

Gabled Urbanism

Design Goal



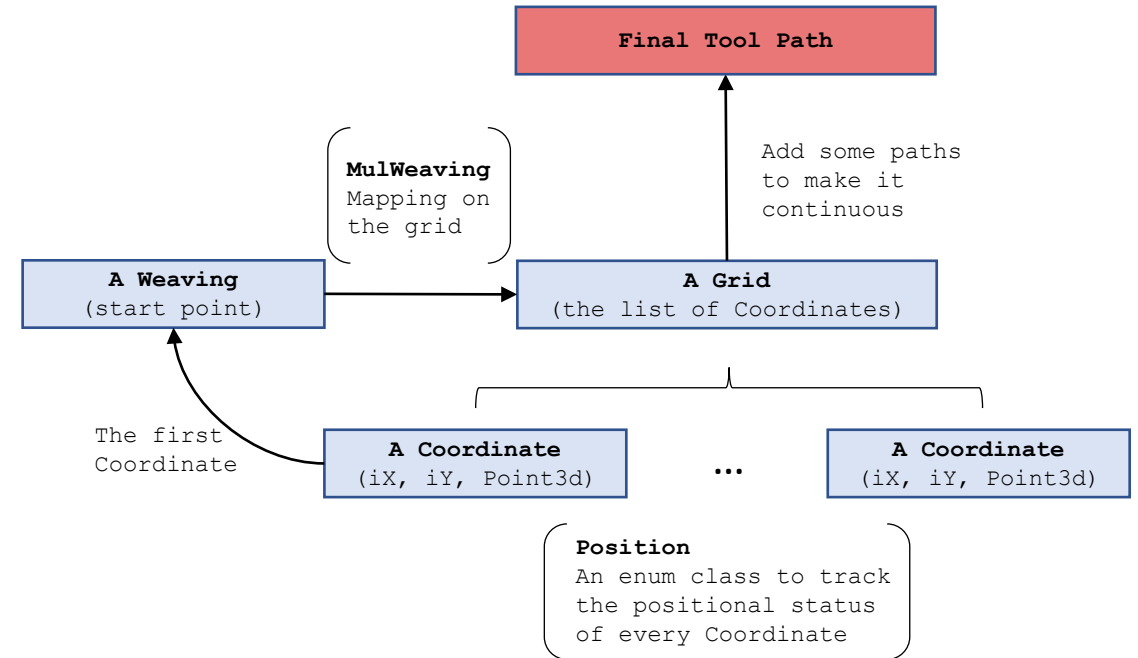
// This project is inspired by the urban fabric registered by **a continuous landscape of gable roofs** in historical European towns. The design will address this endless repetitive pattern of gable-ness through a code that makes the tool path “weave” around the mill board not only planarly but along the Z-axis as well to carve out the form.

// Image:
<https://www.britannica.com/technology/gable>

The Code | Data Structure

```
98 //An enum for documenting the positional status of each Coordinate.
99 public enum Position...
105 1
106 //A Coordinate class that documents a point coordinate and its X,Y indices.
107 class Coordinate...
137 2
138 //A grid class that is defined by int res, double size, and a list of Coordinates.
139 class Grid...
257 3
258 //A Weaving class of the polyline moving along z-axis.
259 public class Weaving...
303 //A method to draw multiple weaving pattern.
304 public Polyline MulWeaving(Weaving w, int n)...
305
```

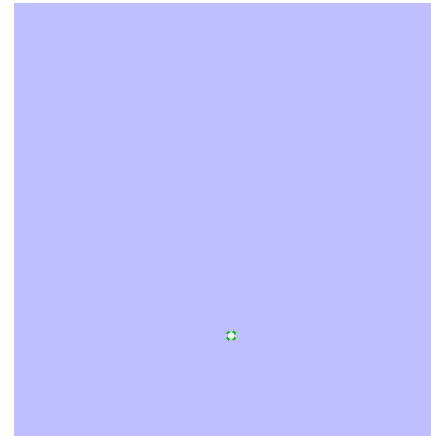
// The code is basically comprised of three major classes as components: the Coordinate class, the Grid class, and the Weaving class.



The Code | Data Structure

Coordinate Class

```
98 //An enum for documenting the positional status of each Coordinate.
99 public enum Position {
100     Inner,
101     OuterX,
102     OuterY,
103     Vertex
104 }
105
106 //A Coordinate class that documents a point coordinate and its X,Y indices.
107 class Coordinate {
108     public int iX, iY;
109     public Point3d origin;
110     public Position pos {get;set;}
111
112     public void ChangePosStatus(Position p) {
113         this.pos = p;
114     }
115
116     public Coordinate() {
117         iX = 0;
118         iY = 0;
119         origin = new Point3d();
120     }
121     public Coordinate(int x, int y, Point3d pt) {
122         this.iX = x;
123         this.iY = y;
124         this.origin = pt;
125     }
126     public void ChangeIndex (int x, int y) {
127         this.iX = x;
128         this.iY = y;
129     }
130     public Point3d DrawPt() {
131         return this.origin;
132     }
133     public void Translate (Vector3d v) {
134         this.origin = this.origin + v;
135     }
136 }
137
```



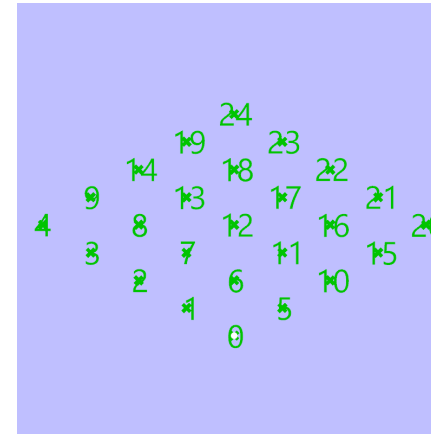
// A **Coordinate** is comprised of its geometric coordinate **Point 3d origin**, its X/Y indices in the Grid **int iX** and **iY**, and its Positional status **enum pos**.

