

# Combinational Logic II

## *Boolean Equations*

### Order of Operations

1) \_\_\_\_\_ 2) \_\_\_\_\_ 3) \_\_\_\_\_

### Circuit Examples

#### *Bubble*

A bubble denotes inversion as shown below

#### *Logic Circuits*

Draw the circuit for:  $A' + (A' \cdot B) + C$

Draw the circuit for:  $(A' + (A' \cdot B)) \oplus (C+A) = D$

Draw the logic circuit for:  $D = ABC + A'(B+C) + A(B') + C$

Draw the logic circuit for:  $D = (A' + B + C) + A(B + C) + B(C') + AC$

What boolean equation does this logic circuit represent?

## Logical Completeness

You can create a circuit for ANY truth table with only \_\_\_\_\_

In addition, you can complete any truth table with only \_\_\_\_\_

You can also complete any truth table with only \_\_\_\_\_

## XOR Gate

| Complete the truth table: |   |       |
|---------------------------|---|-------|
| A                         | B | Out = |
| 0                         | 0 |       |
| 0                         | 1 |       |
| 1                         | 0 |       |
| 1                         | 1 |       |

There are 2 ways for the output of a 2-input xor gate to be 1:

If:

1 - A is \_\_\_\_\_ AND B is \_\_\_\_\_ OR 2 - A is \_\_\_\_\_ AND B is \_\_\_\_\_

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### Schematics

Draw a logic circuit that corresponds with the truth table of an xor gate

## Sum of Products (SOP)

How do we get from a truth table to a logic expression?

### Procedure

- 1) Identify rows with an output equal to \_\_\_\_\_
- 2) Write product terms - AND the inputs together where the \_\_\_ inputs are \_\_\_\_\_
- 3) \_\_\_ the product terms together to form a \_\_\_\_\_

## Examples

| Write the SOP for Out |   |   |     |
|-----------------------|---|---|-----|
| S                     | A | B | Out |
| 0                     | 0 | 0 | 0   |
| 0                     | 0 | 1 | 0   |
| 0                     | 1 | 0 | 1   |
| 0                     | 1 | 1 | 1   |
| 1                     | 0 | 0 | 0   |
| 1                     | 0 | 1 | 1   |
| 1                     | 1 | 0 | 0   |
| 1                     | 1 | 1 | 1   |

Product terms (aka \_\_\_\_\_):  
 \_\_\_\_\_  
 \_\_\_\_\_

Sum of products:  
 \_\_\_\_\_

This is the truth table of a:  
 \_\_\_\_\_

| Write the SOP for Out |   |   |     |
|-----------------------|---|---|-----|
| S                     | A | B | Out |
| 0                     | 0 | 0 | 1   |
| 0                     | 0 | 1 | 0   |
| 0                     | 1 | 0 | 0   |
| 0                     | 1 | 1 | 1   |
| 1                     | 0 | 0 | 1   |
| 1                     | 0 | 1 | 0   |
| 1                     | 1 | 0 | 0   |
| 1                     | 1 | 1 | 1   |

Product terms:  
 \_\_\_\_\_  
 \_\_\_\_\_

Sum of products:  
 \_\_\_\_\_  
 \_\_\_\_\_

**Product of Sums (POS)**

How do we get from a truth table to a logic expression?

**Procedure**

- 1) Identify rows with an output equal to \_\_\_\_\_
- 2) Write sum terms - OR the inputs together where the \_\_\_\_\_ inputs are \_\_\_\_\_
- 3) \_\_\_\_\_ the sum terms together to form a \_\_\_\_\_

## Examples

Write the POS for Out

| S | A | B | Out |
|---|---|---|-----|
| 0 | 0 | 0 | 0   |
| 0 | 0 | 1 | 0   |
| 0 | 1 | 0 | 1   |
| 0 | 1 | 1 | 1   |
| 1 | 0 | 0 | 0   |
| 1 | 0 | 1 | 1   |
| 1 | 1 | 0 | 0   |
| 1 | 1 | 1 | 1   |

