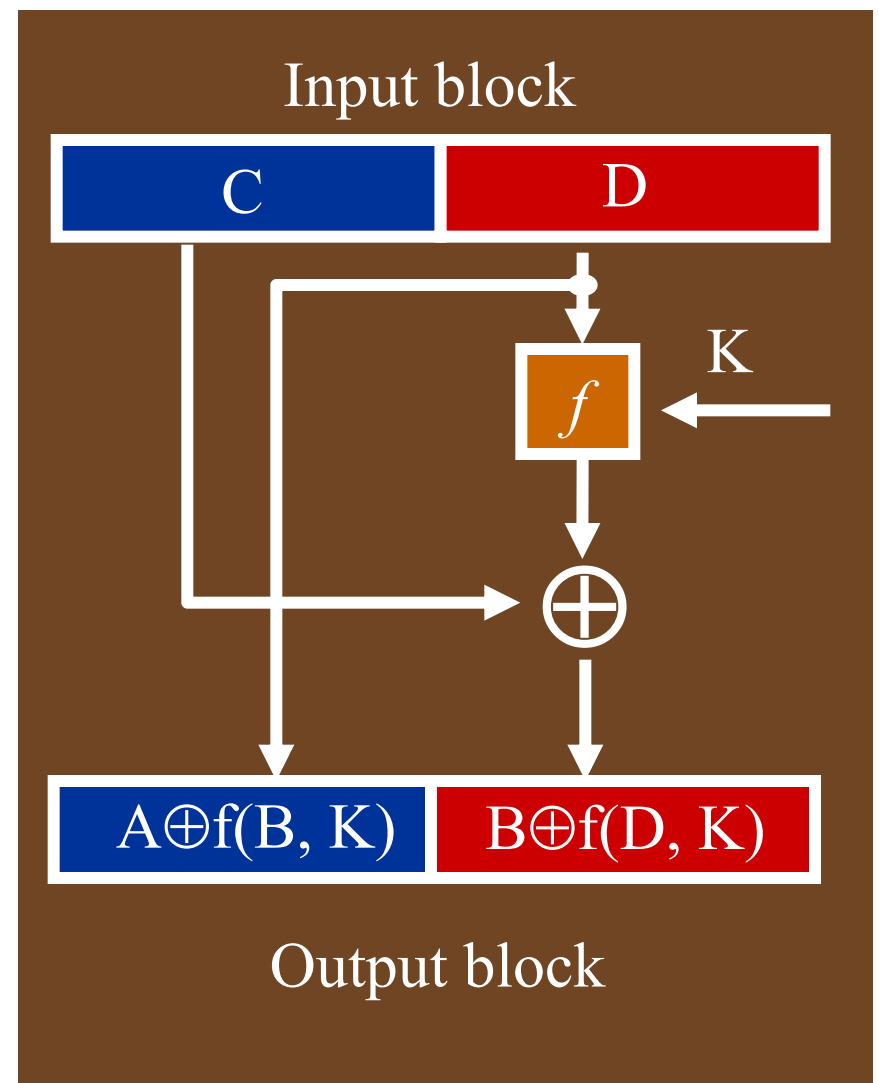
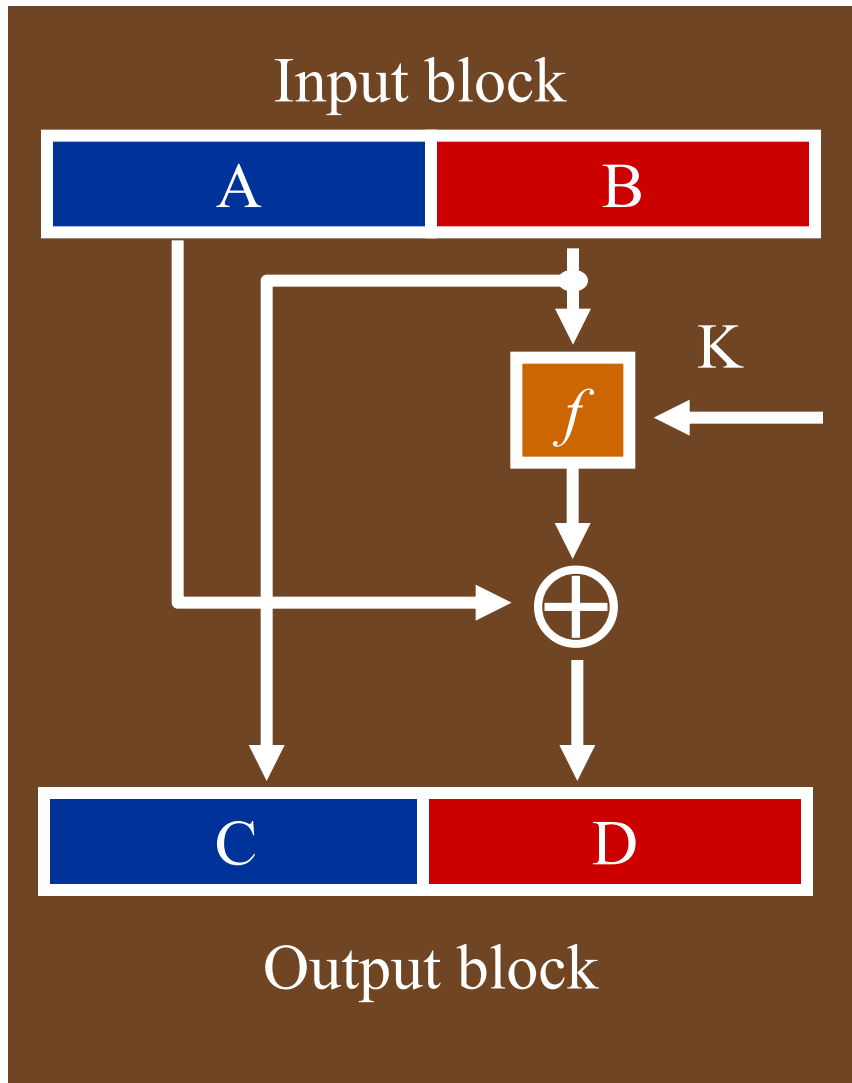