// The starting point of everything is a simple **Coordinate(0, 0, Point3d())** with Position Inner.

// The Coordinate class has methods like ChangePosStatus, ChangeIndex, **DrawPt**, and Translate.

The Code | Data Structure Grid Class

```
138 //A grid class that is defined by int res, double size, and a list of Coordinates.
139 class Grid {
140     public double size;
141     public int res;
142     public List<Coordinate> cLst = new List<Coordinate>();
143
144     public Grid() {
145         size = 0.0;
146         res = 0;
147     }
148
149     public Grid(int res, double size, Point3d start) {
150         this.size = size;
151         this.res = res;
152         double interval = size / (res - 1);
153         List<Coordinate> cLst = new List<Coordinate>();
154         for (int i = 0; i < res; i++) {
155             for (int j = 0; j < res; j++) {
156                 Coordinate c = new Coordinate(i, j, new Point3d(i * interval + start.X, j * interval + start.Y, start.Z));
157                 if (c.iX == res - 1 && c.iY == res - 1) {
158                     c.ChangePosStatus(Position.Vertex);
159                 } else if (c.iX == res - 1 && c.iY < res - 1) {
160                     c.ChangePosStatus(Position.OuterX);
161                 } else if (c.iY == res - 1 && c.iX < res - 1) {
162                     c.ChangePosStatus(Position.OuterY);
163                 } else {
164                     c.ChangePosStatus(Position.Inner);
165                 }
166                 cLst.Add(c);
167             }
168         }
169         this.cLst = cLst;
170     }
171
172     public void ChangeRes(int r) {
173         this.res = r;
174         foreach (Coordinate c in this.cLst) {
175             if (c.iX == r - 1 && c.iY == r - 1) {
176                 c.ChangePosStatus(Position.Vertex);
177             } else if (c.iX == r - 1 && c.iY < r - 1) {
178                 c.ChangePosStatus(Position.OuterX);
179             } else if (c.iY == r - 1 && c.iX < r - 1) {
180                 c.ChangePosStatus(Position.OuterY);
181             } else {
182                 c.ChangePosStatus(Position.Inner);
183             }
184         }
185     }
186
187     public void ChangeSize(double s) {
188         this.size = s;
189     }
190
191     public Coordinate GetCoordinate(int x, int y) {
192         List<Coordinate> cLst = this.cLst;
193         foreach (Coordinate c in cLst) {
194             if (c.iX == x && c.iY == y) {
195                 return c;
196             }
197         }
198         return new Coordinate();
199     }
200
201     public List<Point3d> DrawGridPts() {
202         List<Coordinate> newLst = this.cLst;
203         List<Point3d> result = new List<Point3d>();
204         foreach (Coordinate item in newLst) {
205             result.Add(item.DrawPt());
206         }
207         return result;
208     }
209
210     public void TranslateGrid(Vector3d v) {
211         foreach (Coordinate c in this.cLst) {
212             c.origin = c.origin + v;
213         }
214     }
215 }
```



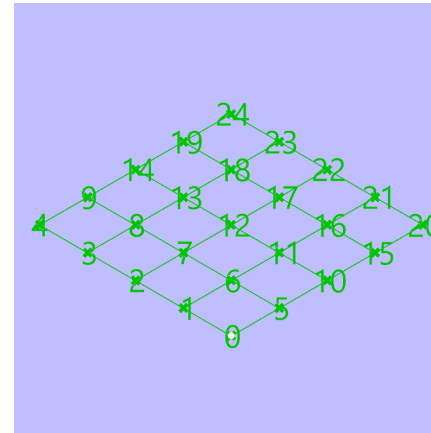
// A **Grid** is comprised of a **list of Coordinates cLst**, its resolution **int res**, and its size **double size**.

// The constructor of Grid class **reassigns the Position class** to each Coordinate element in its cLst, for instance, the 4/9/14/19 will be assigned to OuterY, the 20/21/22/23 will be assigned to OuterX, the 24 will be Vertex, and the rest will be Inner.

// The Grid class has methods like ChangeRes, ChangeSize, **DrawGridPts**, and TranslateGrid.

The Code | Data Structure Grid Class

```
217 public Polyline DrawGridLine() {
218     List<Point3d> pts = this.DrawGridPts();
219     Polyline result = new Polyline();
220     int k = 0;
221
222     Point3d temp_pt = this.GetCoordinate(0, 0).origin;
223     for(int j = 0; j < res; j++){
224         for(int i = 0; i < res; i++){
225             if(j % 2 == 0){
226                 temp_pt = pts[k];
227                 result.Add(temp_pt);
228             }else{
229                 temp_pt = pts[k + res - 1 - 2 * i];
230                 result.Add(temp_pt);
231             }
232             k++;
233         }
234     }
235     result.Add(this.GetCoordinate(0, res - 1).origin);
236     result.Add(this.GetCoordinate(0, 0).origin);
237
238     int l = 0;
239     temp_pt = this.GetCoordinate(0, 0).origin;
240     for(int j = 0; j < res; j++){
241         for(int i = 0; i < res; i++){
242             if(j % 2 == 0){
243                 temp_pt = pts[i * res + j];
244                 result.Add(temp_pt);
245             }else{
246                 temp_pt = pts[l + (res - j) * (res - 1) - i * (res + 1)];
247                 result.Add(temp_pt);
248             }
249             l++;
250         }
251     }
252
253     return result;
254 }
255
256 }
257 }
```



// The most important method in Grid class is **DrawGridLine**. This method allows a continuous tool path going through the whole grid with minimal length of overlapped path.

