

## Tracing the Galactic Origins of Selected Four G-type Stars in the Solar Neighbourhood

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### ABSTRACT

We present a multi-method investigation of four metal-poor G-type main-sequence stars to resolve their Galactic origins. By combining high-resolution spectroscopy from PolarBase, photometric/astrometric data from *Gaia* DR3, and spectral energy distribution (SED) modelling, we derive precise stellar parameters, chemical abundances, kinematics and Galactic orbital parameters. The stars HD 22879, HD 144579, HD 188510, and HD 201891 show effective temperatures of  $5855 \pm 110$ ,  $5300 \pm 160$ ,  $5370 \pm 60$ , and  $5880 \pm 90$  K; surface gravities of  $4.40 \pm 0.18$ ,  $4.52 \pm 0.37$ ,  $4.57 \pm 0.13$ , and  $4.48 \pm 0.18$  cgs; and metallicities of  $-0.86 \pm 0.08$ ,  $-0.55 \pm 0.12$ ,  $-1.60 \pm 0.07$ , and  $-1.15 \pm 0.07$  dex, respectively. Kinematic analysis suggests that HD 22879, HD 144579, and HD 201891 are potential bulge-origin escapees, possibly ejected by the Galactic bar or spiral arm perturbations. HD 188510, however, shows halo-like dynamics, including a retrograde orbit. Chemical abundance trends ( $[\alpha/\text{Fe}]$  vs.  $[\text{Fe}/\text{H}]$ ) reveal mixed origins, challenging kinematic classifications. This discrepancy highlights the importance of integrative methodologies in Galactic archaeology. We associate HD 22879, HD 144579, and HD 201891 with the bulge globular cluster NGC 6441, NGC 5927, and NGC 6544, respectively. HD 188510's retrograde motion and low metallicity align with ejection from the halo globular cluster NGC 5139 ( $\omega$  Cen). These results illustrate the complex interplay of dynamical processes—including bar resonances, spiral arm perturbations, and tidal stripping—in depositing metal-poor stars into the solar neighborhood.

**Keywords:** Solar neighborhood (1509) — Chemical abundances (224) — Stellar kinematics (1608) — Stellar dynamics (1596)

### 1. INTRODUCTION

Older stellar populations in the Milky Way retained traces of metal enrichment from the early universe. Analyzing stellar elemental abundances, ages, and kinematics offers insights into the sources of metal enrichment, notably Pop III stars. Studying the chemical composition of stars with varying metal levels is crucial for understanding Galactic evolution (B. E. Reddy et al. 2003; A. Frebel 2010; D. Yong et al. 2013; M. R. Hayden et al. 2015; C. Battistini & T. Bensby 2016). Examining the chemical abundances of metal-poor stars in the atmosphere provides observational data that can be compared with the theoretical models of nucleosynthesis in the first metal-poor massive stars that ended as supernovae. Analyzing trends in element abundance ratios relative to metal content can help trace the chemical

history of the Milky Way (T. C. Beers & N. Christlieb 2005; A. Frebel & J. E. Norris 2015a).

The chemical compositions and kinematic characteristics of these stars can be compared with models of Galactic chemical evolution to elucidate the early chemical enrichment processes of galaxies. J. W. Chamberlain & L. H. Aller (1951) disclosed the presence of metal-poor stars like HD 19445 and HD 140283, initiating the investigation. Today, highly metal-poor stars like SMSS 0313-6708 have also been identified. T. C. Beers & N. Christlieb (2005) classified stars based on their metal content, from super metal-rich (SMR) stars to extremely metal-poor (EMP) stars. Stars with metal content exceeding 0.5 dex are termed super metal-rich (SMR), while those below -6 dex are classified as ultra metal-poor (UMP). Within the intermediate range, stars fall into categories such as metal-poor (MP,  $\leq -1$  dex), very metal-poor (VMP,  $\leq -2$  dex), extremely

metal-poor (EMP,  $\leq -3$  dex), ultra-metal-poor (UMP,  $\leq -4$  dex), and hypermetal-poor (HMP,  $\leq -5$  dex).

The evolution of the Milky Way can be further understood by studying metal-poor stars to provide insights into early star formation and galaxy mergers. K. Freeman & J. Bland-Hawthorn (2002) suggest that these stars reveal the formation history of our Galaxy. The chemical composition of metal-poor stars reflects the conditions of the early universe and the effects of initial supernovae. A. Bonaca et al. (2017) traced the past mergers of the Milky Way by examining the Galactic orbits of metal-poor stars, showing radial migrations from the center to distant regions. Additionally, S. Salvadori & A. Ferrara (2009) emphasized the role of these stars in clarifying the chemical enrichment history of the Galaxy and the effects of early supernovae. J. Tumlinson (2010) highlights the importance of metal-poor stars in the outer Milky Way for Galactic formation processes. Analyzing the chemical and dynamic characteristics of these stars is essential for reconstructing the early stages of Galactic evolution. S. Hirano et al. (2014) investigate the mass distribution of Pop III stars and the factors influencing their formation, revealing a wide mass spectrum ranging from 10 to 1,000  $M/M_{\odot}$ .

The classification of stellar populations based on fundamental astrophysical parameters has transitioned from simple kinematic criteria to sophisticated multi-dimensional analysis. O. J. Eggen et al. (1962) introduced the first systematic framework by correlating stellar kinematics and metallicities, proposing a dichotomy between the halo and disk populations. This was later augmented by G. Gilmore & N. Reid (1983), who identified the thick disk as a separate Galactic component. Recent spectroscopic campaigns such as GALAH (S. Buder et al. 2018) and APOGEE (S. R. Majewski et al. 2017) have employed chemical tagging techniques, leveraging [X/Fe] abundance ratios to trace star formation sites. In recent years, datasets from *Gaia* ( Gaia Collaboration et al. 2016a, 2018, 2023) and complementary ground-based spectroscopic programs have revolutionized the field, offering unprecedented resolution to trace the hierarchical assembly of the Galaxy and the history of star formation.

Metal-poor stars serve as critical tracers of the chemical evolution of the Milky Way because their atmosphere preserves the nucleosynthetic signatures of their progenitor populations. Stars with intermediate iron abundances ( $-2.5 < [\text{Fe}/\text{H}] (\text{dex}) < -1$ ) are likely formed from gas enriched by the ejecta of double-stability supernovae, retaining the chemical imprints of the first stellar generation (140–260  $M_{\odot}$ ; S. Salvadori et al. 2019). Numerous studies have focused on the halo regions of

the Galaxy, where the mean metallicity ranges from  $[\text{Fe}/\text{H}] = -1.6$  dex in the inner halo to  $[\text{Fe}/\text{H}] = -2.2$  dex in the outer halo (K. Bekki & M. Chiba 2001); however, the origin and evolutionary pathways of metal-poor stars remain incompletely understood. Recent investigations combining stellar orbits, kinematics, and chemical abundance (for example, A. Bonaca et al. 2019; P. Di Matteo et al. 2019) have advanced our knowledge of their Galactic distribution and dynamic histories.

However, a review of the literature revealed that detailed chemical abundance analyses of metal-poor stars are scarce (C. B. Pereira et al. 2017; M. Marişmak et al. 2024; S. A. Şentürk et al. 2024; N. Holanda et al. 2024). Notably, except for C. B. Pereira et al. (2017), the cited studies represent comprehensive work conducted by the project team members as part of this research initiative. C. B. Pereira et al. (2017) analyzed HD 55496, a metal-poor star enriched in slow neutron-capture (s-process) elements, proposing its potential origin as a second-generation GC star. However, their conclusion favoring a dwarf galaxy progenitor, derived solely from abundance trends without comparative kinematic or dynamical evidence, warrants critical scrutiny.

In contrast, the foundational work of T. Şahin & S. Bilir (2020) established a robust framework for studying metal-poor stars. Their high-resolution spectroscopic analysis of selected F-type stars in the northern Galactic Hemisphere, combined with Bayesian age recalibrations and kinematic-orbit dynamic modeling, provided novel insights into the physical nature (population type) and Galactic origins of metal-poor stars. The updated atmospheric parameters and age determination for HD 84937, a *Gaia* benchmark star, are the key outcomes. Crucially, the Galactic orbital parameters calculated for these stars, mirroring the methodology of the current project, were employed to verify population classifications. A persistent challenge in metal-poor star studies is the significant discrepancies in reported atmospheric parameters and derived abundances across the literature.

These inconsistencies have been emphasized in recent studies by project teams (T. Şahin & S. Bilir 2020; M. Marişmak et al. 2024; S. A. Şentürk et al. 2024), hinders definitive conclusions about their characteristic properties (kinematic, dynamic, and composition-based) and origins. For instance, simulations by P. Di Matteo et al. (2019) demonstrated how orbital dynamics and chemical evolution jointly shape the distribution of metal-poor stars near the Galactic center; however, observational validation remains limited. Systematic spectral, kinematic, and dynamic orbital analyses of highly proper motion (HPM) stars offer a pathway for resolving these

uncertainties. By correlating precise abundance patterns with orbital histories, future studies may disentangle the contributions of ancient supernovae, accretion events, and in-situ formation to the metal-poor stellar inventory.

In this study, we determined the fundamental astrophysical parameters and Galactic origins of four G spectral-type main-sequence stars, HD 22879, HD 144579, HD 188510, and HD 201891, in different metal abundance ranges selected from the solar neighborhood. The remainder of this paper is organized as follows: Section 2 introduces the data used in this study, including spectroscopic, photometric, and astrometric observations. Section 3 focuses on the results obtained from spectral energy distribution analysis, photometric and astrometric analyses, spectral analysis, and kinematic and dynamic orbit analyses. Finally, Section 4 summarizes the findings and discusses the membership of the studied stars to Galactic populations and their possible Galactic origins.

## 2. DATA

### 2.1. *Ground-based: High-Resolution Spectroscopy*

To identify suitable target stars, we initially selected G-type stars from the ELodie Stellar Library (C. Soubiran et al. 2003). Of the 545 G-type stars in this catalog, 173 were cross-matched with the entries in *Gaia* Data Release 3 (DR3; Gaia Collaboration et al. 2021). We subsequently refined this subset by focusing on the HPM stars. Potential spectroscopic binaries were systematically excluded via cross-examination with the SIMBAD astronomical database (M. Wenger et al. 2000). This process yielded a preliminary sample of 90 G-type HPM stars. To ensure data quality, we imposed a threshold of renormalized unit weight error (RUWE) of 1.4, following the recommendations of L. Lindegren et al. (2021). RUWE values below this threshold indicate robust astrometric solutions as they quantify the consistency between the observed stellar positions and model predictions. The application of these criteria produced a metallicity-constrained sample of 74 G-type HPM stars. The final target prioritization considered three key factors: (1) confinement to main-sequence stars (evidenced by surface gravities  $\log g > 4.0$ ), (2) availability of high-quality observational data (particularly high-resolution spectra), and (3) precise *Gaia* DR3 astrometric measurements (trigonometric parallax and proper motion components), which are essential for deriving reliable stellar parameters. Through this multi-stage selection process, we identified four metal-poor stars in the solar neighborhood that satisfied all criteria. The complete target sample is presented in Table 1.

The spectra, which are downloaded from the POLAR-BASE library<sup>4</sup>, consist of approximately 4,700 stellar spectra across different luminosity classes, ranging from spectral types O4 to M8 (P. Petit et al. 2014). Stellar spectra were obtained from the region of the electromagnetic spectrum between 3,700 and 10,000 Å. The library also contains the spectra of a large number of metal-poor stars for the study of the early universe and the formation of the Milky Way. The high-resolution and high-(S/N) spectra of the four stars were obtained using the ESPaDOnS and Narval high-resolution spectrometers, and their basic data are listed in Table 1.

We employed LIME code (T. Şahin 2017) to normalize the spectra within the spectral library. The LIME code facilitated line identification in the continuum-normalized spectrum, providing associated atomic data such as the Rowland multiplet number (RMT),  $\log gf$ , and lower-level excitation energy (L.E.P.). Atomic data were sourced from the NIST<sup>5</sup> and VALD<sup>6</sup>. The majority of the identified lines exhibited good isolation, making them suitable for equivalent width (EW) analysis performed using the LIME code. The LIME code was instrumental in performing equivalent width (EW) analysis on the majority of well-isolated identified lines.

**Table 1.** Name, spectral type, spectrograph,  $S/N$ , radial velocity and observation date of four stars from the POLAR-BASE database. The spectral types of the program stars were obtained from SIMBAD. The corrected POLARBASE spectra accounted for the reported heliocentric radial velocities, which were cross-checked by the Solar spectrum.

Star	HD 22879	HD 144579	HD 188510	HD 201891
Spectral Type	G0VmF2	G8V	G5V:	G5V
Spectrograph	Narval	ESPaDOnS	Narval	Narval
$S/N$	226.96	149.52	105.67	143.99
$V_R$ (km s $^{-1}$ )	120.18	-59.61	-192.72	-44.69
Obs. Date	12.11.2010	12.03.2017	11.08.2010	16.08.2010

### 2.2. *Space-based: Comprehensive Data from Gaia DR3*

The *Gaia* satellite, launched in 2013 by the European Space Agency (ESA), provides photometric, astrometric, and spectroscopic observations of Galactic and extragalactic sources to create a three-dimensional spatial and velocity map of the Milky Way, aiming to measure the spatial and velocity distributions of stars and determine their astrophysical properties, such as effec-

<sup>4</sup> <http://polarbase.irap.omp.eu/>

<sup>5</sup> NIST Atomic Spectra Database <http://physics.nist.gov/PhysRefData/ASD>

<sup>6</sup> VALD Atomic Spectra Database <http://vald.astro.uu.se>

**Table 2.** Astrometric and spectroscopic data of the four programme stars from the *Gaia* DR3 catalogue.

Star	HD 22879	HD 144579	HD 188510	HD 201891
$\alpha$ (hh:mm:ss)	03 40 22.06	16 04 56.79	19 55 09.67	21 11 59.03
$\delta$ (dd:mm:ss)	-03 13 01.12	+39 09 23.43	+10 44 27.39	+17 43 39.89
$l$ ( $^{\circ}$ )	189.7665	62.3693	49.9314	66.7067
$b$ ( $^{\circ}$ )	-43.1192	48.2726	-8.9179	-20.4288
$\mu_{\alpha} \cos \delta$ (mas yr $^{-1}$ )	$690.795 \pm 0.032$	$-570.872 \pm 0.016$	$-38.395 \pm 0.022$	$-122.133 \pm 0.019$
$\mu_{\delta}$ (mas yr $^{-1}$ )	$-213.443 \pm 0.028$	$52.633 \pm 0.017$	$290.612 \pm 0.014$	$-899.404 \pm 0.015$
$\varpi$ (mas)	$38.325 \pm 0.031$	$69.641 \pm 0.014$	$26.278 \pm 0.020$	$29.877 \pm 0.021$
$V_R$ (km s $^{-1}$ )	$120.58 \pm 0.13$	$-59.44 \pm 0.12$	$-192.22 \pm 0.17$	$-44.33 \pm 0.12$
$T_{\text{eff}}$ (K)	$5926^{+1}_{-2}$	$5300^{+4}_{-14}$	-	-
$\log g$ (cgs)	$4.32 \pm 0.01$	$4.57^{+0.03}_{-0.02}$	-	-
[Fe/H] (dex)	$-1.61^{+0.07}_{-0.03}$	$-0.20 \pm 0.02$	-	-

tive temperature and surface gravity, to understand the structure, formation, and evolution of the Galaxy ( [Gaia Collaboration et al. 2016b](#)). The first data release (DR1) was published in 2016, followed by DR1, DR2, EDR3, and DR3, to date [Gaia Collaboration et al. \(2016a, 2018, 2021, 2023\)](#). The third release of data the *Gaia* mission (*Gaia* DR3; [Gaia Collaboration et al. 2023](#)) offers unprecedented precision in astrometry, photometry, and radial velocity measurements for more than 1.8 billion objects. The photometric data collected in the  $G$ ,  $G_{\text{BP}}$ , and  $G_{\text{RP}}$  bands provide insights into various stellar properties. The effective temperature, luminosity, radius, surface gravity, and metallicity are interconnected properties that provide a holistic view of stellar physics. The three-band photometric data ( $G$ ,  $G_{\text{BP}}$ ,  $G_{\text{RP}}$ ), combined with astrometric data ( $\alpha$ ,  $\delta$ ,  $\mu_{\alpha} \cos \delta$ ,  $\mu_{\delta}$ ,  $\varpi$ ) and spectroscopic measurements ( $V_R$ ), allow for the accurate and detailed derivation of the fundamental stellar parameters. In this study, we used *Gaia* DR3 data to determine the basic astrophysical parameters and Galactic origins of the four stars. The astrometric and spectroscopic data of the four stars analyzed by querying the database and model atmospheric parameters calculated by the *Gaia* consortium are listed in Table 2.

### 3. RESULTS

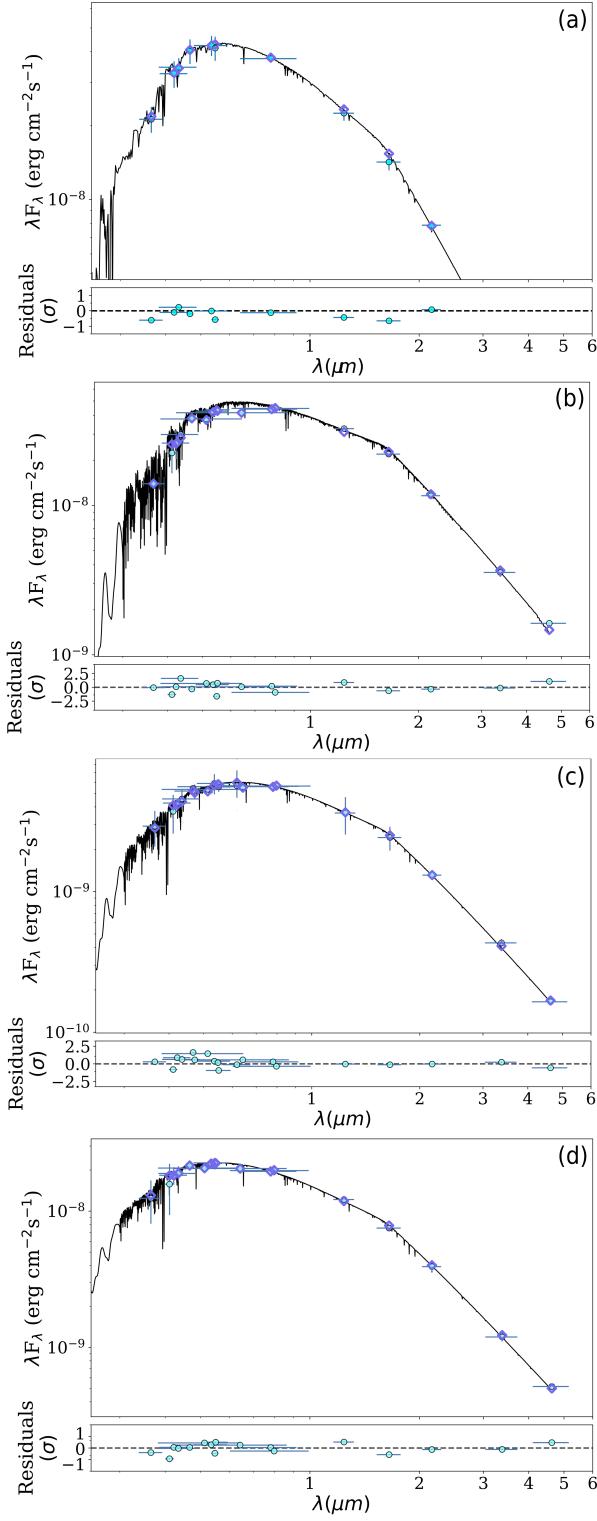
#### 3.1. Spectral Energy Distribution Analysis

The spectral energy distribution (SED) fitting was performed using the Python package SpectralA1 eneRgy dIstribution bAyesian moDel averagiNg fittEr (ARIADNE), which aims to use Bayesian model averaging to incorporate information from as many different atmospheric model grids to arrive at accurate and precise stellar parameters ([J. I. Vines & J. S. Jenkins 2022](#)). ARIADNE has been used with synthetic spectral model libraries, such as PHOENIX v2 ([T. O. Husser et al. 2013](#)) and ([F. Castelli & R. L. Kurucz 2003](#)), which are frequently referenced in the literature, to determine the

values of the effective temperature ( $T_{\text{eff}}$ ), surface gravity ( $\log g$ ), iron abundance [Fe/H],  $V$ -band extinction ( $A_V$ ), and distance ( $d$ ). In addition, MIST evolution models ([T. D. Morton 2015](#); [A. Dotter 2016](#)) have been used to calculate the mass ( $M$ ), stellar radius ( $R$ ), and age ( $\tau$ ) of stars. While fitting the SEDs, the program first used the current astrometric and photometric data of the stars *Gaia* DR3 ([Gaia Collaboration et al. 2023](#)) catalogue. In general, luminosity data in the wavelength range  $0.1 \leq \lambda (\mu\text{m}) \leq 5$  of the electromagnetic spectrum were used to generate SED fitting of the stars.

