

Q 2b .

Gini (Rainy)

$$= 1 - \left(\frac{4}{10}\right)^2 - \left(\frac{6}{10}\right)^2 = 0.48$$

$$\begin{aligned} \text{Gini (Windy = P)} &= 1 - \left(\frac{4}{7}\right)^2 - \left(\frac{3}{7}\right)^2 \\ &= 0.4897 \end{aligned}$$

$$\text{Gini (A Windy = F)} = 1 - \left(\frac{0}{3}\right)^2 - \left(\frac{3}{3}\right)^2 = 0$$

$$\begin{aligned} \text{Gini Windy (D)} &= \left(\frac{7}{10}\right) \text{Gini (Windy = P)} + \\ &\quad \frac{3}{10} (\text{Gini (Windy = F)}) \end{aligned}$$

$$= \frac{7}{10} \times 0.4897 + \frac{3}{10} \times 0$$

$$= 0.3427$$

$$\Delta \text{ gini (Windy)} = \text{Gini (Rainy)} - \text{Gini Windy (D)}$$

$$= 0.48 - 0.3427$$

$$= 0.1373$$

$$\begin{aligned} \text{Gini (cloudy=T)} &= 1 - \left(\frac{3}{4}\right)^2 - \left(\frac{1}{4}\right)^2 \\ &= 0.375 \end{aligned}$$

$$\begin{aligned} \text{Gini (cloudy=F)} &= 1 - \left(\frac{1}{2}\right)^2 - \left(\frac{5}{6}\right)^2 \\ &= 0.277 \end{aligned}$$

$$\begin{aligned} \text{Gini cloudy (D)} &= \frac{4}{10} (\text{Gini (cloudy=T)}) + \\ &\quad \frac{6}{10} (\text{Gini (cloudy=F)}) \\ &= 0.4 \times 0.375 + 0.6 \times 0.277 \\ &= 0.3162 \end{aligned}$$

$$\begin{aligned} \Delta \text{Gini (cloudy)} &= \text{Gini (Rainy)} - \text{Gini (cloudy (D))} \\ &= 0.48 - 0.3162 \\ &= 0.1638 \end{aligned}$$

Gini Cloudy (D) > Gini Windy (D) so
cloudy would be the splitting attribute