// It basically goes as s-shape in one direction to draw the path along the Y-axis and then change its direction to draw it along the X-axis.

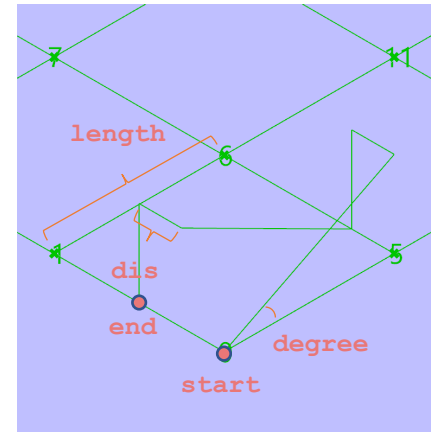
The Code | Data Structure

Weaving Class

```

259 //A Weaving class of the polyline moving along z-axis.
260 public class Weaving {
261     public Point3d start = new Point3d();
262     public Point3d end = new Point3d();
263     public double dis;
264     public double length;
265     public double degree;
266
267     public Weaving() {
268     }
269
270     public Weaving(Point3d start, double dis, double length, double degree) {
271         this.start = start;
272         this.end = new Point3d(start.X, start.Y + dis * 2.0, start.Z);
273         this.dis = dis;
274         this.length = length;
275         this.degree = degree;
276     }
277
278     public void ChangeStart() {
279         Point3d newStart = this.end;
280         this.start = newStart;
281         this.end = new Point3d(this.start.X, this.start.Y + dis * 2.0, this.start.Z);
282     }
283
284     public Polyline DrawOne () {
285         Polyline poly = new Polyline();
286         double dz = Math.Tan(this.length) * Math.PI * this.degree;
287         poly.Add(this.start);
288         Point3d pt2 = new Point3d(start.X + this.length, start.Y, start.Z + dz);
289         Point3d pt3 = new Point3d(pt2.X, pt2.Y + this.dis, pt2.Z);
290         Point3d pt4 = new Point3d(pt3.X, pt3.Y, pt3.Z - dz);
291         Point3d pt5 = new Point3d(pt4.X - this.length, pt4.Y, pt4.Z + dz);
292         Point3d pt6 = new Point3d(pt5.X, pt5.Y + this.dis, pt5.Z);
293
294         poly.Add(pt2);
295         poly.Add(pt3);
296         poly.Add(pt4);
297         poly.Add(pt5);
298         poly.Add(pt6);
299         poly.Add(this.end);
300
301         return poly;
302     }
303 }

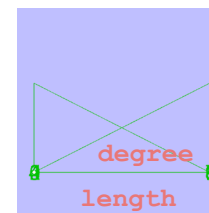
```



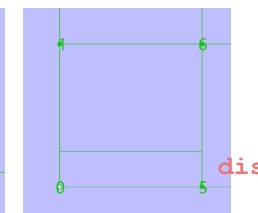
// A Weaving class generates a polyline that forms a **shape of X** in **sectional view** through its DrawOne function.

// The constructor takes a start point, the degree of the inclining angle, the distance of the turn, and the length of the whole span.

// The **ChangeStart** method will be used to use the current "end" point as a "start" for next Weaving segment.



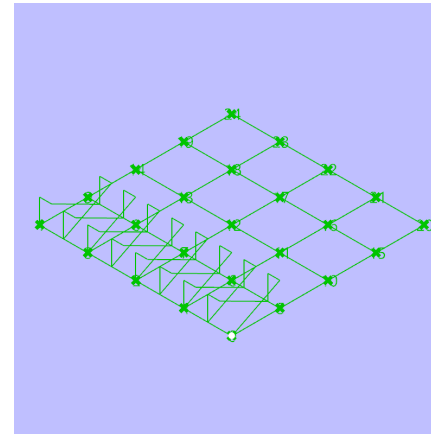
Section



Plan

The Code | Data Structure Weaving Class

```
309 //A method to draw multiple weaving pattern.
310 public Polyline MulWeaving(Weaving w, int n){
311     int i = 0;
312     Polyline poly = new Polyline();
313     while (i < n){
314         Polyline result = w.DrawOne();
315         poly.AddRange(result);
316         w.ChangeStart();
317         i++;
318     }
319     return poly;
320 }
```

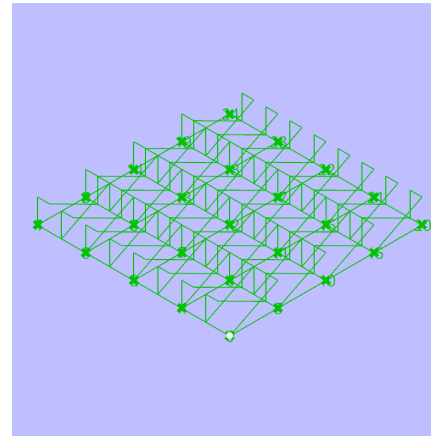


// The **MulWeaving** method is used to generate multiple Weaving segment into a polyline by using **ChangeStart** through a **while loop**.