The Swap Operation

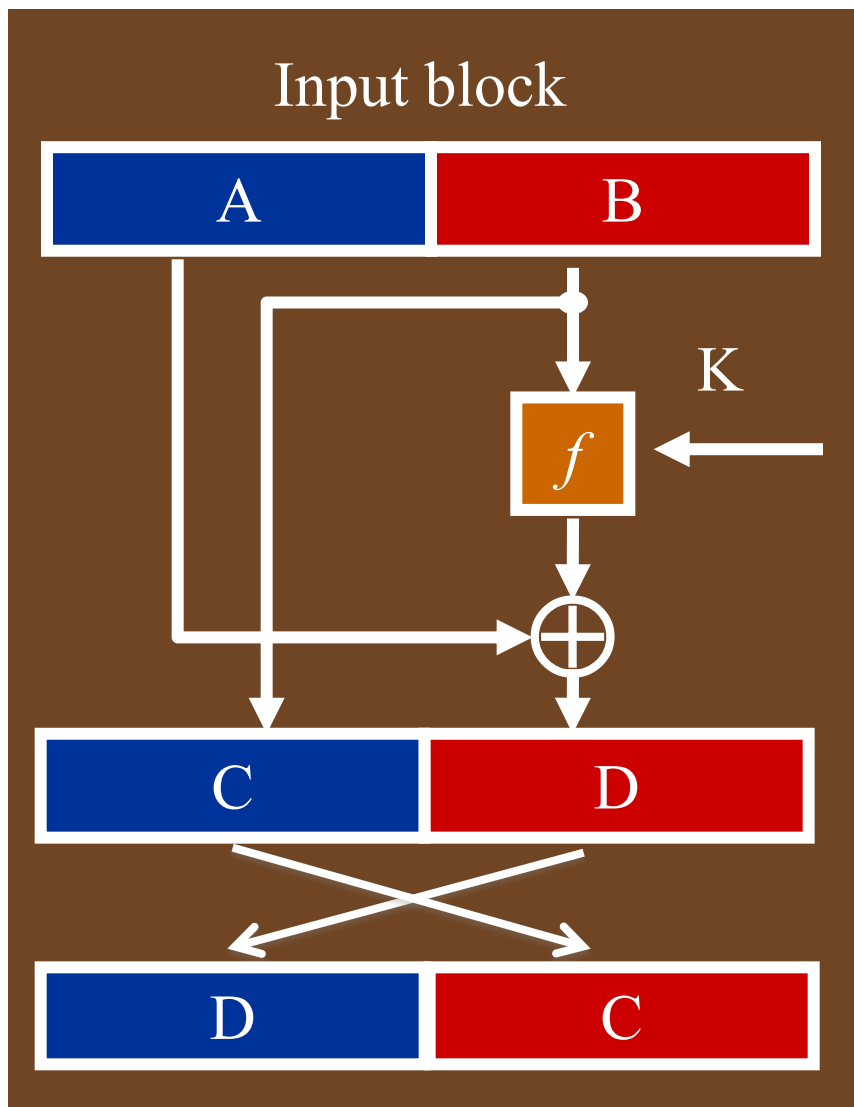
- For the Feistel cipher, why do we need the final swap step?



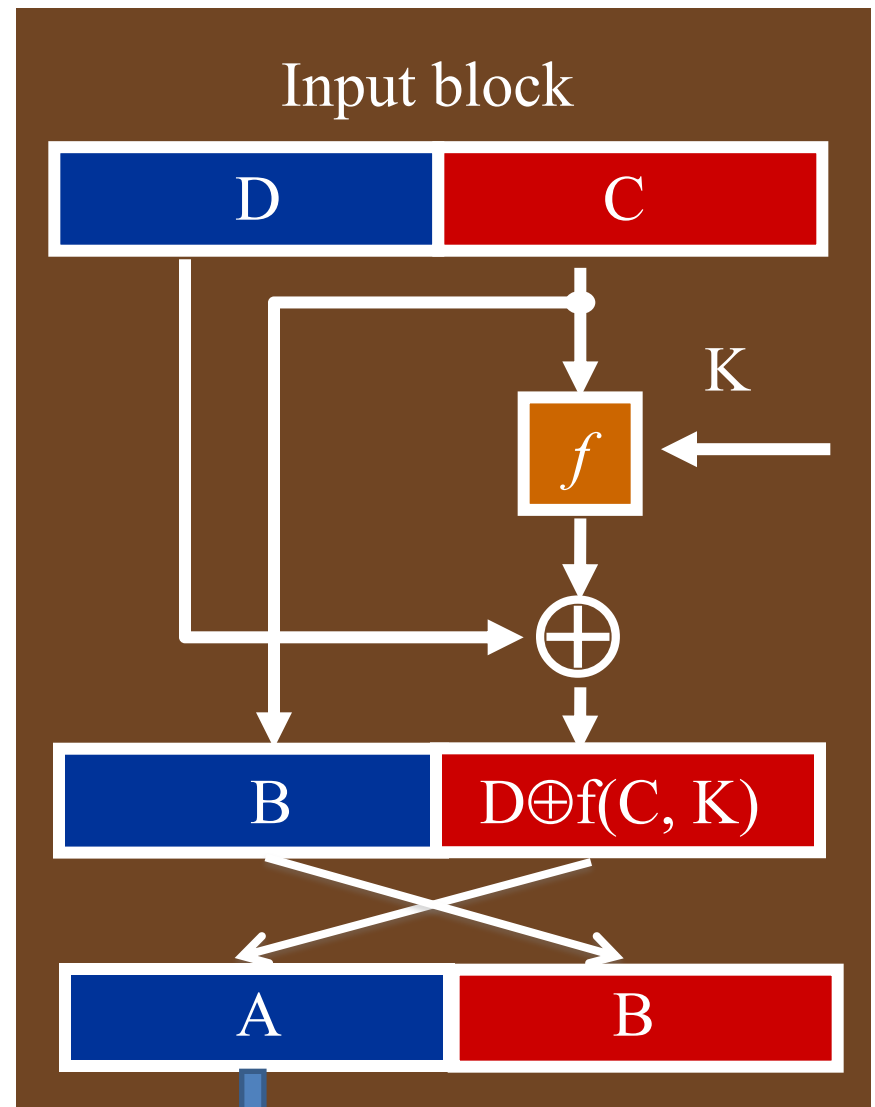
Without Swap



Without swap, we cannot decrypt to A and B!