We collected broadband photometric data from various catalogues to fit the SED, including TYCHO  $B$  and  $V$  ([ESA 1997](#)), *Gaia* DR3  $G$ ,  $G_{\text{BP}}$ , and  $G_{\text{RP}}$  ([Gaia Collaboration et al. 2023](#)), TESS  $T$  ([G. R. Ricker et al. 2014](#)), 2MASS  $J$ ,  $H$ , and  $K_s$  ([M. F. Skrutskie et al. 2006](#)), and WISE  $W1$  and  $W2$  ([E. L. Wright et al. 2010](#)). We noticed that incorporating *GALEX* FUV/NUV and Stromgren  $ubv$  photometry significantly degrades the quality of our fits. This results in unreliable posterior constraints and frequent large discrepancies between the models and data ([C. K. Harada et al. 2024](#)). Consequently, we excluded *GALEX* FUV/NUV and Stromgren  $ubv$  photometry from SED analyses. In ARIADNE, we used the extinction law of [E. L. Fitzpatrick \(1999\)](#).

We determined that using 1,000 live points and a stopping criterion of  $d \log z = 0.5$  produced stable and well-converged posterior distributions. Figure 1 shows the SED fitting results (e.g. [D. C. Dursun et al. 2024](#)). [F. Castelli & R. L. Kurucz \(2003\)](#) model can accurately represent the SED of HD 22879 and HD 188510. The best-fitting parameters with their 68% confidence intervals for HD 22879 and HD 188510, respectively, are as follows:  $T_{\text{eff}} = 5985 \pm 30$  K,  $T_{\text{eff}} = 5580 \pm 26$  K,  $\log g = 4.5 \pm 0.03$  cgs,  $\log g = 4.74 \pm 0.03$  cgs, and  $R = 1.08 \pm 0.01 R_{\odot}$ ,  $R = 0.69 \pm 0.01 R_{\odot}$ . The PHOENIX v2 [T. O. Husser et al. \(2013\)](#) model accurately represented the



**Figure 1.** Best-fitting SED model for HD 22879 (a), HD 144579 (b), HD 188510 (c), and HD 201891 (d). The black curve represents the best-fitting model, whereas the cyan pluses and circles denote the retrieved photometric measurements. The blue diamonds correspond to synthetic photometry.

SED of HD 144579 and HD 201891. The best-fitting parameters for these stars, respectively, are as follows:  $T_{\text{eff}} = 5263 \pm 21$  K,  $T_{\text{eff}} = 5886 \pm 20$  K,  $\log g = 4.53 \pm 0.04$  cgs,  $\log g = 4.51 \pm 0.03$  cgs, and  $R = 0.79 \pm 0.01 R_{\odot}$ ,  $R = 1.01 \pm 0.01 R_{\odot}$ . We then estimated the stellar masses of stars based on the derived surface gravity and radius.

### 3.2. Photometric and Astrometric Analyses

The age of stars is often investigated using color magnitude diagrams (CMDs), which provide insights into stellar populations. With the advent of the *Gaia* era, precise proper motions and trigonometric parallaxes of stars in the solar neighborhood are now available with milli-arcsecond (mas) accuracy, whereas *Gaia* DR3 photometric data are delivered with milli-magnitude precision. These advancements have enabled the placement of the four stars studied herein on the  $M_G \times (G_{\text{BP}} - G_{\text{RP}})_0$  plane. In addition, by estimating the photometric metallicities of these stars, it was possible to determine their ages.

The *Gaia* DR3 provided photometric ( $G$ ,  $G_{\text{BP}}$ , and  $G_{\text{RP}}$ ) and astrometric ( $\varpi$ ) data that were used for age determination (see Table 2). The extinction coefficients ( $A_{\lambda}/A_V$ ) for the *Gaia* photometric system bands  $G$ ,  $G_{\text{BP}}$ , and  $G_{\text{RP}}$  were obtained from J. A. Cardelli et al. (1989), with values of 0.83627, 1.08337, and 0.63439, respectively. The following relationships were used to correct each filter for interstellar extinction (see also R. Canbay et al. 2023; S. Jyisan et al. 2025).

$$G_0 = G - A_G = G - 0.83627 \times A_V \quad (1)$$

$$(G_{\text{BP}})_0 = G_{\text{BP}} - A_{G(\text{BP})} = G_{\text{BP}} - 1.08337 \times A_V \quad (2)$$

$$(G_{\text{RP}})_0 = G_{\text{RP}} - A_{G(\text{RP})} = G_{\text{RP}} - 0.63439 \times A_V \quad (3)$$

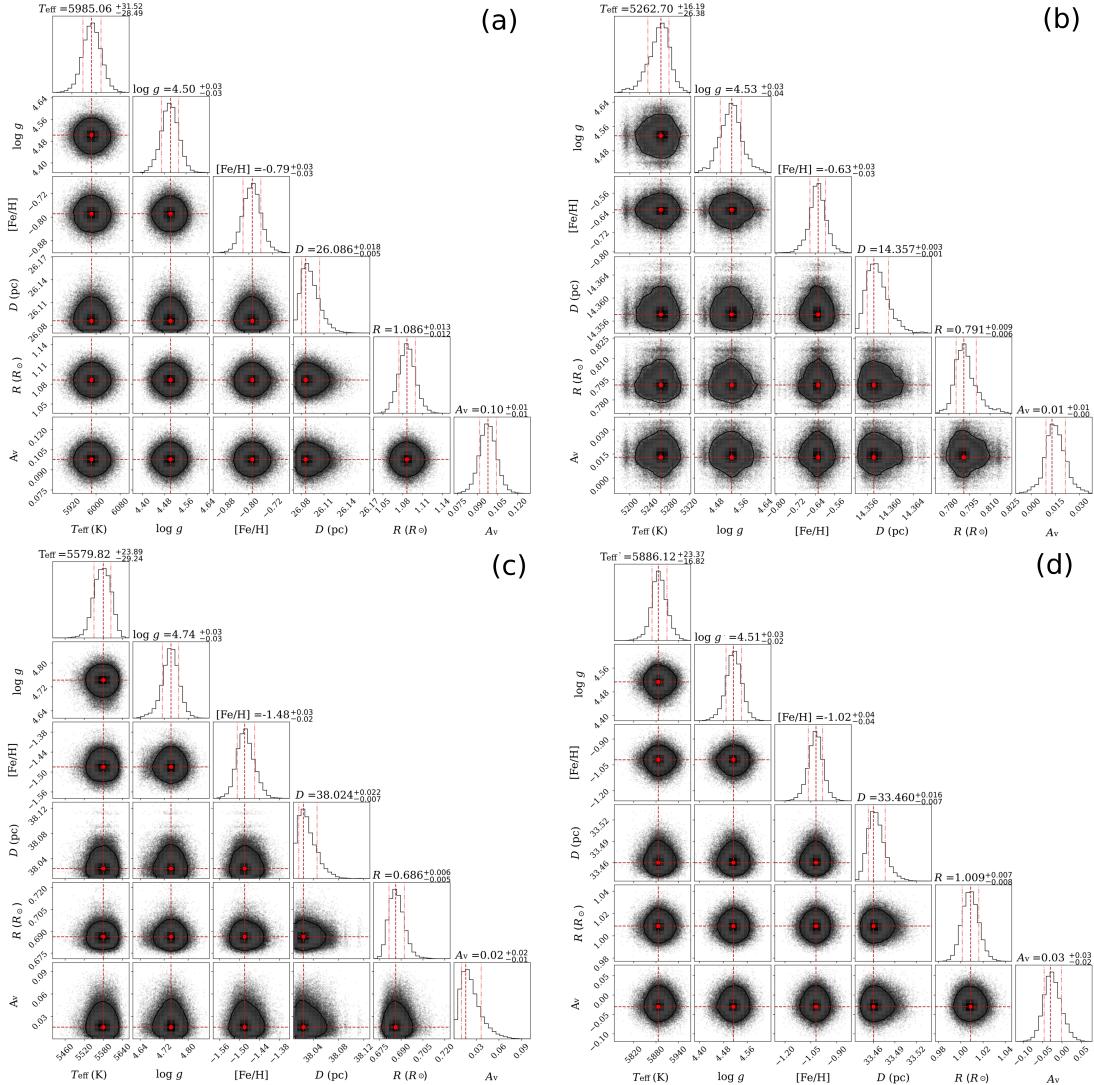
Thus, the *Gaia* DR3 ( Gaia Collaboration et al. 2023) photometric data of stars were corrected for interstellar extinction, and the errors are listed in Table 3. Subsequently, the  $G$  absolute magnitudes of the stars were calculated using the following distance relation:

$$M_G = G - 5 \times \log d + 5 - A_G \quad (4)$$

Here,  $M_G$  is the absolute magnitude of the star,  $G$  is the apparent magnitude,  $A_G$  is the extinction in the  $G$  band, and  $\varpi$  is the trigonometric parallax of the star. Given a star's distance  $d(\text{pc}) = 1000/\varpi$  (mas), by differentiating both sides, the error in the absolute magnitude of the  $G$  band ( $\Delta M_G$ ) was calculated using the following relation:

$$\Delta M_G = \frac{5}{d \times \ln 10} \times \Delta d + \Delta A_G \quad (5)$$

Here,  $\Delta A_G$  represents the error in the  $G$  band extinction, whereas  $\Delta d$  corresponds to the distance error arising from the trigonometric parallax measurements. The



**Figure 2.** Posterior distributions from the best-fit SED model for HD 22879 (a), HD 144579 (b), HD 188510 (c), and HD 201891 (d) are shown. Red points indicate mean posteriors, and red vertical lines represent 16, 50 and 84 percentiles.

**Table 3.** The photometric ( $G$ ,  $G_{\text{BP}}$ ,  $G_{\text{RP}}$ ) and astrometric ( $\varpi$ ) data from *Gaia* DR3, along with the extinction values in the  $G$  band ( $A_G$ ), the derived absolute magnitudes ( $M_G$ ), and the de-reddening colors ( $(G_{\text{BP}} - G_{\text{RP}})_0$ ), are reported for the four metal-poor stars. The parameters are provided in mag.

Star	$G$	$G_{\text{BP}}$	$G_{\text{RP}}$	$A_G$	$M_G$	$(G_{\text{BP}} - G_{\text{RP}})_0$
HD 22879	$6.536 \pm 0.003$	$6.822 \pm 0.003$	$6.075 \pm 0.004$	$0.079 \pm 0.005$	$4.374 \pm 0.002$	$0.704 \pm 0.005$
HD 144579	$6.461 \pm 0.003$	$6.843 \pm 0.003$	$5.898 \pm 0.004$	$0.012 \pm 0.001$	$5.675 \pm 0.001$	$0.944 \pm 0.005$
HD 188510	$8.647 \pm 0.003$	$8.973 \pm 0.003$	$8.138 \pm 0.004$	$0.017 \pm 0.002$	$5.744 \pm 0.002$	$0.834 \pm 0.005$
HD 201891	$7.231 \pm 0.003$	$7.501 \pm 0.003$	$6.781 \pm 0.004$	$0.017 \pm 0.001$	$4.607 \pm 0.001$	$0.719 \pm 0.005$

distance error was calculated using the following equation:

$$\Delta d = \frac{1000}{\varpi^2} \times \Delta \varpi \quad (6)$$

The obtained  $G$ -band absolute magnitudes ( $M_G$ ), along with their associated errors, are listed in Table 3. To determine the ages of stars from their astrometric and photometric data,  $M_G$  and  $(G_{BP} - G_{RP})_0$  are provided in Table 3. The CMDs were constructed for each star.

### 3.3. Spectral Analysis

This study utilized the local thermodynamic equilibrium (LTE) ATLAS9 model atmospheres (ODFNEW) from F. Castelli & R. L. Kurucz (2004) to conduct an abundance analysis on a sample of G-type stars. We used the MOOG LTE line analysis code<sup>7</sup> (C. Sneden 1974) to calculate the elemental abundances of the program stars. The methodology adopted for the abundance analysis and atomic data sources are consistent with those used in previous studies by T. Şahin & D. L. Lambert (2009), T. Şahin et al. (2011), T. Şahin et al. (2016), T. Şahin & S. Bilir (2020), T. Şahin et al. (2023), M. Marişmak et al. (2024), S. A. Şentürk et al. (2024), and T. Şahin et al. (2024). The preceding sections discuss the employed line list, atomic data, and derivation of stellar parameters.

The determination of the effective temperature ( $T_{\text{eff}}$ ) and other stellar parameters, such as the microturbulence ( $\xi$ ) and surface gravity ( $\log g$ ), are critical aspects of the analysis of the stellar atmosphere.  $T_{\text{eff}}$  was derived using the excitation balance method, which relies on neutral spectral lines with varying excitation potentials, specifically focusing on Fe I lines. The selected  $T_{\text{eff}}$  ensures that the derived abundance exhibits no dependence on the lower excitation potential (L.E.P.) of the spectral lines.

Microturbulence, which characterizes small-scale gas motion within the stellar atmosphere, is determined by applying the traditional criterion that the abundance of neutral or singly ionized species (e.g., Fe I) remains independent of the reduced equivalent width ( $EW/\lambda$ ). This analysis was conducted under the assumption of local thermodynamic equilibrium (LTE). For the Fe I lines, the conditions of independence from both the L.E.P. and  $EW/\lambda$  were simultaneously enforced.

Furthermore, microturbulence was individually determined using the Fe I, Fe II, Ti I, Ti II, Cr I, and Cr II lines. For each model, the dispersion in the abundances of Fe, Ti, and Cr was computed over a range of  $\xi$  values from 0 to 1.5 km s<sup>-1</sup>. As shown in Figure 4, this approach

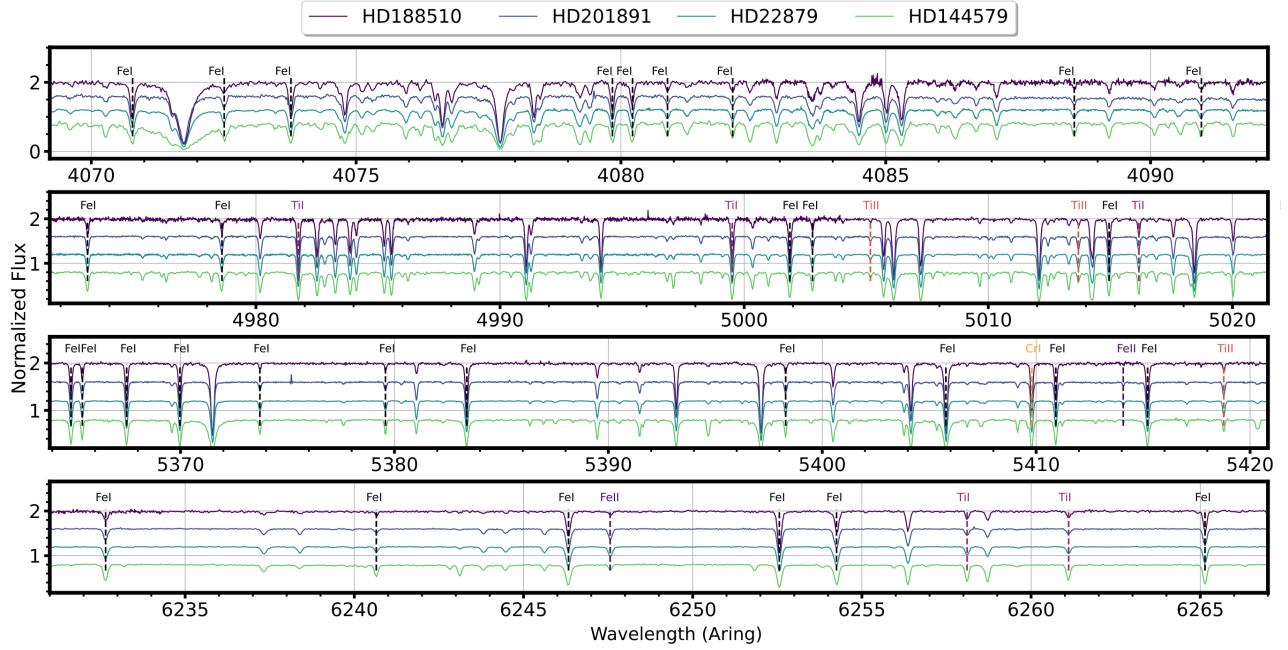
was applied to all stars analyzed in this study. For example, in the case of HD 22879 (top panel), the Fe I, Fe II, and Ti I lines yielded a micro-turbulent velocity of  $\approx 1.0$  km s<sup>-1</sup>. For the same star, the Cr I, and Ti II lines indicate a value of  $\approx 0.8$  km s<sup>-1</sup>, which is consistent with the results of classical spectroscopic analysis (Table 4). For HD 144579, the Fe I, Fe II, and Ti I lines exhibited minimal sensitivity to  $\xi$  across the range of  $0.0 \approx 0.8$  km s<sup>-1</sup>, whereas the Cr I lines suggested a microturbulent velocity of 0.8 km s<sup>-1</sup>. For HD 188510, the Ti II lines indicated microturbulence values between 0.5 and 0.6 km s<sup>-1</sup>, whereas the Fe I, Ti I and Cr I lines suggested values ranging from 0.0 to 0.5 km s<sup>-1</sup>. For HD 201891, the Fe I, Fe II, Ti I, and Ti II lines indicated a microturbulent velocity range of 0.7 to 1.2 km s<sup>-1</sup>, highlighting the uncertainty in the microturbulence value derived from classical spectroscopic analysis. A comparison of the two methods demonstrates that the estimated uncertainties in the microturbulence for all stars are consistent with those obtained from the classical spectroscopic analysis.

$\log g$  was constrained by enforcing the ionization equilibrium, ensuring that the Fe I and Fe II lines yielded consistent iron abundances. This analysis was performed using MOOG software. The metallicity ([Fe/H]) was iteratively adjusted to obtain agreement between the derived iron abundance and the initial abundance used to construct the model atmosphere. Convergence of the derived abundances was achieved by iteratively varying  $T_{\text{eff}}$ ,  $\log g$ , and  $\xi$  within the model.

The uncertainty in the derived effective temperature arises from the error in the slope of the relationship between the Fe I abundance and L.E.P. of the lines. For HD 22879, a temperature variation of  $\pm 110$  K results in a significant change in the slope. Similarly, a  $1\sigma$  discrepancy in [X/H] abundance between neutral and ionized Fe lines corresponded to a shift of approximately 0.2 dex in  $\log g$ . For HD 144579, this approach yielded uncertainties of  $\pm 160$  K for  $T_{\text{eff}}$  and  $\pm 0.37$  dex for  $\log g$ . The atmospheric parameters derived for all the stars are summarized in Table 4.

