GLOSSARY FOR ISYE 6501 INTRODUCTION TO ANALYTICS MODELING

(Organized alphabetically; for topic-by-topic glossary, see other file)

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1-norm Similar to rectilinear distance; measures the sum of the lengths of each

dimension of a vector from the origin. If $z=(z_1,z_2,\dots,z_m)$ is a vector

in an m-dimensional space, then its 1-norm is

 $\sqrt[1]{|z_1|^1 + |z_2|^1 + \dots + |z_m|^1} = |z_1| + |z_2| + \dots + |z| = \sum_{i=1}^m |z_i|.$

2-norm Similar to Euclidian distance; measures the straight-line length of a

vector from the origin. If $z=(z_1,z_2,...,z_m)$ is a vector in an mdimensional space, then its 2-norm is $\sqrt[2]{(z_1)^2+(z_2)^2+\cdots+(z_m)^2}=$

 $\sqrt[2]{\sum_{i=1}^m (z_i)^2}.$

A/B testing Test of two alternatives to see if either one leads to better outcomes.

Accuracy Fraction of data points correctly classified by a model; equal to

 $\frac{TP+TN}{TP+FP+TN+FN}.$

Action In ARENA, something that is done to an entity.

Additive seasonality Seasonal effect that is added to a baseline value (for example, "the

temperature in June is 10 degrees above the annual baseline").

Adjusted R-squared/Adjusted

 R^2

Variant of R² that encourages simpler models by penalizing the use of

too many variables.

AIC Akaike information criterion

Akaike information criterion

(AIC)

Model selection technique that trades off between model fit and model complexity. When comparing models, the model with lower AIC

is preferred. Generally penalizes complexity less than BIC.

Algorithm Step-by-step procedure designed to carry out a task.

Analysis of Variance/ANOVA Statistical method for dividing the variation in observations among

different sources.

Approximate dynamic

program

Dynamic programming model where the value functions are

approximated.

Arc Connection between two nodes/vertices in a network. In a network

model, there is a variable for each arc, equal to the amount of flow on the arc, and (optionally) a capacity constraint on the arc's flow. Also

called an edge.

Area under curve/AUC Area under the ROC curve; an estimate of the classification model's

accuracy. Also called concordance index.

ARIMA Autoregressive integrated moving average.

Arrival rate Expected number of arrivals of people, things, etc. per unit time -- for

example, the expected number of truck deliveries per hour to a

warehouse.

Assignment problem Network optimization model with two sets of nodes, that finds the

best way to assign each node in one set to each node in the other set.

Attribute A characteristic or measurement – for example, a person's height or

the color of a car. Generally interchangeable with "feature", and often with "covariate" or "predictor". In the standard tabular format, a

column of data.

Autoregression Regression technique using past values of time series data as

predictors of future values.

Autoregressive integrated moving average (ARIMA)

Time series model that uses differences between observations when

data is nonstationary. Also called Box-Jenkins.

Backward elimination Variable selection process that starts with all variables and then

iteratively removes the least-immediately-relevant variables from the

model.

Balanced design Set of combinations of factor values across multiple factors, that has

the same number of runs for all combinations of levels of one or more

factors.

Balking An entity arrives to the queue, sees the size of the line (or some other

attribute), and decides to leave the system.

Bayes' theorem/Bayes' rule Fundamental rule of conditional probability: $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$.

Bayesian Information criterion

(BIC)

Model selection technique that trades off model fit and model

complexity. When comparing models, the model with lower BIC is preferred. Generally penalizes complexity more than AIC.

Bayesian regression Regression model that incorporates estimates of how coefficients and

error are distributed.

Bellman's equation Equation used in dynamic programming that ensures optimality of a

solution.

Bernoulli distribution Discrete probability distribution where the outcome is binary, either 0

or 1. Often, 1 represents success and 0 represents failure. The

probability of the outcome being 1 is p and the probability of outcome

being 0 is q = 1 - p, where p is between 0 and 1.

Bias Systematic difference between a true parameter of a population and

its estimate.

BIC Bayesian information criterion

Binary data Data that can take only two different values (true/false, 0/1,

black/white, on/off, etc.).

Binary integer program Integer program where all variables are binary variables.

Binary variable Variable that can take just two values: 0 and 1.

Binomial distribution Discrete probability distribution for the exact number of successes, k,

out of a total of n iid Bernoulli trials, each with probability p:

 $\Pr(k) = \binom{n}{k} p^k (1-p)^{n-k}.$

Blocking Factor introduced to an experimental design that interacts with the

effect of the factors to be studied. The effect of the factors is studied

within the same level (block) of the blocking factor.

Box and whisker plot Graphical representation data showing the middle range of data (the

"box"), reasonable ranges of variability ("whiskers"), and points

(possible outliers) outside those ranges.

Box-Cox transformation Transformation of a non-normally-distributed response to a normal

distribution.

Branching Splitting a set of data into two or more subsets, to each be analyzed

separately.