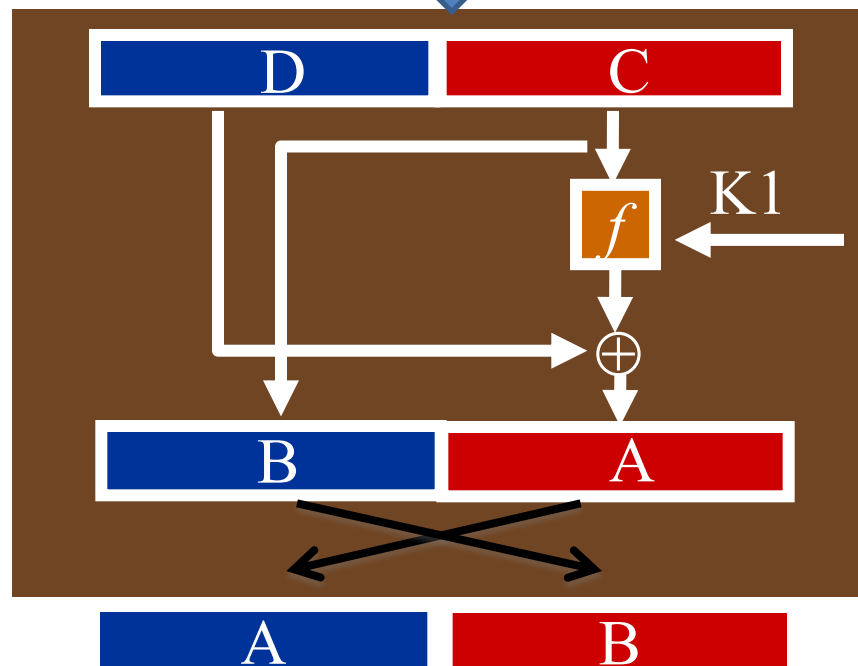
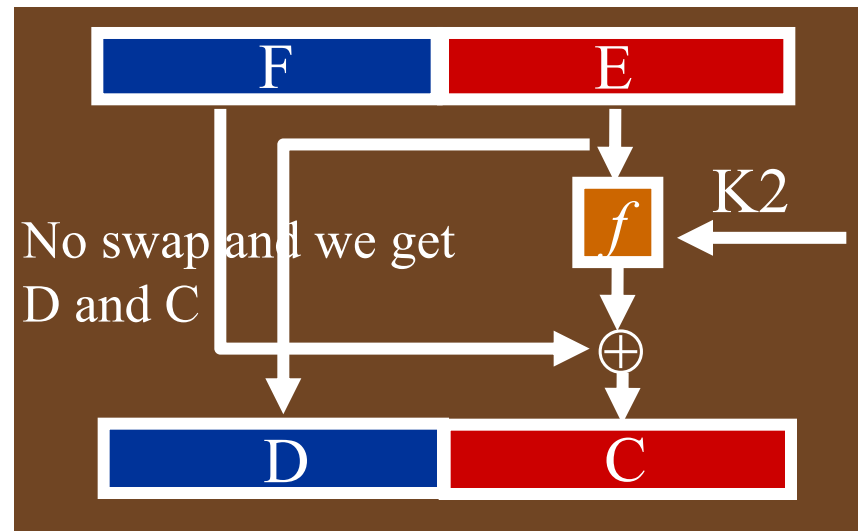
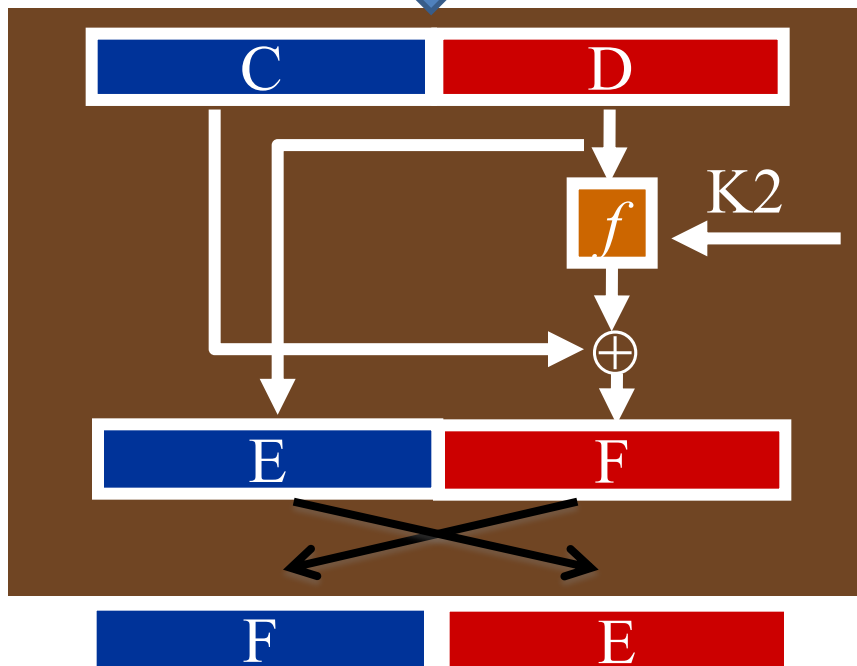
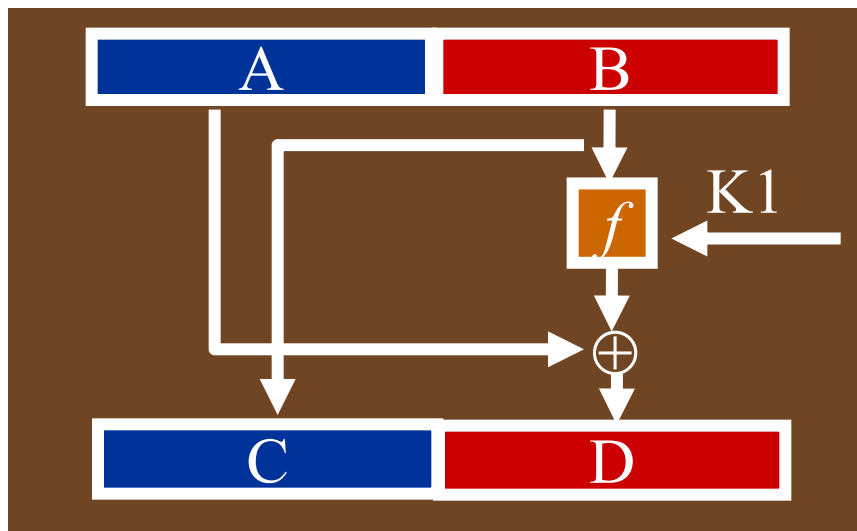


