

Assignment 4 Example

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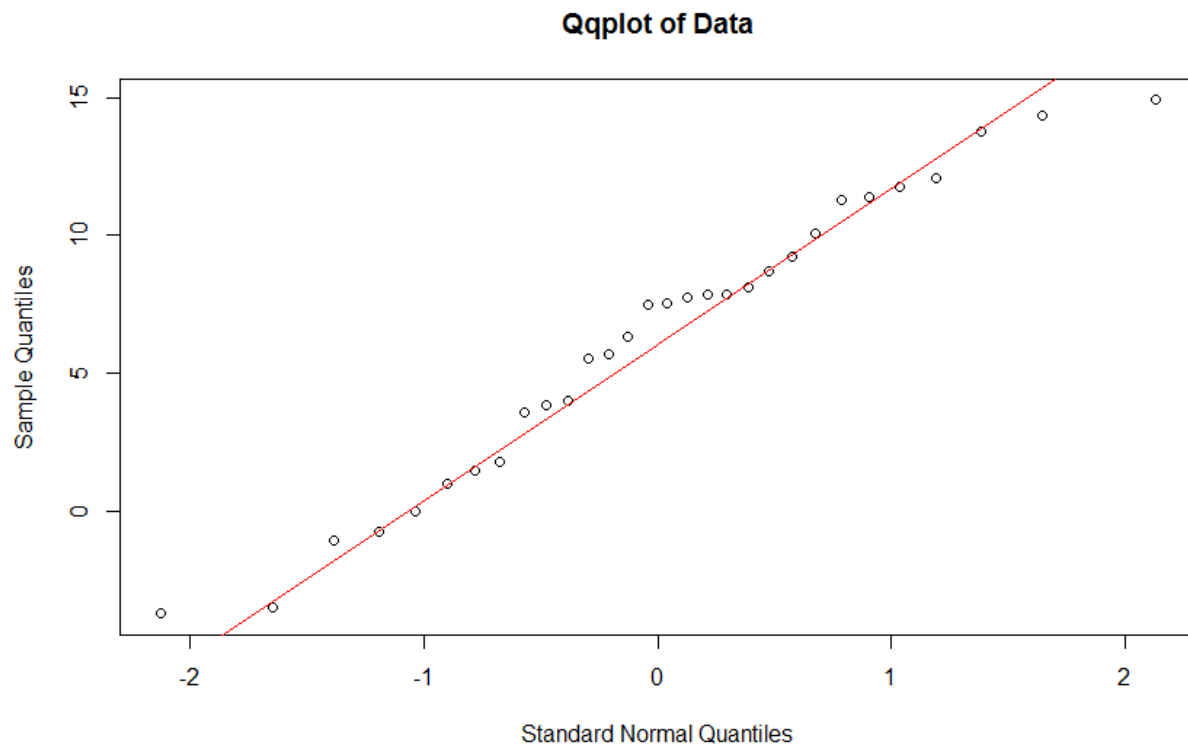
UWaterloo ID: 20456458

Problem 1: Fill in the information below based on your data which were generated using your ID number as the seed for the random number generator.

model = 1

$\mu = 8$

$\sigma = 5$



Based on the qqplot indicate how well the Gaussian model fits the data. Justify your conclusion.

$\mu_0 = 9$

```
> t.test(y, mu=mu0, conf.level=0.95)
```

One Sample t-test

```
data: y
t = -2.8669, df = 29, p-value = 0.007643
alternative hypothesis: true mean is not equal to 9
95 percent confidence interval:
 4.336738 8.219928
sample estimates:
mean of x
 6.278333
```

value of test statistic for testing $H: \mu = \mu_0$ is: -2.8669

degrees of freedom of t distribution = 29

p-value for testing $H: \mu = \mu_0$ equals 0.007643

95% confidence interval for μ is: [4.336738, 8.219928]

Insert your conclusion regarding $H: \mu = \mu_0$ here.

sample mean = 6.278333

$\sigma_0 = 7$

sample variance = 27.03675

p-value for testing $H: \sigma = \sigma_0$ equals 0.04895834

Insert your conclusion regarding $H: \sigma = \sigma_0$ here.