Sum terms (aka \_\_\_\_\_):

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Product of sums:

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Write the POS for Out

| S | A | B | Out |
|---|---|---|-----|
| 0 | 0 | 0 | 1   |
| 0 | 0 | 1 | 0   |
| 0 | 1 | 0 | 0   |
| 0 | 1 | 1 | 1   |
| 1 | 0 | 0 | 1   |
| 1 | 0 | 1 | 0   |
| 1 | 1 | 0 | 0   |
| 1 | 1 | 1 | 1   |

Sum terms:

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Product of sums:

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PLA: P \_\_\_\_\_ L \_\_\_\_\_ A \_\_\_\_\_

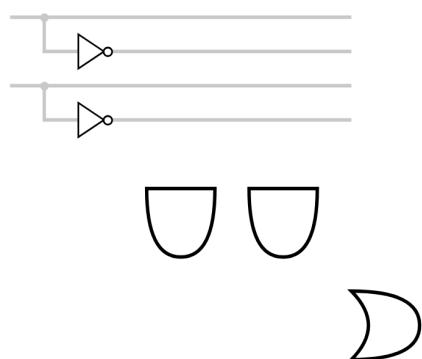
A structured logic element that takes a set of \_\_\_\_\_

and \_\_\_\_\_ of logic.

Draw the basic form of a PLA

**Example**

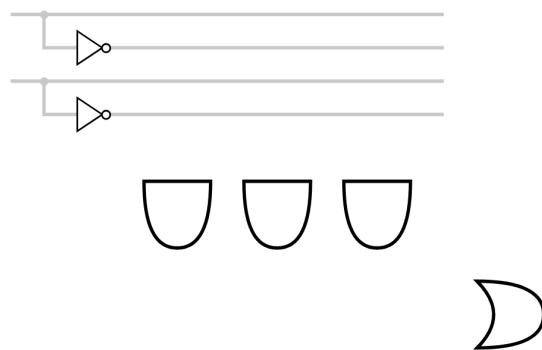
Implement the logic for an XOR gate as a PLA



**Example**

Implement this truth table as a PLA

| A | B | S | C |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |



This PLA implements logic as a \_\_\_\_\_

**Examples**

Given: Truth table

(fill in values for D in the truth table)

Solve: 1) Draw the circuit 2) Write the corresponding Boolean expression for the output



| A | B | C | D |
|---|---|---|---|
| 0 | 0 | 0 |   |
| 0 | 0 | 1 |   |
| 0 | 1 | 0 |   |
| 0 | 1 | 1 |   |
| 1 | 0 | 0 |   |
| 1 | 0 | 1 |   |
| 1 | 1 | 0 |   |
| 1 | 1 | 1 |   |

Given: Truth table  
(fill in values for D and E in the truth table)

Solve: 1) Draw the circuit 2) Write the corresponding Boolean expressions for the outputs



| A | B | C | D | E |
|---|---|---|---|---|
| 0 | 0 | 0 |   |   |
| 0 | 0 | 1 |   |   |
| 0 | 1 | 0 |   |   |
| 0 | 1 | 1 |   |   |
| 1 | 0 | 0 |   |   |
| 1 | 0 | 1 |   |   |
| 1 | 1 | 0 |   |   |
| 1 | 1 | 1 |   |   |



Given: Circuit  
(finish drawing this circuit)

Solve: 1) Complete the truth table 2) Write the corresponding Boolean expression for the output



| A | B | C | D |
|---|---|---|---|
| 0 | 0 | 0 |   |
| 0 | 0 | 1 |   |
| 0 | 1 | 0 |   |
| 0 | 1 | 1 |   |
| 1 | 0 | 0 |   |
| 1 | 0 | 1 |   |
| 1 | 1 | 0 |   |
| 1 | 1 | 1 |   |



Given: Circuit  
(finish drawing this circuit)