The determination of elemental abundance may be subject to various uncertainties. These include factors associated with the accuracy of  $gf$  values and potential deviations from the local thermodynamic equilibrium (LTE) in the formation processes of atomic spectral lines. To ensure the accuracy of  $gf$  values and mitigate systematic errors, we derived solar abundances using stellar line measurements. Equivalent widths were measured from the solar flux atlas of R. L. Kurucz et al. (1984) and analyzed with a solar model atmosphere selected from the F. Castelli & R. L. Kurucz (2004) grid, adopting the parameters  $T_{\text{eff}} = 5790$  K and  $\log g = 4.40$

<sup>7</sup> <http://www.as.utexas.edu/~chris/moog.html>



**Figure 3.** Small regions of the spectra for HD 188510, **HD 201891**, HD 22879, and HD 144579. For convenience, the spectra were shifted vertically. A selection of neutral and ionized lines used in the analysis are indicated by a vertical dashed line.

cgs,  $[Fe/H] = 0$  dex, and a microturbulence of  $\xi = 0.66$  km s $^{-1}$ . The derived solar abundance values are listed in Table 5. Our results satisfactorily reproduced the solar abundances and aligned closely with the values reported in the critical review by M. Asplund et al. (2009). These solar abundances were used to reference stellar abundances to solar values, thereby performing the analysis differentially with respect to the Sun. In Table 5,  $\log \epsilon$  is the logarithm of abundance. The number of lines used in this analysis has also been provided. The errors reported in the  $\log \epsilon$  abundances are represented by a  $1\sigma$  line-to-line scatter in abundance.

In this study, the abundances of Fe I and Fe II were used to derive the atmospheric model parameters. For the Fe I lines, we incorporated 1D non-LTE corrections using the methodology of I and the INSPECT program (v1.0). Previous studies (M. Bergemann et al. 2012; K. Lind et al. 2012; T. Bensby et al. 2014) have suggested that non-LTE effects are negligible for Fe II lines. Specifically, K. Lind et al. (2012) demonstrated that departures from the LTE for Fe II lines with low excitation potentials (<8 eV) in stars with metallicities  $[Fe/H] > -3$  dex were minimal. To assess the influence of non-LTE corrections on atmospheric parameter determination, we adopted the approach outlined in K. Lind et al. (2012, see Figures 4, 5, and 7). For most metal-poor stars in our sample, the resulting corrections to the atmospheric parameters were small, with temperature adjustments not exceeding the reported errors on  $T_{\text{eff}}$  listed in Table 4.

**Table 4.** Model atmospheric parameters of the four program stars.

Star	$T_{\text{eff}}$	$\log g$	$[Fe/H]$	$\xi$
	(K)	(cgs)	(dex)	(km s $^{-1}$ )
HD 22879	$5855 \pm 110$	$4.40 \pm 0.18$	$-0.86 \pm 0.08$	$0.95 \pm 0.50$
HD 144579	$5300 \pm 160$	$4.52 \pm 0.37$	$-0.55 \pm 0.12$	$0.00 \pm 0.80$
HD 188510	$5370 \pm 60$	$4.57 \pm 0.13$	$-1.60 \pm 0.07$	$0.17 \pm 0.50$
HD 201891	$5880 \pm 90$	$4.48 \pm 0.18$	$-1.15 \pm 0.07$	$1.03 \pm 0.50$

For HD 22879, Si I shows a minor NLTE correction of -0.005 dex, derived from six spectral lines, suggesting a minimal deviation from the LTE assumptions. Ti I exhibits a significant NLTE effect with an average correction of 0.221 dex based on 21 spectral lines, whereas Ti II shows a slight negative correction of -0.002 dex from seven lines. Cr I and Mn I display positive NLTE corrections of 0.145 and 0.201 dex, respectively. In addition, Fe I and Fe II had NLTE corrections of 0.017 dex and 0.006 dex, calculated from 51 and six spectral lines, respectively. The highest NLTE correction was observed for Co I (0.275 dex) although it was derived from only two spectral lines.

For HD 144579, the NLTE corrections range from 0.00 dex (for Si I) to 0.14 dex (for Ti I). Among the analyzed elements, Mg I exhibited a minor NLTE correction of 0.02 dex, derived from a single spectral line. Ti I demonstrates a more substantial correction of 0.14 dex, based on 26 spectral lines, whereas Ti II presents a slightly

**Table 5.** Solar abundances obtained by employing the solar model atmosphere from F. Castelli & R. L. Kurucz (2004) compared to the photospheric abundances from M. Asplund et al. (2009). The abundances presented in bold typeface were measured by synthesis, while the remaining elemental abundances were calculated using the line EWs.  $\Delta \log \epsilon_{\odot}(X) = \log \epsilon_{\odot}(X)_{\text{This study}} - \log \epsilon_{\odot}(X)_{\text{Asplund}}$

Species	This study $\log \epsilon_{\odot}(X)$ (dex)	N	M. Asplund et al. (2009)			$\Delta \log \epsilon_{\odot}(X)$ (dex)	
			$\log \epsilon_{\odot}(X)$				
				(dex)			
Na I	6.16 ± 0.07	2	6.24 ± 0.04		-0.08		
Mg I	7.62 ± 0.03	5	7.60 ± 0.04		0.02		
Al I	6.45 ± 0.03	8	6.45 ± 0.03		0.00		
Si I	7.50 ± 0.07	12	7.51 ± 0.03		-0.01		
Ca I	6.34 ± 0.08	18	6.34 ± 0.04		0.00		
Sc I	3.12 ± 0.00	1	3.15 ± 0.04		-0.03		
Sc II	3.23 ± 0.08	7	3.15 ± 0.04		0.08		
Ti I	4.96 ± 0.09	43	4.95 ± 0.05		0.01		
Ti II	4.99 ± 0.08	12	4.95 ± 0.05		0.04		
V I	3.90 ± 0.03	5	3.93 ± 0.08		-0.03		
Cr I	5.71 ± 0.07	19	5.64 ± 0.04		0.07		
Cr II	5.64 ± 0.14	3	5.64 ± 0.04		0.00		
Mn I	5.62 ± 0.13	13	5.43 ± 0.05		0.19		
Fe I	7.54 ± 0.09	132	7.50 ± 0.04		0.04		
Fe II	7.51 ± 0.04	17	7.50 ± 0.04		0.01		
Co I	4.90 ± 0.14	6	4.99 ± 0.07		-0.05		
Ni I	6.28 ± 0.09	54	6.22 ± 0.04		0.06		
Zn I	4.60 ± 0.00	2	4.56 ± 0.05		0.04		
Sr I	2.86 ± 0.00	1	2.87 ± 0.07		-0.01		
Y II	2.20 ± 0.04	2	2.21 ± 0.05		-0.01		
Zr II	2.70 ± 0.00	1	2.58 ± 0.04		0.12		
Ba II	2.52 ± 0.19	4	2.18 ± 0.09		0.32		
Ce II	1.58 ± 0.02	2	1.58 ± 0.04		0.00		
Nd II	1.33 ± 0.09	3	1.42 ± 0.04		-0.09		
Sm II	0.95 ± 0.00	1	0.96 ± 0.04		-0.01		

lower correction of 0.06 dex from five lines. Cr I and Mn I displayed moderate NLTE corrections of 0.08 dex and 0.12 dex, respectively. Iron-group elements exhibit relatively small NLTE effects, with Fe I and Fe II having corrections of 0.02 dex and 0.00 dex, based on 61 and 6 spectral lines, respectively. Co I, derived from five spectral lines, exhibits an NLTE correction of 0.13 dex, indicating a modest deviation from the LTE.

For HD 188510, NLTE corrections varied significantly across different elements, with values ranging from -0.001 dex (Fe II) to 0.342 dex (Co I). Among the species studied, Ca I exhibited a small NLTE correction of 0.027 dex, based on two spectral lines. Ti I had a more pronounced correction of 0.223 dex (from eight lines), whereas Ti II had a much smaller correction of 0.001 dex (from four lines), indicating a stronger NLTE effect in neutral titanium than in its singly ionized counter-

**Table 6.** The abundances of the observed species for HD 22879, HD 144579, HD 188510, and HD 201891 are presented. The abundances presented in bold typeface are measured by synthesis.

Species	HD 22879			HD 144579			HD 188510			HD 201891		
	[X/Fe]	$\sigma$	N	[X/Fe]	$\sigma$	N	[X/Fe]	$\sigma$	N	[X/Fe]	$\sigma$	N
Na I	0.07	0.08	2	0.21	0.06	1	-	-	-	-	-	-
Mg I	0.16	0.09	3	0.17	0.10	2	0.25	0.07	2	0.23	0.09	2
Al I	0.07	0.02	2	0.33	0.04	2	-	-	-	0.17	0.03	2
Si I	0.27	0.03	9	0.27	0.05	6	-	-	-	-	-	-
Ca I	0.26	0.03	12	0.32	0.04	10	0.24	0.05	3	0.18	0.03	8
Sc II	0.15	0.03	7	0.29	0.06	6	-0.17	0.05	1	0.17	0.04	4
Ti I	0.23	0.03	27	0.42	0.04	29	0.20	0.05	10	0.17	0.03	7
Ti II	0.34	0.04	7	0.39	0.06	5	0.32	0.05	4	0.32	0.04	10
V I	-	-	-	0.52	0.06	4	-	-	-	-	-	-
Cr I	-0.09	0.03	16	0.06	0.05	15	-0.06	0.05	5	-0.13	0.04	10
Cr II	-0.10	0.10	2	0.13	0.11	2	-	-	-	0.08	0.09	1
Mn I	-0.40	0.09	4	-0.05	0.06	9	-0.30	0.08	2	-0.46	0.05	3
Fe I	-0.03	0.02	92	0.07	0.04	104	0.02	0.04	36	-0.03	0.03	51
Fe II	0.00	0.03	14	0.00	0.05	11	0.00	0.06	3	0.00	0.04	8
Co I	-0.11	0.08	2	0.23	0.10	6	0.03	0.07	1	0.09	0.06	1
Ni I	-0.02	0.03	27	0.08	0.04	32	-0.17	0.06	2	-0.05	0.05	10
Zn I	0.03	0.07	2	0.15	0.04	2	0.04	0.04	1	0.00	0.08	2
Sr I	-0.15	0.02	1	-0.12	0.04	1	-	-	-	-	-	-
Y II	-0.03	0.06	2	-0.06	0.05	2	-	-	-	-0.08	0.04	2
Zr II	0.32	0.02	1	-0.12	0.04	1	-	-	-	-	-	-
Ba II	-0.36	0.10	2	-0.44	0.12	2	-0.36	0.11	2	-0.27	0.10	2
Ce II	-0.05	0.03	1	-	-	-	-	-	-	-	-	-
Nd II	0.13	0.06	1	-	-	-	-	-	-	-	-	-

part. Cr I and Mn I displayed moderate-to-significant NLTE effects, with corrections of 0.209 and 0.304 dex, respectively. Iron-group elements show minor NLTE effects, with Fe I and Fe II having corrections of 0.008 dex (from 61 lines) and -0.001 dex (from one line), respectively. However, Co I, which is based on a single spectral line, exhibited the highest NLTE correction (0.342 dex).

In the case of HD 201891, the analysis revealed varying degrees of non-LTE corrections across different elements. Mg I shows a modest correction of 0.029 dex, as determined from a single spectral line. Ca I exhibited an average correction of 0.023 dex, based on the analysis of the six lines. The most pronounced corrections were evident in Fe I and Co I, with non-LTE differences of 0.202 dex (derived from 27 lines) and 0.415 dex (based on one line), respectively. Conversely, elements such as Ti II and Fe II showed negligible corrections.

The abundances obtained for all stars using their PolarBase spectra are listed in Table 6, where [X/Fe] represents logarithmic abundance considering the abundance of Fe II. The error in [X/Fe] is the square root of the sum of the squares of the errors in [X/H]<sup>8</sup> and [Fe/H]. The formal abundance errors resulting from uncertainties in

<sup>8</sup> [X/H] is the logarithmic abundance ratio of hydrogen to the corresponding solar value.

**Table 7.** The influence of model atmospheric parameter uncertainties on the precision of the derived elemental abundances for four metal-poor stars.

Species	HD 22879				HD 144579				
	$\Delta T_{\text{eff}}$	$\Delta \log g$	$\Delta [\text{Fe}/\text{H}]$	$\Delta \xi$	$\Delta T_{\text{eff}}$	$\Delta \log g$	$\Delta [\text{Fe}/\text{H}]$	$\Delta \xi$	
Na I	+0.03	-0.02	+0.00	-0.02	Na I	0.10	-0.06	0.02	-0.02
Mg I	+0.07	+0.00	+0.00	-0.08	Mg I	0.22	-0.13	0.03	-0.11
Al I	+0.05	+0.02	+0.01	-0.07	Al I	0.08	0.02	0.00	-0.01
Si I	+0.02	+0.01	+0.00	-0.01	Si I	0.00	0.04	0.02	-0.01
Ca I	+0.05	-0.03	+0.00	-0.06	Ca I	0.13	-0.13	0.02	-0.06
Sc II	+0.02	+0.06	+0.02	-0.06	Sc II	0.00	0.13	0.04	-0.06
Ti I	+0.07	+0.00	+0.00	-0.05	Ti I	0.19	-0.10	0.01	-0.10
Ti II	+0.02	+0.05	+0.02	-0.09	Ti II	0.00	0.13	0.04	-0.07
V I	—	—	—	—	V I	0.22	0.00	0.00	-0.09
Cr I	+0.05	-0.01	+0.00	-0.07	Cr I	0.17	-0.12	0.02	-0.10
Cr II	-0.03	+0.07	+0.01	-0.02	Cr II	-0.06	0.12	0.03	-0.07
Mn I	+0.06	-0.01	+0.00	-0.08	Mn I	0.16	-0.11	0.03	-0.11
Fe I	+0.06	-0.01	+0.01	-0.06	Fe I	0.13	-0.07	0.03	-0.08
Fe II	-0.01	+0.06	+0.01	-0.07	Fe II	-0.07	0.16	0.04	-0.06
Co I	+0.04	-0.02	+0.00	-0.11	Co I	0.12	-0.01	0.03	-0.06
Ni I	+0.04	+0.00	+0.00	-0.03	Ni I	0.08	0.00	0.03	-0.05
Zn I	+0.03	-0.02	+0.01	-0.10	Zn I	0.00	0.00	-0.01	-0.02
Sr I	+0.04	+0.01	+0.01	-0.03	Sr I	0.16	-0.07	0.02	-0.16
Y II	+0.03	+0.06	+0.01	-0.11	Y II	0.03	0.10	0.02	-0.13
Zr II	+0.04	+0.07	+0.02	-0.10	Zr II	0.03	0.11	0.05	-0.13
Ba II	+0.03	+0.02	+0.02	-0.12	Ba II	0.04	0.08	0.05	-0.12
Ce II	+0.03	+0.05	+0.02	-0.02	Ce II	—	—	—	—
Nd II	+0.04	+0.07	+0.02	-0.03	Nd II	—	—	—	—

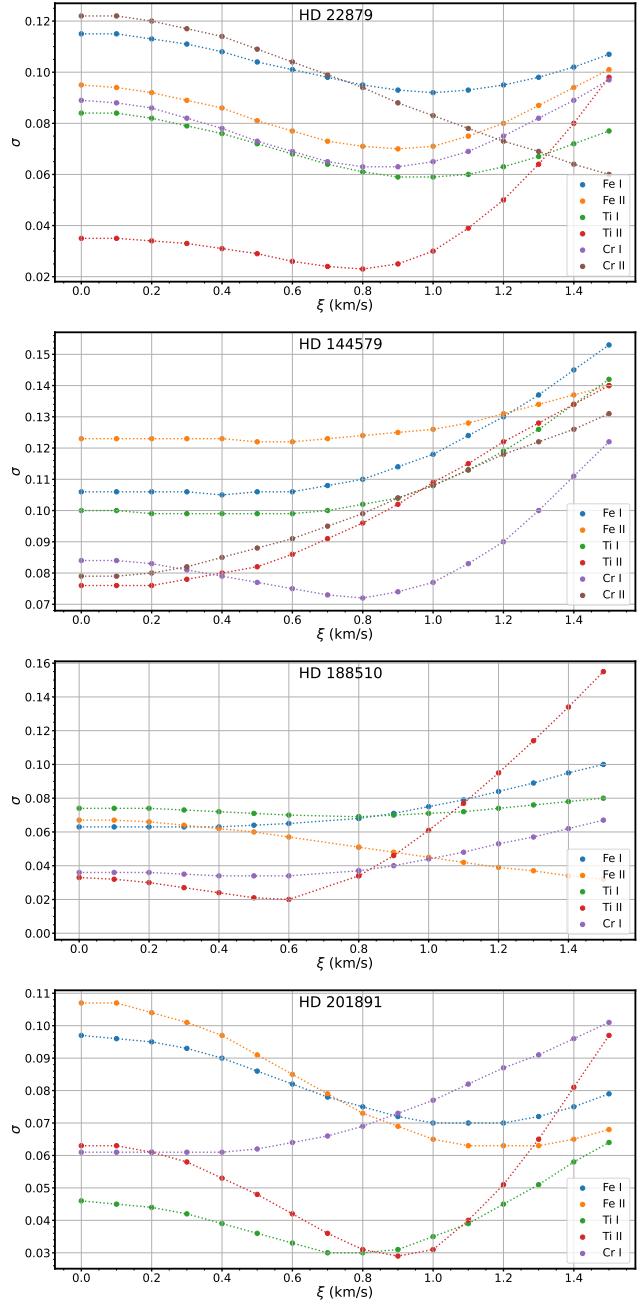
Species	HD 188510				HD 201891				
	$\Delta T_{\text{eff}}$	$\Delta \log g$	$\Delta [\text{Fe}/\text{H}]$	$\Delta \xi$	$\Delta T_{\text{eff}}$	$\Delta \log g$	$\Delta [\text{Fe}/\text{H}]$	$\Delta \xi$	
Na I	—	—	—	—	Na I	—	—	—	
Mg I	+0.10	+0.01	+0.03	-0.03	Mg I	+0.09	+0.02	+0.01	-0.05
Al I	—	—	—	—	Al I	+0.03	+0.05	+0.03	-0.01
Si I	—	—	—	—	Si I	—	—	—	
Ca I	+0.04	-0.02	+0.01	-0.01	Ca I	+0.06	-0.01	+0.01	-0.03
Sc II	+0.01	+0.03	+0.01	-0.01	Sc II	+0.03	+0.05	+0.01	-0.08
Ti I	+0.06	-0.02	+0.00	-0.03	Ti I	+0.09	-0.01	+0.01	-0.05
Ti II	+0.02	+0.02	+0.02	-0.04	Ti II	+0.03	+0.06	+0.01	-0.06
V I	—	—	—	—	V I	—	—	—	
Cr I	+0.07	-0.02	+0.00	-0.04	Cr I	+0.08	-0.01	+0.01	-0.06
Cr II	—	—	—	—	Cr II	-0.01	+0.04	+0.01	-0.06
Mn I	+0.03	-0.01	+0.00	-0.04	Mn I	+0.07	-0.04	+0.02	-0.09
Fe I	+0.06	-0.02	+0.01	-0.03	Fe I	+0.07	-0.01	+0.01	-0.06
Fe II	-0.01	+0.06	+0.01	-0.01	Fe II	+0.00	+0.06	+0.01	-0.08
Co I	+0.07	-0.05	+0.02	-0.06	Co I	+0.11	-0.04	+0.01	-0.21
Ni I	+0.03	+0.00	+0.01	-0.02	Ni I	+0.06	+0.00	+0.01	-0.03
Zn I	+0.00	+0.02	+0.00	-0.02	Zn I	+0.03	-0.02	+0.01	-0.05
Sr I	—	—	—	—	Sr I	—	—	—	
Y II	—	—	—	—	Y II	+0.04	+0.04	+0.01	-0.04
Zr II	—	—	—	—	Zr II	—	—	—	
Ba II	+0.04	+0.00	+0.03	-0.06	Ba II	+0.05	+0.02	+0.04	-0.11

atmospheric parameters  $T_{\text{eff}}$ ,  $\log g$ , and  $\xi$  are summarized in Table 7 for changes relative to the model.

#### 3.4. Stellar Age Estimation

In this study, determining the ages of the analyzed stars is important for understanding their origins. Therefore, stellar ages were estimated using a Monte Carlo Markov Chain (MCMC) method that employs maximum likelihood estimation and an isochrone grid based on two different input sets.