CART Classification and regression trees.

Categorical data Data that classifies observations without quantitative meaning (for

example, colors of cars) or where quantitative amounts are categorized

(for example, "0-10, 11-20, ...").

Causation Relationship in which one thing makes another happen (i.e., one thing

causes another).

Chance constraint A probability-based constraint. For example, a standard linear

constraint might be $Ax \leq b$. A similar chance constraint might be

 $Pr(Ax \le b) \ge 0.95$.

Change detection Identifying when a significant change has taken place in a process.

Classification The separation of data into two or more categories, or (a point's

classification) the category a data point is put into.

Classification tree Tree-based method for classification. After branching to split the data,

each subset is analyzed with its own classification model.

Classifier A boundary that separates the data into two or more categories. Also

(more generally) an algorithm that performs classification.

Clique A set of nodes where each pair is connected by an arc.

Cluster A group of points identified as near/similar to each other.

Cluster center In some clustering algorithms (like k-means clustering), the central

point (often the centroid) of a cluster of data points.

Clustering Separation of data points into groups ("clusters") based on

nearness/similarity to each other. A common form of unsupervised

learning.

Collective outlier A set of data points that is (uncommonly) different from others – for

example, a missing heartbeat in an electrocardiogram; we don't know exactly which millisecond it should've happened in, but collectively

there's a set of milliseconds that it's missing from.

Concave function A function f() where for every two points x and y, f(cx + (1 -

 $(c)(y) \ge f(cx + (1-c)y)$ for all $(c)(x) \ne 0$ for all $(c)(x) \ne 0$ and 1. In two dimensions, this means if the points (x, f(x)) and (y, f(y)) are connected with a straight line, the line is always below [or equal to] the function's curve between those two points. If $(c)(x) \ne 0$ is concave, then

-f() is convex.

Concordance index Area under the ROC curve; an estimate of the classification model's

accuracy. Also called AUC.

Confusion matrix Visualization of classification model performance.

Constant A number that remains the same.

Constraint Part of an optimization model that describes a restriction on the

solution (the values of the variables).

Contextual outlier A data point that is (uncommonly) far from other data points related to

it – for example, in Atlanta, a 90-degree (Fahrenheit) day in winter is an

outlier, but a 90-degree day in summer is not.

Continuous-time simulation A simulation that models a system continuously, at every instant of

time; continuous-time simulation models are often based on

differential equations.

Control (1) A variable whose value remains constant for all runs of an

experiment, so changes in this variable don't affect the experiment.
(2) Design an experiment where some factors ("controls" by definition

(1)) are held constant to avoid them affecting the outcome.

Convex function A function f() where for every two points x and y, f(cx + (1 -

 $f(cx) \leq f(cx + (1-c)y)$ for all f(c) = 0 between 0 and 1. In two dimensions, this means if the points f(c) = 0 and f(c) = 0 are

connected with a straight line, the line is always above [or equal to] the function's curve between those two points. If f() is convex, then -f()

is concave.

Convex hull (of a set of points) Smallest convex shape that the set of points is contained in.

Convex optimization model An optimization model where the objective function is to minimize a

convex function (or maximize a concave function) and the constraints

define a convex set of feasible solutions.

Convex quadratic function A second-order polynomial function that is convex.

Convex quadratic program A mathematical program where a convex quadratic function of the

variables is minimized, subject to linear constraints.

Convex set A set of points for which a straight line drawn between any two points

in the set, stays inside the set. A circle is a convex set. A set shaped like the letter "U" is not convex; the line between the two points on

top goes outside of the set.

Cooperative game theory A game theory setting where the participants are also working

together to achieve some goal, while also competing in some way.

Corrected AIC Improved version of AIC, especially when sample size is small.

Correlation Relationship in which two things are likely to happen together,

regardless of whether one causes the other. (There is also a

quantitative statistical definition measuring the amount of correlation.)

Covariate A characteristic or measurement that can be used to estimate the

value of something – for example, a person's height or the color of a car. A "feature" or "attribute"; in the standard tabular format, a

column of data.

Cross-validation Validation technique where a model is tested on data different from

what it was trained on.

CUSUM Change detection method that compares observed distribution mean

with a threshold level of change. Short for "cumulative sum".

Data point Observation/record of (perhaps multiple) measurements for a single

member of a population or data set. In the standard tabular format, a

row of data.

Decision Choice of action.

Decision point Place in a simulation where there is a branch (or decision to be made

or observed).

Decision tree Tree-based method for decision-making. After branching to split the

data, each subset is analyzed with its own decision model (or just has

its own decision applied).

Deep learning Neural network-type model with many hidden layers.

Descriptive analytics Loosely speaking, the use of analytics to explain or describe what has

happened.

Design of experiments Choosing a set of tests to be made to find the effect of input variables

on an outcome.

Deterministic simulation Simulation with no randomness/uncertainty, so results are the same

each run.

Detrending Removal of trend, such as a change in the mean over time, from time-

series data.