Solve: 1) Complete the truth table 2) Write the corresponding Boolean expression for the outputs



| A | B | C | D | E |
|---|---|---|---|---|
| 0 | 0 | 0 |   |   |
| 0 | 0 | 1 |   |   |
| 0 | 1 | 0 |   |   |
| 0 | 1 | 1 |   |   |
| 1 | 0 | 0 |   |   |
| 1 | 0 | 1 |   |   |
| 1 | 1 | 0 |   |   |
| 1 | 1 | 1 |   |   |



Given: Truth table  
(fill in values for D in the truth table)

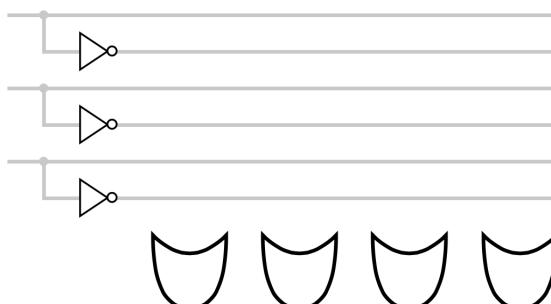
Solve: 1) Draw the circuit 2) Write the corresponding Boolean expression for the output



| A | B | C | D |
|---|---|---|---|
| 0 | 0 | 0 |   |
| 0 | 0 | 1 |   |
| 0 | 1 | 0 |   |
| 0 | 1 | 1 |   |
| 1 | 0 | 0 |   |
| 1 | 0 | 1 |   |
| 1 | 1 | 0 |   |
| 1 | 1 | 1 |   |

Given: Truth table  
(fill in values for D and E in the truth table)

Solve: 1) Draw the circuit 2) Write the corresponding Boolean expressions for the outputs

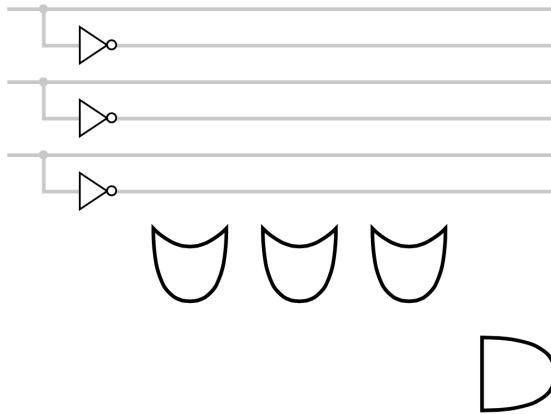


| A | B | C | D | E |
|---|---|---|---|---|
| 0 | 0 | 0 |   |   |
| 0 | 0 | 1 |   |   |
| 0 | 1 | 0 |   |   |
| 0 | 1 | 1 |   |   |
| 1 | 0 | 0 |   |   |
| 1 | 0 | 1 |   |   |
| 1 | 1 | 0 |   |   |
| 1 | 1 | 1 |   |   |

D  
D

Given: Circuit  
(finish drawing this circuit)

Solve: 1) Complete the truth table 2) Write the corresponding Boolean expression for the output



| A | B | C | D |
|---|---|---|---|
| 0 | 0 | 0 |   |
| 0 | 0 | 1 |   |
| 0 | 1 | 0 |   |
| 0 | 1 | 1 |   |
| 1 | 0 | 0 |   |
| 1 | 0 | 1 |   |
| 1 | 1 | 0 |   |
| 1 | 1 | 1 |   |

Given: Circuit  
(finish drawing this circuit)

Solve: 1) Complete the truth table 2) Write the corresponding Boolean expressions for the outputs



D  
D  
D

| A | B | C | D | E |
|---|---|---|---|---|
| 0 | 0 | 0 |   |   |
| 0 | 0 | 1 |   |   |
| 0 | 1 | 0 |   |   |
| 0 | 1 | 1 |   |   |
| 1 | 0 | 0 |   |   |
| 1 | 0 | 1 |   |   |
| 1 | 1 | 0 |   |   |
| 1 | 1 | 1 |   |   |