

The Brogrammers (Reagan Leonard, Jackson Lee, Jack Sparrow)

Test Plans

- Reagan
 - Queue_Template_Test_Plan (assuming Max_Length = 5)
 - Enqueue
 - Test 1 (lower boundary/typical case):
 - Input: E = 3, Q = <>
 - Expected Output: E = <3>, Q = <3>
 - Test 2 (upper boundary case):
 - Input: E = 5, Q = <1, 2, 3, 4>
 - Expected Output: E = <5>, Q = <1, 2, 3, 4, 5>
 - Test 3 (requires clause not met):
 - Input: E = 12, Q = <4, 6, 2, 9, 10>
 - Expected Output: Error, Max_Length exceeded!
 - Dequeue
 - Test 1 (requires clause not met):
 - Input: R = <>, Q = <>
 - Expected Output: Error, Q must contain an element!
 - Test 2 (lower boundary case):
 - Input: R = <>, Q = <2>
 - Expected Output: R = <2>, Q = <>
 - Test 3 (typical case):
 - Input: R = <>, Q = <5, 6, 8>
 - Expected Output: R = <5>, Q = <6, 8>
 - Swap_First_Entry
 - Test 1 (lower boundary)
 - Input: E = 3, Q = <1>
 - Expected Output: E = <1>, Q = <3>
 - Test 2 (upper boundary)
 - Input: E = 17, Q = <6, 9, 12, 18, 4>
 - Expected Output: E = <6>, Q = <17, 9, 12, 18, 4>
 - Test 3 (typical case)
 - Input: E = 5, Q = <3, 4, 5>
 - Expected Output: E = <3>, Q = <5, 4, 5>
 - Length
 - Test 1 (empty queue)
 - Input: Q = <>
 - Expected Output: Length = 0
 - Test 2 (lower boundary)
 - Input: Q = <9>
 - Expected Output: Length = 1
 - Test 3 (upper boundary)
 - Input: Q = <2, 4, 6, 8, 10>
 - Expected Output: Length = 5