Diagnostic odds ratio Ratio of the odds that a data point in a certain category is correctly

classified by a model, to the odds that a data point not in that category

is incorrectly classified by the model; equal to $\frac{TP/FN}{FP/TN} = \frac{TN \times TP}{FN \times FP}$.

Diet problem Classical optimization model for finding the least-costly set of foods

that meets all dietary requirements.

Differencing Using the difference of successive values in time series data, rather

than the values themselves. Sometimes nonstationary data will have

stationary differences.

Dimension A feature of the data points (for example, height or credit score). (Note

that there is also a mathematical definition for this word.)

Discrete-event simulation A simulation that models a system that changes when specific events

occur.

Distance How far it is between two points -- but there are different ways to

measure it (see Minkowski distance).

Distribution-fitting Determining whether a set of data seems to follow a certain

probability distribution, or determining which of several distributions

the data is close to.

Double exponential

smoothing

Two-parameter exponential smoothing technique that incorporates

trend

Dynamic programming Optimization approach that involves making a sequence of decisions

over time, based on the current state of a system.

Earth Name of many implementations of multi-adaptive regression spline

(MARS) model, because "MARS" is a trademark.

Edge Connection between two nodes/vertices in a network. In a network

model, there is a variable for each edge, equal to the amount of flow on the arc, and (optionally) a capacity constraint on the edge's flow.

Also called an arc.

Eigenvalue Amount by which an eigenvector gets rescaled in a linear

transformation.

Eigenvector Non-zero vector that does not change direction when a linear

transformation is applied to it, but only gets rescaled by the eigenvalue

Elastic net Combination of lasso and ridge regression.

Elbow diagram A graph of improvement in function value as something else (e.g.,

number of clusters) increases or decreases; the spot where

improvement levels out is the "elbow".

EM algorithm Expectation-maximization algorithm.

Empirical Bayes model Model that uses Bayes' theorem to update an initial guess/distribution

based on observed data.

Entity A person/thing moving through a simulation.

Error (per data point) The difference (or absolute difference, squared difference, or other

measure) between the estimate of a piece of data and its true value.

Error (total over data set) The total of all errors in a data set.

Euclidian distance/straight-

line distance

The length of a straight line (the 2-norm distance) between two points. If $x=(x_1,x_2,\ldots,x_m)$ and $y=(y_1,y_2,\ldots,y_m)$ are two points in an m-dimensional space, then the Euclidian distance between them is

 $\sqrt[2]{(x_1 - y_1)^2 + (x_2 - y_2)^2 + \dots + (x_m - y_m)^2} = \sqrt[2]{\sum_{i=1}^m (x_i - y_i)^2}.$

Expectation-maximization algorithm (EM algorithm)

General description of an algorithm with two steps (often iterated), one that finds the function for the expected likelihood of getting the response given current parameters, and one that finds new parameter

values to maximize that probability.

Exploitation Using known information to get good outcomes.

Exploration Finding new/better/more information to determine how to optimize

output.

Exponential distribution A continuous probability distribution of the time between events:

 $f(x) = \lambda e^{-\lambda x}$. If the number of events in a fixed time follows the Poission distribution, then the time between them has the exponential

distribution. The exponential distribution has the memoryless

property.

Exponential smoothing Data smoothing technique in which older observations are assigned

exponentially decresing weights, so more emphasis is given to recent

observations.

Factorial design Tests of different combinations of factor values over multiple factors,

to find each one's effect, and interaction effects, on the outcome.

Fall out Fraction of data points not in a certain category that are incorrectly

classified by a model; equal to $\frac{FP}{TN+FP}$. Also called false positive rate.

False negative (FN)

Data point that a model incorrectly classifies as not being in a certain

category. ("Negative" means the model classified it as not being in the category, and "False" means the model's classification is incorrect.)

Sometimes abbreviated as "FN".

False negative rate Fraction of data points in a certain category that are incorrectly

classified by a model; equal to $\frac{FN}{TP+FN}$. Also called miss rate.

False positive (FP) Data point that a model incorrectly classifies as being in a certain

category. ("Positive" means the model classified it as being in the category, and "False" means the model's classification is incorrect.)

Sometimes abbreviated as "FP".

False positive rate Fraction of data points not in a certain category that are incorrectly

classified by a model; equal to $\frac{FP}{TN+FP}$. Also called fall out.

False omission rate Fraction of data points the model classifies as not in a certain category,

that are really in the category; equal to $\frac{FN}{TN+FN}$

Feasible solution A solution that satisfies a set of constraints.

Feature (1) A characteristic or measurement – for example, a person's height or

the color of a car. Generally interchangeable with "attribute", and often with "covariate" or "predictor". In the standard tabular format, a

column of data. Also called an attribute. (2) A combination of

attributes in a specific format – for example, 0.5×height plus 7×shoe-

size.

FIFO First-in, first-out: The first entity to join a queue is the first one to come

out -- for example, a supermarket checkout line.