With Swap

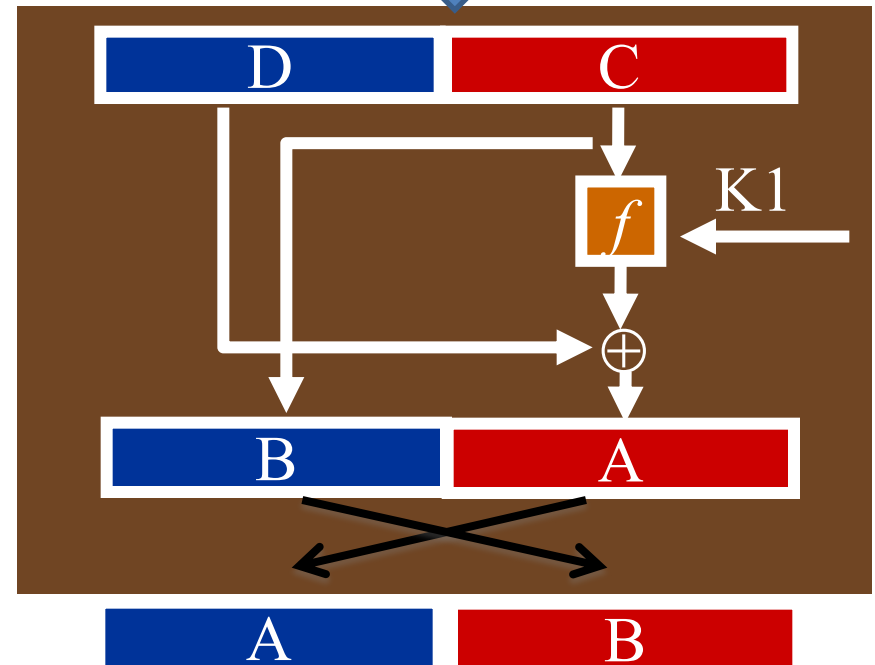
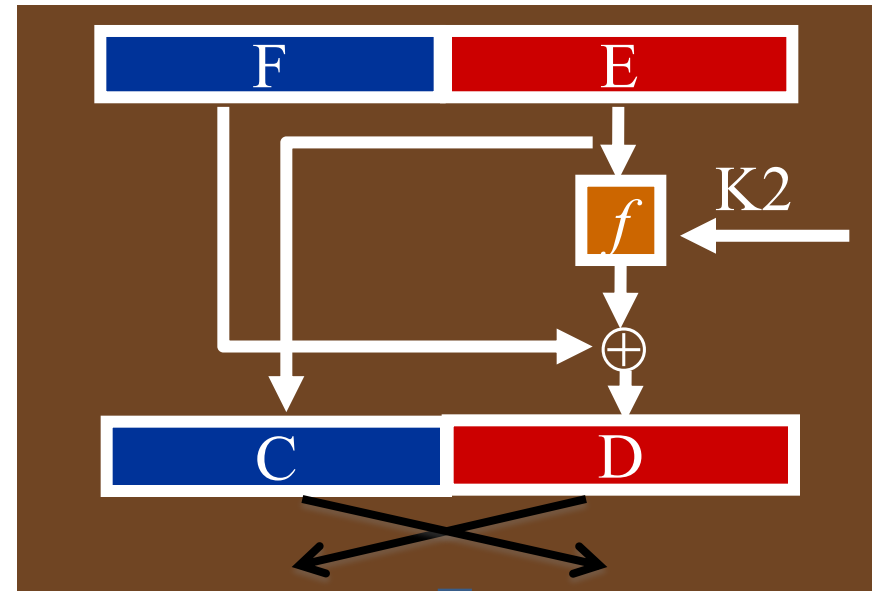
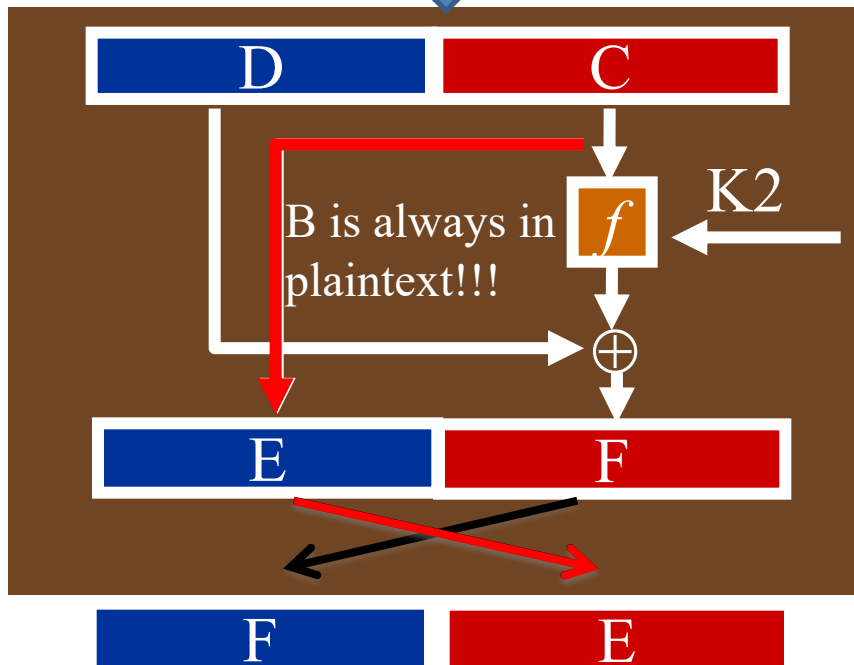
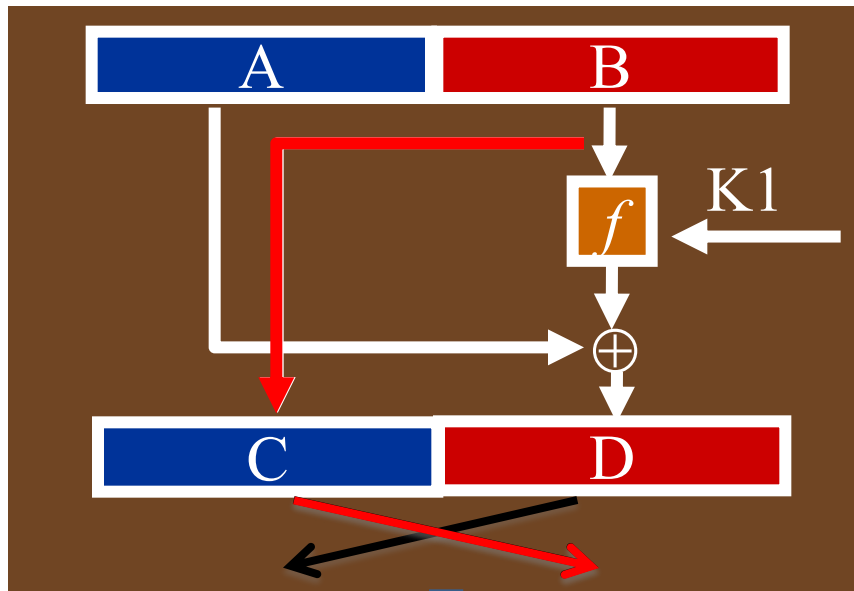


$$\begin{aligned}
 &= D \oplus f(C, K) \\
 &= A \oplus f(B, K) \oplus f(C, K) \\
 &= A \oplus f(C, K) \oplus f(C, K) = A
 \end{aligned}$$

With Swap (two rounds)



What's wrong with this scheme?



Parameters of a Feistel Cipher

- Block size
- Key size
- Number of rounds
- Subkey generation algorithm
- “Scrambling” function f

Summary

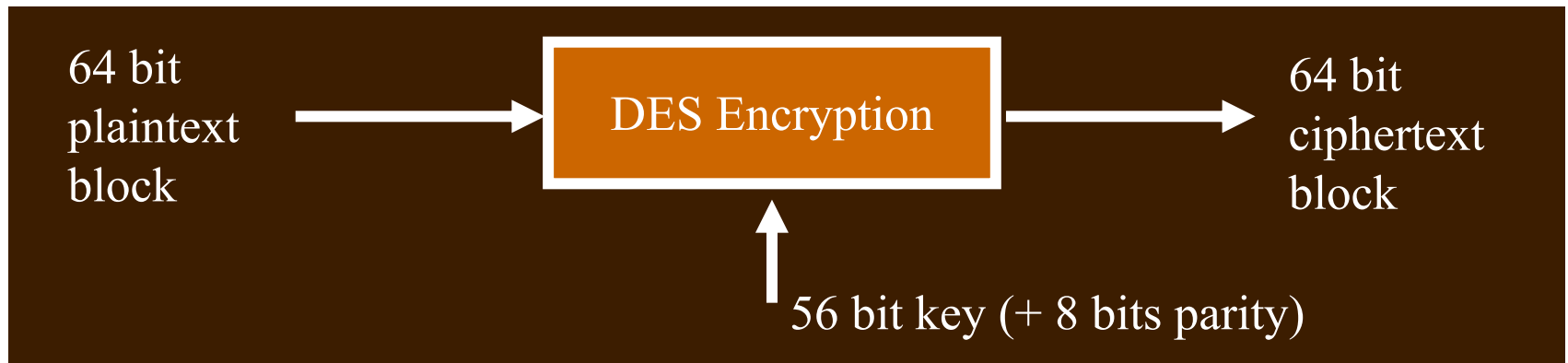
- Decryption is same as encryption, only reversing the order in which round keys are applied
 - Reversability of Feistel cipher derives from reversability of xor \oplus
- Function f can be anything
 - Hopefully something easy to compute
 - There is no need to invert f

DES (Data Encryption Standard)

