# C++ Template Lisp Interpreter

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# 1 Introduction to Template Patterns

Template expansion provides a pure untyped lambda calculus. All equality is extensional and the calculus supports higher-order functions (templates) with annotations at invocation, but not declaration, time. This section goes over the encoding of lambda calculus in the template system.

# 1.1 Encoding constants

Constants are simply structs, classes, or other types that don't take template parameters. It isn't a problem if they do take template parameters, of course; those will simply be specified later once the constant has propagated through the lambda expansion.

```
Listing 1
          examples/introduction/constants.hh
         // Defining a constant term
          struct foo {
            enum {value = 10};
         // Defining a global constant also_foo = foo
          typedef foo also_foo;
          // Defining two templated terms that act as constants
          template<class t> struct has_a_field {
            t field;
          };
      12
         template<int n> struct has_a_number {
            enum \{number = n\};
      15
      16
         };
```

# 1.2 First-order function encoding

The idea is to have structs that represent terms of the calculus. If they are templates, then they represent functions (which are also terms). For example:

```
Listing 2 examples/introduction/first-order-functions.cc

#include <iostream>
#include "constants.hh"

// Defining the identity function, where the result
// can be retrieved by specifying bar<T>::type
```

 $<sup>^{1}</sup>$ This makes it untyped. C++ templates also support function types using nested template syntax – see section 1.4.

```
template<class t> struct bar {
     typedef t type;
8
   }:
   // Defining a global constant identity_result = bar(also_foo)
   // This is analogous to the code 'let identity_result = bar also_foo'
   // in Haskell.
   typedef bar<also_foo>::type identity_result;
14
   int main () {
15
     std::cout << "foo::value</pre>
                   foo::value
                                              << std::endl <<
                  "also_foo::value
                                          = " <<
18
                   also_foo::value
19
                                              << std::endl <<
                  "identity_result::value = " <<
                   identity_result::value
21
                                              << std::endl;
22
   }
```

In practice there is some difficulty already. Notice the use of ::type to retrieve the value of a function application. This slot had to be assumed by the caller; it is analogous to JavaScript code like this:

```
Listing 3 examples/introduction/unfriendly-identity.js

// An unfriendly identity function.
var identity = function (x) {
    return {type: x};
};

// Invocations must now look like this:
var y = identity(x).type;
```

Having issues like this percolating through the design can be a real problem. Unless the slot is passed to every invocation site, invocations will be divergent and will create errors. This means that return values should be unified to a single slot, in this library (and the Boost MPL) called ::type.<sup>3</sup>

So we establish some conventions up front. Whenever you define a constant, it is used as-is without a contained typedef that we have to know about. This is OK because we shouldn't ever make assumptions about the members of types that are used as template parameters.

<sup>&</sup>lt;sup>2</sup>It also must be forwarded, which isn't possible in C++ to the best of my knowledge.

<sup>&</sup>lt;sup>3</sup>This may seem counter-intuitive, since the types here encode values in lambda-calculus. However, it does serve a mnemonic purpose later when value types are used as template parameters, and dependent value-type relations are established. Once this happens it becomes useful to explicitly distinguish between type template parameters and value template parameters.

# 1.3 Higher-order function encoding

Higher-order functions are possible by encoding slots for invocations.<sup>4</sup> We do this by declaring another template inside the first:

```
examples/introduction/higher-order-functions.cc
Listing 4
          #include <iostream>
          #include "constants.hh"
          // Defining the K combinator
          template<class t>
          struct k {
            template<class u>
            struct apply {
              typedef t type;
       10
            };
          };
       11
       12
          // Using that on two types
          typedef has_a_number<5> t1;
       14
          typedef has_a_number<6> t2;
          typedef k<t1>::apply<t2>::type should_be_t1;
       16
          int main () {
       18
            std::cout << "t1::number</pre>
                                                 = " << t1::number
                                                                               << std::endl <<
       19
                          "should_be_t1::number = " << should_be_t1::number << std::endl;</pre>
       20
       21
          }
```

In this example, k has a call slot apply that ultimately provides the value. So, for example,  $k < x > :: apply < y > :: type is equivalent to the more concise <math>k \times y$  in Haskell, or  $((k \times y))$  in Scheme.