The Code | Tool Path Logic

Main Function

```
55 private void RunScript(Point3d start, double size, double degree, int res, int density, ref object _polyline, ref object _timecost, ref object _length, ref object _text, ref object A, ref object B)
56 {
57     Grid g = new Grid(res, size, start);
58     double length = size / (res - 1);
59     int nummberOfTurns = density;
60     double dis = length / (density * 2);
61
62     List<string> text = new List<string>();
63     text.Add("start milling");
64
65
66     int n = 0;
67     Polyline result = new Polyline();
68     while (n < res - 1){
69         Point3d pt = g.GetCoordinate(n, 0).origin;
70         Weaving w = new Weaving(pt, dis, length, degree);
71         Polyline onePoly = MulWeaving(w, density * (res - 1));
72         result.AddRange(onePoly);
73
74         result.Add(pt);
75         n++;
76     }
77
78     A = g.DrawGridPts();
79     B = g.DrawGridLne();
80     result.AddRange(g.DrawGridLne());
81
82     result.MergeColinearSegments(0.01, false);
83
84     double time = result.Length + result.Count * 3;
85
86     text.Add("end milling");
87     _polyline = result;
88     _text = text;
89     _length = result.Length;
90     _timecost = time;
91 }
```



// **Step 1:** Input parameters(**res**, **size**, **start point**) to create a **Grid**.

// **Step 2:** Use the **density** parameter to set the **dis** variable for **Weaving**.

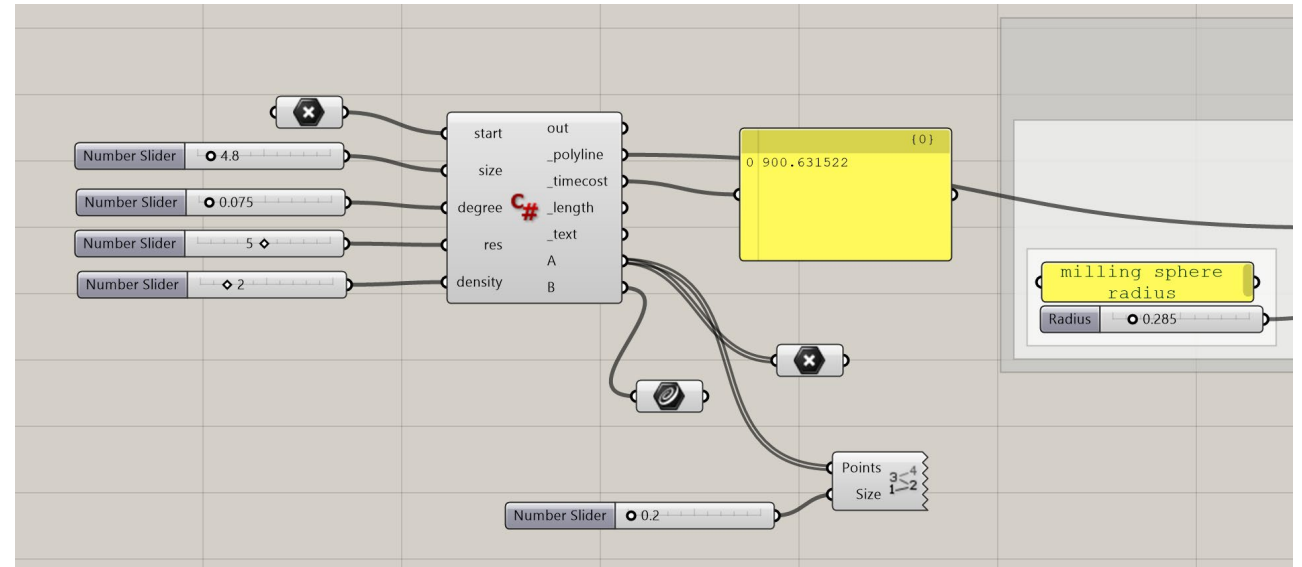
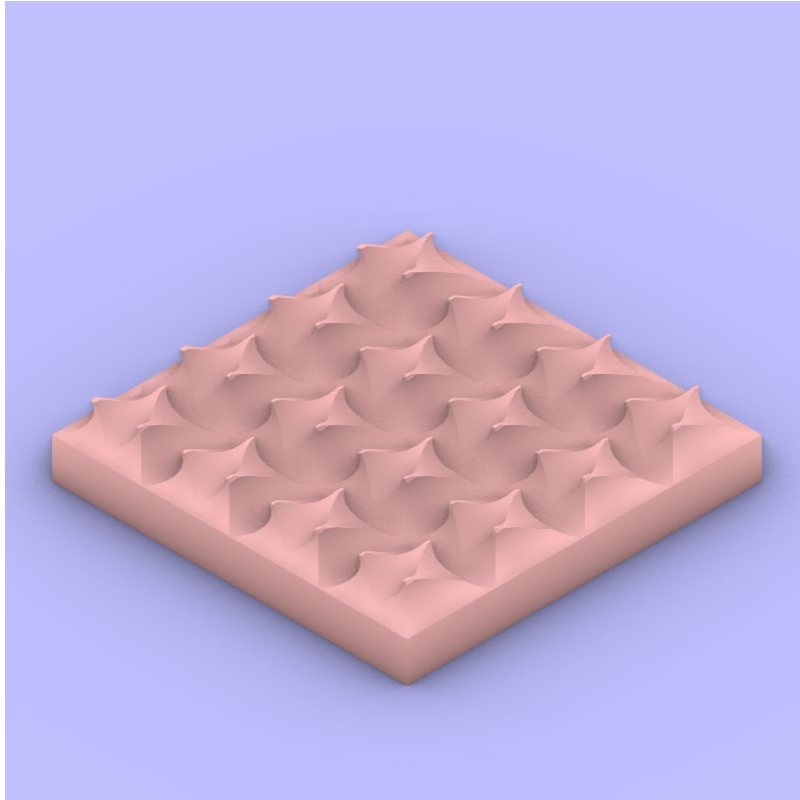
//**Step 3:** Use a while loop to draw multiple Weavings with the parameter **degree** on every column of the Grid, and make sure the **tool path always return to the bottom** to start drawing.

//**Step 4:** **Concatenate** two lists of polylines—the grid and the weaving pattern—and make sure that are **one continuous path**.