Fitting Finding a model (including, if appropriate, a probability distribution)

that is a good description of real effects in a set of data. The model is

sometimes called a "fit".

Fixed charge In optimization models, a cost that depends only on whether

something happens, but not how much – for example, a transaction cost for buying or selling stock that is the same regardless of how many

shares are bought or sold.

Flow In a network model, the amount sent from one node to another along

an arc. In network models, there is a variable for each arc, equal to the amount of flow on the arc, and (optionally) a capacity constraint on the

arc's flow.

Forest A set of multiple trees. Just like in real life.

Forward selection Variable selection process that starts with no variables and then

iteratively adds the most-immediately-relevant variables to the model.

Fractional factorial design Test of a subset of all possible combinations of factor values over

multiple factors. If chosen well, the desired effects of factors and factor

interaction effects can be obtained.

Full factorial design

Test of all possible combinations of factor values over multiple factors

to find each one's effect, and interaction effects, on the outcome.

Game theory The study of competitive strategic decision-making where the outcome

of each participant's actions is dependent on another participant's

actions.

GARCH Generalized autoregressive conditional heteroscedasticity.

Generalized autoregressive conditional heteroscedasticity (GARCH)

Autoregressive method used to model variance in time series data.

Geometric distribution

Discrete probability distribution of the number of iid Bernoulli trials, each with success probability p, before the first success: $\Pr(k) = (1-p)^k p$. Also can be defined as the total number of trials through the first success (so $\Pr(k) = (1-p)^{k-1} p$). To find the number of trials before the first failure, a similar distribution would be $\Pr(k) = p^k (1-p)$.

Global

optimum/maximum/minimum

A solution that achieves the best objective value among all of the feasible solutions; sometimes also used to refer to the best objective value achievable among a set of feasible solutions.

Graph Among other definitions, another name for a network.

Greedy algorithm Algorithm that makes the immediately-best choice at each step.

Heteroscedasticity When the variability of a response is different across the range of

predictor values.

Heuristic Algorithm that is not guaranteed to find the absolute best (optimal)

solution.

Hit rate Fraction of data points in a certain category that are correctly classified

by a model; equal to $\frac{TP}{TP+FN}$; also called the true positive rate,

sensitivity, and recall.

Holt-Winters

Hypothesis test

method/Winters' method

Three-parameter exponential smoothing technique that incorporates trend and seasonality; also called triple exponential smoothing.

Statistical test to determine the probability that a property of a sample

of data is true for the whole population.

iid Independent and identically distributed.

Improving direction Vector of changes to a solution to an optimization problem, such that

the objective function gets better when moving the solution some

10

distance in the vector's direction.

Imputation Inserting values where data is missing.

Independent A is "independent" of B if the probability or probability distribution of

A is not affected by B. For example, whether a coin flip is heads or tails is (I assume) independent of the number of fish in the ocean exactly 100 years ago to this day, but the temperature today is not independent of the temperature yesterday (if it was hot yesterday, it's more likely to be hot today too, etc.).

Independent and identically distributed (iid)

Things that follow the same probability distribution, including the same parameter(s), and whose values are independent of each other. For example, multiple flips of the same coin are iid.

Infinity-norm

Specific case of p-norm when $p=\infty$. Sounds weird, but it just reduces to the largest of the dimensions. If $z=(z_1,z_2,...,z_m)$ is a vector in an m-dimensional space, then its ∞ -norm is $\max_i |z_i|$. If $x=(x_1,x_2,...,x_m)$ and $y=(y_1,y_2,...,y_m)$ are two points in an m-dimensional space, then the ∞ -norm distance between them is $\max_i |x_i-y_i|$.

Initialization

Setting starting values in an algorithm, or setting the first solution value for an "direction/step-size" optimization algorithm.

Integer program

Optimization model where the objective function is a linear function of the variables, the constraints are linear equations and/or linear inequalities in terms of the variables, and some or all variables are restricted to have integer values.

Interaction term

Variable in a model that is the combination of two or more other variables; for example, if x_1 and x_2 are variables, (x_1x_2) is an interaction term/interaction variable.

Interarrival time

The time between two consecutive arrivals of people, things, etc. -- for example, the time between consecutive phone calls to a service hotline.

Iterate

Repeat the same steps of a process.

k-fold cross-validation

Validation technique where data is divided into several parts ("folds"), and each part is used to validate a model fit to the remaining parts. Often a more robust validation approach than splitting data into training and validation sets.

k-means algorithm

Clustering algorithm that defines k clusters of data points, each corresponding to one of k cluster centers selected by the algorithm.

k-Nearest-Neighbor (KNN)

Classification algorithm that defines a data point's category as a

function of the nearest k data points to it.

k-Nearest-Neighbor

regression

Regression model where a data point's response is estimated based on the responses of the k nearest data points with known response.

Kendall notation

Notation to describe various types of queuing models -- for example,

M/M/c (a queue with Poisson arrivals, exponentially-distributed

service times, and c identical servers).