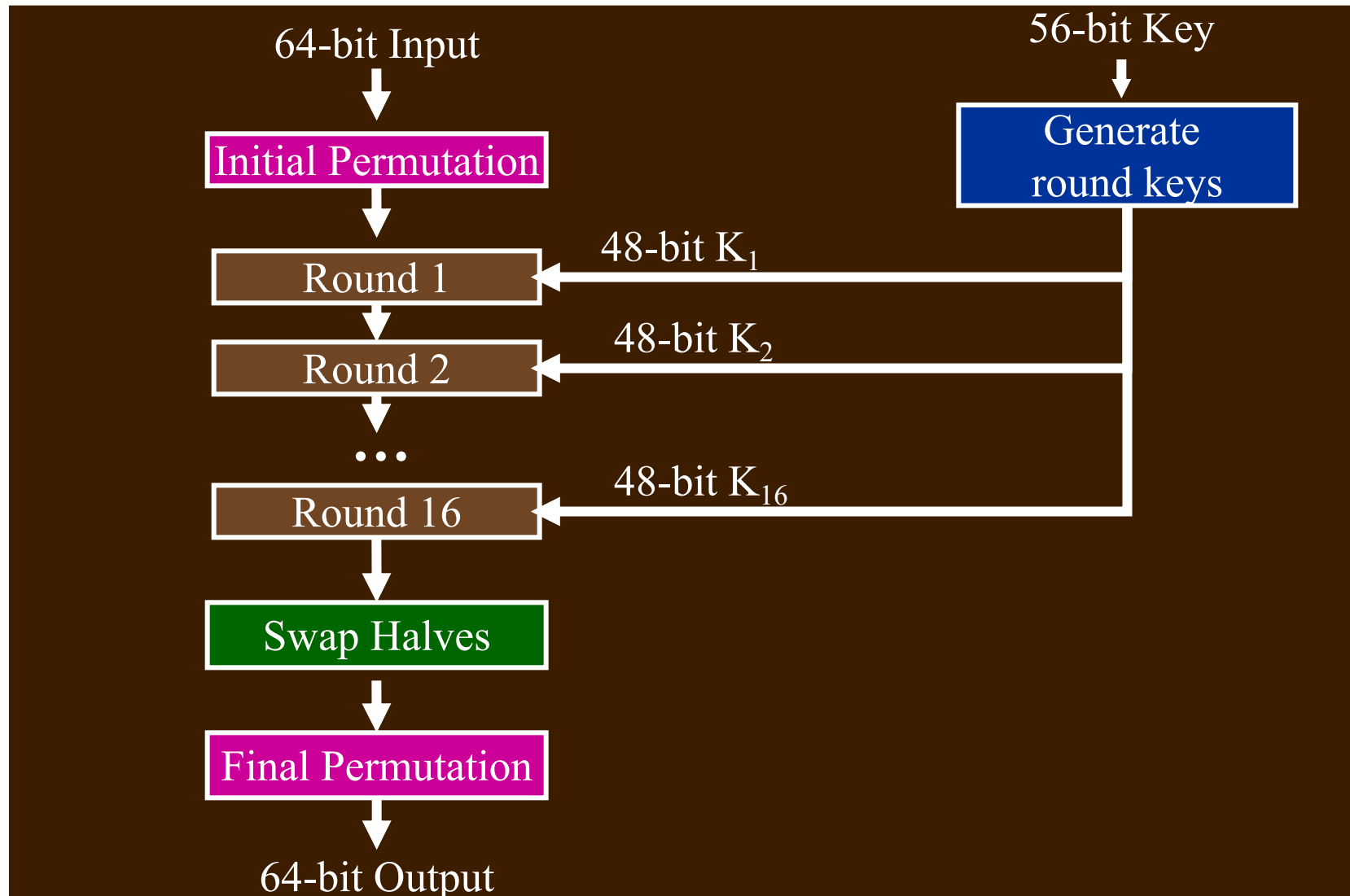
- Standardized in 1976 by NBS
 - proposed by IBM,
 - Feistel cipher
- Criteria (**official**)
 - provide high level of security
 - security must reside in key, not algorithm
 - not patented
 - efficient to implement in hardware
 - must be slow to execute in software

DES Basics

- **Blocks:** 64 bit plaintext input, 64 bit ciphertext output
- **Rounds:** 16
- **Key:** 64 bits
 - every 8th bit is a parity bit, so really 56 bits long



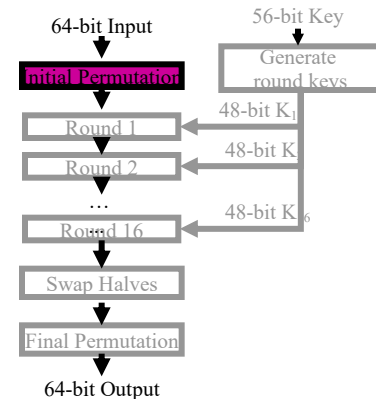
DES Top Level View



Initial and Final Permutations

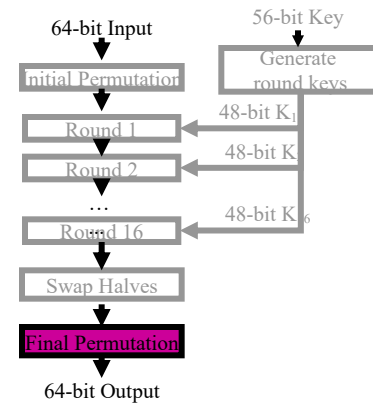
- **Initial** permutation given below
 - input bit #58 → output bit #1, input bit #50 → output bit #2, ...

58	50	42	34	26	18	10	2
60	52	44	36	28	20	12	4
62	54	46	38	30	22	14	6
64	56	48	40	32	24	16	8
57	49	41	33	25	17	9	1
59	51	43	35	27	19	11	3
61	53	45	37	29	21	13	5
63	55	47	39	31	23	15	7



Initial... (Cont'd)

- **Final** permutation is just **inverse** of initial permutation, i.e.,
 - input bit #1 → output bit #58
 - input bit #2 → output bit #50
 - ...

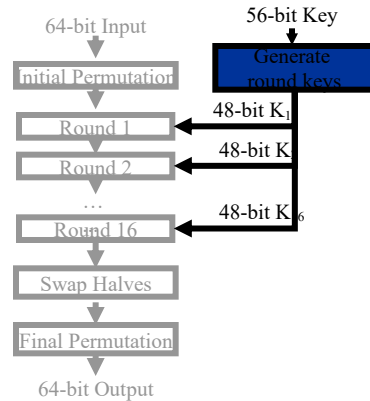


Initial... (Cont'd)

- Note #1: Initial Permutation is fully specified (independent of key)
 - therefore, does not improve security!
 - why needed?
- Note #2: Why is final Permutation needed?
 - to make this a Feistel cipher
 - i.e., the decryption is the reverse of encryption