At this point it should be clear that nothing is standardized here. Top-level functions are invoked directly, whereas returned functions use ::apply<x>. Type results from template invocations are accessed as ::type. One way to go about fixing it is to make a rule that a function gets encoded a bit less directly:

```
Listing 5 examples/introduction/indirect-functions-broken.cc

    // Encoding the K combinator uniformly, but with compile errors
    struct k {
        template<class t>
        struct apply {
            template<class u>
```

<sup>&</sup>lt;sup>4</sup>This is equivalent to the distinction between pure, extensional object-oriented programming and pure, extensional functional programming. In the latter, term juxtaposition (e.g. f x) constitutes invocation of the default slot, generally referred to as *apply*. In the former, slots are explicitly named, as would be the case in a language such as Java – thus juxtaposition has no meaning on its own.

```
6     struct apply {
7         typedef t type;
8      };
9     };
10 };
```

However, if you compile it you get an error stating that you can't define a nested struct with the same name as the outer one. The solution is to use an intermediate ::type dereference to wrap the inner ::apply<x>.

Listing 6 examples/introduction/indirect-functions.cc

```
#include <iostream>
   #include "constants.hh"
   // Encoding the K combinator uniformly
   struct k {
     template<class t>
     struct apply {
       struct type {
         template<class u>
         struct apply {
           typedef t type;
12
         };
       };
     };
14
   };
15
   typedef has_a_number<5> t1;
   typedef has_a_number<6> t2;
   typedef k::apply<t1>:::type::apply<t2>::type should_be_t1;
   int main () {
21
     std::cout << "t1::number</pre>
                                          = " << t1::number
                                                                       << std::endl <<
                   "should_be_t1::number = " << should_be_t1::number << std::endl;
23
24 }
```

At this point a nice pattern emerges. Whenever we apply a function to something, we get its ::type as well. So constants map to themselves, and function invocations are all of the form f::apply<...>::type.

### 1.4 Higher-order function type signatures

C++ lets you specify type signatures for higher-order templates. This can be useful to ensure that a function possesses at least a certain Church arity<sup>5</sup> or takes

<sup>&</sup>lt;sup>5</sup>I use this term to refer to the arity of the uncurried form of the function. For example, the Church arity of  $\lambda x.\lambda y.x$  is 2, since uncurrying yields  $\lambda(x,y).x$ .

at least so many arguments. It also provides some notational convenience at invocation-time.

Here is the Haskell function that we will model in C++ templates:

```
Listing 7 examples/introduction/apply-two-function.hs

apply_two :: ((a, a) -> b) -> a -> b

apply_two f x = f (x, x)
```

In template metaprogramming it isn't possible to express the constraints about values, but we can express constraints about arity and function status:

```
Listing 8 examples/introduction/apply-two-function.cc
       #include <iostream>
       #include "constants.hh"
         // Encoding the type signature as a template parameter specification
          struct apply_two {
            template<template<class arg1, class arg2> class f>
            struct apply {
              struct type {
                template<class x>
       9
                struct apply {
                  typedef f<x, x> type;
                };
      12
      13
              };
            };
      14
      15 };
         // An example value for f
         template<class x, class y>
          struct sample_f {
      19
            typedef x x_type;
            typedef y y_type;
      21
      22 }:
      23
          typedef has_a_number<10> t1;
      24
          typedef has_a_number<12> t2;
          typedef apply_two::apply<sample_f>::type::apply<t1>::type two_of_t1;
      26
         int main () {
      28
            std::cout << "t1::number</pre>
                                                     = " << t1::number << std::endl <<
      29
                         "two_of_t1::x_type::number = " << two_of_t1::x_type::number << std::endl <<
      30
                         "two_of_t1::y_type::number = " << two_of_t1::y_type::number << std::endl;
      32 }
```

The parameter definition < template < class arg1, class arg2> class f> is equivalent to the Haskell type signature f:: (a, b) -> c; none of the indi-

vidual types are specified, but the template must be invoked on two parameters or not invoked at all.<sup>6</sup> The other thing of note is that you can arbitrarily refine the left-hand side; for example:

This is equivalent to composer  $:: ((a \rightarrow b), (c \rightarrow d)) \rightarrow e$ . As far as I know there is no way to specify anything about the return type of a function using template syntax.