Kernel A type of function that computes the similarity between two inputs;

thanks to what's (really!) sometimes known as the "kernel trick", nonlinear classifiers can be found almost as easily as linear ones.

Knot Point where pieces of a spline regression meet.

Lasso/Lasso regression Method for limiting the number of variables in a model by limiting the

sum of all coefficients' absolute values. Can be very helpful when

number of data points is less than number of factors.

Leaf In a tree model, a subset of data from which there is no branching.

Learning Finding/discovering patterns (or rules) in data, often that can be

applied to new data.

LIFO Last-in, first-out: The last entity to join a queue is the first one to come

out -- for example, a stack of papers.

Likelihood Probability that a model with specific parameter values would

generate the actual outcomes in the data.

Linear combination The weighted sum of things. For example, if $x_1, x_2, ..., x_m$ are factors,

then $a_1x_1 + a_2x_2 + \cdots + a_mx_m$ is a weighted sum of them for any

numbers a_1, a_2, \dots, a_m .

Linear equation Equation where a linear function is set equal to a constant or another

linear function.

Linear function Weighted sum of variables, plus a constant: $a_0 + \sum_{i=1}^m a_i x_i$.

Linear inequality Inequality where a linear function is set to be greater-than-or-equal-to

or less-than-or-equal-to a constant or another linear function.

Linear program An mathematical programming model where the objective function is a

linear function of the variables, and the constraints are linear equations and/or linear inequalities in terms of the variables.

Linear regression Regression model where the relationships between attributes and a

response are modeled as linear functions: $y = a_0 + \sum_{i=1}^{m} a_i x_i$.

Local A solution that achieves a better objective value than any feasible

optimum/maximum/minimum solutions that are close to it; sometimes also used to refer to that

solution's objective value.

Logistic regression Regression model that uses an exponential function of variables to

estimate a response that is either between 0 and 1, or must be equal

to 0 or 1: $y = \frac{1}{1+e^{-\left(a_0 + \sum_{i=1}^m a_i x_i\right)}}$. Also called a logit model.

Logit model Regression model that uses an exponential function of variables to

estimate a response between 0 and 1: $y = \frac{1}{1+e^{-\left(a_0 + \sum_{i=1}^m a_i x_i\right)}}$. Also called

a logistic regression.

Louvain algorithm Algorithm for finding highly-connected communities in networks.

Lower tail Lowest-value part of a distribution

Machine Apparatus that can do something; in "machine learning", it often refers

to both an algorithm and the computer it's run on. (Fun fact: before computers were developed, the term "computers" referred to people

who did calculations quickly in their heads or on paper!)

Machine learning Use of computer algorithms to learn and discover patterns or structure

in data, without being programmed specifically for them.

Manhattan distance The sum of the lengths in each dimension between two points (the 1-

norm distance). If $x=(x_1,x_2,\ldots,x_m)$ and $y=(y_1,y_2,\ldots,y_m)$ are two

points in an m-dimensional space, then the rectilinear distance between them is $\sqrt[1]{|x_1-y_1|^1+|x_2-y_2|^1+\cdots+|x_m-y_m|^1}=|x_1-y_1|+|x_2-y_2|+\cdots+|x_m-y_m|=\sum_{i=1}^m|x_i-y_i|.$ Also called

Rectilinear or 1-norm distance.

Mann-Whitney test Nonparametric test to determine whether medians of two

independent or unpaired samples (possibly of different size) are the

same. Also called Wilcoxon sum rank test.

Margin For a single point, the distance between the point and the classification

boundary; for a set of points, the minimum distance between a point in the set and the classification boundary. Also called the separation.

Markov chain Process where a system changes its state in a way that depends only

on its current state.

Markov decision process Markov chain model where decisions are made at some states, and

state transitions have associated rewards.

MARS Multi-adaptive regression splines.

Mathematical programming Mathematical optimization, often using variables, constraints, and

objective function.

Maximization problem Optimization model where the objective is to find the feasible solution

that maximizes the value of the objective function.

Maximum flow problem Network optimization model that finds the most flow that can be sent

from one specific node to another.

Maximum likelihood A method that finds the set of parameter values for which a model is

most likely to generate the actual values of the data.

McNemar's test Nonparametric test for comparing paired samples where the output is

yes/no (or A/B, or 0/1, etc.).

Memoryless (distribution) Probability distributions where the past history of outcomes does not

influence the probability of the outcome of future events. The exponential and geometric distributions have this property.

Memoryless (Markov chain) Property that the next state of the system is dependent only on the

current state, not any previous states.

Minimization problem Optimization model where the objective is to find the feasible solution

that minimizes the value of the objective function.

Minkowski distance (of order

p)

The *p*-norm distance between two points. If $x = (x_1, x_2, ..., x_m)$ and $y = (y_1, y_2, ..., y_m)$ are two points in an *m*-dimensional space, then

the Minkowski distance of order p between them is

 $\sqrt[p]{|x_1 - y_1|^p + |x_2 - y_2|^p + \dots + |x_m - y_m|^p} = \sqrt[p]{\sum_{i=1}^m |x_i - y_i|^p}.$

Misclassified Put into the wrong category by a classifier.