Key Generation: First Permutation

- First step: **throw out 8 parity bits**, then permute resulting 56 bits



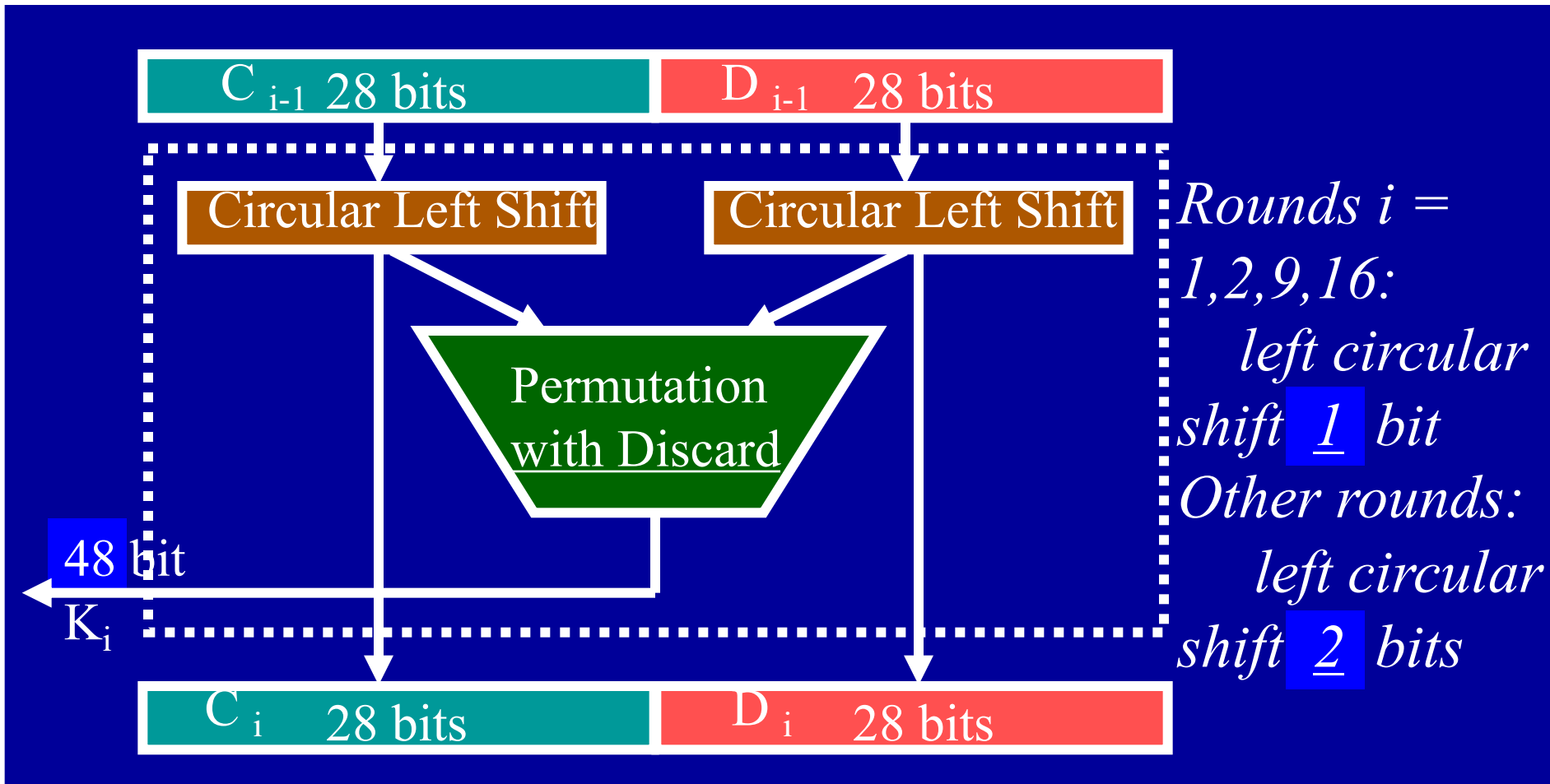
*Parity bits left out:
8, 16, 24, ...*

8 rows

7 columns

57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
63	55	47	39	31	23	15
7	62	54	46	38	30	22
14	6	61	53	45	37	29
21	13	5	28	20	12	4

KeyGen: Processing Per Round



KeyGen: Permutation with Discard

- 28 bits \rightarrow 24 bits, each half of key

Left half of K_i = permutation of C_i

14	17	11	24	1	5
3	28	15	6	21	10
23	19	12	4	26	8
16	7	27	20	13	2

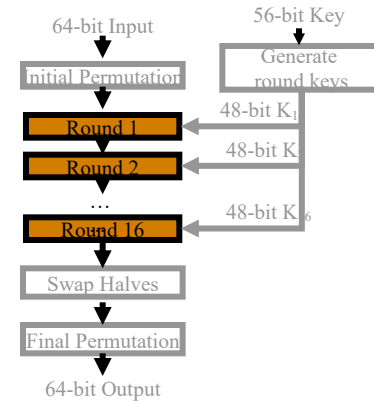
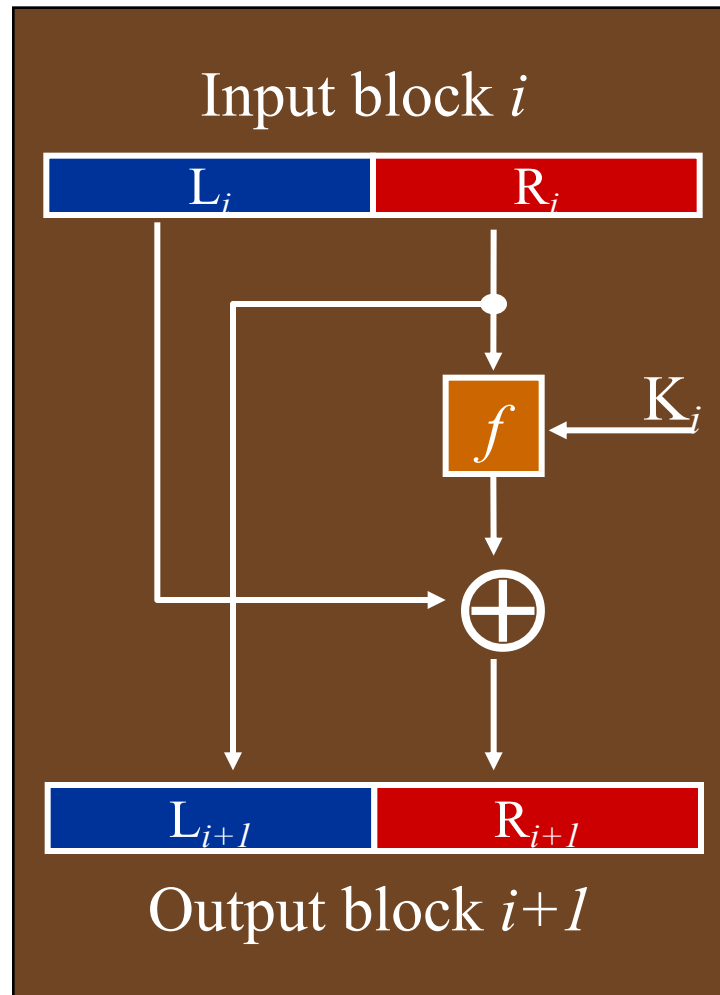
Bits discarded:
9,18,22,25

