

CS403/503 Programming Languages
Spring 2021
Assignment #1

1. Problem 3 of Chapter 3 on Page 157

Answer:

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\langle \text{id} \rangle \rightarrow A \mid B \mid C$

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle * \langle \text{term} \rangle$

$\mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle + \langle \text{term} \rangle$

$\mid \langle \text{factor} \rangle$

$\langle \text{factor} \rangle \rightarrow (\langle \text{expr} \rangle)$

$\mid \langle \text{id} \rangle$

2. Problem 8 of Chapter 3 on Page 158

Answer:

To prove whether the following grammar is ambiguous, one may compare valid leftmost parse trees for the given grammar. If there exists two or more unique trees the reflected grammar is ambiguous; this operation extends to rightmost parse trees as well.

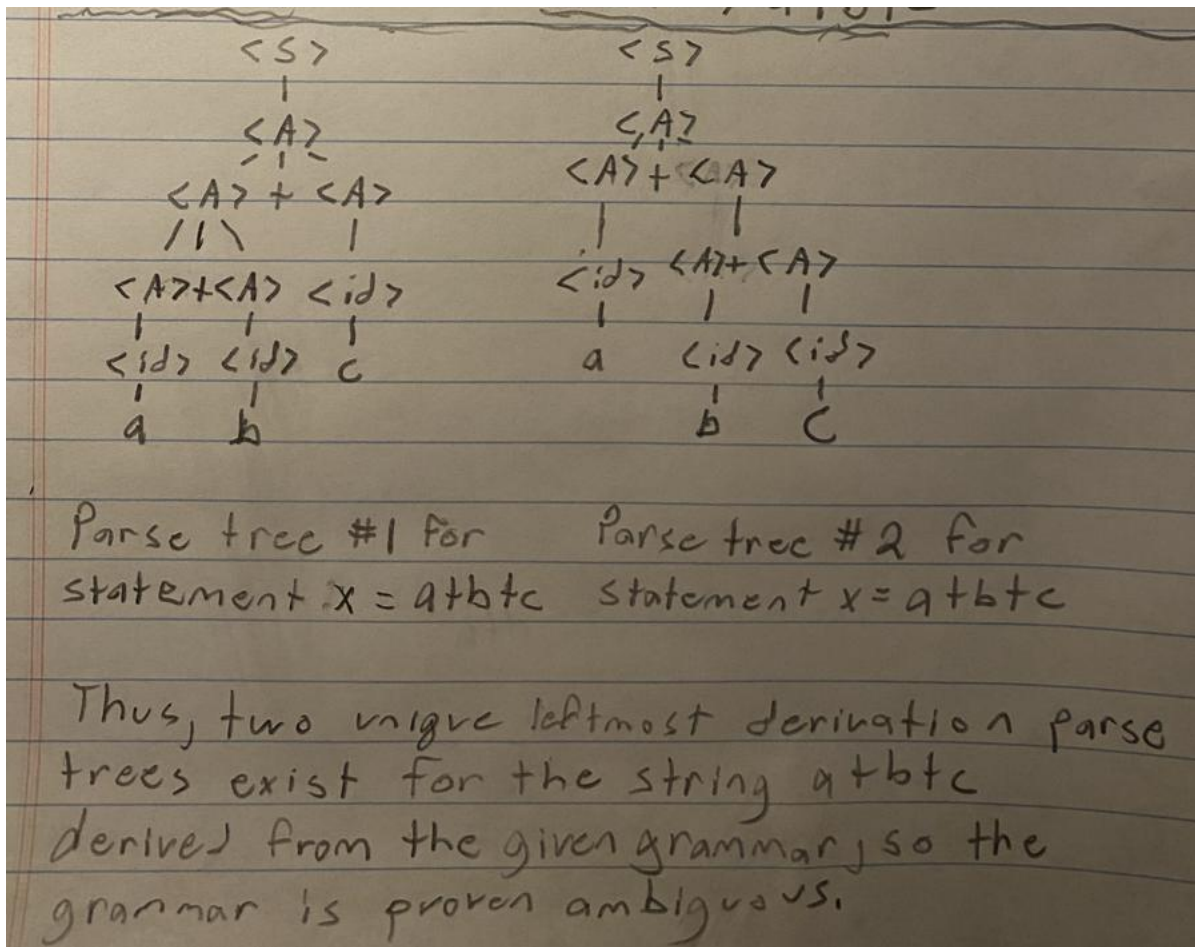
Two unique leftmost derivation parse trees for the grammar:

$\langle S \rangle \rightarrow \langle A \rangle$

$\langle A \rangle \rightarrow \langle A \rangle + \langle A \rangle \mid \langle \text{id} \rangle$

$\langle \text{id} \rangle \rightarrow a \mid b \mid c$

Are illustrated in the embedded photo below:



3. Problem 20 of Chapter 3 on Page 159

Answer:

1) syntax rule: $\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

semantic rule: $\langle \text{expr} \rangle.\text{expected_type} \leftarrow \langle \text{id} \rangle.\text{actual_type}$

2) syntax rule: $\langle \text{id} \rangle \rightarrow A \mid B \mid C$

semantic rule: $\langle \text{id} \rangle.\text{actual_type} \leftarrow \text{look-up}(\langle \text{id} \rangle.\text{string})$

3) syntax rule: $\langle \text{expr} \rangle \rightarrow \langle \text{id} \rangle + \langle \text{expr} \rangle$

semantic rule: $\langle \text{expr} \rangle.\text{actual_type} \leftarrow$
if ($\langle \text{id} \rangle.\text{actual_type} = \text{int}$) and ($\langle \text{expr} \rangle.\text{actual_type} = \text{int}$)
 then int
 else real
end if
predicate: $\langle \text{expr} \rangle.\text{actual_type} == \langle \text{expr} \rangle.\text{expected_type}$

4) syntax rule: $\langle \text{expr} \rangle \rightarrow \langle \text{id} \rangle * \langle \text{expr} \rangle$
semantic rule: $\langle \text{expr} \rangle.\text{actual_type} \leftarrow$
if ($\langle \text{id} \rangle.\text{actual_type} = \text{int}$) and ($\langle \text{expr} \rangle.\text{actual_type} = \text{int}$)
 then int
 else real
end if
predicate: $\langle \text{expr} \rangle.\text{actual_type} == \langle \text{expr} \rangle.\text{expected_type}$

5) syntax rule: $\langle \text{expr} \rangle[1] \rightarrow (\langle \text{expr} \rangle[2])$
semantic rule: $\langle \text{expr} \rangle[1].\text{actual_type} \leftarrow \langle \text{expr} \rangle[2].\text{actual_type}$
predicate: $\langle \text{expr} \rangle[1].\text{actual_type} == \langle \text{expr} \rangle[2].\text{expected_type}$

6) syntax rule: $\langle \text{expr} \rangle \rightarrow \langle \text{id} \rangle$
semantic rule: $\langle \text{expr} \rangle.\text{actual_type} \leftarrow \langle \text{id} \rangle.\text{actual_type}$
predicate: $\langle \text{expr} \rangle.\text{actual_type} == \langle \text{expr} \rangle.\text{expected_type}$

4. Problem 8 of Chapter 4 on Page 194

Answer:

Stack Contents	Input String	Action
0	(id + id) * id \$	Shift 5
0(4	id + id) * id \$	Shift 5
0(4id5	+ id) * id \$	Reduce 6(use GOTO[4, F])
0(4F3	+ id) * id \$	Reduce 4(use GOTO[4, T])
0(4T2	+ id) * id \$	Reduce 2(use GOTO[4, E])
0(4E8	+ id) * id \$	Shift 6
0(4E+6	id) * id \$	Shift 5
0(4E+6id5) * id \$	Reduce 6(use GOTO[6, F])
0(4E+6F3) * id \$	Reduce 4(use GOTO[6, T])
0(4E+6T9) * id \$	Reduce 1(use GOTO[4, E])
0(4E8) * id \$	Shift 11
0(4E8)11	* id \$	Reduce 5(use GOTO[0, (E)])
0F3	* id \$	Reduce 4(use GOTO[6, T])
0T2	* id \$	Shift 7
0T*7	id \$	Shift 5
0T*7id5	\$	Reduce 6(use GOTO[7, F])
0T*7F10	\$	Reduce 3(use GOTO[0, T])
0T2	\$	Reduce 2(use GOTO[0, E])
0E1	\$	Accept