

## Crafting a Compiler

# 4.7

7. A grammar for infix expressions follows:

```

1 Start → E $
2 E    → T plus E
3      | T
4 T    → T times F
5      | F
6 F    → ( E )
7      | num

```

(a) Show the leftmost derivation of the following string.

num plus num times num plus num \$

(b) Show the rightmost derivation of the following string.

num times num plus num times num \$

(c) Describe how this grammar structures expressions, in terms of the precedence and left- or right- associativity of operators.

a)

Start

E\$

T plus E \$

F plus E \$

(E) plus E \$

num plus E \$

num plus T plus E \$

num plus T times F plus E \$

num plus F times F plus E \$

num plus (E) times F plus E \$

num plus num times F plus E \$

num plus num times (E) plus E \$

num plus num times num plus E \$

num plus num times num plus T \$

num plus num times num plus F \$

num plus num times num plus (E) \$

num plus num times num plus num \$

b)

Start

E\$

T plus E \$

T plus T \$

T plus T times F\$

T plus T times (E)\$

T plus T times num\$

T plus F times num \$

T plus (E) times num \$

T plus num times num \$

T times F plus num times num \$

T times (E) plus num times num \$

T times num plus num times num \$

F times num plus num times num \$

(E) times num plus num times num \$

num times num plus num times num \$

c)

The grammar is unambiguous because a left derivation matched the right derivation.

Dragon

4.2.1 a, b, c

**Exercise 4.2.1:** Consider the context-free grammar:

$$S \rightarrow SS + \mid SS * \mid a$$

and the string  $aa + a*$ .

- a) Give a leftmost derivation for the string.
- b) Give a rightmost derivation for the string.
- c) Give a parse tree for the string.
- ! d) Is the grammar ambiguous or unambiguous? Justify your answer.
- ! e) Describe the language generated by this grammar.

a)

S  
SS\*  
SS+S\*  
aS+S\*  
aa+S\*  
aa+a\*

b)

S  
SS\*  
S a\*  
SS + a\*  
Sa +a\*  
aa+a\*

c)