95% confidence interval for sigma squared: [17.14843, 48.86035]

95% confidence interval for sigma: [4.141067, 6.990018]

Problem 2: Fill in the information below based on your data which were generated using your ID number as the seed for the random number generator.

alpha = 2.293382 beta = -2.601833 model = 1

sample correlation = -0.8625526

Call:

`lm(formula = y ~ x)`

Residuals:

Min	1Q	Median	3Q	Max
-21.2398	-5.9288	-0.4623	7.0616	20.0681

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	5.435	2.021	2.69	0.0084 **
x	-2.954	0.175	-16.88	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 9.326 on 98 degrees of freedom

Multiple R-squared: 0.744, Adjusted R-squared: 0.7414

F-statistic: 284.8 on 1 and 98 DF, p-value: < 2.2e-16

estimate of the intercept = 5.435

estimate of the slope = -2.954

degrees of freedom of t distribution = 98

value of test statistic for testing H: no relationship (slope = 0) equals -16.88

p-value for testing the H: no relationship (slope = 0) equals 2.2e-16

Insert your conclusion regarding the hypothesis of no relationship here.

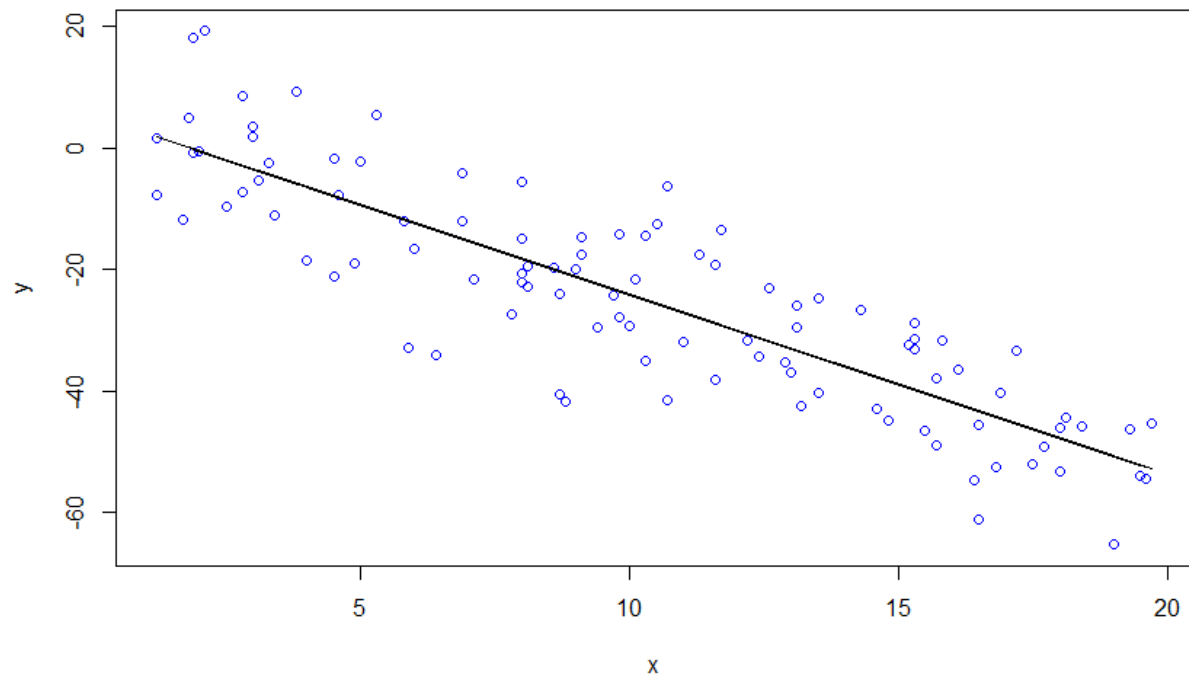
estimate of sigma = 9.326383

95% confidence interval for the slope: [-3.301399, -2.606673]

