

HW6 (due June 10 Saturday)

1- Define **INTEGER PROGRAMMING (IP)** problem as follows :

Given m equations :

$$\sum_{j=1,n} a_{ij} x_j = b_i, \quad i=1, \dots, m$$

in n variables x_j with integer coefficients a_{ij} and b_j , are there solutions with x_j equal to 1 or 0 for each j ? Prove that **IP** is an **NP-complete** problem.

2– Define **3-COLORING (3C)** problem as follows : Given an undirected graph can its vertices colored with three colors such that no two adjacent nodes have the same color. Prove that 3C is an **NP-complete** problem

(Hint : Use a polynomial reduction from **3SAT**)

3 - From the main text : 6.2.3, 6.2.4, 6.3.2