The isochrone grid used for this method was derived from version CMD 3.8<sup>9</sup> of the PARSEC stellar isochrone library (A. Bressan et al. 2012). The properties of the obtained grid are as follows: in the  $\log \tau$  space, steps of 0.05 were employed within the range of  $6 \leq \log \tau \leq$



**Figure 4.** The standard deviation of the Ti, Cr, and Fe abundances from the suite of Ti I, Ti II, Cr I, Cr II, Fe I, and Fe II lines as a function of  $\xi$ .

10.13, while in the metallicity space  $Z$ , an isochrone grid was created with steps of 0.0005 dex in the range of  $0 \leq Z \leq 0.03$ . Although the constructed grid is highly precise, it does not fully represent a continuous space. This limitation introduces uncertainties in age estimates and poses challenges for the walkers used in the MCMC method. To mitigate these issues, interpolation of intermediate points within the grid space is necessary. To

<sup>9</sup> <http://stev.oapd.inaf.it/cgi-bin/cmd>

achieve this, the Delaunay function from Python Scipy library (P. Virtanen et al. 2020) was used. This function enables continuous space within the input grid by performing three-dimensional interpolation among the desired input parameters. Consequently, the obtained solution is free from the uncertainties introduced by the step size of the input grid and provides the continuous space required for the Monte Carlo method.

In this process, a function that represents the desired observational parameters in the grid space was obtained using the Delaunay function, as expressed  $I(Z, \tau, M) \xrightarrow{\text{Delaunay}} \theta$ . Using this function, stellar ages were determined for two different  $\theta$  input parameter sets using the MCMC method and the maximum likelihood approach. The first consists of photometric parameters, where *Gaia* is the photometry and spectroscopic iron abundance, and the second includes spectroscopic parameters, specifically the stellar atmospheric model parameters ( $T_{\text{eff}}$ ,  $\log g$ , and [Fe/H]). These parameters were used to determine the most probable age on the isochrone grid by applying MCMC using the following maximum likelihood function:

$$\log \mathcal{L} = -\frac{1}{2} \sum_i \left( \frac{\theta_i^{\text{obs}} - \theta_i^{\text{model}}}{\sigma_i} \right)^2 \quad (7)$$

where  $\mathcal{L}$  represents the maximum likelihood function. The term  $\theta_i^{\text{obs}}$  denotes the observed parameters, which include  $M_G$  and the  $(G_{\text{BP}} - G_{\text{RP}})_0$  for the photometric input set, as well as the stellar atmospheric model parameters,  $T_{\text{eff}}$ ,  $\log g$ , and [Fe/H], for the spectroscopic input set. The parameter  $\theta_i^{\text{model}}$  corresponds to the model parameters derived from the interpolated isochrone grid, while  $\sigma_i$  represents the observational uncertainties associated with each parameter. This function minimizes the squared differences between the observed and model parameters, weighted by their uncertainties, ensuring an optimal age estimation. The MCMC method explores the parameter space using this log-likelihood function to determine the most probable stellar age.

To derive the final age estimates, the input parameters for each star were processed through 22 walkers and 5,000 iterations. The resulting posterior distributions were used to compute the median age, along with the associated uncertainties, defined as the range within one standard deviation above and below the median. This approach ensures a statistically robust estimation of stellar ages while accounting for the uncertainties inherent in the observational parameters.

The results are summarized in Table 8. The posterior distributions derived from the photometric input parameter and best-fitting age results are visualized on the color-magnitude diagram in Figure 5, whereas the age

estimates obtained from the atmospheric model parameters are presented in the same format as in Figure 6. The other parameters listed in Table 8 were detected using interpolation on the isochrone grid based on the best-fitting solutions.

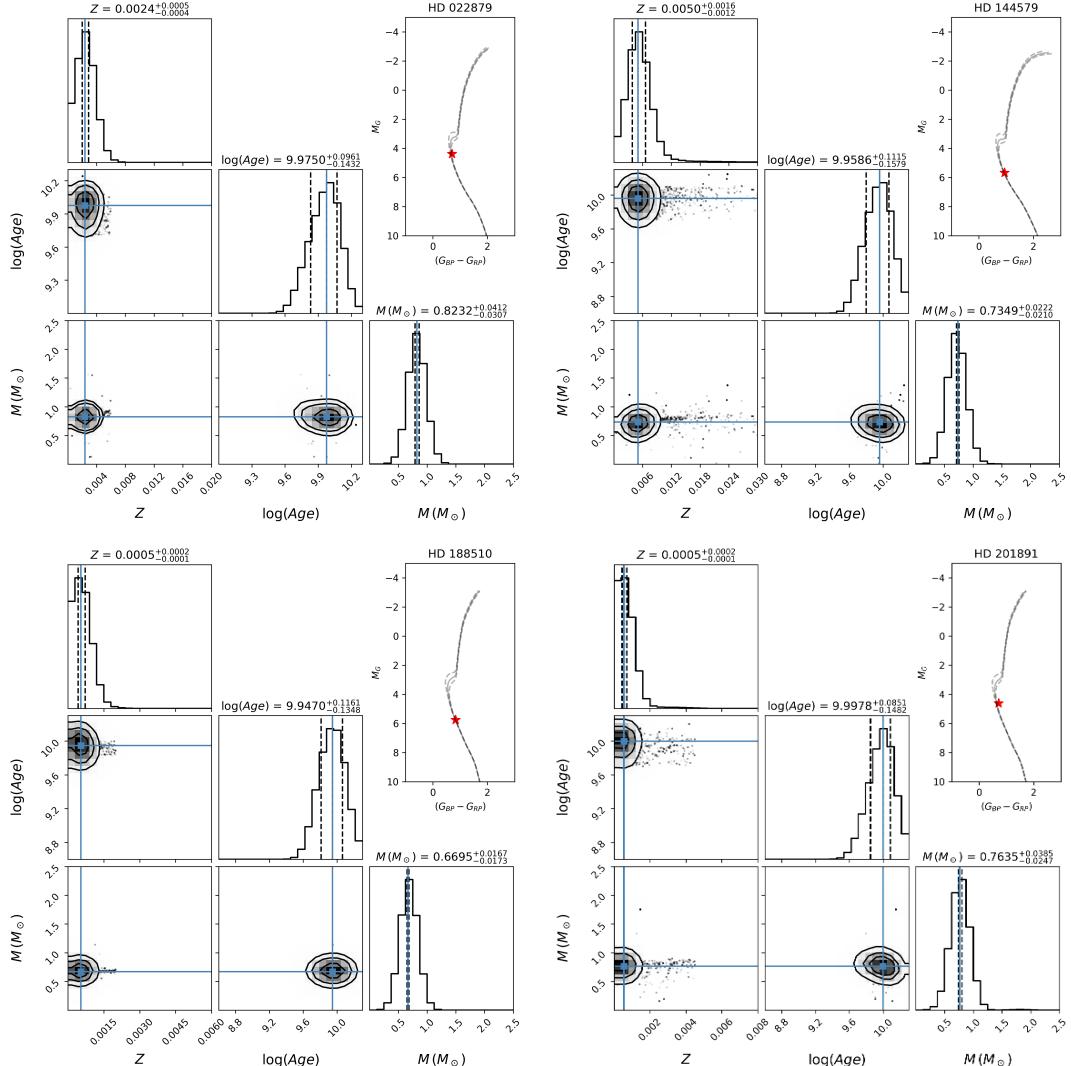
### 3.5. Kinematic and Dynamic Orbit Analyses

The space velocity components of the four selected metal-poor stars, HD 22879, HD 144579, HD 188510, and HD 201891, were computed using the algorithm proposed by D. R. H. Johnson & D. R. Soderblom (1987) for the J2000 epoch.  $U$ ,  $V$ , and  $W$  represent the space velocity components of each star relative to the sun. The transformations adopt a right-handed coordinate system, where  $U$  is positive towards the Galactic center,  $V$  is positive in the direction of Galactic rotation, and  $W$  is positive towards the North Galactic Pole.

The input parameters for the calculations included equatorial coordinates ( $\alpha$ ,  $\delta$ ), radial velocities ( $V_R$ ), proper motion components ( $\mu_\alpha \cos \delta$ ,  $\mu_\delta$ ), and trigonometric parallaxes ( $\varpi$ ), as shown in Table 2. Proper-motion components, trigonometric parallaxes, and radial velocities were obtained from the *Gaia* DR3 catalogue ( Gaia Collaboration et al. 2023). Notably, the data quality from *Gaia* DR3 provides improved precision compared to earlier catalogues, ensuring robust input for velocity computations. A significant factor in determining the uncertainties in the derived space velocity components is the accuracy of the distance estimates, which are inversely related to the trigonometric parallax measurements. For the stars analyzed, the relative parallax errors from *Gaia* DR3 were uniformly low, typically below 0.001. This precision minimizes the propagation of distance errors in the space velocity components, yielding reliable kinematic results.

To achieve precise space velocity components, the first-order correction for the Galactic differential rotation, as described by D. Mihalas & J. Binney (1981), was applied. The corrections for the  $U$  and  $V$  components of the space velocity were calculated as  $-0.91 \leq \Delta U (\text{km s}^{-1}) \leq 3.73$  and  $-0.23 \leq \Delta V (\text{km s}^{-1}) \leq 0.08$ , respectively, whereas the  $W$  component remained unaffected by this first-order approximation. Following differential rotation correction, the space velocity components were adjusted for the peculiar motion of the Sun relative to the local standard of rest (LSR). The adopted values for the Sun's peculiar velocity are  $(U_\odot, V_\odot, W_\odot)_{\text{LSR}} = (8.50 \pm 0.29, 13.38 \pm 0.43, 6.49 \pm 0.26) \text{ km s}^{-1}$ , as reported by B. Coşkunoğlu et al. (2011).

The total space velocity ( $S$ ) of each star was calculated as the square root of the sum of the squares of its space velocity components. The uncertainties in the



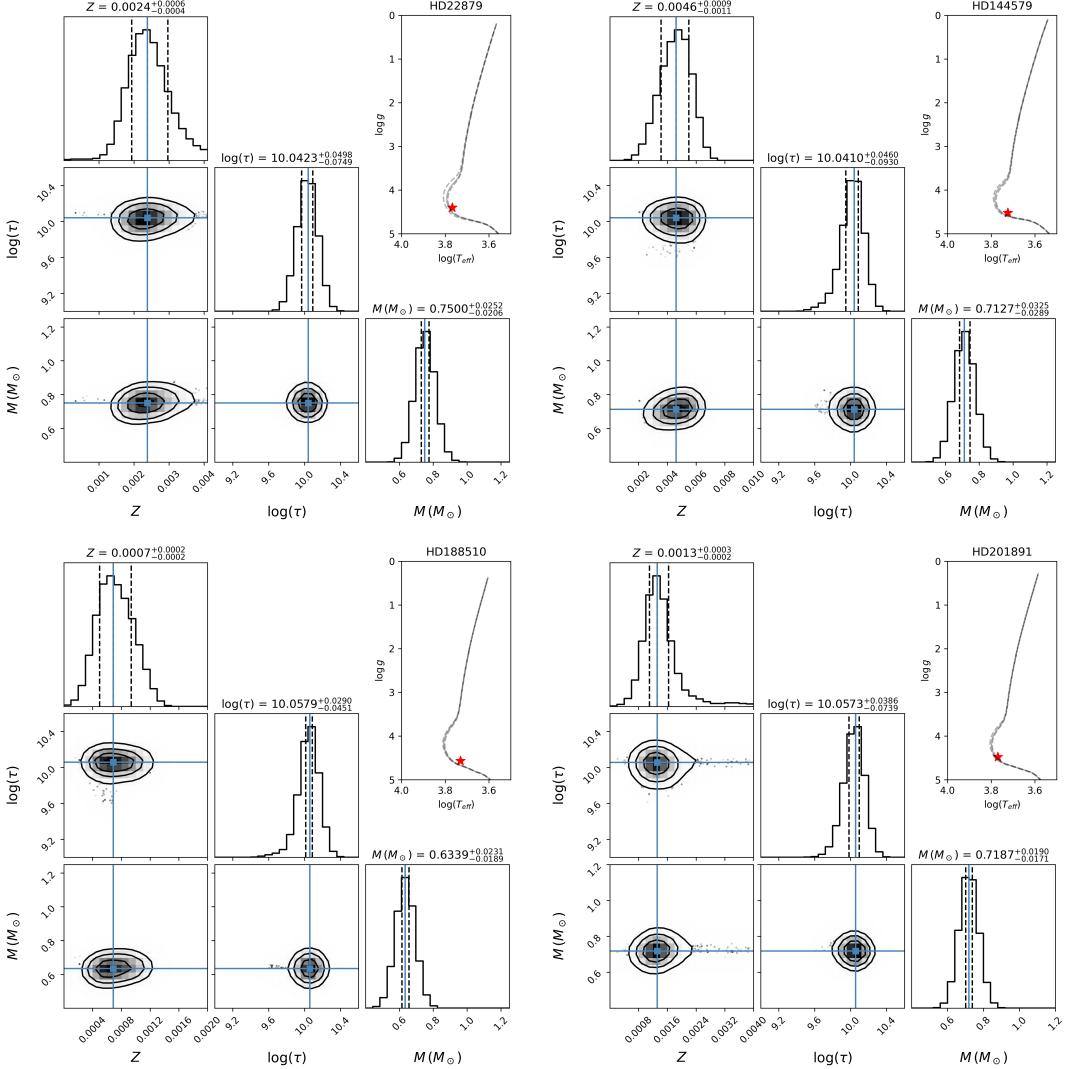
**Figure 5.** Corner plot illustrating the two-dimensional joint and one-dimensional marginalized posterior distributions for the properties of four stars. The contours in the two-dimensional joint posterior distributions represent the confidence levels of 68%, 90%, and 95%. In the one-dimensional posterior distributions, the vertical lines indicate the median and the 16th and 84th percentile confidence intervals. The  $M_G \times (G_{BP} - G_{RP})_0$  CMDs of the stars (red stars) are shown on the right side of the corner plots. The black solid lines are the PARSEC isochrones derived from the median values of the posterior distributions, and black dashed lines indicate the calculated age errors of the stars.

space velocity components ( $U_{\text{err}}$ ,  $V_{\text{err}}$ ,  $W_{\text{err}}$ ) were derived by propagating the errors in the proper-motion components, trigonometric parallaxes, and radial velocities using the methodology of D. R. H. Johnson & D. R. Soderblom (1987). The corrected space velocity components, total space velocities, and associated uncertainties for the four HPM stars—HD 22879, HD 144579, HD 188510, and HD 201891—are provided in Table 9. These results offer critical insights into the Galactic kinematics of these stars, and we applied the kinematic method outlined by T. Bensby et al. (2003). This method assumes that the Galactic space velocity components follow a Gaussian distribution, expressed as

$$P_i(U, V, W) = k \exp \left( -\frac{U_{\text{LSR}}^2}{2\sigma_{i,U}^2} - \frac{(V_{\text{LSR}} - v_{i,a})^2}{2\sigma_{i,V}^2} - \frac{W_{\text{LSR}}^2}{2\sigma_{i,W}^2} \right),$$

$$k = \frac{1}{(2\pi)^{3/2} \sigma_{i,U} \sigma_{i,V} \sigma_{i,W}}, \quad (8)$$

where  $\sigma_U$ ,  $\sigma_V$ , and  $\sigma_W$  represent the characteristic velocity distributions of distinct Galactic populations. These dispersions were as follows: 35, 20, and 16 km s<sup>-1</sup> for the thin disk (D); 67, 38, and 35 km s<sup>-1</sup> for the thick disk (TD); and 160, 90, and 90 km s<sup>-1</sup> for the halo (H). The term  $V_{\text{asym}}$  denotes the asymmetric drift velocity, with values of -15, -46, and -220 km



**Figure 6.** Corner plot illustrating the posterior distributions for four stars, with confidence contours at 68%, 90%, and 95%. One-dimensional distributions indicate the median and 16th/84th percentile intervals. The positions of the stars in the Kiel diagram are shown on the right-hand side of the panels. Definitions are as provided in the previous Figure 5.

$s^{-1}$  for the thin disk, thick disk, and halo, respectively, (T. Bensby et al. 2003, 2005). The probability that a star belongs to one Galactic population relative to another is calculated as the ratio of their Gaussian distribution functions (Equation 8) scaled by the local space density ratios of the respective populations. For each star, the relative probabilities of belonging to a specific Galactic population were computed using the following equations:

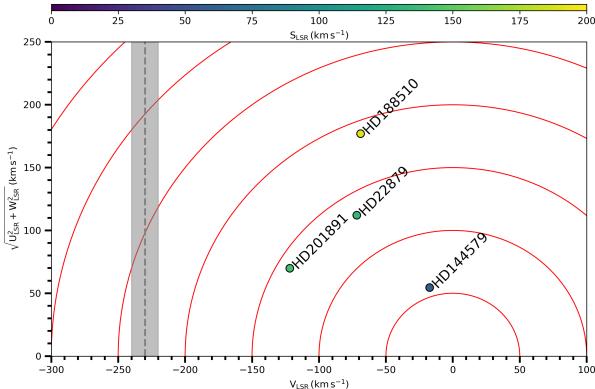
$$TD/D = \frac{X_{\text{TD}}}{X_D} \times \frac{f_{\text{TD}}}{f_D}, \quad TD/H = \frac{X_{\text{TD}}}{X_H} \times \frac{f_{\text{TD}}}{f_H}, \quad (9)$$

where  $X_D$ ,  $X_{\text{TD}}$ , and  $X_H$  are the local space densities of the thin disk, thick disk, and halo, respectively. The values of 0.94, 0.06, and 0.0015 were determined based on the methodology described by S. Karaali et al. (2004); S.

Bilir et al. (2006a,b,c); A. Cabrera-Lavers et al. (2007); S. Bilir et al. (2008); S. İyisan et al. (2025), which utilizes the  $TD/D$  ratio to categorize Galactic population membership. According to this classification, stars are identified as high-probability members of a thin disk when  $TD/D \leq 0.1$ . Stars with  $0.1 < TD/D \leq 1$  are considered low-probability thin-disk members, whereas  $1 < TD/D \leq 10$  indicates a low-probability membership in the thick disk. Finally, stars with  $TD/D > 10$  were classified as high-probability members of a thick disk. The computed  $TD/D$  and  $TD/H$  values for the stars analyzed in this study, summarized in Table 9, provide insights into their Galactic population classifications. A lower  $TD/D$  ratio corresponds to a lower likelihood of thick-disk membership than thin-disk membership.

**Table 8.** Model atmosphere parameters ( $T_{\text{eff}}$ ,  $\log g$ , [Fe/H]), mass ( $M$ ), radius ( $R$ ), and age ( $\tau$ ) values of the four stars analyzed in this study, obtained using spectral energy distribution (SED), photometric and astrometric analysis (Phot. & Astro), and spectral analysis (Spec.) methods. Literature median values (Lit.) are included for comparison.