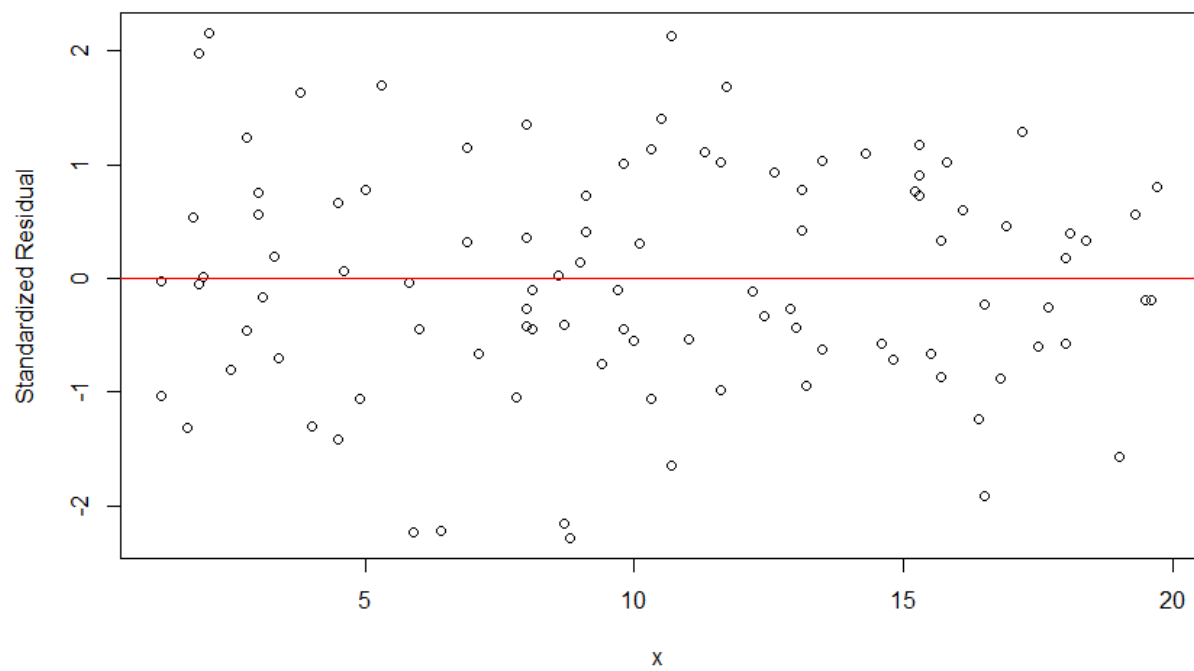
90% confidence interval for the mean response at x=5: [-11.507 -7.162702]

99% prediction interval for the response at x=2: [-25.38452, 24.43904]