I'm not using template types in this project for a couple of reasons. First, declaring formals uses names (I'm actually not sure whether those names are considered reserved by C++, but I assume so). Second, it isn't possible to encode slot types, and all invocation in the lambda-calculus encoding is done with the ::apply slot.

### 1.5 Conditionals

Templates don't model conditionals *per se*. Rather, you can create conditionals by using pattern matching and explicit specialization. There are some weird limitations about this, but here is the basic idea:

```
examples/introduction/specialization.cc
Listing 9
          #include <iostream>
          #include "constants.hh"
          // General case
          template<class t>
          struct piecewise {
            typedef t type;
       8
          // When t = has_a_number<50>, do this instead
      10
          template<>
          struct piecewise<has_a_number<50>>> {
            typedef has_a_number<100> type;
      13
      14
          };
          typedef piecewise<has_a_number<3>>::type general;
          typedef piecewise<has_a_number<50>>>::type specialized;
      17
          int main () {
      19
            std::cout << "general::number</pre>
                                                = " << general::number
                                                                            << std::endl <<
```

<sup>&</sup>lt;sup>6</sup>Note that at this point I'm not referring to invocation using the ::apply convention established earlier. This invocation is just regular template expansion.

```
"specialized::number = " << specialized::number << std::endl;</pre>
```

### 1.5.1 Limitations of inner specialization

Because terminal (i.e. non-expanding) types are extensionally equivalent, pattern matching can be used to reliably specialize template expansions. The only case where this doesn't work is inside a class:

```
Listing 10 examples/introduction/inner-specialization-broken.cc
```

```
1 template<class t>
   struct container {
     template<class u>
     struct piecewise {
       typedef u type;
     };
     // Compiler complains about this:
     template<>
     struct piecewise<int> {
10
       typedef t type;
11
     };
12
13 };
   typedef container<int>::piecewise<int>::type foo;
```

The solution to this problem is to break the inner class outside of the outer one and uncurry its arguments:

```
Listing 11 examples/introduction/inner-specialization.cc
```

```
#include <iostream>
   #include "constants.hh"
   namespace inside_container {
     template<class t, class u>
     struct piecewise {
6
       typedef u type;
     };
     template<class t>
10
     struct piecewise<t, int> {
       typedef t type;
12
     };
13
14
   }
15
   template<class t>
```

```
struct container {
     template<class u>
18
     struct piecewise {
19
       typedef typename inside_container::piecewise<t, u>::type type;
21
     }:
   };
22
23
   typedef has_a_number<1> t1;
   typedef has_a_number<2> t2;
   typedef container<t1>::piecewise<t2>::type general;
   typedef container<t1>::piecewise<int>::type specialized;
27
   int main () {
29
     std::cout << "general::number</pre>
                                         = " << general::number
30
                                                                       << std::endl <<
                   "specialized::number = " << specialized::number << std::endl;</pre>
32
```

The namespace here isn't necessary, but it hides what normally gets hidden when you create an anonymous closure. Also notice that it must be declared before container due to C++'s forward-reference semantics.<sup>7</sup>

# 2 Metaprogramming in Value Space

Without using any particular encoding, this section provides a few examples of template metaprogramming in action. Each example has been factored down by preprocessor macros to show the structure of the code. Also, these examples are not necessarily representative of best practices, nor do they scale well.