Miss rate Fraction of data points in a certain category that are incorrectly

classified by a model; equal to $\frac{FN}{TP+FN}$. Also called false negative rate.

Missing data Values of data that are missing from a data set

Mixed strategy/randomized

strategy

A strategy where a participant's action is determined randomly according to probabilities – for example, in "rock, paper, scissors", someone who randomly chooses between the three options with

probability $\frac{1}{3}$ each is using a mixed strategy.

Model (mathematical) A mathematical description of a system. Because real-life systems are

complex, mathematical models of them are only approximate. In analytics, the term "model" is used in at least three different ways: (1) A general type of mathematical approach, like "regression"; (2) A general type of mathematical approach with specific parameters, like "regression using credit score and income as predictors"; (3) A general type of mathematical approach with specific parameters and values for the parameters, like "regression, with the prediction equal to 100,000,

plus 100 times credit score, plus 3 times income".

Modularity Measure of the density of connections between communicates in a

network.

Module In ARENA, a building-block of a simulation, or the process, resource,

etc. it represents.

Most optimal Please don't say this (or "more optimal"). "Optimal" means "best", and

"most best" or "more best" are not proper English.

Moving average Smoothing technique that replaces data values with the mean of a

number of consecutive observed values.

Multi-adaptive regression splines (MARS)

Specific regression spline model that has become commonly-used. Abbreviation "MARS" is a trademark, so many versions are called

"earth".

Multi-armed bandit

Model that allows the tradeoff between exploration of unknown resources and exploitation of known resources to optimize output.

Multiplicative seasonality

Seasonal effect that is multiplied by a baseline value (for example, "the temperature in June is 20% higher than the annual baseline").

Multiplier

A term that something is multiplied by. For example, to change units from meters to centimeters, the multiplier is 100.

Negative likelihood ratio

Ratio of the fraction of data points in a certain category that are misclassified as not in the category, to the fraction of data points not in the category that are correctly classified as not being in the category; FN/(FN+TP)

equal to (1-sensitivity)/specificity = $\frac{FN/(FN+TP)}{TN/(TN+FP)}$.

Negative predictive value

Fraction of data points classified as not in a certain category that are really not in that category; equal to $\frac{TN}{TN+FN}$.

Network

Model where locations (nodes or vertices) are connected by arcs or

edges, with flow on the arcs from node to node.

Network optimization

problem

Optimization problem that can be modeled as a network with nodes and arcs, where each variable represents the flow on an arc, with constraints to ensure that the flow into each node equals the flow out of it, and to put a capacity on the flow on each arc.

Neural network

A machine learning model that itself is modeled after the workings of neurons in the brain.

Node

Location in a network. In a network model, there is a constraint for each node to ensure that the incoming flow equals the outgoing flow. Also called a vertex.

Non-convex program

Optimization model where the constraint set is not convex, and/or the objective function is to minimize a nonconvex function or to maximize a nonconcave function.

Non-negativity constraints

Constraints that require variables to be greater than or equal to zero.

Nonparametric test

Statistical test that makes no assumptions about the population distribution from which the data is sampled. Nonparametric tests often focus on the median.

Norm/distance norm

A function that measures the size/length of a vector and satisfies some basic technical properties that are beyond the scope of this course. In this course, we focus on Minkowski norm (or p-norm).

Continuous probability distribution: $f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$. Model error is often assumed to be seen as a function of the continuous probability distribution. Normal distribution

is often assumed to be normally distributed (for example, in linear

regression).

Objective function Part of an optimization model that measures the quality of a solution

(the values of the variables).

Observation (1) A measurement of one attribute of a data point. (2) A measurement

of all attributes of a data point (i.e., a full row of data). (3) The act of

watching/measuring/recording something.

Optimal Best possible, while satisfying all constraints.

Optimal solution A solution that satisfies a set of constraints, and has the best-possible

objective value.

Finding the values of variables/decisions that yield the best value of an Optimization

objective function while satisfying a set of constraints (restrictions).

The relative size of something, often denoted by multiples of 10 so that Order of magnitude

> difference in the order of magnitude of two numbers is the difference in how many digits they haves. So, loosely speaking, a 2-digit number is one order of magnitude smaller than a 3-digit number, a 7-digit number is two orders of magnitude smaller than a 9-digit number, two

4-digit numbers have the same order of magnitude, etc.

Orthogonal At right angles to one another (like "perpendicular" but generalized to

more dimensions). Statistically, if two attributes are orthogonal then

they are independent.

Outcome A variable of interest that a model tries to estimate or predict.

Outlier A data point or set of points that's far from the rest in one way or

another (see point outlier, contextual outlier, collective outlier).