Parameter	Method	HD 22879	HD 144579	HD 188510	HD 201891
$T_{\text{eff}}$ (K)	SED	$5985 \pm 30$	$5263 \pm 21$	$5580 \pm 26$	$5886 \pm 20$
	Phot. & Astro.	$6332 \pm 50$	$5501 \pm 40$	$5766 \pm 45$	$6139 \pm 40$
	Spec.	$5855 \pm 110$	$5300 \pm 160$	$5370 \pm 60$	$5880 \pm 90$
	Lit.	$5848 \pm 90$	$5276 \pm 64$	$5489 \pm 143$	$5902 \pm 80$
$\log g$ (cgs)	SED	$4.50 \pm 0.03$	$4.53 \pm 0.04$	$4.74 \pm 0.03$	$4.51 \pm 0.03$
	Phot. & Astro.	$4.30 \pm 0.08$	$4.58 \pm 0.10$	$4.65 \pm 0.05$	$4.60 \pm 0.08$
	Spec.	$4.40 \pm 0.18$	$4.52 \pm 0.37$	$4.57 \pm 0.13$	$4.48 \pm 0.18$
	Lit	$4.24 \pm 0.22$	$4.41 \pm 0.24$	$4.44 \pm 0.32$	$4.34 \pm 0.17$
[Fe/H] (dex)	SED	$-0.78 \pm 0.03$	$-0.63 \pm 0.03$	$-1.48 \pm 0.03$	$-1.02 \pm 0.04$
	Phot. & Astro.	$-0.81 \pm 0.07$	$-0.48 \pm 0.08$	$-1.44 \pm 0.07$	$-1.45 \pm 0.07$
	Spec.	$-0.86 \pm 0.08$	$-0.55 \pm 0.12$	$-1.60 \pm 0.07$	$-1.15 \pm 0.07$
	Lit	$-0.84 \pm 0.08$	$-0.47 \pm 0.05$	$-1.60 \pm 0.19$	$-1.04 \pm 0.12$
$M$ ( $M_{\odot}$ )	SED	$0.79 \pm 0.02$	$0.72 \pm 0.02$	$0.66 \pm 0.02$	$0.87 \pm 0.01$
	Phot. & Astro.	$0.82 \pm 0.04$	$0.73 \pm 0.02$	$0.67 \pm 0.02$	$0.76 \pm 0.04$
	Spec.	$0.75 \pm 0.02$	$0.71 \pm 0.03$	$0.63 \pm 0.02$	$0.72 \pm 0.02$
$R$ ( $R_{\odot}$ )	SED	$1.08 \pm 0.01$	$0.79 \pm 0.01$	$0.69 \pm 0.01$	$1.01 \pm 0.01$
	Phot. & Astro.	$1.05 \pm 0.02$	$0.72 \pm 0.15$	$0.64 \pm 0.06$	$0.85 \pm 0.07$
	Spec.	$0.82 \pm 0.03$	$0.71 \pm 0.11$	$0.61 \pm 0.05$	$0.76 \pm 0.08$
$\tau$ (Gyr)	SED	$13.08 \pm 1.95$	$12.63 \pm 2.79$	$12.54 \pm 3.57$	$13.15 \pm 2.13$
	Phot. & Astro.	$9.44 \pm 1.25$	$9.09 \pm 1.35$	$8.85 \pm 1.20$	$9.95 \pm 1.30$
	Spec.	$11.02 \pm 1.15$	$10.99 \pm 1.15$	$11.42 \pm 1.09$	$11.41 \pm 1.15$



**Figure 7.** The positions of the stars on the Toomre diagram. The stars were color-coded according to their space velocity errors. The color scale in the upper panel shows the errors in total space velocity. The red curves in the figure represent velocity values of  $50 \text{ km s}^{-1}$ , whereas the dashed line in the gray region corresponds to a velocity of  $S_{\text{LSR}} = -230 \text{ km s}^{-1}$  (L. Necib & T. Lin 2022).

To calculate the Galactic orbital parameters of four metal-poor stars, we utilized the GALPY library, a Python-based tool for Galactic dynamics developed by J. Bovy (2015). In this study, we adopted a Galactic radius  $R_{\text{gc}} = 8 \text{ kpc}$  (S. R. Majewski 1993) and a vertical

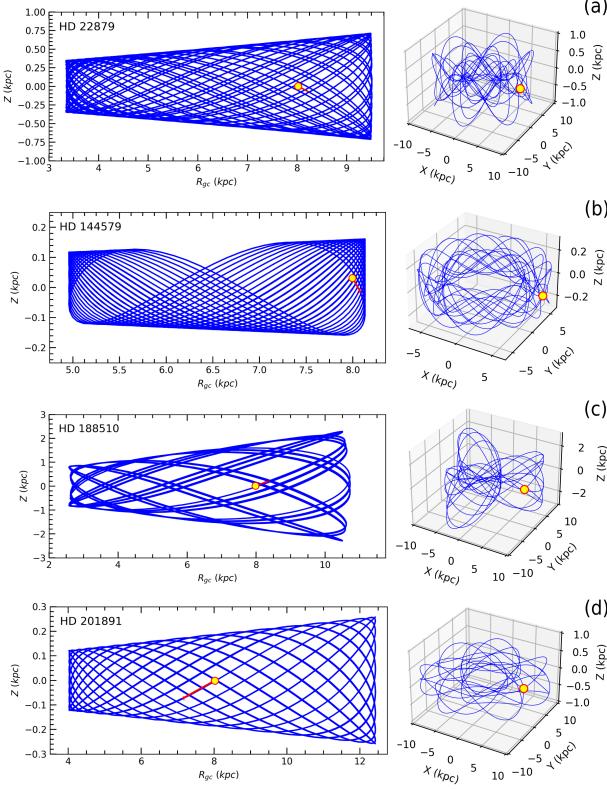
distance of the Sun from the Galactic plane  $Z_{\odot} = 27 \pm 4 \text{ pc}$  following (H.-W. Chen et al. 2001). The Milky Way was modeled using the GALPY potential *MWPotential2014*, which incorporates the gravitational influences of three components: the bulge, disk, and halo. For the bulge component, we employed a spherical power-law density profile, as described by J. Bovy (2015) and given by

$$\rho(r) = A \left( \frac{r_1}{r} \right)^{\alpha} \exp \left[ - \left( \frac{r}{r_c} \right)^2 \right]. \quad (10)$$

In this expression,  $r_1$  and  $r_c$  are the reference and cut-off radii, respectively. Parameter  $A$  denotes the amplitude of the potential in the mass density units, while  $\alpha$  represents the inner power of the profile. For the Galactic disk, we adopted the potential model proposed by M. Miyamoto & R. Nagai (1975), which is expressed as:

$$\Phi_{\text{disk}}(R_{\text{gc}}, z) = - \frac{GM_d}{\sqrt{R_{\text{gc}}^2 + (a_d + \sqrt{z^2 + b_d^2})^2}} \quad (11)$$

where  $z$  is the vertical distance from the Galactic plane,  $R_{\text{gc}}$  is the radial distance from the Galactic center, and  $M_d$  is the mass of the is the mass of the Galactic disk. The constants  $a_d$  and  $b_d$  represent the scale length and



**Figure 8.** The orbits of the HD 22879 (a), HD 144579 (b), HD 188510 (c), and HD 201891 (d) around the Galactic center. The red-ringed yellow circles in the panels indicate the current positions of the stars, and the red arrows show their direction of motion.

height of the disk, respectively. For the halo potential, we use the model proposed by J. F. Navarro et al. (1996):

$$\Phi_{\text{halo}}(r) = -\frac{GM_s}{R_{\text{gc}}} \ln \left( 1 + \frac{R_{\text{gc}}}{r_s} \right) \quad (12)$$

In this equation,  $r_s$  and  $M_s$  correspond to the scale radius and mass of the Galactic dark matter halo, respectively. The orbital trajectories of the four metal-poor stars around the Galactic center were computed using time steps of 1 Myr, with a total integration period of 13 Gyr. For the orbital parameter calculations, we used the same input data as those used to determine the space-velocity components. The apo- and peri-galactic distances ( $R_a$  and  $R_p$ ), the mean galactocentric distance, defined as  $R_m = (R_a + R_p)/2$ , along with eccentricity ( $e_p$ ), and the maximum distance from the Galactic plane ( $Z_{\max}$ ) were obtained for each star. Eccentricity of the Galactic orbit was calculated using the following equation:  $e_p = (R_a - R_p)/(R_a + R_p)$ . The calculated  $Z_{\max}$  values were nearly identical to the axisymmetric model applied to the Galactic potential solutions. The resulting orbital parameters for the stars computed using the

GALPY code are listed in Table 9. In addition, the Galactic orbits of the four stars projected onto the  $X - Y$  and  $X - Z$  planes are illustrated in Figure 8, illustrating their vertical distance from the Galactic plane ( $Z$ ) and their distance from the Galactic center ( $R_{\text{gc}}$ ) (e.g. T. Yontan et al. 2022; S. Taşdemir & T. Yontan 2023; T. Yontan 2023; T. Yontan & R. Canbay 2023; G. Yucel et al. 2024). The closed orbits were reconstructed by integrating the star's present-day astrometric and radial velocity data backward in time along with the estimated age. Left panels display the motion of these stars within the Galaxy as a function of their distance from  $R_{\text{gc}}$  and  $Z$ , respectively. The right panels illustrate the variation in the stars' Galactic positions over time in terms of their  $X$ ,  $Y$ , and  $Z$  coordinates (e.g. W. H. Elsanhoury et al. 2025; S. Taşdemir & D. C. Çınar 2025; A. A. Haroon et al. 2025).

#### 4. SUMMARY AND DISCUSSION

This study investigated the astrophysical and chemical properties of four metal-poor main-sequence stars in the solar neighborhood using several independent methods: SED, photometric, astrometric, and high-resolution spectroscopic analyses. The model atmosphere parameters, fundamental stellar properties, and Galactic kinematics were derived using data from *Gaia* DR3 and the PolarBase library. The consistency of these methods was evaluated, and population classifications and potential escape scenarios from GCs were examined to determine the Galactic origins of the stars.

To evaluate the accuracy and precision of the model atmospheric parameters derived for the four metal-poor main-sequence stars analyzed in this study, previous spectroscopic studies were examined. Most studies have focused on chemical abundance, Galactic evolution, and stellar populations. However, no prior work, except for T. Şahin & S. Bilir (2020) and M. Marişmak et al. (2024), has combined multiple techniques to determine the fundamental astrophysical parameters of these stars, thus underscoring the originality of this study. Literature surveys revealed that HD 22879, HD 144579, HD 188510, and HD 201891 were identified in 139, 48, 57, and 83 spectroscopic studies, respectively, up to January 1, 2025. The ranges of atmospheric parameters reported in the literature are  $5100 < T_{\text{eff}} (\text{K}) < 6250$ ,  $3.3 < \log g (\text{cgs}) < 5.0$ , and  $-2 < [\text{Fe}/\text{H}] (\text{dex}) < -0.5$  (Figure 9). However, several gaps and inconsistencies remain in the literature regarding atmospheric parameters and chemical abundances. For HD 22879, previous studies have reported effective temperatures ( $T_{\text{eff}}$ ) ranging from 5486 to 6058 K and surface gravities ( $\log g$ ) between 3.3 and 4.6 cgs, with metallicity ([Fe/H]) esti-

mates varying from  $-0.51$  to  $-0.97$  dex. Additionally, the ionization balance between the Fe I and Fe II lines has not been consistently achieved across studies, suggesting potential systematic errors in the adopted atmospheric models or line parameters. HD 144579 has been characterized with  $T_{\text{eff}}$  values between 5139 K and 5446 K,  $\log g$  from 4.1 to 4.8 cgs, and [Fe/H] from  $-0.55$  to  $-0.76$  dex. Despite its frequent use as a calibration star, there is a lack of consensus on its microturbulence, with values ranging from 0.6 to 1.0 km s $^{-1}$ . HD 188510, with reported  $T_{\text{eff}}$  values of 5379–5618 K,  $\log g$  of 4.3–4.7 cgs, and [Fe/H] of  $-0.77$  to  $-1.88$  dex, have been studied less extensively than other stars. HD 201891 exhibits  $T_{\text{eff}}$  values between 5730 K and 6000 K,  $\log g$  from 4.0 to 4.3 cgs, and [Fe/H] from  $-1.10$  to  $-0.90$  dex. This study derived model atmospheric parameters and fundamental properties (mass, radius, and age) of four stars using three independent methods. A comparison with the medians and standard deviations in the literature (Table 8) shows overall consistency. However, discrepancies were identified, such as the photometric and astrometric temperatures of HD 22879 and the metallicity of HD 144579, which fall outside the reported ranges.

In the following subsections, the results of the spectroscopic studies of stars in the literature are compared with the results obtained in this study.

#### 4.1. Individual Stars in the Literature

A comprehensive comparison with previous spectroscopic studies is essential to contextualize our findings within the broader framework of stellar abundance analyses. In this section, we study the consistency of our derived atmospheric parameters and chemical abundances with the values reported in the literature for each star in our sample.

##### 4.1.1. HD 22879

The first comprehensive abundance analysis of HD 22879 was conducted by [B. Edvardsson et al. \(1993\)](#), who derived the atmospheric parameters  $T_{\text{eff}} = 5826$  K and  $\log g = 4.27$  cgs, reporting a metallicity of [Fe/H] =  $-0.84$  dex and an  $\alpha$ -enhancement of  $[\alpha/\text{Fe}] = +0.25$  dex. Our study derived atmospheric parameters consistent with these literature values, and the  $\alpha$ -element abundances presented here align with those reported by [B. Edvardsson et al. \(1993\)](#). Subsequent work by [P. Jofré et al. \(2015\)](#) refined the metallicity to [Fe/H] =  $-0.86 \pm 0.05$  dex using high-resolution HARPS spectra, along with the updated parameters of  $T_{\text{eff}} = 5868 \pm 89$  K and  $\log g = 4.27 \pm 0.03$  cgs.

The  $\alpha$ -rich composition of HD 22879 was corroborated by GALAH DR4, which reported enhanced [X/Fe] ratios of  $0.33 \pm 0.01$  dex for Mg and  $0.21 \pm 0.01$  dex for Si.

[P. E. Nissen et al. \(2024\)](#) recently analyzed HD 22879 through a differential spectroscopic approach relative to the Sun, focusing on Sc II, V I, and Co I abundances. Their adoption of revised photometric temperatures yielded  $T_{\text{eff}}$  values approximately 100 K higher than those in earlier studies, although their final spectroscopically derived  $T_{\text{eff}}$  and  $\log g$  agreed closely with our determinations. [P. E. Nissen et al. \(2024\)](#) reported 3D-corrected metallicities of [Fe/H] =  $-0.86$  dex and  $-0.85$  dex, consistent with our result of [Fe/H] =  $-0.86 \pm 0.08$  dex. The authors applied 3D non-LTE corrections to the Mg I 5711.1 Å line—the sole Mg line analyzed, yielding [Mg I/Fe] = 0.34 dex. Although uncertainties for individual abundances were not provided, their [X/Fe] ratios for Na, Si, Ca, Sc, Ti, and Ni align closely (within 0.03 dex) with those derived in this work. Notably, our Mg abundances were determined using three Mg I lines that were evaluated for blending effects using the Solar Flux Atlas.

##### 4.1.2. HD 144579

The study by [R. da Silva et al. \(2015\)](#) analyzed the high-resolution spectra of FGK stars, encompassing both planet-hosting and non-planet-hosting stars, to determine photospheric parameters, masses, ages, and elemental abundances. A comparison between the elemental abundances derived in this study and those reported by [R. da Silva et al. \(2015\)](#) reveals both consistencies and notable discrepancies. Stellar atmospheric parameters show strong agreement between the two studies, suggesting that differences in derived abundances are not driven by systematic parameter uncertainties, but rather by atomic data variations, line selection, or methodological approaches.

The [Mg/Fe] and [Mn/Fe] ratios align with uncertainties: this study reports [Mg/Fe] =  $0.17 \pm 0.10$  dex and [Mn/Fe] =  $-0.05 \pm 0.06$  dex, consistent with literature values of [Mg/Fe] =  $0.20 \pm 0.08$  dex and [Mn/Fe] =  $-0.09 \pm 0.06$  dex. However, significant discrepancies are observed for [Si/Fe], [Ca/Fe], [Ti/Fe], and [V/Fe]. For [Si/Fe], a shared silicon line at 5793.08 Å exhibits a 0.06 dex offset in  $\log gf$  values. In the case of [Ca/Fe], although both studies employed five common calcium lines, our result ( $0.32 \pm 0.04$  dex) exceeds the literature value ( $0.16 \pm 0.09$  dex). This divergence is partially attributable to systematic offsets in oscillator strengths ( $\log gf$ ), which differ by  $0.13 \pm 0.11$  dex between line lists. Such discrepancies in the atomic data can directly propagate into abundance offsets of comparable magnitudes.

For [Ti/Fe], the 12 shared Ti I lines exhibited  $\log gf$  differences of  $0.11 \pm 0.08$  dex (this study minus the lit-

erature), introducing a systematic bias that likely contributes to the abundance discrepancy. Conversely, the two common Ti II lines show excellent agreement in  $\log gf$  values. The most pronounced disparity occurred in [V/Fe], where our measurement ( $0.52 \pm 0.06$  dex) substantially exceeded the value reported by R. da Silva et al. (2015) ( $0.21 \pm 0.12$  dex). This discrepancy is particularly notable because the studies employed entirely distinct vanadium lines; R. da Silva et al. (2015) relied on weak V lines sensitive to continuum placement or blending, whereas our analysis utilized V lines that are relatively stronger and validated for blending effects via the solar flux spectrum. The line lists and atomic data adopted in this study were calibrated to reproduce solar abundances in the solar flux spectrum.

G. Tautvaišienė et al. (2021) analyzed high-resolution spectra of 506 solar-neighborhood F, G, and K stars, including HD 144579, to investigate trends in n-capture element-to-iron ratios. The derived atmospheric parameters for HD 144579 ( $T_{\text{eff}} = 5296 \pm 48$  K,  $\log g = 4.59 \pm 0.30$  cgs, and  $[\text{Fe}/\text{H}] = -0.65 \pm 0.11$  dex) are consistent with those reported in Table 4. Among the shared elements, strontium abundances agree within 0.1 dex, while yttrium abundances differ by only  $+0.01$  dex. The barium abundance reported by G. Tautvaišienė et al. (2021) also fell within our reported uncertainty range.

A. A. John et al. (2023) conducted a comprehensive search for planetary systems around HD 144579, a G8V-type star with high proper motion, using HARPS-N spectroscopic data. Kinematic analysis classified the star as a member of the thick-disk population, with no detected planetary companions. The derived atmospheric parameters ( $T_{\text{eff}} = 5296 \pm 37$  K,  $\log g = 4.67 \pm 0.08$  cgs,  $[\text{Fe}/\text{H}] = -0.65 \pm 0.04$  dex), and  $\alpha$ -enhancement ( $[\alpha/\text{Fe}] = 0.26$  dex) are consistent with the values reported in this study.

#### 4.1.3. HD 188510

The study by J. P. Fulbright (2000) provides a comprehensive analysis of the abundances and kinematics of 168 metal-poor stars, including HD 188510, using high-resolution spectroscopy. The derived atmospheric parameters,  $T_{\text{eff}} = 5370 \pm 60$  K,  $\log g = 4.57 \pm 0.13$  cgs, and  $[\text{Fe}/\text{H}] = -1.60 \pm 0.07$  dex, align closely with those reported by J. P. Fulbright (2000), who performed the first detailed spectroscopic analysis of HD 188510. Their results ( $T_{\text{eff}} = 5325 \pm 150$  K,  $\log g = 4.6 \pm 0.2$  cgs,  $[\text{Fe}/\text{H}] = -1.6 \pm 0.3$  dex) and  $\alpha$ -element abundances ( $[\text{Mg}/\text{Fe}] = 0.26$ ,  $[\text{Ca}/\text{Fe}] = 0.27$ ,  $[\text{Ti}/\text{Fe}] = 0.28$ ,  $[\text{Cr}/\text{Fe}] = 0.04$  dex) are consistent with our findings. However, the  $[\text{Ni}/\text{Fe}]$  and  $[\text{Ba}/\text{Fe}]$  ratios exhibit a notable discrepancy of  $\approx 0.2$  dex.