//**Step 5:** Calculate the **time** and the **length**.

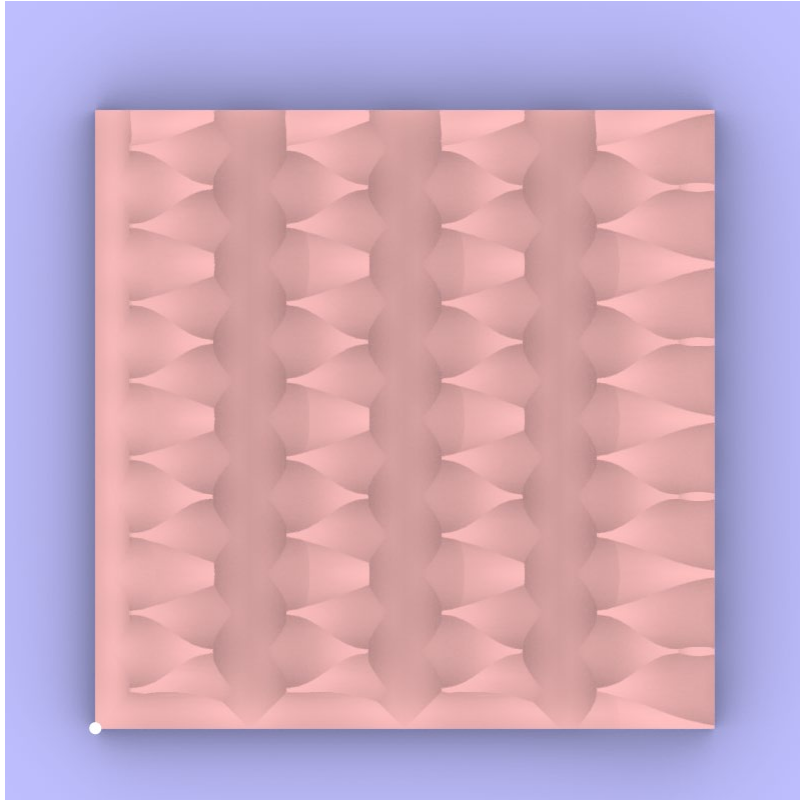
The Design | Iteration 1

A steep gabled urbanism

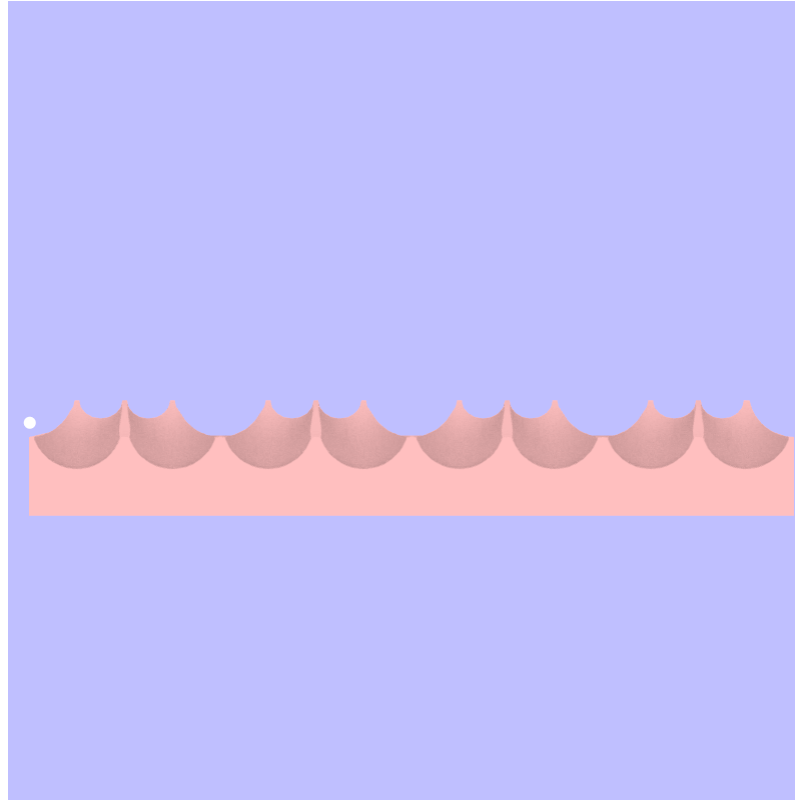


```
// Configuration:  
Size: 4.8; degree: 0.075 (*Pi); res: 5; density: 2
```

The Design | Iteration 1
A steep gabled urbanism



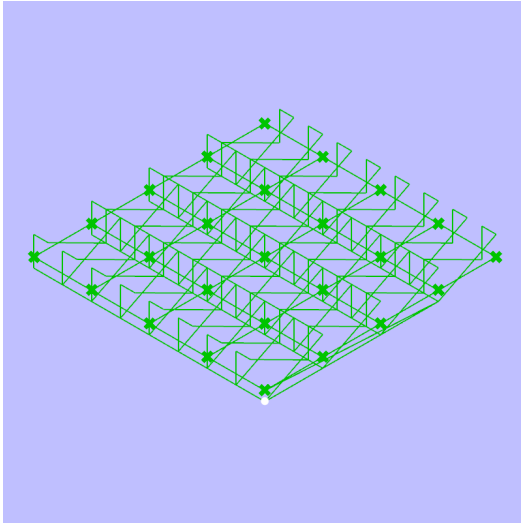
Plan



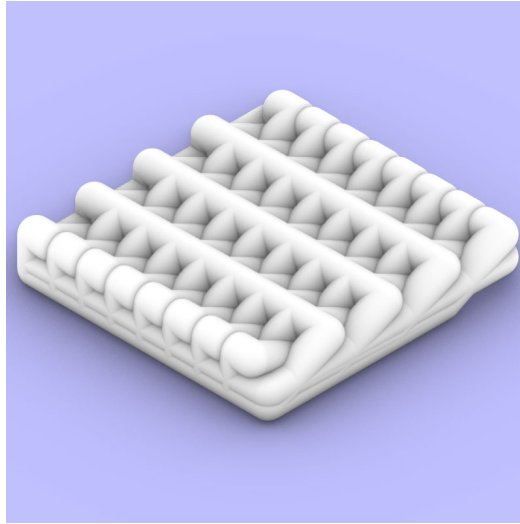
Section

```
g.TranslateGrid(new Vector3d(0.0, 0.0, 0.2));  
  
// Slightly adjust the grid to make  
sure there is not undercuts on Z-  
axis.
```