# 2.1 Fibonacci numbers (explicit specialization)

This is some metaprogramming in value-space. Constants are evaluated and folded at compile-time, so the expression term below can be used to perform arithmetic evaluation. This example defines one general form of fibonacci, and two specific forms for an inductive process with two base cases. It also shows the lack of generality of piecewise definitions; while it is possible to specify a template for given values, implementing the classic compact definition of the function:

$$f(n) = \begin{cases} f(n-1) + f(n-2) & n \ge 2\\ n & n < 2 \end{cases}$$

is not possible through specialization without enumerating every value of n below or above 2. In this section we implement a more straightforward definition:

<sup>&</sup>lt;sup>7</sup>Despite this, template expansion is generally lazy in other ways.

$$f(n) = \begin{cases} 0 & n = 0\\ 1 & n = 1\\ f(n-1) + f(n-2) & \text{otherwise} \end{cases}$$

The compact definition is possible, however. The key is to encode that condition separately and specialize on a boolean parameter. That is implemented in section 2.2.

```
Listing 12
           examples/introduction/fibonacci.cc
           #include <iostream>
           #define letrec(name, params, defaults, expression) \
             template params \
             struct name defaults { \
               enum { value = expression }; \
           #define call(name, params...) (name<params>::value)
           letrec(fibonacci, <int n>, , call(fibonacci, n - 1) + call(fibonacci, n - 2))
           letrec(fibonacci, <>, <0>, 0)
           letrec(fibonacci, <>, <1>, 1)
       14
           int main () {
             std::cout << "fibonacci<10>::value = " << fibonacci<10>::value << std::endl;</pre>
       16
       17
```

### 2.2 Fibonacci numbers (piecewise definition)

As mentioned in section 2.1, it is possible to encode the Fibonacci function using a general conditional instead of explicitly specializing the two base values of 0 and 1. This example doesn't motivate its full utility (better would be a densely piecewise function such as the absolute value), but you can easily extrapolate from the design pattern.

The first step is to isolate the cases. For the piecewise Fibonacci function:

$$f(n) = \begin{cases} n & n < 2\\ f(n-1) + f(n-2) & n \ge 2 \end{cases}$$

A boolean contains enough information to encode which branch should be taken. I'll use n < 2 as the predicate, so a value of true should result in n while a value of false should result in f(n-1) + f(n-2).

Here is the obvious way to go about it, though it doesn't work because of mutual dependencies in the definitions:

```
Listing 13 examples/introduction/fibonacci-piecewise-broken.cc
        1 template <bool n_lt_2, int n>
          struct fibonacci_case {
             enum { value = fibonacci<n - 1>::value + fibonacci<n - 2>::value };
          };
        6 template <int n>
           struct fibonacci_case <true, n> {
             enum { value = n };
       10
       11 template <int n>
       12 struct fibonacci {
             enum { value = fibonacci_case<(n < 2), n>::value };
       14 };
             C++ needs to know about template types before you hit them. Because
           there isn't a way to forward-define templates, we have to get a little bit more
           creative:
Listing 14 examples/introduction/fibonacci-piecewise.cc
          #include <iostream>
       2
        3 template <class f, bool n_lt_2, int n>
          struct fibonacci_case {
             enum { value = f::template recursive<n - 1>::value +
                            f::template recursive<n - 2>::value };
          };
        9
          template <class f, int n>
       struct fibonacci_case <f, true, n> {
             enum { value = n };
       11
          };
       12
       13
          struct fibonacci_piecewise {
             template <int n>
       15
             struct recursive {
               enum { value = fibonacci_case<fibonacci_piecewise, (n < 2), n>::value };
       17
             };
       18
       19 };
       20
       21 template <int n>
          struct fibonacci {
             enum { value = fibonacci_piecewise::template recursive<n>::value };
       24 };
```

25

```
int main () {
   std::cout << "fibonacci<10>::value = " << fibonacci<10>::value << std::endl;
}</pre>
```

Note the wrapping of fibonacci\_piecewise::recursive. This is necessary because within the scope of a template, the name of the templated construct refers to the specialized form, not the template itself. For example:

Listing 15 examples/introduction/self-reference-broken.cc
 template <int n>
 struct foo {
 typedef foo bar;
 };
 typedef foo<10>::bar should\_be\_a\_template;

typedef should\_be\_a\_template<10> problem;

In this example, should\_be\_a\_template isn't a template at all; it's the expanded form of foo, which has already been specialized to foo<10>. The compiler complains when typedefing problem because we are trying to expand something that isn't a template.