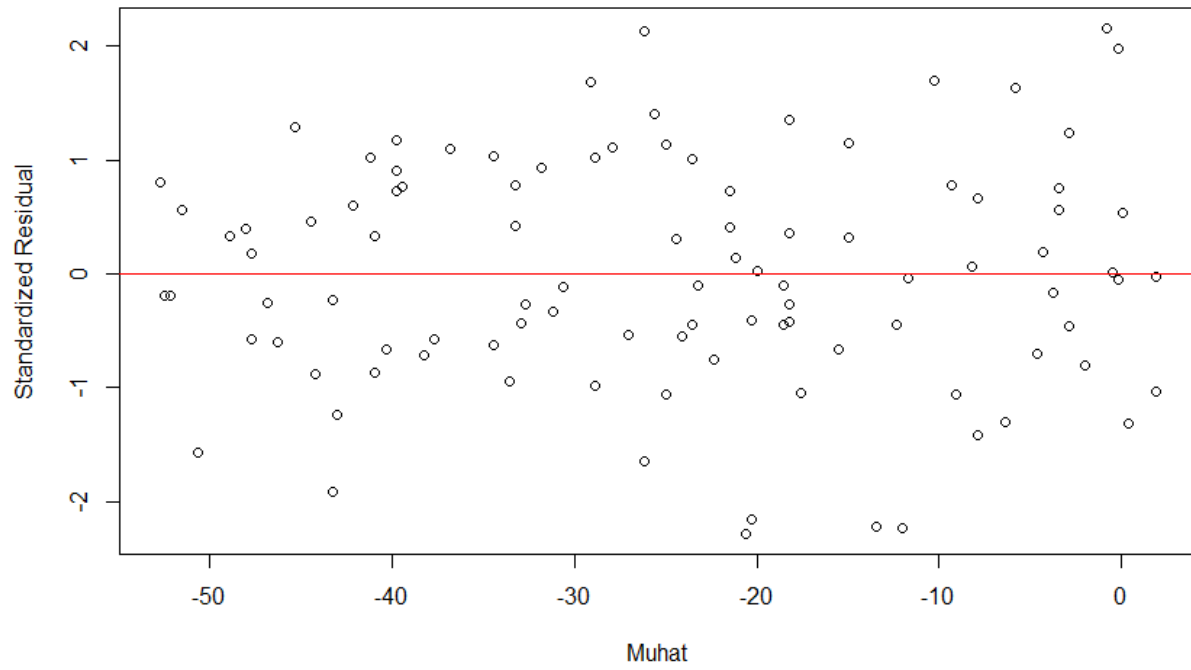
Scatterplot with Fitted Line



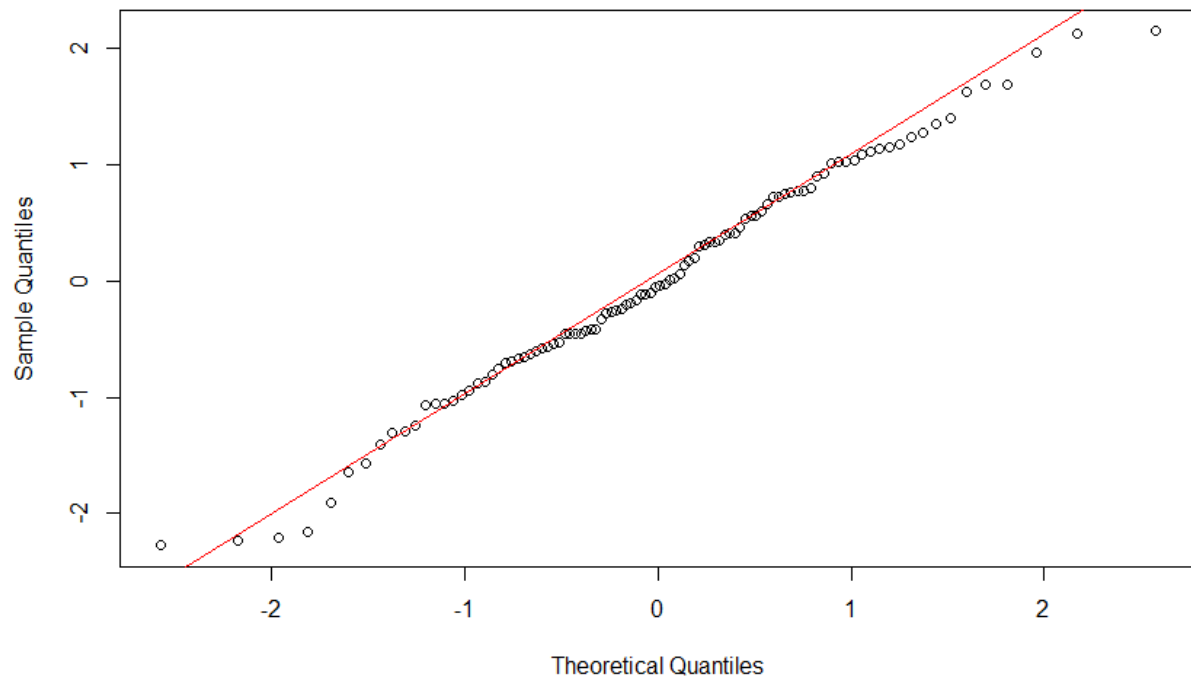
Residual vs x



Residual vs Muhat



Qqplot of Residuals



Based on the scatterplot with fitted line and the residual plots discuss the fit of the simple linear model to your data. Be sure to comment on each plot. Indicate clearly what you expect to see for each plot if the model assumptions hold and what you observe for your data.

Problem 3: Fill in the information below based on your data which were generated using your ID number as the seed for the random number generator.

mu1 = -3.171255 mu2 = -0.371706 sigma = 5

```
> t.test(y1, y2, mu=0, var.equal=TRUE, conf.level=0.95)
      Two Sample t-test
data:  y1 and y2
t = -2.7641, df = 63, p-value = 0.007477
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -4.6087821 -0.7410274
sample estimates:
 mean of x  mean of y
-2.8103333 -0.1354286
```

The value of the test statistic for testing $H: \mu_1 = \mu_2$ equals -2.7641

degrees of freedom of t distribution = 63

p-value for testing $H: \mu_1 = \mu_2$ equals 0.007477

Insert your conclusion regarding $H: \mu_1 = \mu_2$ here.

95% confidence interval for the difference in means: [-4.6087821, -0.7410274]

sample means:

$$\bar{y}_1 = -2.8103333$$

$$\bar{y}_2 = -0.1354286$$

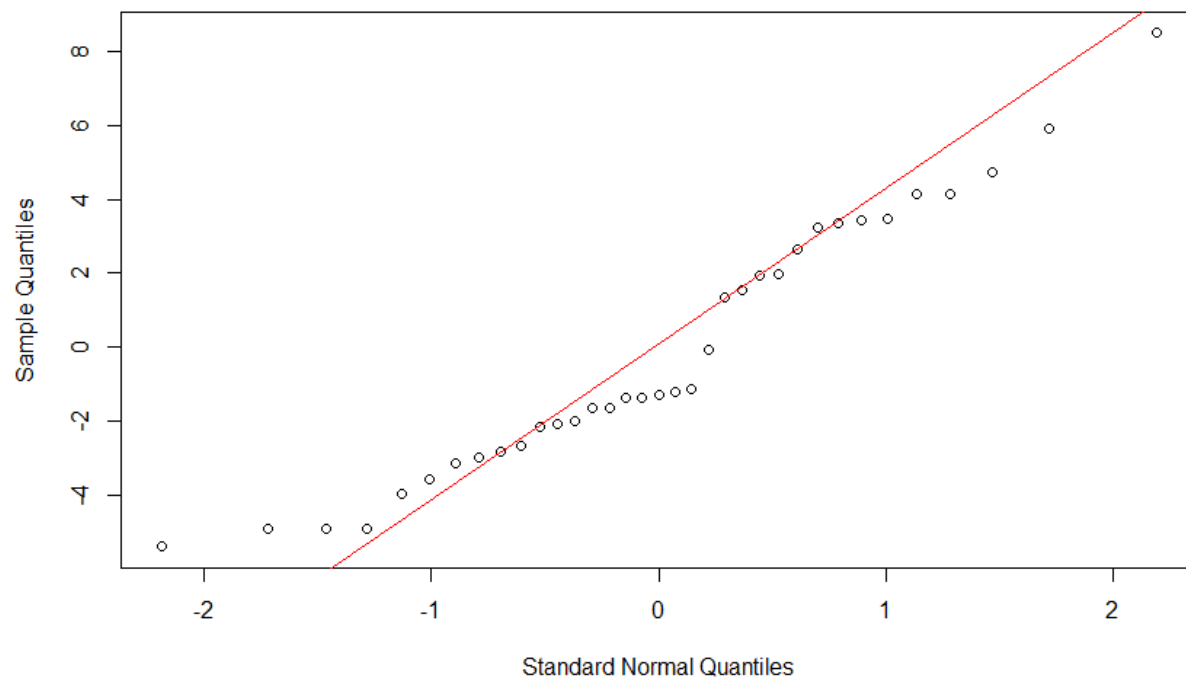
sample standard deviations:

$$s_1 = 4.298046$$

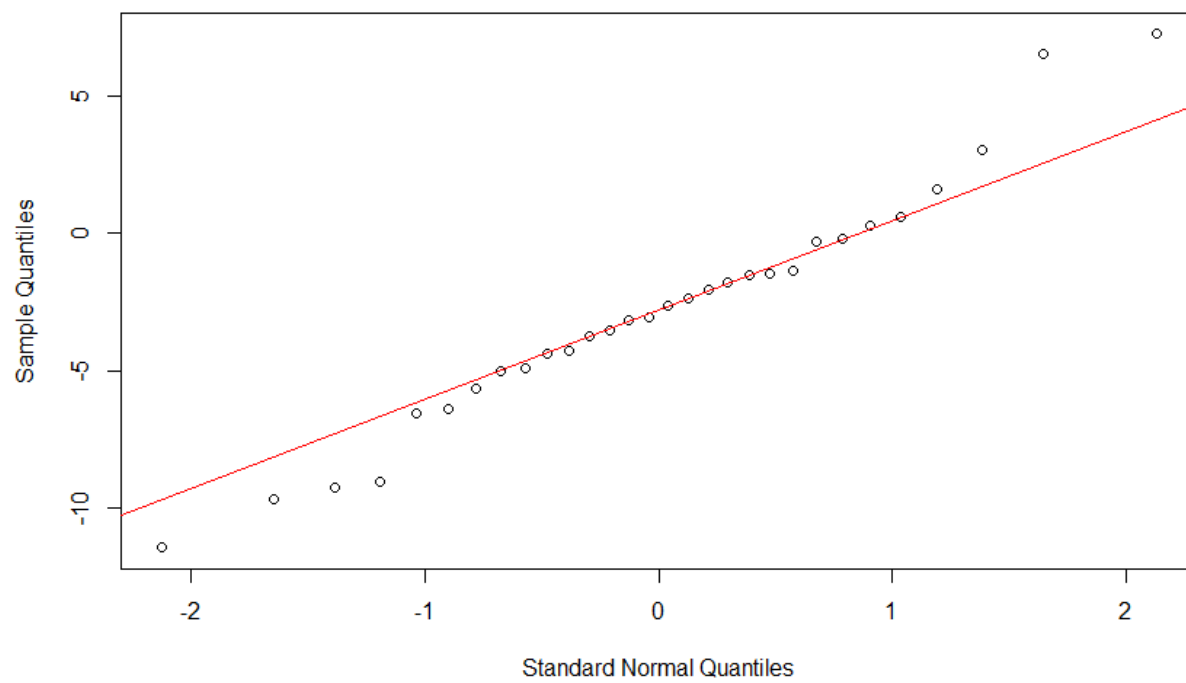
$$s_2 = 3.503656$$

$$\text{pooled estimate of sigma} = 3.889532$$

Qqplot of Data



Qqplot of Data



Based on the qqplots indicate how well the Gaussian model fits each data set. Justify your conclusions.