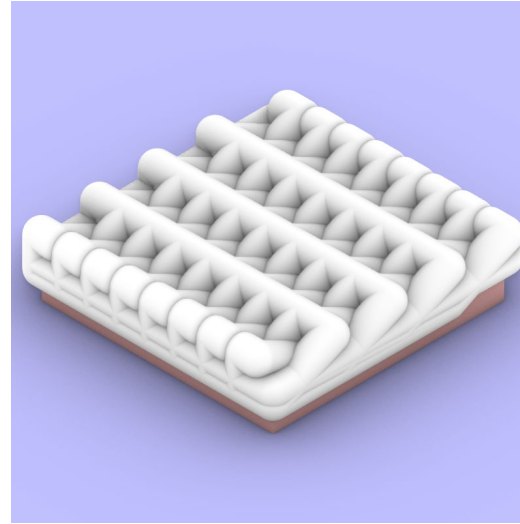
The Design | Iteration 1
A steep gabled urbanism



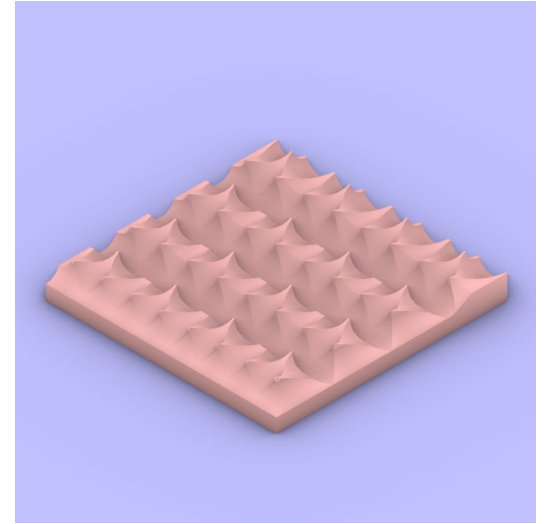
Tool Path



Nozzle

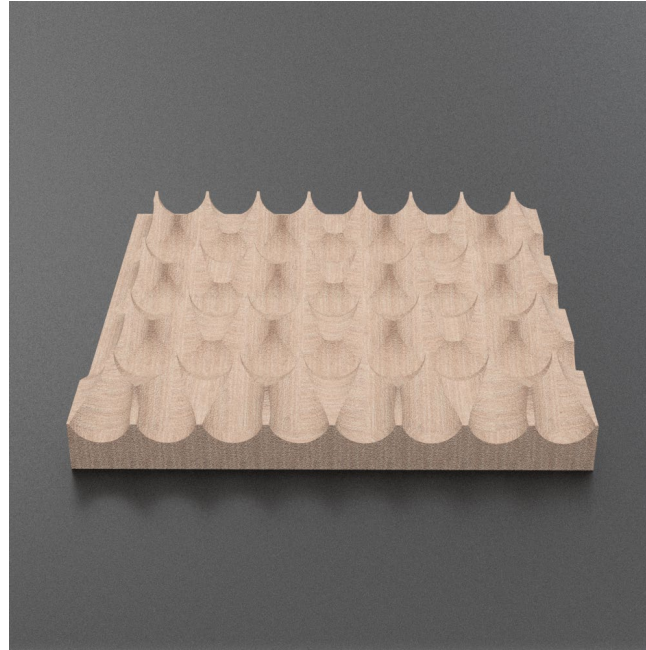


Boolean Out



Milled Block

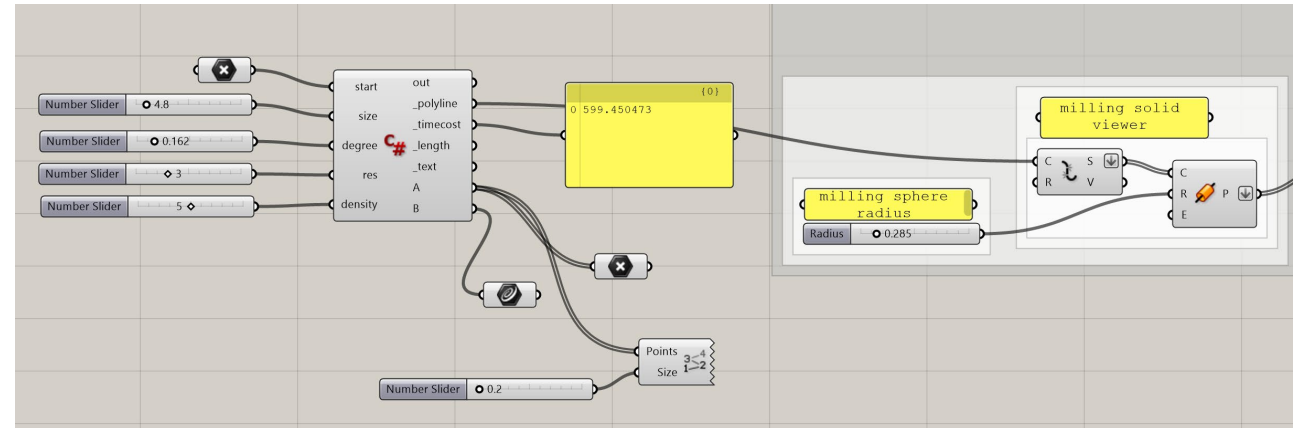
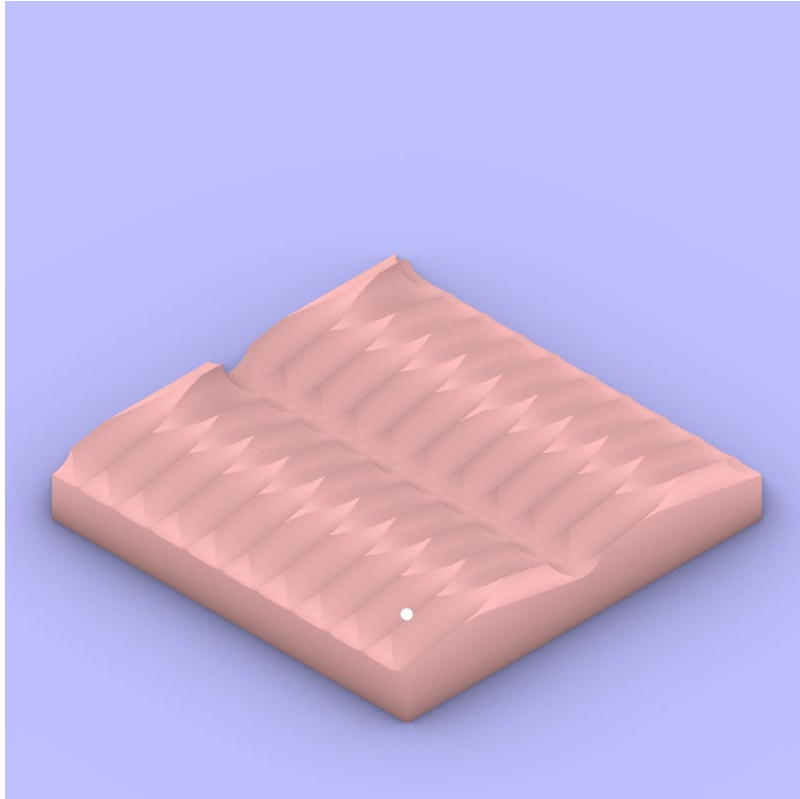
The Design | Iteration 1
A steep gabled urbanism



// This iteration creates a 4*4 city block with steep and pointy gables. At the street level a continuous set of building-scale facades is registered through the steep gables.