The solution is to wrap the template inside a non-template outer struct, as the working Fibonacci example demonstrates. This enables you to refer unambiguously to the outer struct and then explicitly dereference the inner template, which will not be specialized at that point.

### 2.3 Linked list

This is a simple model of a data structure in value-space. For scalability it would be better to use types for the head and tail, but for simplicity the example is restricted to using values.

The q function in this example works around a limitation of the preprocessor. Section 3.1 covers this in more detail.

function(cons, q(class X, class Y), car = X::value, cdr = Y::value);

# 2.4 Church-encoded lists, map, and filter

This is a more involved example that uses curried templates and a Church encoding. Note the transition between value-space and type-space achieved by using select. select effectively serves as a map from bool to either head or tail.

```
Listing 17
          examples/introduction/church-lists.cc
           #include <iostream>
          #define fn(args...)
                                      template <args> struct
           #define lambda(args...)
                                      template <args> struct apply
           #define lift(name, xs...) template <xs> class name
           #define call(v, xs...)
                                      typename v::template apply<xs>::type
           #define let(var, value...) private: typedef value var
           #define ret(value...)
                                      public: typedef value type
           #define val(e)
                                      public: struct type { enum { value = e }; }
       12
           struct head {lambda(class h, class t) {ret(h);};};
           struct tail {lambda(class h, class t) {ret(t);};};
       14
       15
          namespace _select {
       16
             lambda(bool b)
                              {ret(head);};
             lambda() <false> {ret(tail);};
       18
       19
           struct select {
       21
             lambda(class t) {ret(call(_select, t::type::value));};
       23
       24
           fn(class h, class t) cons {
             lambda(class f) {
       26
               ret(call(f, h, t));
       27
             };
       28
```

```
};
29
30
   struct nil {
31
     typedef int type;
33
34
   struct map {
35
     lambda(class f, class cell) {
        let(mapped_head, call(f, call(cell, head)));
37
       let(mapped_tail, call(map, f, call(cell, tail)));
38
       ret(cons<mapped_head, mapped_tail>);
39
40
41
     lambda(class f) <f, nil> {
42
       ret(nil);
43
44
     };
45
   };
46
   struct filter {
47
     lambda(class f, class cell) {
48
        let(h,
                            call(cell, head));
49
        let(filtered_tail, call(filter, f, call(cell, tail)));
50
       let(choices,
                            cons<cons<h, filtered_tail>, filtered_tail>);
51
        let(selector,
                            call(select, call(f, h)));
52
53
       ret(call(choices, selector));
54
     };
55
56
     lambda(class f) <f, nil> {
57
       ret(nil);
58
59
     };
   };
60
61
   fn(int n) int_wrap {
     val(n);
63
   };
64
65
   fn(class x) plus {
     lambda(class y) {
67
       val(x::type::value + y::type::value);
     };
69
   };
70
71
   fn(int n) is_divisible_by {
     lambda(class x) {
73
       val(x::type::value % n == 0);
```

```
};
   };
77
   int main () {
     typedef cons<int_wrap<5>, cons<int_wrap<6>, nil>>
                                                                  the_list:
     typedef plus<int_wrap<6>>
                                                                   the_function;
80
     typedef is_divisible_by<3>
                                                                   the_criterion;
81
      typedef filter::apply<the_criterion, the_list>::type
                                                                  the_short_list;
     typedef map::apply<the_function, the_short_list>::type the_result;
83
     typedef the_result::apply<head>
                                                                   should_be_seven;
84
85
     std::cout << "head(map(x -> x + 6, filter(x % 3 == 0, list(5, 6)))) = " << stable >= 0, list(5, 6)))
                    should_be_seven::type::value << std::endl;</pre>
87
88
   }
```