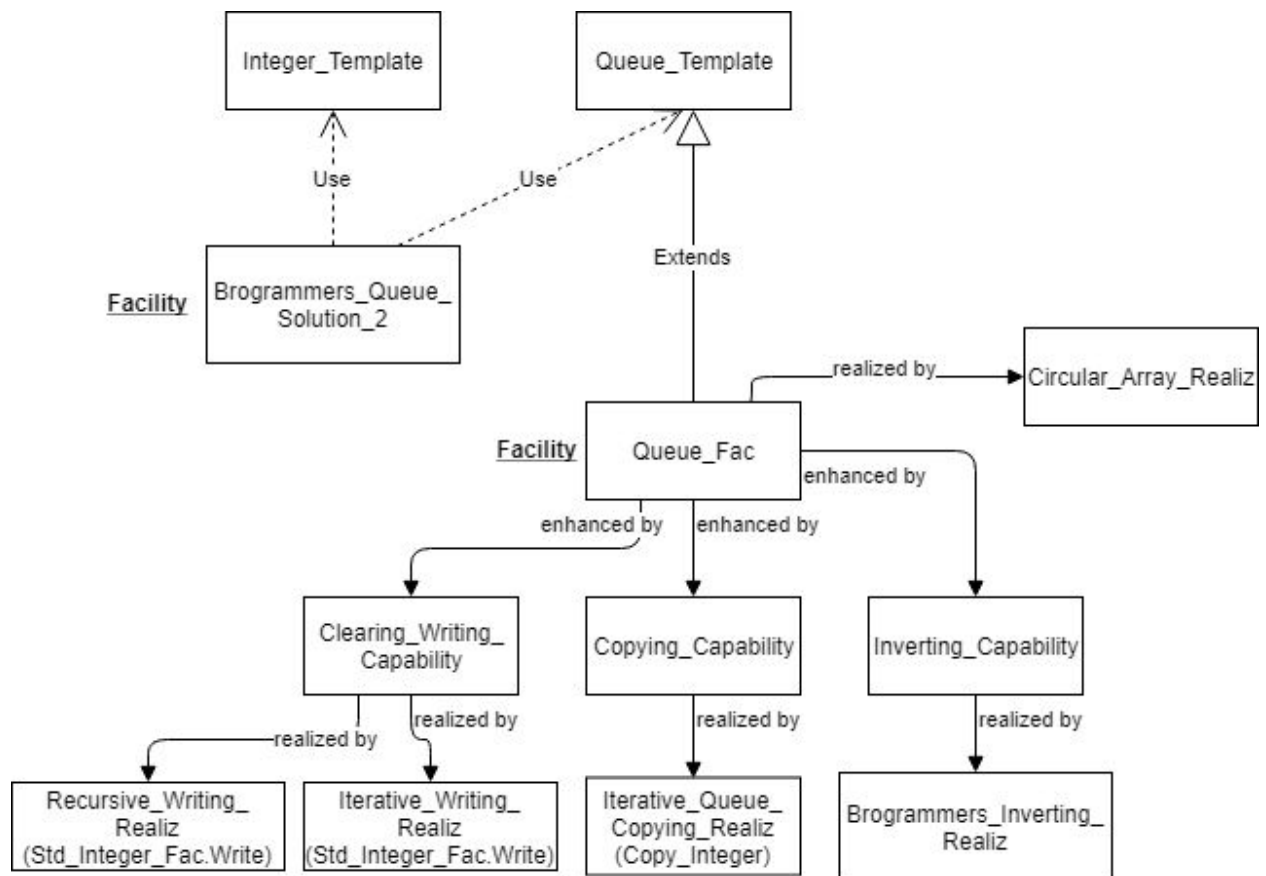
- Rem_Capacity
 - Test 1 (empty queue)
 - Input: Q = <>
 - Expected Output: Rem_Capacity = 5
 - Test 2 (typical case)
 - Input: Q = <2, 3, 4>
 - Expected Output: Rem_Capacity = 2
 - Test 3 (full queue!)
 - Input: Q = <6, 7, 8, 9, 10>
 - Expected Output: Rem_Capacity = 0
 - Clear
 - Test 1 (queue already empty)
 - Input: Q = <>
 - Expected Output: Q = <>
 - Test 2 (typical case)
 - Input: Q = <1, 4, 7>
 - Expected Output: Q = <>
 - Test 3 (upper boundary)
 - Input: Q = <10, 15, 20, 25, 30>
 - Expected Output: Q = <>
- Jackson
 - Search_Store_Template(assuming Max_Capacity = 5)
 - Add (restores k: Key; updates S: Store);
 - Lower Boundary
 - Input: k = 3, S = {};
 - Output: k = 3, S = {3};
 - Upper boundary
 - Input: k = 7, S = {1,2,3,4}
 - Output: k = 7, S = {1,2,3,4,7}
 - Requires clause not met
 - Input: k = 3, S = {1,2,3,4}
 - Output: Error, k cannot already exist in S
 - Remove (restores k: Key; updates S: Store);
 - Lower boundary
 - Input: k = 3, S = {3}
 - Output: k = 3, S = {}
 - Typical case
 - Input: k = 2, S = {1,2,3,4}
 - Output: k = 2, S = {1,3,4}
 - Requires Clause not met
 - Input: k = 4, S = {1,2,3}
 - Output: Error. K must be within S
 - Remove_Any (replaces k: Key; updates S: Store);
 - Lower boundary
 - Input: k = 3, S = {3}

- Output: $k = 3, S = \{\}$
 - Upper Boundary
 - Input: $k = 5, S = \{1,2, 3,4,5\}$
 - Output: $k=5, S= \{1,2,3,4\}$
 - Difficult case
 - Input: $k = 3, S = \{1,2\}$
 - Output: $k = 3, S = \{1,2\}$
- Is_Present(restores k: Key; restores S: Store): Boolean;
- Lower Boundary
 - Input: $k = 3, S = \{3\}$
 - Output: True.
 - Typical Case
 - Input: $k = 4, S = \{1,2,3\}$
 - Output: False.
 - Upper Boundary
 - Input: $k = 2, S = \{1,2,3,2,4\}$
 - Output: True
- Key_Count (restores S: Store): Integer;
- Lower Boundary
 - Input: $S = \{\}$
 - Output: 0
 - Upper Boundary
 - Input: $S = \{5,5,5,5,5\}$
 - Output: 5
 - Typical Case
 - Input: $S = (2,2,2)$
 - Output: 3
- Rem_Capacity (restores S: Store): Integer;
- Lower Boundary
 - Input: $S = \{\}$
 - Output: 5
 - Upper Boundary
 - Input: $S = \{5,5,5,5,5\}$
 - Output: 0
 - Typical Case
 - Input: $S = (2,2,2)$
 - Output: 2
- Clear (clears S: Store);
- Lower Boundary
 - Input: $S = \{\}$
 - Output: $S = \{\}$
 - Upper Boundary
 - Input: $S = \{5,5,5,5,5\}$
 - Output: $S = \{\}$