Right half of K_i = permutation of D_i

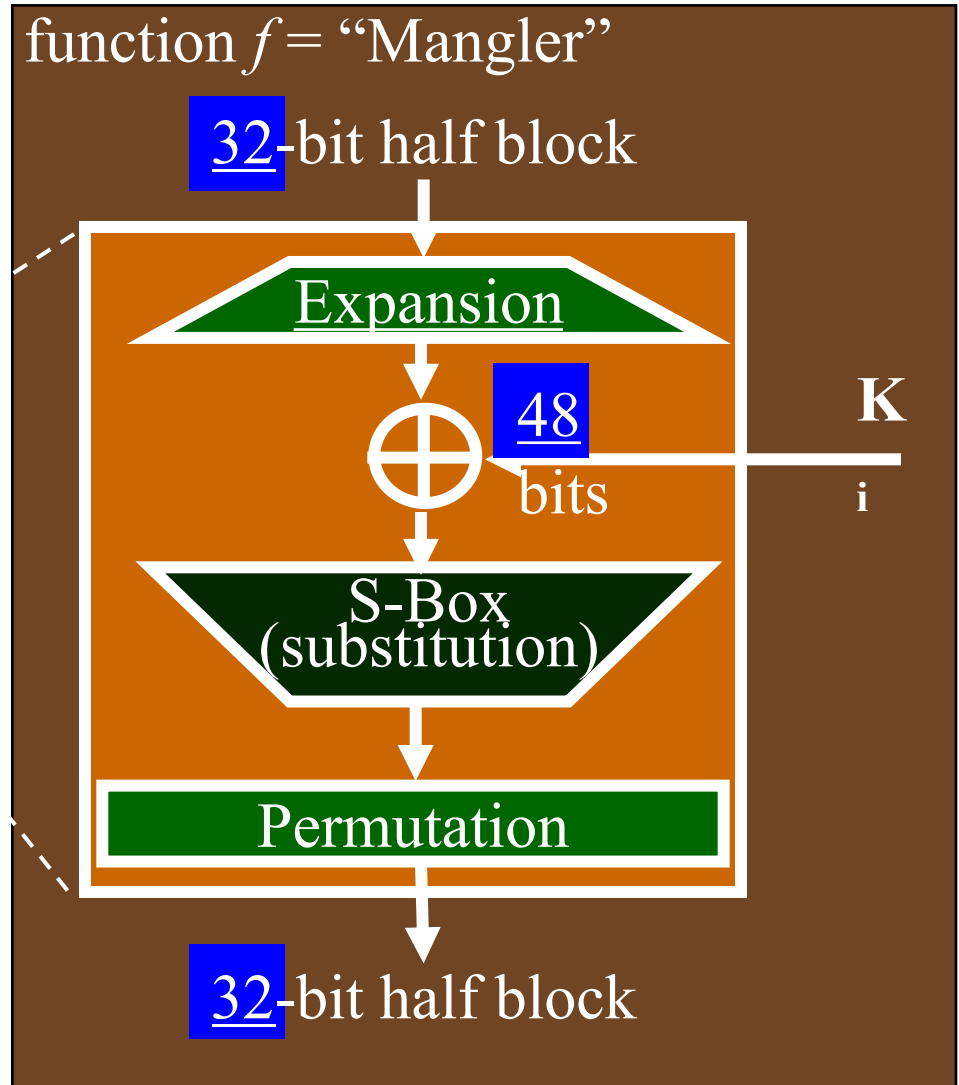
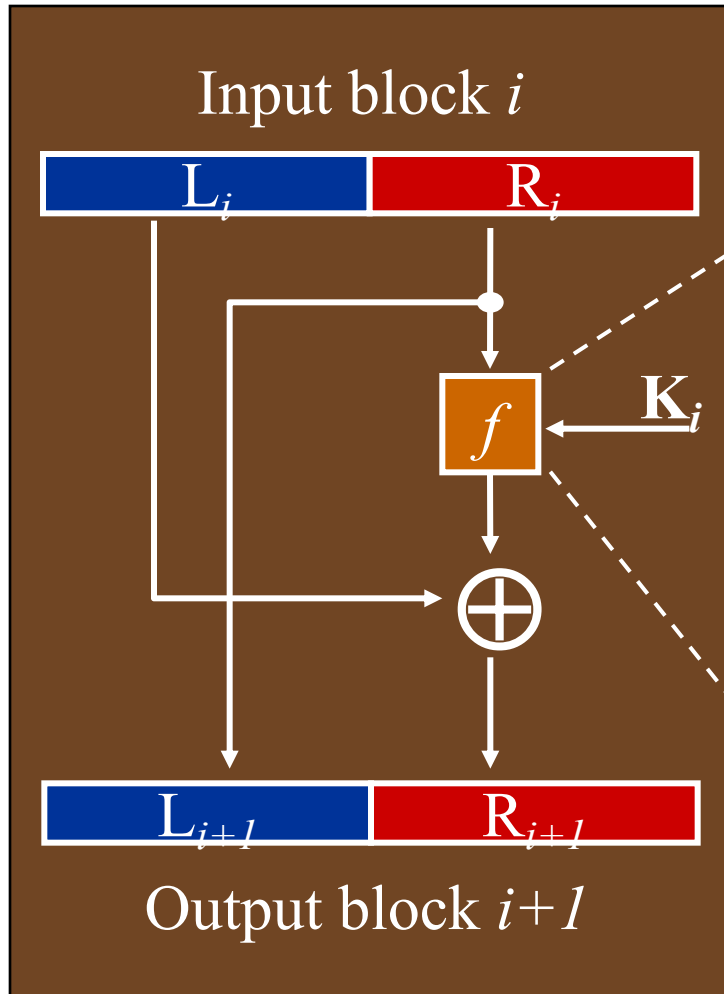
41	52	31	37	47	55
30	40	51	45	33	48
44	49	39	56	34	53
46	42	50	36	29	32

Bits discarded:
35,38,43,54

One DES (Feistel) Round



DES Round: f (Mangler) Function



f : Expansion Function

- 32 bits \rightarrow 48 bits

these bits are repeated

32	1	2	3	4	5
4	5	6	7	8	9
8	9	10	11	12	13
12	13	14	15	16	17
16	17	18	19	20	21
20	21	22	23	24	25
24	25	26	27	28	29
28	29	30	31	32	1

$f: S_1$ (Substitution)

Each row and column contain different numbers

I2/I3/I4/I5 →		0	1	2	3	4	5	6	...	F
← I1/I6	0	E	4	D	1	2	F	B	-----	
	1	0	F	7	4	E	2	D	-----	
	2	4	1	E	8	D	6	2	-----	
	3	F	C	8	2	4	9	1	-----	

Example: input = 100110, output = 1000
input = 101101, output = ?

f : Permutation

- 32bits \rightarrow 32bits

16	7	20	21
29	12	28	17
1	15	23	26
5	18	31	10
2	8	24	14
32	27	3	9
19	13	30	6
22	11	4	25

DES Implementation

- That's it!
- Operations
 - Permutation
 - Swapping halves
 - Substitution (S-box, table lookup)
 - Bit discard
 - Bit replication
 - Circular shift
 - XOR
- Hard to implement? HW: No, SW: Yes

Principles for S-Box Design

- S-box is the **only** non-linear part of DES
- Each **row** in the S-Box table should be a permutation of the possible output values
- Output of one S-box should affect other S-boxes in the following round

Desirable Property: **Avalanche Effect**

- Roughly: a small change in either the plaintext or the key should produce a big change in the ciphertext
- Better: any output bit should be inverted (flipped) with probability 0.5 if any input bit is changed
 - What is the expected number of different bits between two length- n random bit streams?
 - $0.5n$ (Bernoulli distribution)
- f function
 - must be difficult to un-scramble
 - should achieve avalanche effect
 - output bits should be uncorrelated

DES Avalanche Effect: Example

- 2 plaintexts with **1** bit difference:
0x**0**0000000000000000 and
0x**8**0000000000000000
encrypted using the same key:
0x016B24621C181C32
- Resulting **ciphertexts** differ in **34** bits
(out of 64)
- Similar results when **keys** differ by 1 bit

Example (cont'd)

- An experiment: number of rounds vs. number of bits difference

Round #	0	1	2	3	4	5	6	7	8
Bits changed	1	6	21	35	39	34	32	31	29

9	10	11	12	13	14	15	16
42	44	32	30	30	26	29	34

DES: **Keys to Avoid** Using

- “**Weak keys**”: These are keys which, after the first key permutation, are:
 - 28 0' s followed by 28 0' s
 - 28 1' s followed by 28 1' s
 - 28 0' s followed by 28 1' s
 - 28 1' s followed by 28 0' s
- Property of weak keys
 - Easy clue for brute force attacks.
 - Sixteen identical subkeys.
 - Encrypting twice produces the original plaintext.

Weak keys

- Alternating ones + zeros
(0x01010101010101)
- Alternating 'F' + 'E' (0xFEFEFEFEFEFEFEFE)
- 0xE0E0E0E0F1F1F1F1
- 0x1F1F1F1F0E0E0E0E
- DES *weak keys* produce sixteen identical subkeys

More Keys to Avoid!