I. U. Roederer et al. (2014) conducted detailed chemical analyses of 313 metal-poor stars, including HD 188510, and reported no significant radial velocity variations for this star. Their derived surface gravity ( $\log g = 4.10 \pm 0.27$  cgs) exhibits notable inconsistency with our results. As discussed in their Section 9.4.1, I. U. Roederer et al. (2014) explicitly noted that their  $[\text{X}/\text{Fe}]$  abundance ratios were systematically higher than those reported in previous surveys. To investigate this discrepancy, we employed the Stellar Parameters and Chemical Abundance Estimator (SP\_Ace) code (C. Boeche & E. K. Grebel 2016), which generates real-time spectral models using a Generalized Curve of Growth (GCOG) library. Our SP\_Ace analysis yielded  $T_{\text{eff}} = 5128 \pm 18$  K,  $\log g = 4.48 \pm 0.07$  cgs, and  $[\text{Fe}/\text{H}] = -1.65 \pm 0.02$  dex. These values confirm the robustness of our  $\log g$  determination, but suggest an 80 K lower  $T_{\text{eff}}$  compared to I. U. Roederer et al. (2014). Despite the disagreement in  $\log g$  between the two studies, key elemental ratios, such as  $[\text{Mg}/\text{Fe}]$ ,  $[\text{Ca}/\text{Fe}]$ ,  $[\text{Ti}/\text{Fe}]$ , and  $[\text{Zn}/\text{Fe}]$ , reported by I. U. Roederer et al. (2014) align closely with our findings (within 0.1 dex), while  $[\text{Mn}/\text{Fe}]$  differs by only 0.05 dex. In their recent study, S. Mittal & I. U. Roederer (2025) reanalyzed the stellar parameters of metal-poor stars, including HD 188510, and compared their results with those of I. U. Roederer et al. (2014). They reported systematically warmer effective temperatures across all evolutionary tracks, thus resolving this discrepancy. The derived parameters ( $T_{\text{eff}} = 5549 \pm 36$  K,  $\log g = 4.67 \pm 0.15$  cgs, and  $[\text{Fe}/\text{H}] = -1.50 \pm 0.3$  dex) showed a marked increase in  $T_{\text{eff}}$  compared to their 2014 values.

P. Santos-Peral et al. (2023) characterized magnesium and calcium abundances in the X-shooter Spectral Library (XSL), including HD 188510 (designated X0697). Using the ULYSS package (M. Koleva et al. 2009) tied to the PASTEL catalog (C. Soubiran et al. 2016), they derived  $T_{\text{eff}} = 5531$  K and  $\log g = 4.29$  cgs. Their automated code GAUGUIN (A. Bijaoui et al. 2012; A. Recio-Blanco et al. 2016), part of the *Gaia*-RVS pipeline, reported  $[\text{Mg}/\text{Fe}] = 0.51 \pm 0.03$  and  $[\text{Ca}/\text{Fe}] = 0.33 \pm 0.02$  dex. Notably, GAUGUIN iteratively determines the continuum placement within local spectral windows, a process that is sensitive to normalization intervals. No magnesium lines are shared between the studies, and our  $[\text{Mg}/\text{Fe}] = 0.25 \pm 0.07$  dex derives from the spectral synthesis of the 4571 and 5711 Å lines, while P. Santos-Peral et al. (2023) analyzed ionized calcium triplet lines in the NIR. Our  $[\text{Ca}/\text{Fe}] = 0.24 \pm 0.05$  dex, based on optical lines (5512 Å and 6493 Å), highlights differences in line selection and spectral regions.

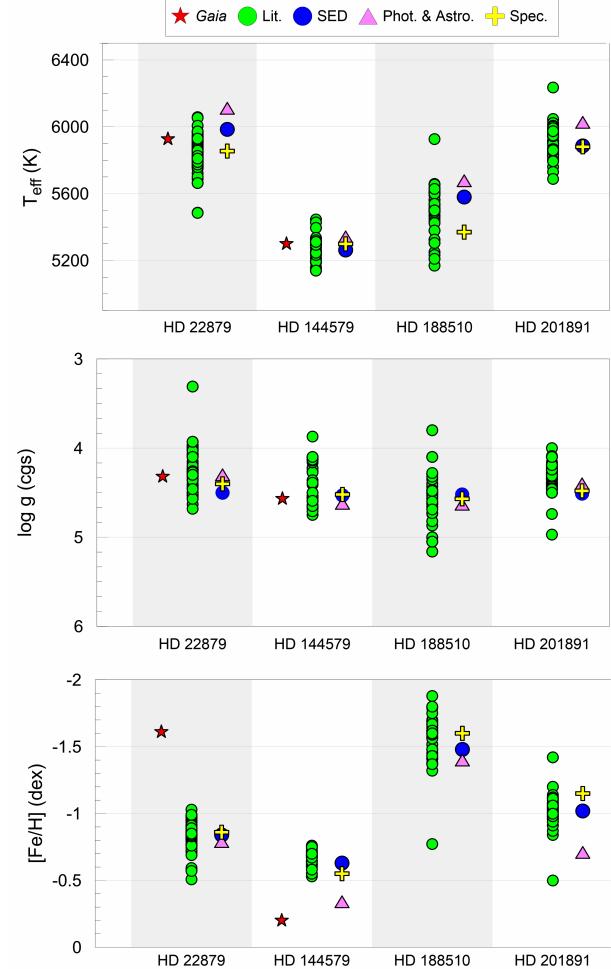
#### 4.1.4. HD 201891

C. Soubiran et al. (2024) have introduced an updated set of *Gaia* FGK benchmark stars, including HD 201891, with derived parameters  $T_{\text{eff}}$  and  $\log g$  consistent with those reported in this study. The authors highlighted the persistent scarcity of metal-poor stars in the solar neighborhood within their catalogue, emphasizing that the current version does not fully represent the metallicity distribution. In this context, the four metal-poor stars analyzed in this study, including HD 201891, serve as critical benchmarks. K. Hawkins et al. (2016) previously expanded the *Gaia* Benchmark Stars catalogue with five metal-poor candidates ( $-1.3 < [\text{Fe}/\text{H}] \text{ (dex)} < -1.0$ ), designating HD 201891 as a robust candidate for calibrating and validating stellar atmospheric parameters. Their compilation from the PASTEL database (C. Soubiran et al. 2016) reported  $T_{\text{eff}} = 5883 \pm 68 \text{ K}$ ,  $\log g = 4.33 \pm 0.15 \text{ cgs}$ , and  $[\text{Fe}/\text{H}] = -1.05 \pm 0.08 \text{ dex}$  (see Table 1; K. Hawkins et al. 2016), with dispersions in the stellar parameters reflecting variations across literature. These values closely align with the results of this study. In addition, their IRTF-derived  $T_{\text{eff}} = 5948 \pm 80 \text{ K}$  and  $\log g = 4.30 \pm 0.04 \text{ cgs}$  (based on stellar evolutionary tracks and angular diameter measurements) agree with our parameters within uncertainties.

For this  $\alpha$ -enhanced metal-poor halo star, B. Edvardsson et al. (1993) reported  $T_{\text{eff}} = 5867 \text{ K}$ ,  $\log g = 4.46 \text{ cgs}$ , and  $[\text{Fe}/\text{H}] = -1.06 \text{ dex}$ , which are consistent with our results. Their derived  $[\alpha/\text{Fe}] = 0.27 \pm 0.09 \text{ dex}$  (averaged over Mg, Si, Ca, and Ti abundances) further corroborates the  $\alpha$ -rich composition identified in this study.

#### 4.2. Galactic Population Types

To analyze the radial and vertical kinetic energies of the stars, a Toomre diagram was generated, marking four metal-poor stars, as shown in Figure 7. The space velocity ( $S$ ) of these four stars is below  $230 \text{ km s}^{-1}$ , which corresponds to the velocity of the Sun around the Galactic center (J. Bovy & S. Tremaine 2012). According to P. E. Nissen (2004), stars belonging to a thin disk typically exhibit space velocities of  $S < 60 \text{ km s}^{-1}$ , whereas thick-disk stars exhibit a broader range, with velocities in the range of  $80 < S \text{ (km s}^{-1}) < 180$ . The space velocity of halo stars in the vicinity of the Sun exceeds  $180 \text{ km s}^{-1}$ . Based on the kinematic criteria of P. E. Nissen (2004), HD 188510 stars in the same area were classified as members of the halo population. Under the kinematic criteria delineated in (T. Bensby et al. 2003), three stars in the present sample have  $TD/D$  values greater than 10 (see Table 9), indicating their membership in the halo population. Conversely, HD 144579,



**Figure 9.** Comparison of stellar atmospheric parameters derived from *Gaia* catalogue data and three different methods with literature values. The red star symbols represent *Gaia* results, pink triangles indicate photometric and astrometric analysis, green circles correspond to literature values, blue circles denote SED analysis results, and yellow plus signs show parameters determined via spectroscopic analysis.

with a  $TD/D$  value of less than 10, is classified as a thin-disk star.

In this study, Galactic orbital parameters were employed to examine the population membership of stars. For this purpose, the stars are plotted in the  $Z_{\text{max}} \times R_{\text{gc}}$  plane, where  $Z_{\text{max}}$  increases with the vertical eccentricity, as shown in Figure 8. Additionally, based on studies of Galactic structures (S. Karaali et al. 2003; S. Ak et al. 2007a,b; S. Bilir et al. 2008; B. Coşkunoğlu et al. 2012; S. Bilir et al. 2012; O. Plevne et al. 2015; S. Tunçel Güçtekin et al. 2019), stars located within 2 kpc from the Galactic plane are classified as members of the thin disk, those between 2 and 5 kpc belong to the thick disk, and stars situated beyond 5 kpc are considered halo members. When analyzing the spatial distribution

**Table 9.** Parameters and population types including their kinematic, dynamical orbital and chemical properties of the four studied stars.

Parameter	HD 22879	HD 144579	HD 188510	HD 201891
Kinematic Parameters				
$U_{\text{LSR}}$ (km s $^{-1}$ )	-106.62 $\pm$ 0.16	-54.50 $\pm$ 0.11	-156.13 $\pm$ 0.33	66.38 $\pm$ 0.12
$V_{\text{LSR}}$ (km s $^{-1}$ )	-71.76 $\pm$ 0.09	-17.31 $\pm$ 0.02	-68.91 $\pm$ 0.28	-121.79 $\pm$ 0.15
$W_{\text{LSR}}$ (km s $^{-1}$ )	-34.56 $\pm$ 0.15	-0.95 $\pm$ 0.08	83.36 $\pm$ 0.11	-21.78 $\pm$ 0.10
$TD/D$	66	0.01	$1.62 \times 10^5$	$1.31 \times 10^4$
Population Type:	Halo	Thin Disk	Halo	Halo
Galactic Orbit Parameters				
$R_a$ (pc)	9514	8132	10745	12427
$R_p$ (pc)	3349	4958	2637	4022
$R_m$ (pc)	6431	6545	6691	8225
$Z_{\text{max}}$ (pc)	712	161	2289	258
$e$	0.48	0.24	0.61	0.51
$R_a$ (pc)	9419	<b>11583</b>	<b>12726</b>	<b>11729</b>
$R_p$ (pc)	2209	<b>4082</b>	<b>2139</b>	<b>2501</b>
$R_m$ (pc)	5814	<b>7832</b>	<b>7432</b>	<b>7115</b>
$Z_{\text{max}}$ (pc)	705	<b>222</b>	<b>3027</b>	<b>341</b>
$e$	0.62	0.48	0.71	0.65
$T_p$ (Myr)	189	182	207	245
Population Type:	Thin Disk	Thin Disk	Thick Disk	Thin Disk
Abundances				
[Mg/Fe] (dex)	0.16 $\pm$ 0.09	0.17 $\pm$ 0.10	0.25 $\pm$ 0.07	0.23 $\pm$ 0.09
[Si/Fe] (dex)	0.27 $\pm$ 0.03	0.27 $\pm$ 0.05	—	—
[Ca/Fe] (dex)	0.26 $\pm$ 0.03	0.32 $\pm$ 0.04	0.24 $\pm$ 0.05	0.18 $\pm$ 0.03
[Ti/Fe] (dex)	0.23 $\pm$ 0.03	0.42 $\pm$ 0.04	0.17 $\pm$ 0.03	0.20 $\pm$ 0.05
[Fe/H] (dex)	-0.86 $\pm$ 0.08	-0.55 $\pm$ 0.12	-1.60 $\pm$ 0.07	-1.15 $\pm$ 0.07
Population Type:	Thick Disk	Thick Disk	Halo	Halo

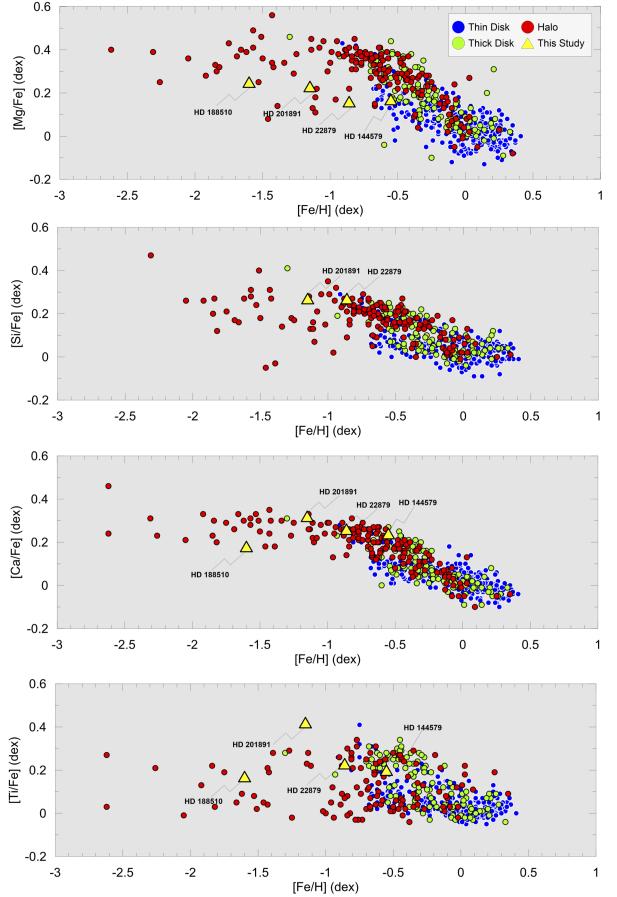
MW: MWPotential2014 (J. Bovy 2015),  
MWBS: DehnenBarPotential (W. Dehnen 2000; G. Monari et al. 2016),  
SpiralArmsPotential (D. P. Cox & G. C. Gómez 2002).

of the stars in the sample, three stars were identified as thin disk members and one star was categorized as a member of the thick disk.

To chemically distinguish the stellar populations, the sample analyzed by T. Bensby et al. (2014) was considered because of the insufficient number of stars in this study’s dataset. Their method provides a homogeneous analysis of main-sequence stars of intermediate spectral types. Using spectroscopic data obtained with ESO’s 1.5m, 2.2m, and 3.6m telescopes (SOFIN, FIES, UVES, and HARPS spectrographs), T. Bensby et al. (2014) conducted detailed abundance analyses of 714 F- and G-type dwarf stars near the Sun. The derived parameters included elements (e.g., O, Na, Mg, Al, Si, Ca, Ti, Cr, Fe, Ni, Zn, Y, and Ba), stellar ages, kinematics, and Galactic orbital properties.

Among the stars examined in this study, HD 22879, HD 144579, HD 188510, and HD 201891 were identified in the catalogue by T. Bensby et al. (2014). The chemical abundances [Mg/Fe], [Si/Fe], [Ca/Fe], [Ti/Fe], and [Fe/H], along with kinematic criteria were used to classify the star populations. Figure 10 shows stars mapped onto the [X/Fe] versus [Fe/H] planes, where X represents Mg, Si, Ca, and Ti. T. Bensby et al. (2014) classified stars with  $TD/D \leq 1$  as thin disk,  $1 < TD/D \leq 10$  as thick disk, and  $TD/D > 10$  as halo stars.

In the analyzed sample, stars with lower metallicity ([Fe/H]) tended to exhibit higher [Mg/Fe], [Si/Fe],



**Figure 10.** The chemical and kinematic classification of Galactic populations for the stars examined in this study, compared to 714 FGK stars from T. Bensby et al. (2014). The red circle denotes a halo star, the green circle indicates a thick-disk star, the blue circle represents a thin-disk star, and the yellow triangle corresponds to the four stars analyzed in this study.

[Ca/Fe], and [Ti/Fe] ratios, whereas metal-rich stars showed lower values of these abundances. The computed abundances for HD 22879, HD 144579, HD 188510, and HD 201891 were plotted for comparison. In the study by N. Nieuwmunster et al. (2023), it was shown that the [Mg/Fe] abundance of stars in the bulge region is comparatively lower than that of other Galactic components. The derived Mg abundance was reported to be, on mean, 0.14 dex lower than those in previous studies, and this decrease was suggested to be due to the increased sensitivity of the Mg lines used to non-LTE effects. It was further demonstrated that Mg abundance exhibits the steepest declining trend with metallicity and that the scatter observed in inner bulge stars at supersolar metallicities is more pronounced (F. Matteucci & L. Greggio 1986; J. Lian et al. 2020). This trend indicates that the contribution of Type Ia supernovae

(SN Ia) to iron production became dominant, leading to relatively lower Mg abundances. Conversely, the contribution of  $\alpha$  elements from the core-collapse supernovae (SN II) appears to be more limited than that of the outer disk and halo regions (A. McWilliam 2016). Consequently, the relatively low [Mg/Fe] ratio observed in bulge stars implies that the star formation history in this region may have been influenced by the gas enriched in iron and that the long-term chemical evolution has been significantly shaped by SN Ia contributions (J. Lian et al. 2020). The results indicate that HD 188510 and HD 201891 are members of the halo population, whereas HD 22879 and HD 144579 occupy the transition region between the thick disk and halo.

#### 4.3. Dynamical Origins Beyond Tidal Escape: Motivation for Identifying Non-Coherently Ejected Stars

While tidal stripping remains the canonical mechanism through which GCs lose stars—producing extended, coherent tidal tails—an increasing body of theoretical and observational evidence reveals that this process alone cannot account for all GC escapees (O. Y. Gnedin et al. 1999; J. Binney & S. Tremaine 2008; A. H. W. Küpper et al. 2012). In particular, a population of non-coherently ejected stars—those not aligned with any identifiable stream—can arise from both internal and external dynamical mechanisms and may now be observed as chemically distinct field stars in the Galactic halo or thick disk.

The escape of stars from GCs occurs through a diverse set of mechanisms broadly categorized into gradual evaporation and dynamical ejection. Evaporation is primarily driven by two-body relaxation and tidal stripping, which act over long timescales to remove stars near the escape energy (N. C. Weatherford et al. 2023). In contrast, dynamical ejection encompasses rapid, high-velocity events, such as strong gravitational interactions (e.g., binary-single and binary-binary encounters), three-body binary formation (3BBF), and supernova-induced kicks. These interactions can impart escape velocities far exceeding those achieved through tidal evaporation (G. Fragione & R. Capuzzo-Dolcetta 2016; N. C. Weatherford et al. 2023, 2024). This study highlights 3BBF, particularly in the presence of massive black holes, as a previously underappreciated but significant contributor to high-speed escapers. Additional channels include stellar evolution recoil, gravitational wave-driven mergers, and tidal disruption events.

These internal processes are especially effective in post-core-collapse clusters or those retaining a black hole subsystem, as the increased central densities and en-

counter rates enhance ejection activity (N. C. Weatherford et al. 2023). Additionally, asymmetric supernova kicks and gravitational-wave recoil from compact object mergers can further contribute to high-velocity ejections (G. Fragione & R. Capuzzo-Dolcetta 2016; T. Cabrera & C. L. Rodriguez 2023).

Equally significant are external dynamical perturbations experienced by GCs along their orbits in the Galactic potential. As clusters pass through the Galactic disk, interact with the bar or spiral arm resonances, or undergo pericentric passages near the bulge, time-varying tidal forces can rapidly heat the cluster and trigger an enhanced mass loss (O. Y. Gnedin et al. 1999). Such processes can expel stars in directions that are not strictly aligned with Lagrange points, contributing to a diffuse and incoherent distribution of former cluster members. These stars may appear as spatial or kinematic outliers and are easily missed in stream-based searches.

Understanding the mechanisms responsible for stellar escape is therefore essential for interpreting the subsequent trajectories and present-day locations of these stars within the Galactic potential. The methodology employed in this study—integrating high-resolution chemical abundances, precise *Gaia* DR3 astrometry, and full Galactic orbit modeling—provides a powerful tool for detecting such non-tidally ejected GC stars. By identifying outliers in orbital eccentricity, angular momentum, or vertical action, and contrasting them with their chemical signatures, it is possible to trace stars whose escape dynamics deviate from stream-like behavior.