- Typical Case
 - Input: S= (2,2,2)
 - Output: S = {}
- Jack
 - Globally_Bounded_List_Template
 - Advance (updates P: List);
 - Test 1: Requires Clause Not Met
 - Input: P = <3, 4, 5>; P.Prec = <3, 4, 5>; P.Rem = <>
 - Output: Error! P.Rem must contain an entry!
 - Test 2: P.Rem Lower Boundary
 - Input: P = <8, 9, 10, 7>; P.Prec = <8, 9, 10>; P.Rem = <7>
 - Output: P = <8, 9, 10, 7>; P.Prec = <8, 9, 10, 7>; P.Rem = <>
 - Test 3: P.Prec Lower Boundary
 - Input: P = <1, 2, 3, 4, 5>; P.Prec = <>; P.Rem = <1, 2, 3, 4, 5>
 - Output: P = <1, 2, 3, 4, 5>; P.Prec = <1>; P.Rem = <2, 3, 4, 5>
 - Reset (updates P: List);
 - Test 1: P.Prec Is Empty (lower boundary)
 - Input: P = <3, 4, 5>; P.Prec = <>; P.Rem = <3, 4, 5>
 - Output: P = <3, 4, 5>; P.Prec = <>; P.Rem = <3, 4, 5>
 - Test 2: P.Prec Upper Boundary
 - Input: P = <6, 7, 8, 9>; P.Prec = <6, 7, 8, 9>; P.Rem = <>
 - Output: P = <6, 7, 8, 9>; P.Prec = <>; P.Rem = <6, 7, 8, 9>
 - Test 3: Typical Case
 - Input: P = <7, 7, 7, 7, 7>; P.Prec = <7, 7, 7>; P.Rem = <7, 7>
 - Output: P = <7, 7, 7, 7, 7>; P.Prec = <>; P.Rem = <7, 7, 7, 7, 7>
 - Is_Rem_Empty (restore P: List): Boolean;
 - Test 1: P.Rem Lower Boundary
 - Input: P = <7, 5, 7>; P.Prec = <7, 5, 7>; P.Rem = <>
 - Output: True
 - Test 2: P.Rem Upper Boundary
 - Input: P = <8, 8>; P.Prec = <>; P.Rem = <8, 8>
 - Output: False
 - Test 3: Typical Case
 - Input: P = <5, 4, 3, 2>; P.Prec = <5, 4>; P.Rem = <3, 2>
 - Output: False
 - Insert (alters New_Entry: Entry; updates P: List);
 - Test 1: Empty List
 - Input: New_Entry = <1>; P = <>; P.Prec = <>; P.Rem = <>

- Output: New_Entry = <0>; P = <1>; P.Prec = <>; P.Rem = <1>
- Test 2: P.Rem Lower Boundary
 - Input: New_Entry: <9>; P = <3, 3, 3>; P.Prec = <3, 3, 3>; P.Rem = <>
 - Output: New_Entry: <0>; P = <3, 3, 3, 9>; P.Prec = <3, 3, 3>; P.Rem = <9>
- Test 3: Typical Case
 - Input: New_Entry = <4>; P = <1, 2, 3, 5, 6>; P.Prec = <1, 2, 3>; P.Rem = <5, 6>
 - Output: New_Entry = <0>; P = <1, 2, 3, 4, 5, 6>; P.Prec = <1, 2, 3>; P.Rem = <4, 5, 6>
- Remove (replaces Entry_Removed: Entry; updates P: List);
 - Test 1: Requires Clause Not Met
 - Input: P = <1, 2, 3>; P.Prec = <1, 2, 3>; P.Rem = <>; Entry_Removed = <>
 - Output: Error! P.Rem must contain an entry!
 - Test 2: Typical
 - Input: P = <18, 9, 3, 1>; P.Prec = <18>; P.Rem = <9, 3, 1>;
 - Output: P = <18, 3, 1>; P.Prec = <18>; P.Rem = <3, 1>; Entry_Removed = <9>
 - Test 3: P.Rem Lower Boundary
 - Input: P = <7, 7, 7, 7, 7>; P.Prec = <7, 7, 7, 7>; P.Rem = <7>
 - Output: P = <7, 7, 7, 7>; P.Prec = <7, 7, 7, 7>; P.Rem = <>; Entry_Removed = <7>
- Advance_to_End (updates P: List);
 - Test 1: P.Prec Lower Boundary
 - Input: P = <6, 6, 6>; P.Prec = <>; P.Rem = <6, 6, 6>
 - Output: P = <6, 6, 6>; P.Prec = <6, 6, 6>; P.Rem = <>
 - Test 2: P.Prec Upper Boundary
 - Input: P = <8, 8, 8, 9>; P.Prec = <8, 8, 8, 9>; P.Rem = <>
 - Output: P = <8, 8, 8, 9>; P.Prec = <8, 8, 8, 8>; P.Rem = <>
 - Test 3: Typical
 - Input: P = <3, 4, 5>; P.Prec = <3>; P.Rem = <4, 5>
 - Output: P = <3, 4, 5>; P.Prec = <3, 4, 5>; P.Rem = <>
- Swap_Remainders (updates P, Q: List);
 - Test 1: P.Rem & Q.Rem Lower Boundaries
 - Input: P = <2, 2, 2>; P.Prec = <2, 2, 2>; P.Rem = <>; Q = <1, 1, 1>; Q.Prec = <1, 1, 1>; Q.Rem = <>
 - Output: P = <2, 2, 2>; P.Prec = <2, 2, 2>; P.Rem = <>; Q = <1, 1, 1>; Q.Prec = <1, 1, 1>; Q.Rem = <>
 - Test 2: P.Rem & Q.Rem Upper Boundaries