The use of cons to represent the possible outcomes of a decisional isn't a new idea. It's key to the use of select, which will return either head or tail. We then apply the cons cell to that outcome to obtain the conditional result. The only problem with this approach is that both possibilities end up getting evaluated regardless of the condition. So in general, church-encodings of booleans and other conditionals has the caveat that it may cause infinite recursion. Most conditionals should probably be implemented using specialization (see section 2.2) to avoid this problem.

# 3 Preprocessor Definitions

The goal of this section is to implement a layer of abstraction over the base template constructs. Roughly, the operations are:

- 1. Defining a global constant
- 2. Defining a local variable
- 3. Applying a function to an expression
- 4. Returning a value from a function
- 5. Defining a named function

Each of these operations has a standard form. The definition of a shorthand for each is given in the following subsections.

<sup>&</sup>lt;sup>8</sup>There are two for item 3; one form is used outside of a function body and the other is used inside. The difference has to do with disambiguating template expansions and is covered in section 3.4. Also a great article about the role of typename in C++, its uses, and its limitations: http://pages.cs.wisc.edu/~driscoll/typename.html.

# 3.1 Preprocessor limitations

One notable limitation of the C preprocessor when working with templates is that it doesn't treat < and > as nested parentheticals. This has the unfortunate effect of splitting on commas that separate template parameters, e.g.:

```
#define f(x) ...

template<class x, class y>
struct foo {...};

f(foo<bar, bif>); // Error here; too many arguments
```

In value-space you can deal with this by explicitly parenthesizing expressions, but parentheses aren't a transparent construct in type-space. The way I'm getting around this for now is to make macros variadic and always put any template invocations at the end:

```
#define f(x...) typedef x bar;
```

This will preserve the commas in the original expression, although its use may be limited to the GNU preprocessor.<sup>10</sup>

### 3.2 Global constants

A global constant is just a standalone struct. To encode this, we create the def() macro, which basically just expands out to struct. However, it is a bit clearer than its expansion, especially in the context of defining functions and values.

This module, like all of the preprocessor utilities, can be enabled and disabled multiple times during preprocessing. This prevents the macros from interfering with regular code, which ultimately enables clearer macro naming. The mechanism that governs enabling and disabling is the LISP\_PREPROCESSOR\_DEFINE preprocessor variable. If defined, then the header is run in "definition mode" and will create macros. Otherwise it will undefine the macros. You can see whether a macro is defined as well; each header file defines a macro called LISP\_PREPROCESSOR\_X\_ENABLED, where X is the upper-case name of the header file. This macro is undefined when the header is disabled.

Note that you shouldn't ever include this header file directly. See section 3.8 for a simple interface to enable and disable preprocessor macros.

### Listing 18 preprocessor/def.hh

<sup>&</sup>lt;sup>9</sup>It wouldn't be possible for it to do the right thing here anyway, since the preprocessor sees code before types have been defined. However, template punctuation was an unfortunate choice considering its ambiguity with relational operators, and the fact that relational operators are always ungrouped while template parameter delimiters are always grouped.

<sup>&</sup>lt;sup>10</sup>A more standard way to do this is to use the \_\_VA\_ARGS\_\_ builtin and an anonymous ellipsis.

```
#ifdef LISP_PREPROCESSOR_DEFINE
# define LISP_PREPROCESSOR_DEF_ENABLED
# define def(name) struct name
#else
# undef LISP_PREPROCESSOR_DEF_ENABLED
# undef def
# endif
```