Incorporating both coherent and stochastic escape mechanisms into our interpretation of stellar kinematics is essential for a complete understanding of the Milky Way’s assembly history. It reinforces the importance of dynamical context when identifying field stars of GC origin, especially in the absence of tidal structures.

##### 4.3.1. Galactic Possible Origins

The presence of high-proper-motion, metal-poor stars near the Sun is a phenomenon that T. Şahin & S. Bilir (2020) attributed to stars potentially ejected from globular clusters (GCs). To understand the Galactic origins of the two stars analyzed in this study, their orbital parameters as well as the orbits of GCs within the Milky Way were reconstructed using available observational data, including equatorial coordinates, distances, proper motions, and radial velocities sourced from the literature (H. Baumgardt et al. 2019; E. Vasiliev & H. Baumgardt 2021). Detailed kinematic and dynamic analyses were performed for 170 known GCs in our Galaxy.

We utilized the Galactic potential models from J. Bovy (2015), implemented in the GALPY Python library,

to calculate the orbital parameters of the GCs, along with symmetric (MWPOTENTIAL2014) and asymmetric (MWPOTENTIAL2014 + DEHNENBARPOTENTIAL + SPIRALARMSPOTENTIAL) Galactic potential models. The DEHNENBARPOTENTIAL (W. Dehnen 2000) was implemented as a function, generalized to three dimensions following the approach outlined by G. Monari et al. (2016), along with the implementation of the SPIRALARMSPOTENTIAL from D. P. Cox & G. C. Gómez (2002). These calculations spanned from the present day to 13 billion years, considering orbital motions represented by 20 million data points. A time interval of 650 years between consecutive points was chosen after multiple trials to balance precision and computational efficiency. This approach provides sufficient resolution for capturing the interactions between stars and GCs, with multicore processors enabling faster computations. The estimated the Galactic orbital parameters of the analyzed stars are listed in Table 9.

The orbital parameters HD 22879, HD 144579, HD 188510, and HD 201891, including their equatorial coordinates, proper motion components, trigonometric parallaxes, and radial velocities, were derived from the *Gaia* DR3 catalogue (Gaia Collaboration et al. 2023). The approach applied to these stars for orbital modelling follows the same methodology used for stars in GCs. The stellar trajectories were calculated to extend back 13 Gyr of alignment using the same procedure applied to the GCs orbital computations. However, the encounter probabilities were only evaluated for the periods after star formation, omitting any pre-formation epochs from the analysis.

In this study, the synchronous orbital paths of four stars were examined to determine their proximity to the centers of approximately 170 GCs (E. Vasiliev & H. Baumgardt 2021), specifically within the region defined by the five tidal radii. At each time step, the distance between the stars and GC centers was evaluated. If the calculated separation was found to be less than five tidal radii, an encounter was considered to have occurred. The encounter parameters, including the relative velocity ( $\Delta\nu$ ) and position ( $\Delta\theta$ ), were computed according to the following set of equations:

$$\Delta\theta = \sqrt{(X_s - X_{GC})^2 + (Y_s - Y_{GC})^2 + (Z_s - Z_{GC})^2}, \quad (13)$$

$$\Delta\nu = \sqrt{(U_s - U_{GC})^2 + (V_s - V_{GC})^2 + (W_s - W_{GC})^2}. \quad (14)$$

where  $\Delta\theta$  represents the spatial separation between the star and GC in the Cartesian coordinate system at a specific time  $\tau$ . Likewise,  $\Delta\nu$  denotes the difference in the velocity components between the star and the GC. The position coordinates  $X$ ,  $Y$ , and  $Z$  represent the respec-

tive locations of the objects, while  $U$ ,  $V$ , and  $W$  indicate the corresponding space-velocity components. If multiple encounters occurred between the GC and star over several time steps, the probability for that time interval was derived by summing the probabilities of the individual encounters. In cases where encounters occurred at multiple time steps, the highest probability observed across these time intervals was selected for each GC and compared with the probabilities of encounters with other clusters. The probability of the position ( $P(\theta)$ ) and velocity ( $P(\nu)$ ) differences, assuming a Gaussian distribution over an extended time frame, was computed using the following equations (see also M. Marışmak et al. 2024):

$$P(\theta) = \frac{1}{\sqrt{2\pi R_{\text{tidal}}}} \times \exp\left(-\frac{(\Delta\theta)^2}{2 \times R_{\text{tidal}}}\right), \quad (15)$$

$$P(\nu) = \frac{1}{\sqrt{2\pi V_{\text{escape}}}} \times \exp\left(-\frac{(\Delta\nu)^2}{2 \times V_{\text{escape}}}\right). \quad (16)$$

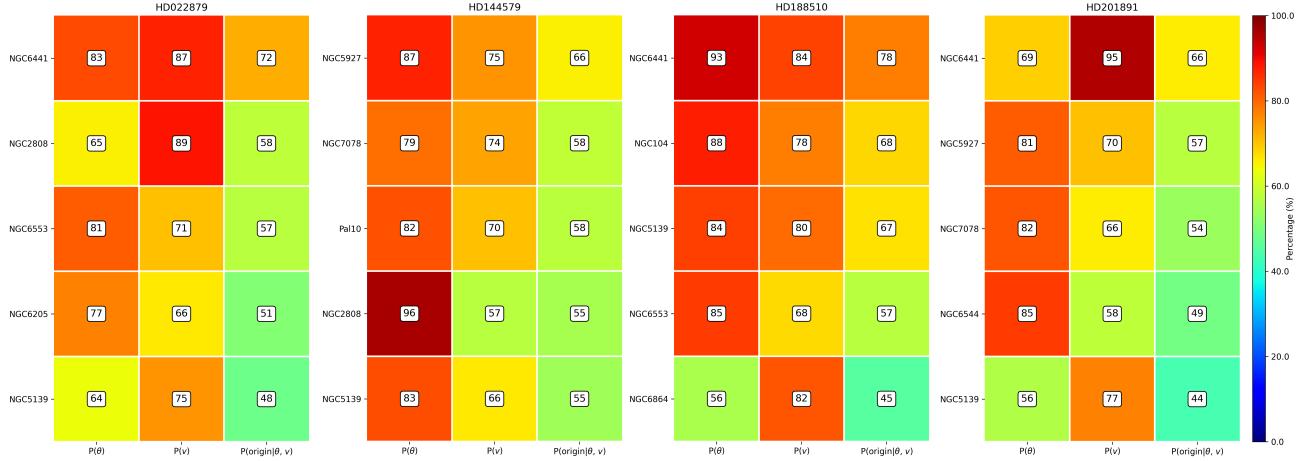
In this context,  $R_{\text{tidal}}$  represents five times the tidal radius of the cluster and  $V_{\text{escape}}$  denotes the escape velocity of the GC. These values are sourced from the 4th version of the Milky Way GC Database<sup>10</sup>. For the joint evaluation of the spatial and velocity probabilities for each GC, the product of the two probability values, denoted by  $P(\text{origin}|\theta, \nu)$ , was employed, and the following equation was applied:

$$P(\text{origin}|\theta, \nu) = P(\theta) \times P(\nu), \quad (17)$$

The probabilities derived from the spatial and velocity comparisons of HD 22879, HD 144579, HD 188510, and HD 201891 with 170 GCs in the Milky Way (E. Vasiliev & H. Baumgardt 2021), along with their combined probability values, are illustrated in Figure 11 as probability matrices that highlight the five most probable GCs. Table 10 summarizes the encounter probabilities and provides an additional diagnostic framework for exploring the dynamic origins of four stars. These probabilities were determined through detailed kinematic analyses of stars and GCs.

To evaluate the potential dynamical escape scenarios from GCs, we analyzed the spatial and kinematic alignment of four target stars with known GCs. While encounter probabilities provide initial clues, they are insufficient to conclusively trace the stellar kinematic origins. To augment this analysis, we compared the stars' ages ( $\tau$ ) and iron abundances ([Fe/H]) with those of candidate GCs, compiling the literature-derived values for

<sup>10</sup> <https://people.smp.uq.edu.au/HolgerBaumgardt/globular/>



**Figure 11.** Likelihood of stars encountering various GCs, based on spatial and velocity parameters. The matrix displays three key probability values: spatial probability ( $P(\theta)$ ), velocity probability ( $P(v)$ ), and combined probability ( $P(\text{origin}|\theta, v)$ ) for each cluster. Colors in the matrix reflect the probability values, as indicated by the scale.

these parameters in Table 10. A critical methodological consideration involves reconstructing Galactic orbits under the influence of gravitational perturbations. For stars hypothesized to have escaped from GCs, we backward-integrated their current velocities, positions, and ages to model their orbital trajectories around the Galactic center. This approach accounts for Galactic potential perturbations and yields closed Galactic orbits, thereby enabling the derivation of their orbital parameters. Importantly, these reconstructions represent backward extrapolations from present-day conditions rather than direct recordings of past motions. The resulting orbits, calculated in tandem with the trajectories of the candidate GCs, are shown in Figure 12. This methodology assumes that escaped stars may retain similar orbital paths to their parent clusters if perturbations (e.g., tidal interactions or dynamical heating) do not drastically alter their trajectories. However, inherent uncertainties in backward integration, such as incomplete knowledge of the time evolution of galactic potential, limit the precision of these reconstructions.

For HD 22879, it was determined that the metallicity and age parameters of NGC 6441 were closely aligned with the values obtained for this star, which was one-quarter of the value derived in this study. This comparison provides significant evidence that HD 22879 may have escaped the NGC 6441, a bulge GC ( $Z_{\max} \approx 1.1$  kpc).

The kinematic behavior of star HD 144579 indicates compatibility with the escape scenario of NGC 5927 in terms of both position and velocity. Based on a literature review, the age ( $\tau$ ) and iron ([Fe/H]) abundances reported for NGC 5927 aligned well with the parameters calculated for HD 144579 in this study, which were determined to be one-quarter lower for the cluster. These

findings offer robust evidence to support the possibility that HD 144579 escapes from NGC 5927, a bulge GC ( $Z_{\max} \approx 0.8$  kpc)

For HD 188510, it was revealed that its position and velocity were compatible with those of NGC 6441, with a probability of  $P(\text{origin}|\theta, v) = 78\%$ . However, the iron ([Fe/H]) abundance and age of the clusters derived from the literature differed significantly from those of the star. This discrepancy limits the escape scenario of HD 188510 from NGC 6441. Further analysis considered four other candidate clusters, revealing that NGC 5189, with an escape probability of  $P(\text{origin}|\theta, v) = 67\%$ , exhibited better consistency in terms of [Fe/H] abundance and age. These findings support the escape scenario of HD 188510 from NGC 5189, which is a halo member GC ( $Z_{\max} \approx 2.8$  kpc) with a metallicity [Fe/H] =  $-1.53$  dex. As demonstrated in Appendix A, an animation of the HD 188510 encounter with NGC 6441 is presented.

The final star analyzed, HD 201891, demonstrated compatibility with the escape scenario from the bulge GC NGC 6441, with a probability of  $P(\text{origin}|\theta, v) = 66\%$ . In contrast, among the five candidate GCs examined, NGC 6544, a bulge Gc ( $Z_{\max} \approx 1.1$  kpc), exhibited a lower escape probability of  $P(\text{origin}|\theta, v) = 49\%$  but showed greater consistency in terms of iron ([Fe/H]) abundance and age parameters when compared to the values derived for HD 201891.

The chemical composition of stars originating from GCs serves as a key diagnostic tool for tracing their origins and evolutionary history. As shown in Table 10, the iron abundances of the stars were in general agreement with the metallicities of their associated globular clusters, thereby supporting the hypothesis that these stars originated from these systems. However, subtle differences in the [Fe/H] values may reflect the effects of

**Table 10.** The Galactic coordinates ( $l$ ,  $b$ ), position ( $P(\Theta)$ ), velocity ( $P(\nu)$ ) and their combined probability values ( $P(\text{origin}|\Theta, \nu)$ ) maximum distance away from the Galactic plane ( $Z_{\max}$ ), iron ([Fe/H]) abundances and ages ( $\tau$ ), and population types (Pop) of the five most probable clusters under the scenario of the four stars leaving the GCs. The last column of the table contains the reference for [Fe/H] abundances and ages.

Cluster	$l$ ( $^{\circ}$ )	$b$ ( $^{\circ}$ )	$P(\Theta)$ (%)	$P(\nu)$ (%)	$P(\text{origin} \Theta, \nu)$ (%)	$Z_{\max}$ (kpc)	[Fe/H] (dex)	$\tau$ (Gyr)	Pop	Ref.
<b>NGC 6441</b>	353.532	-5.005	83	87	72	1.1	-0.65	10.44	Bulge	1
NGC 2808	282.193	-11.253	65	89	58	2.2	-1.32	10.93	Disk	2
NGC 6553	005.250	-3.023	81	71	57	0.7	-0.10	13.00	Bulge	3
NGC 6205	059.009	40.912	77	66	51	6.2	-1.48	13.49	Halo	2
NGC 5139	309.102	14.968	64	75	48	2.8	-1.53	12.75	Halo	4
HD22879	—	—	—	—	—	—	-0.86±0.08	10.02±1.15	—	—
<b>NGC 5927</b>	326.604	4.860	87	75	66	0.8	-0.49	12.25	Bulge	5
PAL 10	052.436	2.725	82	70	58	1.1	-0.10	—	Disk	6
NGC 4372	300.993	-9.884	72	59	43	2.0	-2.34	12.50	Bulge	7
NGC 104	305.895	-44.889	45	91	41	3.2	-0.81	13.54	Halo	2
NGC 1851	244.513	-35.036	64	44	28	11.5	-1.14	12.27	Halo	2
HD144579	—	—	—	—	—	—	-0.55±0.12	10.99±1.15	—	—
NGC 6441	353.532	-5.006	93	84	78	1.1	-0.65	10.44	Bulge	2
NGC 104	305.895	-44.889	88	78	68	3.2	-0.81	13.54	Halo	2
<b>NGC 5139</b>	309.102	14.968	84	80	67	2.8	-1.53	12.75	Halo	5
NGC 6864	020.303	-25.748	56	82	45	12.0	-1.16	9.98	Halo	8
NGC 6569	000.481	-6.681	69	56	39	2.2	-0.79	10.90	Bulge	9
HD188510	—	—	—	—	—	—	-1.60±0.07	11.42±1.09	—	—
NGC 6441	353.532	-5.0060	69	95	66	1.1	-0.65	10.44	Bulge	2
NGC 5927	326.604	4.8600	81	70	57	0.8	-0.49	12.25	Bulge	5
NGC 7078	065.012	-27.312	82	66	54	4.5	-2.36	13.28	Halo	2
<b>NGC 6544</b>	005.838	-2.204	85	58	49	1.1	-1.44	12.00	Bulge	10
NGC 5139	309.102	14.968	56	77	44	2.8	-1.53	12.75	Halo	5
HD201891	—	—	—	—	—	—	-1.15±0.07	11.41±1.15	—	—

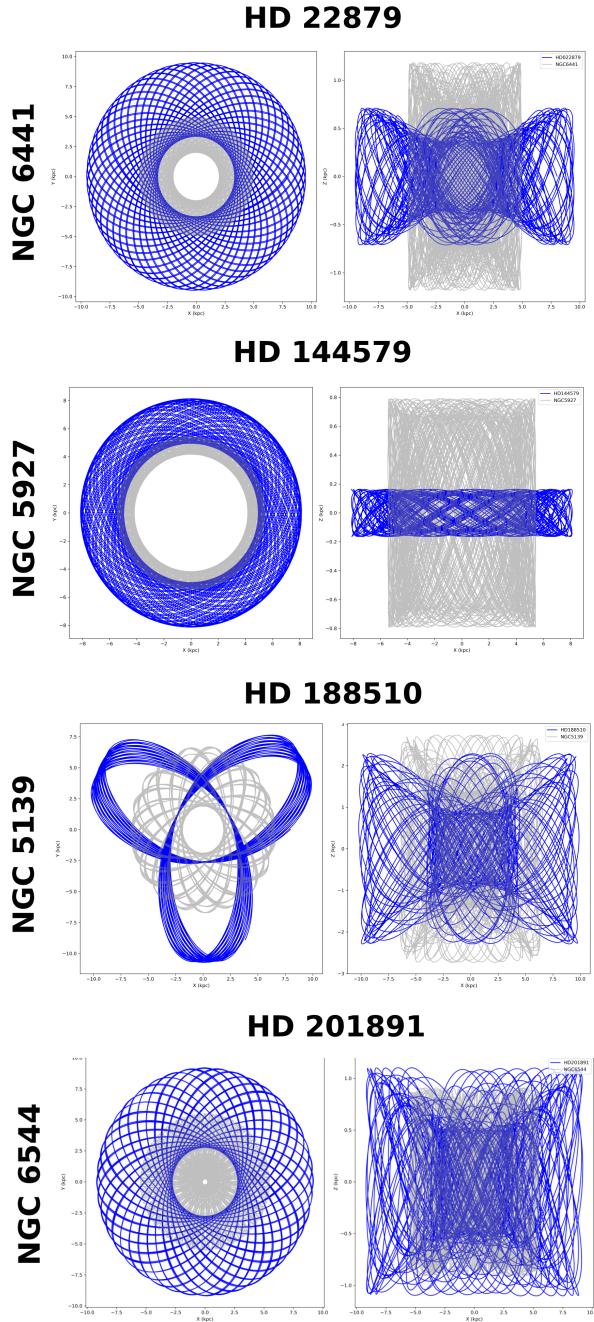
(1) Y. Zhang et al. (2012) (2) D. Valcin et al. (2020), (3) C. Montecinos et al. (2021), (4) A. T. Baldwin et al. (2016), (5) C. Usher et al. (2019), (6) E. Bica et al. (2006), (7) M. Kovalev et al. (2019), (8) E. N. Kirby et al. (2016), (9) V. A. Marsakov et al. (2019), (10) F. Gran et al. (2021).

chemical self-enrichment within the clusters or possible contamination from field populations.

For instance, HD 22879 is linked to NGC 6441, a metal-rich bulge cluster with  $[\text{Fe}/\text{H}] = -0.65$  dex, while the star exhibits a slightly lower iron abundance of  $[\text{Fe}/\text{H}] = -0.86 \pm 0.08$  dex. A similar trend is observed for HD 144579, which is associated with NGC 5927 ( $[\text{Fe}/\text{H}] = -0.49$  dex) but has a slightly lower metallicity of  $[\text{Fe}/\text{H}] = -0.55 \pm 0.12$  dex. These minor discrepancies may be attributed to variations in enrichment histories or differences in measurement techniques. HD 188510, likely originating from NGC 5139 ( $\omega$  Centauri), showed excellent agreement in iron abundance ( $[\text{Fe}/\text{H}] = -1.60 \pm 0.07$  dex) compared to the metallicity of the cluster ( $[\text{Fe}/\text{H}] = -1.53$  dex). This consistency strengthens the case for NGC 5139, which is the

progenitor of dynamically unbound stars in the Galactic halo. In contrast, HD 201891 exhibited a slightly higher metallicity ( $[\text{Fe}/\text{H}] = -1.15 \pm 0.07$  dex) than its associated bulge cluster, NGC 6544 ( $[\text{Fe}/\text{H}] = -1.44$  dex), suggesting either a different star formation history within the cluster or enrichment from external sources.

These abundance comparisons, along with dynamic evidence, provide strong support for the GC origin hypothesis of these stars. Future studies should focus on detailed chemical abundance patterns, including  $\alpha$  and neutron-capture elements of GCs, to further refine the connection between these stars and their host GCs. The elemental abundance patterns of stars and their associated GCs provide additional evidence supporting their possible origins, as shown in Figure 13. The chemical compositions of stars largely align with those of their re-



**Figure 12.** The Galactic orbits on the Galactic  $X - Y$  and  $X - Z$  planes have been calculated for the GC of which the four stars studied are members with the highest probability. The blue line indicates the orbits of the stars, while the gray lines represent the orbits of the GCs.