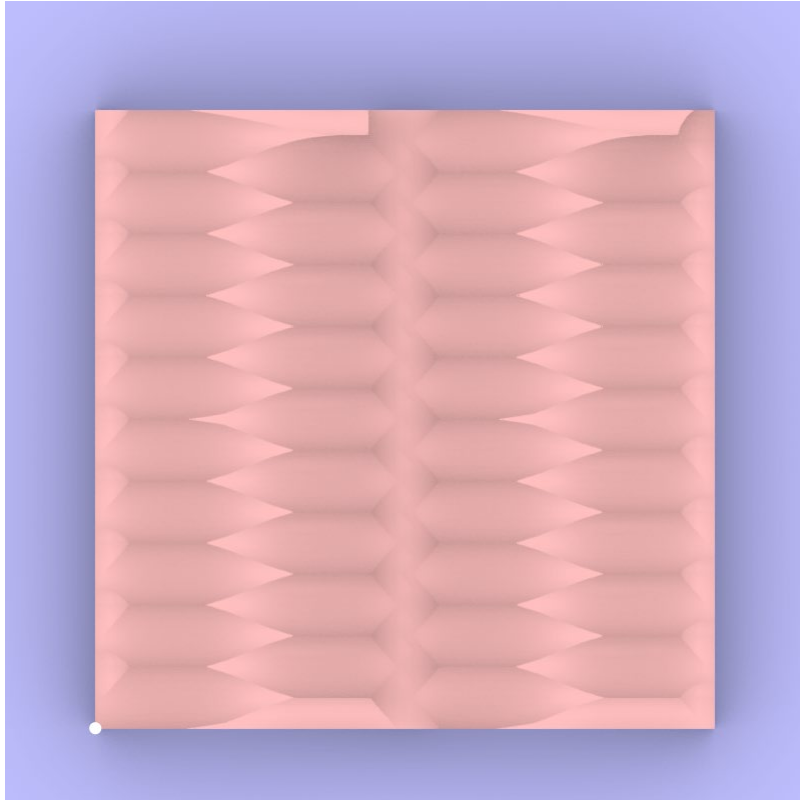
The Design | Iteration 2

A gradual gabled urbanism

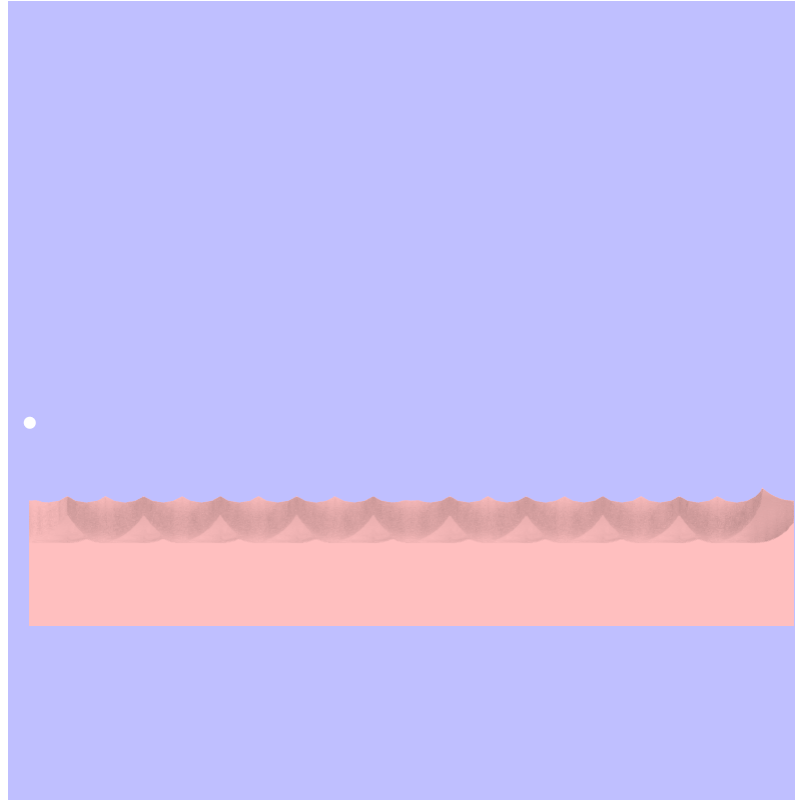


```
// Configuration:  
Size: 4.8; degree: 0.162 (*Pi); res: 3; density: 5  
  
// Lower resolution but higher density of gables
```

The Design | Iteration 2
A gradual gabled urbanism



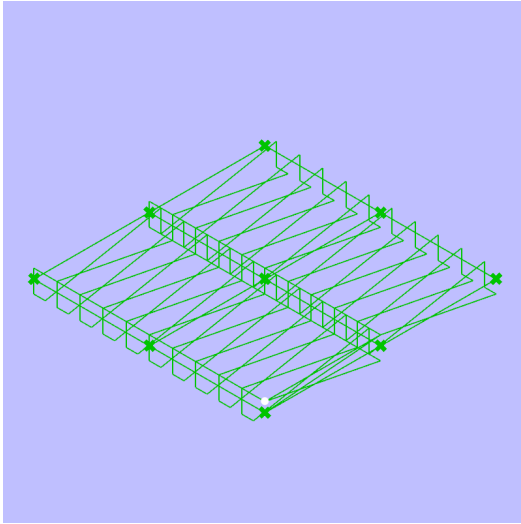
Plan



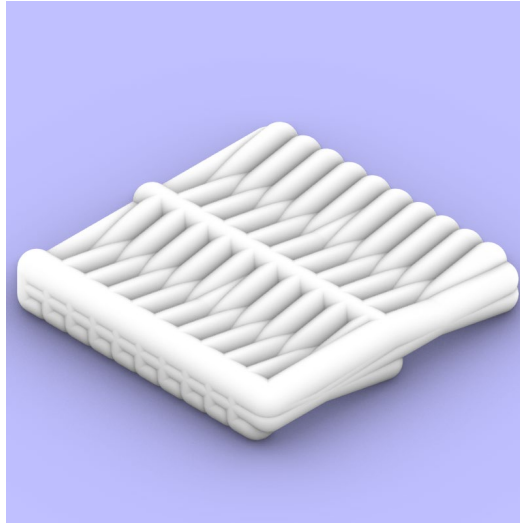
Section

```
g.TranslateGrid(new Vector3d(0.0, 0.0, -0.2));  
  
// Slightly adjust the grid to make  