- Input: P = <7, 7, 7, 7>; P.Prec = <>; P.Rem = <7, 7, 7, 7>; Q = <6, 6, 6>; Q.Prec = <>; Q.Rem = <6, 6, 6>
 - Output: P = <6, 6, 6>; P.Prec = <>; P.Rem = <6, 6, 6>; Q = <7, 7, 7, 7>; Q.Prec = <>; Q.Rem = <7, 7, 7, 7>;
- Test 3: Typical
 - Input: P = <2, 4, 6, 8>; P.Prec = <2, 4>; P.Rem = <6, 8>; Q = <1, 3, 5>; Q.Prec = <1, 3>; Q.Rem = <5>
 - Output: P = <2, 4, 5>; P.Prec = <2, 4>; P.Rem = <5>; Q = <1, 3, 6, 8>; Q.Prec = <1, 3>; Q.Rem = <6, 8>
- Is_Prec_Empty (restores P: List): Boolean;
 - Test 1: P.Prec Lower Boundary
 - Input:
 - Output:
 - Test 2: P.Prec Upper Boundary
 - Input:
 - Output:
 - Test 3: Typical
 - Input:
 - Output:
- Clear (clears P: List)
 - Test 1: Empty List
 - Input: P = <>; P.Prec = <>; P.Rem = <>
 - Output: P = <>; P.Prec = <>; P.Rem = <>
 - Test 2: One Entry List
 - Input: P = <2>; P.Prec = <>; P.Rem = <2>
 - Output: P = <>; P.Prec = <>; P.Rem = <>
 - Test 3: Typical
 - Input: P = <6, 8, 0>; P.Prec = <6, 8>; P.Rem = <0>
 - Output: P = <>; P.Prec = <>; P.Rem = <>



(Here's all of our final code, *juuust* in case!)

```
Facility Brogrammers_Queue_Solution_2;  
uses Integer_Template, Queue_Template;
```

```
Operation Copy_Integer(replaces C: Integer; restores Orig: Integer);  
    ensures C = Orig;  
Procedure  
    C := Orig;  
end Copy_Integer;
```

```
Facility Queue_Fac is Queue_Template(Integer, 3)  
    realized by Circular_Array_Realiz  
    enhanced by Inverting_Capability  
    realized by Brogrammers_Inverting_Capability  
    enhanced by Copying_Capability  
    realized by Iterative_Queue_Copying_Realiz(Copy_Integer)  
    (*enhanced by Clearing_Writing_Capability  
    realized by Iterative_Writing_Realiz(Std_Integer_Fac.Write)*)  
    (*enhanced by Clearing_Writing_Capability  
    realized by Recursive_Writing_Realiz(Std_Integer_Fac.Write)*);
```

--This operation was completed by Reagan

```
Operation Rotate (updates Q: Queue);  
    requires 1 <= |Q|;  
    ensures Q = Prt_Btwn(1, |#Q|, #Q) o Prt_Btwn(0, 1, #Q) and 1 <= |Q|;
```

```
Procedure  
Var R: Integer;
```

```
Dequeue(R, Q);  
Enqueue(R, Q);
```

```
end Rotate;
```