- “Semi-weak keys”: These are keys which, after the first key permutation, are:
 1. 28 0' s followed by alternating 0' s and 1' s
 2. 28 0' s followed by alternating 1' s and 0' s
 - ...
 12. Alternating 1' s and 0' s followed by alternating 1' s and 0' s
- Property of semi-weak keys
 - For a semi-weak key pair (K_1, K_2) , $K_1\{K_2\{m\}\} = m$ and $K_2\{K_1\{m\}\} = m$

Semi-weak key pairs

- 0x011F011F010E010E and 0x1F011F010E010E01
- 0x01E001E001F101F1 and 0xE001E001F101F101
- 0x01FE01FE01FE01FE and 0xFE01FE01FE01FE01
- 0x1FE01FE00EF10EF1 and 0xE01FE01FF10EF10E
- 0x1FFE1FFE0EFE0EFE and 0xFE1FFE1FFE0EFE0E
- 0xE0FEE0FEF1FEF1FE and 0xFEE0FEE0FEF1FEF1
- $K_1\{K_2\{m\}\} = m$ and $K_2\{K_1\{m\}\} = m$

DES Key Size

- 56 bits is currently too small to resist brute force attacks using readily-available hardware
- Ten years ago it took \$250,000 to build a machine that could crack DES in a few hours
- Now?

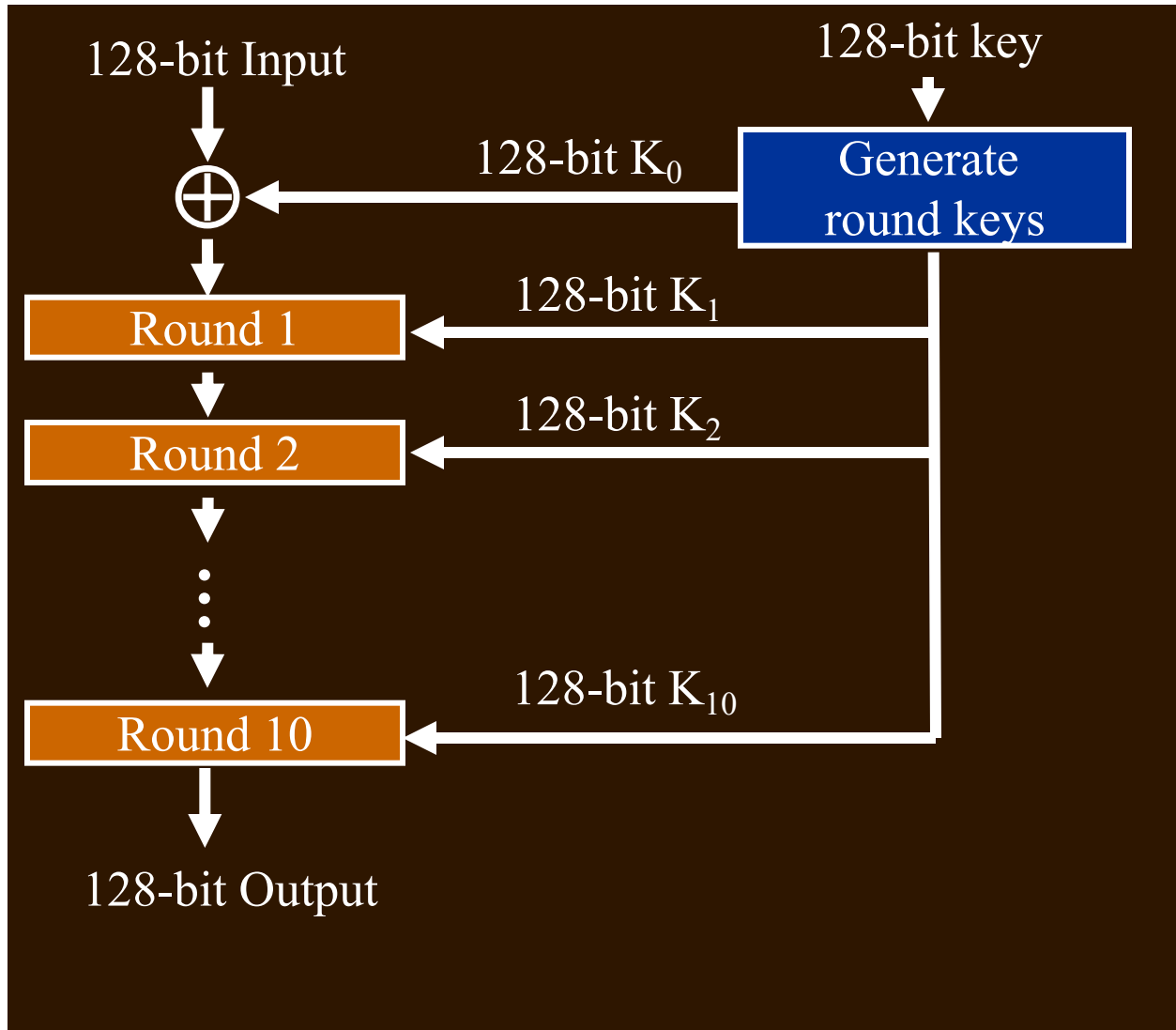
Cryptanalysis of DES

- **Differential cryptanalysis** exploits differences between encryptions of two different plaintext blocks
 - provides insight into possible key values
- **Linear cryptanalysis** requires known plaintext / ciphertext pairs, analyzes relationships to discover key value
- No attacks on DES so far are significantly better than brute force attacks, for comparable cost

Advanced Encryption Standard (AES)

- Selected from an **open** competition, organized by NSA
 - winner: Rijndael algorithm, standardized as AES
- Some similarities to DES (rounds, round keys, alternate permutation+substitution)
 - but **not** a Feistel cipher
- Block size = 128, or 192, or 256 bits
- Key sizes = 128 (10 rounds), 192 (12 rounds), or 256 (14 rounds)

AES-128 Overview



Does AES Have Avalanche
Property?

Examples of AES Encryption

Input String	Key	Output String (HEX)
ABCDEFGH IJKLMN OP	1 1223344556677889900AABBCCDDEEFF	BC4784A37D6F46452656B993D53393F5
ABCDEF G H IJKLMN OP	0 1223344556677889900AABBCCDDEEFF	855866490543FDF6504FC84088FEDCA0
ABCDEF F H IJKLMN OP	11223344556677889900AABBCCDDEEFF	372CCA446C0D391C4381392344630EE1

Input String(HEX)	Key	Output String (HEX)
00000000000000000000000000000000	000000000000000000000000000000 0	66E94BD4EF8A2C3B884CFA59CA342B2E
000000000000000000000000000000 0	000000000000000000000000000000 1	0545AAD56DA2A97C3663D1432A3D1C84
000000000000000000000000000000 1	00000000000000000000000000000001	A17E9F69E4F25A8B8620B4AF78EEFD6F

AES Assessment

- No known successful attacks on full AES
 - Best attacks work on 7–9 rounds
- For brute force attacks, AES-128 needs much more effort than DES

Attacks on AES

- **Differential Cryptanalysis**: based on how differences in inputs correlate with differences in outputs
 - greatly reduced due to high number of rounds
- **Linear Cryptanalysis**: based on correlations between input and output

Attacks on AES (Cont'd)

- Side Channel Attacks
- Timing Attacks: measure the time it takes to do operations
 - some operations, with some operands, are much faster than other operations, with other operand values
 - provides clues about what internal operations are being performed, and what internal data values are being produced

Attacks on AES (Cont'd)

- Side Channel Attacks
- Power Attacks: measures power to do operations
 - changing one bit requires considerably less power than changing many bits in a byte