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```

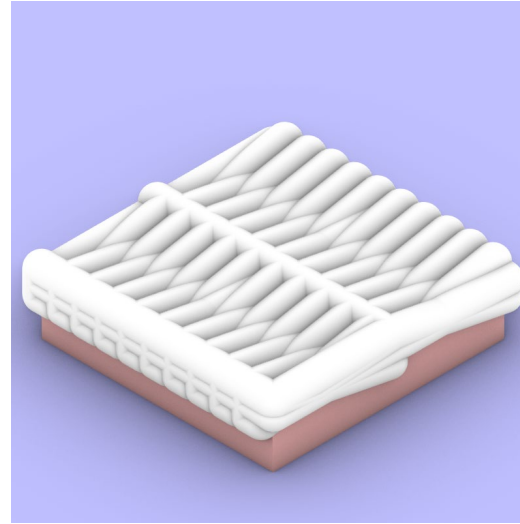
The Design | Iteration 2
A gradual gabled urbanism



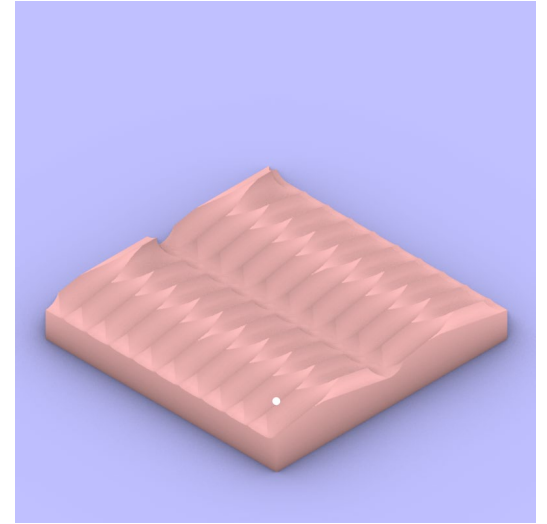
Tool Path



Nozzle



Boolean Out



Milled Block

The Design | Iteration 2
A gradual gabled urbanism



// This iteration creates a 2*2 city block with gradual and flat gables. At the street level the gables have not become architecture yet but remains in a semi-landscape and semi-building formal gesture.