(*I had several repeated errors on line 19 and 23. I was originally overthinking this code and trying to put a loop in here until I realized that was completely unnecessary.*)

--This operation was completed by Jackson

```
Operation Split_Into(clears P: Queue; replaces E: Integer; replaces Q: Queue);  
    requires 1 <= |P|;  
    ensures #P = Q o <E>;
```

```
Procedure  
Dequeue(E,P);
```



```

Clear(Q);
While ( 1 <= Length(P) )
    maintaining #P = Q o <E> o P;
    decreasing |P|;
do
    Enqueue(E,Q);
    Dequeue(E,P);

end;

```

end Split_Into;

(*my difficulty with this part was largely in figuring out where to place the E and Q values, I at first had the idea to place the Dequeue below the while statement and change the while statement to $1 < \text{Length}(P)$ but i quickly realized this cause problems for the body of the while loop and was overall unnecessary due to the E value being set to the last value in P automatically.*)

--This operation was completed by Jack

Operation Combine (updates P: Queue; alters E: Integer; clears Q: Queue);

```

--Combines the contents of two Queues with a new entry between them
requires |P| + 1 + |Q| <= 3;
ensures P = #P o <#E> o #Q;

```

Procedure

--Place E onto P

```

Enqueue(E, P);

```

--This while loop goes through Q taking its entries and

--putting them onto the end of P

```

While(1 <= Length(Q))
    maintaining #P o <#E> o #Q = P o Q;
    decreasing |Q|;
do
    Dequeue(E, Q);
    Enqueue(E, P);
end;

```

--I had an issue concerning the maintaining specification I was

--using for my While loop. I had originally tried using temporary

--variables and kept running into problems with that particular line.

--So I simplified my code and then Enqueued E onto P earlier so that

--I would be able to use E to move entries from Q onto P. My

--maintaining statement was simplified and proved immediately.

end Combine;

--This operation was completed by Reagan
Operation Read_Queue(replaces Q: Queue);
--informally ensures that Q has inputs in reverse order

requires $|Q| \leq 3$;

ensures $1 \leq |Q|$;

Procedure

Var E: Integer;

Clear(Q);

While ($1 \leq \text{Rem_Capacity}(Q)$)
decreasing $3 - |Q|$;

do

Read(E);

Enqueue(E, Q);

end;

end Read_Queue;

(*This was very difficult for me. At first, I didn't know how to complete this using only Enqueue and Dequeue. Then I realized it would work if I used the Inject_at_Front enhancement. I also struggled with what the invariant should be until I realized that I couldn't really be more specific than a vague one (using length). Then I had to change the loop condition to make sure I was checking that I had enough room in T and that Q wasn't getting too small. Then it worked!*)

--This operation was completed by Jackson

Operation Write_Queue(clears Q:Queue);

-- informally ensures output has the contents of #Q in order

requires $1 \leq |Q|$;

Procedure

Var T: Queue;

Var A: Integer;

Dequeue(A, Q);

While ($1 \leq \text{Length}(Q)$)
maintaining $\#Q = T \circ \langle A \rangle \circ Q$;
decreasing $|Q|$;

do

Enqueue(A, T);

Dequeue(A, Q);

end;

end Write_Queue;

```

(*)
  Operation Copy_Queue(restores Q : Queue; replaces Q_Copy: Queue);
  ensures Q_Copy = Q;
  Procedure
  Var E: Entry;
  Var T: Queue;
  Clear(Q_Copy);
  Dequeue(E, Q);
  While ( 1 <= Depth(Q) )
    maintaining #Q = T o Q;
    decreasing |Q|;
  do
    Enqueue(E, T);
    Enqueue(E, Q_Copy);
    Dequeue(E, Q);
  end;
  Q := T;

end Copy_Queue;
*)

```

--This operation was completed by Jack

Operation Main();

--Main program that calls all five operations

Procedure

Var P: Queue;

Var E: Integer;

Var Q: Queue;

Read_Queue(P);

--Rotates P so its first Integer is at the end

Rotate(P);

--Takes P's last Integer and puts it in E while

--Taking the rest of P's contents and puts them into Q

Split_Into(P, E, Q);

--Combines contents of the empty queue P, element E, and Q

--This should restore the contents of P to #P

Combine(P, E, Q);

Invert(P);

```
Copy_Queue(P, Q);
```

```
--Makes sure output for P is in correct order
```

```
Write_Queue(P);
```

```
end Main;
```

```
end Brogrammers_Queue_Solution_2;
```