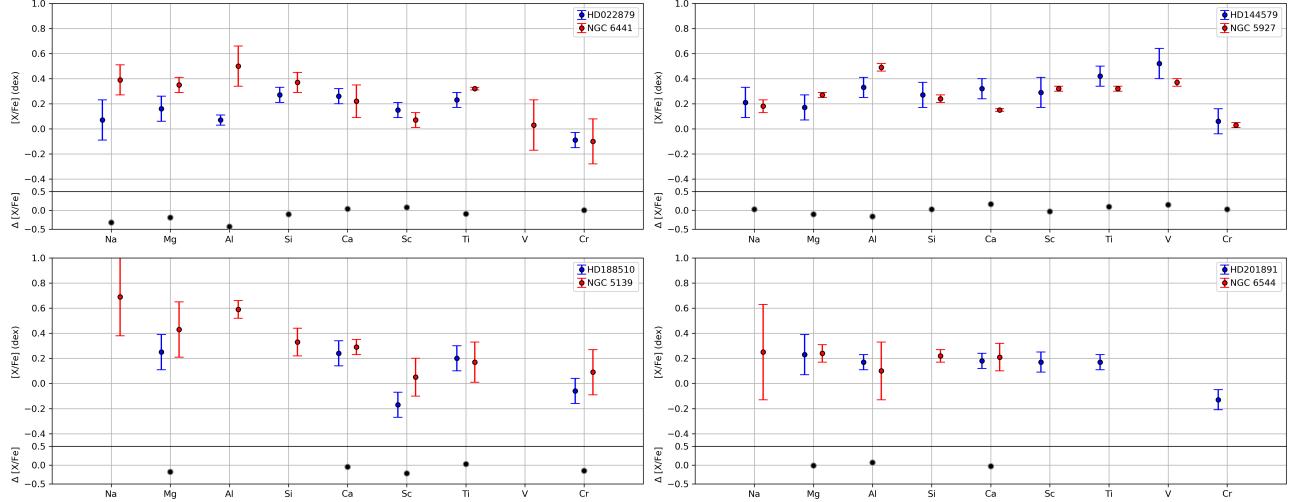
spective GC, particularly in elements such as magnesium (Mg), aluminum (Al), and calcium (Ca), which serve as key tracers of nucleosynthesis in massive stars. However, certain elements, including sodium (Na) and vanadium (V), exhibit notable deviations, with stars display-

ing abundance differences relative to their associated clusters. These discrepancies may result from intrinsic chemical inhomogeneities within clusters, evolutionary effects, or contamination from field populations. Specifically, HD 22879 and HD 144579 exhibit slightly lower Mg and Al abundances than NGC 6441 and NGC 5927, respectively, while HD 188510 and HD 201891 show  $\alpha$ -element abundance patterns that are broadly consistent with those of NGC 5139 and NGC 6544. Such detailed chemical abundance comparisons, in conjunction with kinematic evidence, provide important constraints on the mechanisms by which stars are dynamically ejected from GCs into the Galactic field.

In conclusion, considering the positions, velocities, iron and individual abundances, and ages of the four stars analyzed in this study, it was determined that HD 22879 likely escaped from NGC 6441, HD 144579 from NGC 5927, HD 188510 from NGC 5139, and HD 201891 from NGC 6544. These findings indicate that, except for HD 188510, the escape scenarios of the other three stars originated from the bulge GCs. M. Lucey et al. (2022) classified Galactic GCs based on their orbital parameters, adopting criteria to distinguish bulge, disk, and halo populations. Bulge GCs generally consist of objects that satisfy the conditions  $R_a \leq 5$  kpc and  $Z_{\max} \leq 2.5$  kpc (M. Lucey et al. 2022). This implies that bulge GCs are unlikely to reach the solar neighborhood in terms of their Galactic orbits. However, the ability of the four metal-poor stars analyzed in this study to leave the bulge region for the solar neighborhood remains an unresolved mystery.

Globular clusters are capable of dynamically ejecting individual stars through internal gravitational interactions, such as three-body encounters or close binary scattering (cf. T. Cabrera & C. L. Rodriguez 2023; N. C. Weatherford et al. 2023, 2024). These ejected stars, as they traverse through the Galactic potential, can interact with large-scale structural features such as spiral arms and the central bar, particularly within the resonance regions. Such interactions induce significant changes in the orbits of the stars, enabling them to travel considerable distances from their birthplaces, even reaching regions near the Solar neighborhood.

Among these Galactic resonances, the corotation resonance (CR) and the outer Lindblad resonance (OLR) are particularly influential in altering stellar angular momenta, which consequently leads to notable modifications in orbital radii and geometries. In this context, I. Minchev & B. Famaey (2010) demonstrated that the overlap of bar and spiral resonances allows stars to effectively disperse throughout the galactic disk. Similarly, R. Roškar et al. (2008), through high-resolution simu-



**Figure 13.** Element abundance patterns ( $[X/\text{Fe}]$ ) for four stars (blue) and GCs (red). Each panel compares the chemical abundances of a star with those of a globular cluster, showing variations across different elements (Na, Mg, Al, Si, Ca, Sc, Ti, V, and Cr). Error bars represent the measurement uncertainties. The lower section of each panel illustrates the abundance differences ( $\Delta[X/\text{Fe}]$ ) between the star and the GC.

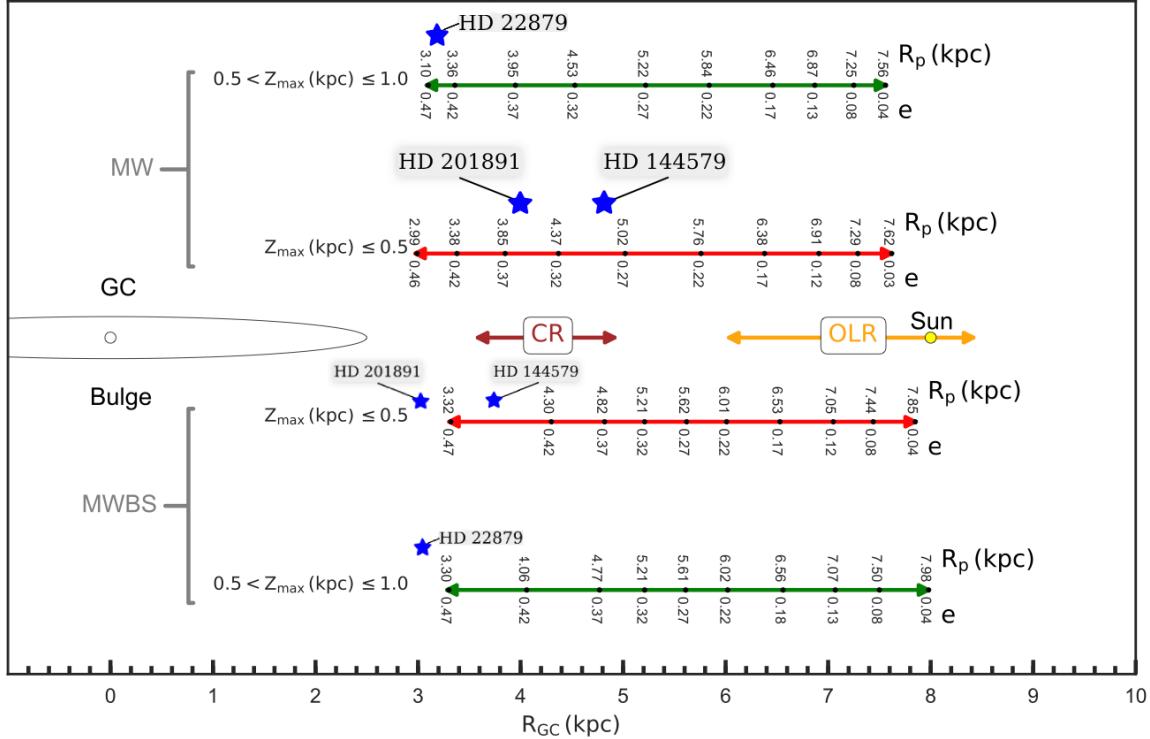
lations, showed that stars can migrate far from their formation radii because of resonant interactions with spiral arms while maintaining nearly circular orbits during the process. This orbital migration is not confined solely to dynamical effects; when combined with stellar chemical compositions and ages, it offers crucial insights into the structural and evolutionary characteristics of the Galaxy. The study by Ö. Önal Taş et al. (2018), based on RAVE data, provided statistical evidence of how stars in the solar neighborhood are influenced by Galactic resonances and highlighted the impact of these resonances on stellar metallicity gradients and kinematic structures.

Tracking the orbits of stars that have escaped from GCs is of paramount importance for a comprehensive understanding of Galactic structure and evolution. The analysis of these orbits, particularly through numerical modeling supported by high-precision astrometric observations, such as those from the *Gaia* mission (Gaia Collaboration et al. 2016b), has proven to be essential for elucidating the interactions between migrating stars and Galactic resonant structures. In conclusion, the orbital modifications of GC escapees through interactions with Galactic resonances play a key role in understanding radial migration processes extending to the solar neighborhood and present a rich field for future research endeavors.

To investigate the effects of Galactic perturbations, Ö. Önal Taş et al. (2018) analyzed radial metallicity gradients and dynamical structures in the solar neighborhood using orbital parameters derived from symmetric and asymmetric Galactic potential models. Their

study used red clump (RC) stars from the fourth data release of the Radial Velocity Experiment (RAVE DR4, G. Kordopatis et al. 2013), focusing on metallicity gradients as functions of two parameters: (1) the maximum vertical distance from the Galactic plane ( $Z_{\max}$ ) and (2) orbital eccentricity ( $e$ ). The steepest gradient of  $-0.065 \pm 0.005$  dex kpc $^{-1}$  was identified for stars with  $0 < Z_{\max}$  (kpc)  $\leq 0.5$  and low eccentricity ( $e \leq 0.1$ ), while the shallowest gradient ( $-0.014 \pm 0.006$  dex kpc $^{-1}$ ) corresponded to the same  $Z_{\max}$  range but higher eccentricity ( $e \leq 0.5$ ). For stars with  $Z_{\max} > 1$  kpc, the gradients flattened or became positive, exhibiting no dependence on orbital eccentricity. The authors suggested that the observed gradient variations within  $Z_{\max} = 1$  kpc result from dynamic interactions between the stellar orbits and the resonance points of the Galactic bar, as depicted schematically in Figure 14.

Ö. Önal Taş et al. (2018) analyzed the mean perigalactic radius ( $R_p$ ) and orbital eccentricity ( $e$ ) of RC stars within different maximum the Galactic height ( $Z_{\max}$ ) ranges. Among the four stars considered in this study, their vertical orbital motion excursions were examined under both symmetric and asymmetric Galactic potential models. Within these models, HD 201891 and HD 144579 are found to remain within the  $Z_{\max} < 0.5$  kpc interval, while HD 22879 falls within the  $0.5 < Z_{\max}$  (kpc)  $< 1$  range (see Table 9). However, HD 188510, with a  $Z_{\max}$  value of 2.2 kpc, is outside the scale established by Ö. Önal Taş et al. (2018). When the  $R_p$  values of both stars are considered, HD 144579 and HD 22879 are found to be consistent with the proposed symmetric and asymmetric Galactic potential model



**Figure 14.** Ö. Önal Taş et al. (2018) showing the Galactic center, bulge, corotation resonance (CR), outer Lindblad resonance (OLR) (W. Dehnen 2000), and the Sun’s position ( $R_0 = 8$  kpc). It also illustrates the metallicity variation within the two  $Z_{\max}$  ranges ( $0 < Z_{\max}$  (kpc)  $\leq 0.5$ , and  $0.5 < Z_{\max}$  (kpc)  $\leq 1$ ) based on the MW and MWBS models represented by different colors. The blue star symbol represents the three stars studied in this study.

scales in both  $R_p$  and  $e$ . In contrast, HD 201891 exhibits an eccentricity value approximately 0.15 higher than the expected range. Overall, the results largely agree with the scale suggested by Ö. Önal Taş et al. (2018). Additionally, this study investigated the escape scenarios of stars from GCs based on kinematic and dynamical considerations.

Specifically, stars HD 22879, HD 144579, and HD 201891 are hypothesized to have escaped from NGC 6441, NGC 5927, and NGC 6544 GCs. To assess this scenario, the perigalactic and apogalactic radii ( $R_p$  and  $R_a$ ) of these clusters were examined. The globular cluster parameters were obtained from H. Baumgardt et al. (2019), with the values for the NGC 6441, NGC 5927, and NGC 6544 clusters given by  $(R_p, R_a) = (1.00, 3.91)$  kpc,  $(3.99, 5.42)$  kpc, and  $(0.62, 5.49)$  kpc, respectively. Considering the orbital paths of these GCs around the Galactic center, all three stars appear to be kinematically associated with their respective GCs. The escape mechanism from GCs can occur at any point along the orbit, and may be influenced by perturbative forces within the Galactic disk, potentially leading to the orbit of these stars in the solar neighborhood (H. Baumgardt & M. Hilker 2018). In this context, orbital analyses and dynamical

modeling are crucial for understanding possible escape scenarios and the role of these stars in the broader context of Galactic evolution.

This analysis suggests that three of the stars (HD 22879, HD 144579, and HD 201891) may have reached the solar neighborhood after evaporating from GCs located in the bulge region of the Galaxy, driven by resonances associated with the Galactic bar and spiral arms. In contrast, HD 188510 is likely to have been separated from halo NGC 5139. As noted above, the standard Milky Way model was adopted to compute the Galactic orbits of these stars. The orbital analyses indicate a potential association between the studied stars and bulge GCs, highlighting the importance of considering additional dynamical influences—such as those arising from the Galactic bar and spiral arms—in future orbit modeling.

The results obtained from orbit analyses under the MWBS potential for the four stars are summarized in Table 9. When these results are placed within the schematic diagram obtained for the MWBS model (Figure 14), it becomes evident that relative to the standard MW model, the stars may follow orbits that can penetrate deeper into the inner regions of the Galaxy. More complex potential calculations further support

that three of the studied stars could have traveled from their parent GCs to the solar vicinity by escaping from regions where the co-rotation effect of the Galactic bar is dominant.

Additionally, the fact that all four stars are G-type main-sequence stars with ages comparable to those of GCs suggests that they are old enough to have plausibly moved from their parent clusters to the solar neighborhood. These results predict that a fraction of metal-poor stars in the solar neighborhood may originate from disrupted or evaporated GCs, especially those associated with the Galactic bar. The distinct chemical signatures observed in these stars further emphasize the role of detailed abundance analyses in tracing their Galactic origins. Despite the use of high-resolution spectral data and space-based photometric and astrometric observations, precise population classification of these stars remains challenging. This study underscores the necessity of high-resolution spectroscopy and space-based observations of GCs to refine our understanding of the Galactic origins of metal-poor stars.

#### 4.4. Future Works and Sights

As new data from various sky survey programmes is obtained on a daily basis, our understanding of the structural and evolutionary processes of our Galaxy is being significantly expanded. In particular, *Gaia* DR4 data, which are expected to be released in the near future, will enable the kinematic and dynamical orbital parameters of stars to be determined more accurately and precisely. This development holds immense potential for unravelling the enigmatic origins and intrinsic nature of metal-poor stars.

In parallel to these upcoming efforts, recent high-resolution spectroscopic studies have already made significant strides in characterizing metal-poor stellar populations. Surveys such as COMBS I/II/III (M. Lucey et al. 2019, 2021; M. Lucey et al. 2022) SDSS/SEGUE (E. Caffau et al. 2011) and the Pristine Survey (K. A. Venn et al. 2020; N. F. Martin et al. 2024; A. Viswanathan et al. 2025) have delivered high-quality abundance measurements for large samples of metal-poor stars, probing nucleosynthetic signatures and Galactic chemical evolution. Individual high-resolution studies (e.g., J. E. Norris et al. 2013; A. E. García Pérez et al. 2013; S. C. Keller et al. 2014; A. Frebel & J. E. Norris 2015b) have further resolved the detailed chemistry of ultra metal-poor stars, offering critical insights into early stellar generations. These efforts complement large-scale projects like GALAH survey (S. Buder et al. 2024) and LAMOST (H.-N. Li et al. 2015), which combine moderate- and high-resolution

spectroscopy to map metallicity gradients and substructures in the halo.

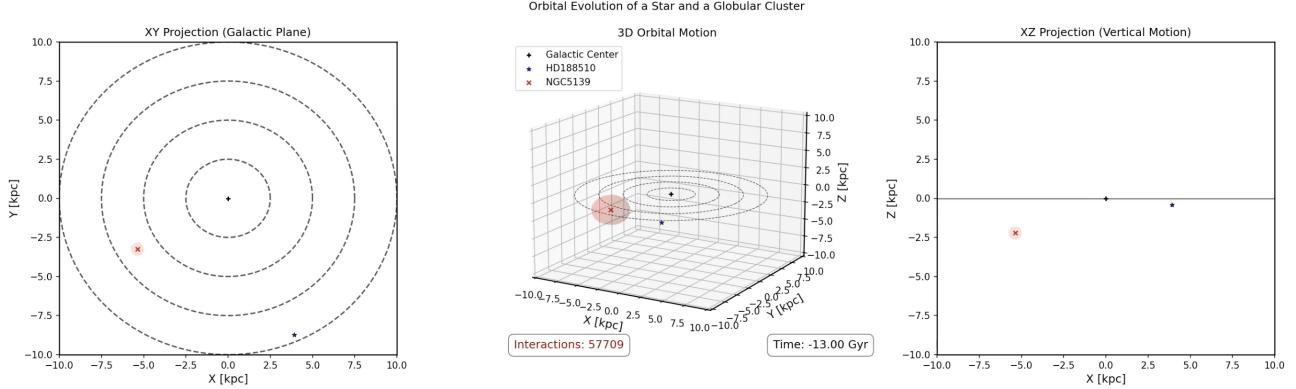
Beyond the data provided by *Gaia*, large-scale observing projects such as 4MOST (R. S. de Jong et al. 2012), H3 (C. Conroy et al. 2019), and Milky Way Mapper (J. A. Kollmeier et al. 2017) aim to study the chemical evolution of our Galaxy through high-resolution and high signal-to-noise ratio spectra obtained at different wavelengths, while also providing radial velocity measurements, which are essential data for kinematic analyses. These programs will synergize with existing high-resolution campaigns (e.g., TOPos E. Caffau et al. 2013) to bridge gaps between kinematic and chemical diagnostics for metal-poor populations.

In the near future, these high-accuracy data will facilitate the detection and deeper understanding of the origin of the structures of uncertain origin that are the subject of our study, as well as structural anomalies caused by intrinsic gravitational interactions beyond the chemical and dynamical evolution of our Galaxy. Consequently, it is anticipated that the solution approaches developed in this study will provide a framework for further analyses with larger and more sensitive data sets.

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*Software:* LIME (T. Şahin 2017), MOOG (C. Sneden 1974), GALPY (J. Bovy 2015), MWPotential2014 (J.



**Figure 15.** Orbital evolution of HD 188510 and NGC 5139 ( $\omega$  Cen) in the MWpotential2014. The left panel shows the top-down ( $X - Y$ ) projection in the Galactic plane, with dashed circles indicating constant Galactocentric radii. The central panel illustrates the full 3D orbital motion, while the right panel presents the vertical ( $X - Z$ ) projection, highlighting motion perpendicular to the Galactic plane. The Galactic center is marked with a black cross, HD 188510 with a blue star, and NGC 5139 with a red cross, which corresponds to 5 tidal radii. The figure represents to a backward to 13 Gyr, with a total of 57,709 interaction calculations performed. An animated version showing the orbital evolution over 13 Gyr back integration is available as a supplementary material. The animation captures the full 3D motion, including projection onto the Galactic plane and vertical oscillations relative to it. The total duration of the animation is 1 min 20 s.

Bovy 2015), DehnenBarPotential (W. Dehnen 2000; G. Monari et al. 2016), SpiralArmsPotential (D. P. Cox &

G. C. Gómez 2002), ARIADNE (J. I. Vines & J. S. Jenkins 2022).

## APPENDIX

### A. ORBITAL EVOLUTION OF HD 188510 AND NGC 6441

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