

✓ **Congratulations! You passed!**
TO PASS 80% or higher

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GRADE
100%

Projection onto a 1-dimensional subspace

LATEST SUBMISSION GRADE

100%

1. Compute the projection matrix that allows us to project any vector $\mathbf{x} \in \mathbb{R}^3$ onto the subspace spanned by the basis

2 / 2 points

vector $\mathbf{b} = \begin{bmatrix} 1 \\ 2 \\ 2 \end{bmatrix}$.

Do the exercise using pen and paper. You can use the formula slide that comes with the corresponding lecture.

- ☐ $\begin{bmatrix} 1 & 2 & 2 \\ 2 & 4 & 4 \\ 2 & 4 & 4 \end{bmatrix}$
- ☐ $\begin{bmatrix} 1 \\ 9 \end{bmatrix}$
- ☒ $\frac{1}{9} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 4 & 4 \\ 2 & 4 & 4 \end{bmatrix}$

✓ **Correct**
Well done!

2. Given the projection matrix

2 / 2 points

$$\frac{1}{25} \begin{bmatrix} 9 & 0 & 12 \\ 0 & 0 & 0 \\ 12 & 0 & 16 \end{bmatrix}$$

project $\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ onto the corresponding subspace, which is spanned by $\mathbf{b} = \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$.

Do the exercise using pen and paper.

- ☐ $\frac{1}{25} \begin{bmatrix} 5 \\ 10 \\ 10 \end{bmatrix}$
- ☒ $\frac{1}{25} \begin{bmatrix} 21 \\ 0 \\ 28 \end{bmatrix}$
- ☐ $\begin{bmatrix} 21 \\ 0 \\ 28 \end{bmatrix}$
- ☐ $\begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix}$

✓ **Correct**
Good job!

3. Now, we compute the **reconstruction error**, i.e., the distance between the original data point and its projection onto a lower-dimensional subspace.

1 / 1 point

Assume our original data point is $\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ and its projection $\frac{1}{9} \begin{bmatrix} 5 \\ 10 \\ 10 \end{bmatrix}$. What is the reconstruction error?

.47

✓ **Correct**
Well done!