Overfitting Building a model that describes random effects instead of or in

> significant addition to the real effects; often caused by having too many factors or parameters compared to the number of data points.

Overfitted models will have high prediction errors.

Paired samples Data with two different outcomes for each data point. Often helpful

> for comparing the method that generated outcome #1 with the method that generated outcome #2 to see which is better.

Parameter A constant whose value determines something about a system,

expression, etc. For example, if we remove a variable from a

regression model whenever its p-value is "too high", above P, then P is

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a parameter, and setting it to different values can mean we get

different models.

Parametric test Statistical test that assumes the data being tested is sampled from a

distribution governed by certain parameter(s). Parametric tests often

focus on the mean.

PCA Principal component analysis.

Perturbation A change (usually small) from the actual or expected value of

something.

p-norm Measures vector length similar to the Minkowski distance of order p.

If $z=(z_1,z_2,\dots,z_m)$ is a vector in an m-dimensional space, then its p-

norm is $\sqrt[p]{|z_1|^p + |z_2|^p + \dots + |z_m|^p} = \sqrt[p]{\sum_{i=1}^m |z_i|^p}$.

Point outlier A data point that is (uncommonly) far from other data points – for

example, an outdoor temperature reading of 200 degrees Fahrenheit.

Poisson distribution A discrete probability distribution of the number of iid events

happening within a fixed time: $\Pr(k) = \frac{\lambda^k e^{-\lambda}}{k!}$. If the time between the events follows the exponential distribution, then the number of events

follows the Poisson distribution.

Poisson regression Regression that assumes the response has a Poisson distribution.

Positive likelihood ratio Ratio of the fraction of data points in a certain category that are

correctly classified as being in that category, to the fraction of data points not in the category that are incorrectly classified as being in the

category; equal to sensitivity/(1-specificity) = $\frac{TP/(TP+FN)}{FP/(FP+TN)}$.

Positive predictive value Fraction of data points classified as being in a certain category that are

really in that category; equal to $\frac{TP}{TP+FP}$. Also called precision.

Precision In analytics, the fraction of data points classified as being in a certain

category that are really in that category; equal to $\frac{TP}{TP+FP}$. Also called

positive predictive value.

Prediction Estimate of what will happen in the future, or of something unknown

(e.g., missing data) that happened.

Predictive analytics Loosely speaking, the use of analytics to estimate or predict what will

happen.

Predictor A characteristic or measurement that is used to estimate ("predict")

the future value of something – for example, a person's height or the color of a car. A "feature" or "attribute"; in the standard tabular

format, a column of data.

Prescriptive analytics Loosely speaking, the use of analytics to suggest or prescribe what's

best to do.

Principal component analysis

(PCA)

Transformation of data into orthogonal dimensions that are ranked by

variance.

Prisoner's dilemma A situation in game theory where each participant would benefit if all

participants act in a certain way, but each participant individually has

incentive to not act that way.

Pruning Removing a branch from a tree.

Pseudo-R-squared/Pseudo-R² Measure similar to R² used for nonlinear regression models where R²

cannot be calculated.

Pure strategy A strategy where a participant's action is deterministic (known with

probability 1) – for example, in "rock, paper, scissors", someone who

always chooses "rock" is using a pure strategy.

p-value (1) In hypothesis testing, probability that results at least as extreme as

those in the data would be observed if the null hypothesis is true. (2) In regression, probability that results at least as extreme as those in the data would be observed if the coefficient of a variable is zero.

p-value fishing Testing many different hypotheses hoping to find one with a low p-

value. This is a bad practice; if enough things are tested, it's likely one will have a low p-value due to randomness, but that doesn't mean it's

a real effect.

Q-Q plot Quantile-quantile plot -- a plot comparing the quantiles of two data

sets, or one data set and a distribution, to see whether they might

have a common distribution.

Quantitative data Data that describes numerical amounts of something – for example,

height and weight.

Queue A line of people, things, etc. waiting to go through or be

processed/served by a resource -- for example, an airport security line.

Queuing The mathematical study of queues.

Random effects Patterns that appear to occur in a subset of data, but only exist due to

random variability in the data and are not part of the system. (Note that there is a different statistical definition for this phrase too.)

Random forest Machine learning model that creates many different trees and returns

their mean output. Can be used with classification trees, regression

trees, decision trees.

Real effects Actual patterns in the system being modeled. Ideally, good models will

reveal real effects.

Recall Fraction of data points in a certain category that are correctly classified

by a model; equal to $\frac{TP}{TP+FN}$; also called sensitivity, hit rate, and true

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positive rate.

Receiver operating characteristic curve (ROC curve)

Graph that plots the true positive rate against the false positive rates

for different classification cutoff thresholds.