### 3.3 Local variables

Within a struct, local variables are prefixed with private.

```
Listing 19 preprocessor/let.hh
```

```
#ifdef LISP_PREPROCESSOR_DEFINE
define LISP_PREPROCESSOR_LET_ENABLED
# define let(name, value...) private: typedef value name
define local_def(name) private: struct name
# define local_def(name)
# undef LISP_PREPROCESSOR_LET_ENABLED
# undef let
# undef local_def
# endif
```

# 3.4 Function application

It is assumed that function application involves dependent types. In that case, the default call(x, ...) works fine. If, however, the function call's types are already resolved and do not depend on template variables, then you will probably want to use  $call_static$  instead.

```
Listing 20 preprocessor/call.hh
```

```
#ifdef LISP_PREPROCESSOR_DEFINE
# define LISP_PREPROCESSOR_CALL_ENABLED
# define call(lhs, rhs...) typename lhs::template apply<rhs>::type
# define call_static(lhs, rhs...) lhs::apply<rhs>::type
# else
# undef LISP_PREPROCESSOR_CALL_ENABLED
# undef call
# undef call
# undef call_static
# endif
```

<sup>&</sup>lt;sup>11</sup>In the C++ sense, not the type-theoretic sense. C++ dependent types are the transitive closure of template variables through the expansion graph.

# 3.5 Returning a value

It is straightforward to return a named value. This always takes the form typedef x type, where x is the value to be returned. For simplicity's sake, I'm going to assume that whatever value should be returned has a name to preserve the uniformity of the return expansion. Note that it is prefixed with public to override any previous local variables that were defined.

# Listing 21 preprocessor/ret.hh 1 #ifdef LISP\_PREPROCESSOR\_DEFINE 2 # define LISP\_PREPROCESSOR\_RET\_ENABLED 3 # define ret(value...) public: typedef value type 4 #else 5 # undef LISP\_PREPROCESSOR\_RET\_ENABLED 6 # undef ret 7 #endif

# 3.6 Defining a named function

To remain in the mindset of the model C++ uses for template specialization, defining a named function is a two-step process. First, you define the outer struct using def() (see section 3.2). Inside that you can specify the cases using the when() macro.

```
Listing 22 preprocessor/when.hh

#ifdef LISP_PREPROCESSOR_DEFINE

# define LISP_PREPROCESSOR_WHEN_ENABLED

# define when(parameters...) template <parameters> struct apply

#else

# undef LISP_PREPROCESSOR_WHEN_ENABLED

# undef when

#endif
```

### 3.7 Defining and returning closures

It is fairly simple to return a closure. The idea is that you create a local named function and then return that by name, so to implement the K combinator, for example, you would do something like this:

```
def(k) {
   when(class x) {
    local_def(inner) {
     when(class y) {
       ret(x);
    };
}
```

```
};
    ret(inner);
};
```

However, that's a bulky representation given that no explicit specialization is occurring. To inline the function definitions, this form can be used instead:

### Listing 23 preprocessor/defun.hh

```
#ifdef LISP_PREPROCESSOR_DEFINE
# define LISP_PREPROCESSOR_DEFUN_ENABLED
# define defun(name, params...) def(name) {}; \
template<params...> struct name::apply
# define local_defun(name, params...) local_def(name) {}; \
template<params...> struct name::apply
# else
# undef LISP_PREPROCESSOR_DEFUN_ENABLED
# undef defun
# undef local_defun
# endif
```

# 3.8 Preprocessor interface

Rather than using the files above, it's better to include these header files to enable or disable the preprocessor macros.

```
Listing 24 preprocessor-enable.hh
```

```
#ifndef LISP_PREPROCESSOR_DEFINE
#define LISP_PREPROCESSOR_DEFINE
#include "preprocessor/all.hh"
#endif
```

Listing 25 preprocessor-disable.hh

```
#ifdef LISP_PREPROCESSOR_DEFINE
#undef LISP_PREPROCESSOR_DEFINE
#include "preprocessor/all.hh"
#endif
```

This file is used internally to include all of the modules listed in the previous subsections:

```
Listing 26 preprocessor/all.hh
```

```
#include "preprocessor/def.hh"
#include "preprocessor/let.hh"
#include "preprocessor/call.hh"
```

```
#include "preprocessor/ret.hh"
#include "preprocessor/when.hh"
#include "preprocessor/defun.hh"
```

### 3.9 Core interface

This header contains some definitions that abstract away details of writing modules. It uses the macro-expanded #includes used throughout the Boost library source code, which indicates that the header file is intended to be included multiple times.

```
Listing 27 core.hh

1 #ifndef CORE_HH
2 #define CORE_HH
3
4 #define LISP_BEGIN_MODULE "preprocessor/module-begin.hh"
5 #define LISP_END_MODULE "preprocessor/module-end.hh"
6
7 #endif
```

Below are the two auxiliary files referenced above. Inside modules the preprocessor macros are enabled, and outside they are disabled. The usage generally looks like this:

```
#include LISP_BEGIN_MODULE()
    // module code
    #include LISP_END_MODULE()

Listing 28 preprocessor/module-begin.hh
    #include "preprocessor-enable.hh"
    namespace lisp {

Listing 29 preprocessor/module-end.hh
    }
    #include "preprocessor-disable.hh"
```

# 4 $\beta$ -Rewrite Representation

This section outlines the conversion process from a simple  $\beta$ -rewrite calculus to template metaprogramming constructs. This rewrite system then is combined with an eval function to form the basis for the metacircular interpreter defined in section ??.

### 4.1 List construct

The  $\beta$  rewrite system assumes the existence of two data types. One is the *term*, which corresponds to a value that might get replaced, and the other is a cons cell of two values. The first step to modeling these things is defining a cons cell, which for this system is Church-encoded:

```
Listing 30
           core/cons.hh
           #ifndef CORE_CONS_HH
           #define CORE_CONS_HH
           #include "core.hh"
           #include LISP_BEGIN_CORE_MODULE()
           defun(cons, class h, class t) {
             local_defun(closure, class f) {
               ret(call(f, h, t));
             };
             ret(closure);
       10
           };
       11
           defun(head, class h, class t) {ret(h);};
           defun(tail, class h, class t) {ret(t);};
       14
           def(nil) {};
       16
           #include LISP_END_CORE_MODULE()
       17
       18
           #endif
Listing 31
           tests/core/cons.cc
           #include "unit-test.hh"
           deftest(cons_instantiation) {
             let(foo, call(cons, n<5>, n<6>));
             let(five, call(head, foo));
             let(six, call(tail, foo));
        8 };
```

### 5 Resources

This section contains extra files that are helpful for running the examples. Note that this library requires your version of gcc to support a fairly recent C++0x draft, as specified by -std=gnu++0x.

# 5.1 Makefile for introduction examples

This makefile will build all of the examples in section 1. It is available in the source distribution as src/examples/introduction/makefile, and should be run from inside src/examples/introduction. Alternatively, all of the examples can be compiled by using the makefile in src/examples.

```
examples/introduction/makefile
Listing 32
           WORKING = first-order-functions higher-order-functions indirect-functions \
                      apply-two-function specialization inner-specialization fibonacci \
        2
                      fibonacci-piecewise linked-list church-lists
           BROKEN
                    = indirect-functions-broken inner-specialization-broken \
                      fibonacci-piecewise-broken self-reference-broken
        8
           BASE_DIR = .../
        9
                    = g++
           CC\_OPTS = -g - Wall - std = gnu + +0x - I\$(BASE\_DIR)
       10
           all: $(WORKING)
           broken: $(BROKEN)
       14
           .PHONY: clean
           clean:
       16
                   rm -f $(WORKING) $(BROKEN)
       18
       19
           %: %.cc
       20
                   $(CC) $(CC_OPTS) $< -o $@ || true
```

### 5.2 Makefile for tests

This makefile builds the unit and integration tests for the Lisp implementation. The tests should fail at compile-time if an assertion is not satisfied. This file should be run from src/tests.