Rectilinear distance

The sum of the lengths in each dimension between two points (the 1-norm distance). If $x = (x_1, x_2, ..., x_m)$ and $y = (y_1, y_2, ..., y_m)$ are two

points in an m-dimensional space, then the rectilinear distance between them is $\sqrt[1]{|x_1-y_1|^1+|x_2-y_2|^1+\cdots+|x_m-y_m|^1}=|x_1-y_1|+|x_2-y_2|+\cdots+|x_m-y_m|=\sum_{i=1}^m|x_i-y_i|$. Also called

Manhattan or 1-norm distance.

Regression Statistical model that describes relationships between variables,

and/or predicts future values of a response..

Regression splines Regression model where different functions are used for different

ranges of the data. Also called spline regression.

Regression tree Tree-based method for regression. After branching to split the data,

each subset is analyzed with its own regression model.

Regularization Addition of term(s) to the model to reduce model complexity or

overfitting. For example, adding a penalty to the objective function in

regression can help reduce overfitting (see ridge regression).

Replication Running a stochastic simulation multiple times to sample the

distribution of possible simulation results. "A replication" also refers

to a single one of many runs of the simulation.

Resource In ARENA, the "doers" – for example, a call center worker at a queue.

Response A variable of interest that a model tries to estimate or predict.

Response surface Sequential experimentation strategy to understand the relationship

between response and input factors, and/or optimize the response.

Ridge regression Method of regularization by limiting the sum of the squares of the

coefficients. Will reduce the magnitude of coefficients, not the

number of variables chosen.

Robust solution A solution that whose worst-case outcome over all possible scenarios

is least bad.

ROC curve Receiver operating characteristic curve.

Root The first, complete data set in a tree model.

R-squared/R² Measure of linear regression model quality, the fraction of variance in

the response that is explained by the model. Also called coefficient of

determination.

Scaling Shrinking or expanding, and moving, the range of data to fit exactly

into a specific interval (for example, between 0 and 1, or between 100

and 800).

Scenario Specific case/instance of an uncertain outcome; one approach to

stochastic optimization is to optimize over a number of scenarios

simultaneously.

Seasonality/cycles Repeating pattern in data values over time, often at consistent

intervals (for example, temperature variations throughout the year

that repeat each year at about the same time).

Seasonality length/cycle

length

Fixed time period at which cycles/seasonalities repeat themselves.

Sensitivity Fraction of data points in a certain category that are correctly classified

by a model; equal to $\frac{TP}{TP+FN}$; also called the true positive rate, hit rate,

and recall.

Sequential game A game in which participants choose their actions one after another, so

participants who choose later have knowledge of the earlier actions.

Service rate Rate at which entities are processed.

Shortest path problem Network optimization model that finds the shortest route in a network

from one specific node to another.

Simplicity (of a model) Having fewer parameters; opposite of complexity of a model. Often

helpful for avoiding overfitting and increasing interpretability.

Simulation A model that imitates the operation or behavior of a real system.

Simultaneous game A game in which all participants choose their actions at the same time.

Single exponential smoothing Exponential smoothing technique with just one parameter, that does

not incorporate trend or seasonality.

Smoothing Time series analysis technique to help filter out underlying

randomness/noise. Examples include moving average, exponential

smoothing, and ARIMA.

Smoothing constant Parameter in exponential smoothing to determine the relative

importance of recent observations and previous estimates. Smoothing constants are between 0 and 1; a higher value indicates more reliance on observation, and a lower value indicates more reliance on previous

estimates.

Solution (in the optimization

sense)

A vector of values, one for each variable in an optimization model.

Specificity Fraction of data points not in a certain category that are correctly

classified by a model; equal to $\frac{TN}{TN+FP}$; also called the true negative

Spline regression Regression model where different functions are used for different

ranges of the data. Also called regression splines.

Stable equilibrium A situation in game theory where, given each participant's current

choice of action, no participant can do better by changing actions.

Standardization Transforming data by subtracting the mean and then dividing by

standard deviation, so that it has mean 0 and variance 1.

State Description of a system's condition.

Stationary process Process whose joint probability distribution and statistical properties

(mean, variance, autocorrelation, etc.) do not vary with time. Examples

include data with trends or cycles.

Steady state In a Markov chain, having the same probability distribution of being in

each state, before and after a transition.

Step size Distance to move in an improving direction, to get to a new solution

given a current solution and an improving direction. The new solution is equal to the old solution, plus the product of the improving direction

and step size.

Stepwise regression Variable selection process that can combine forward selection and

backward regression.

determined according to probabilities.

Stochastic optimization An optimization model that accounts for randomness or uncertainty.

Stochastic simulation Simulation that includes randomness/uncertainty, so results can be

different each run.

Structured data Data that is highly organized, so it can be searched, queried, and

analyzed easily – for example, a table with the name, age, and country

of participants in this course.

Sum-of-squared errors Sum of the squares of all the differences between data and model

output. In regression, this is a measure of variance.

Supervised learning Machine learning where the "correct" answer is known for each data

point in the training set.

Support vector In SVM models, the closest point to the classifier, among those in a

category. (Note that there is a more-technical mathematical definition

too.)

Support vector machine (SVM) Classification algorithm that uses a boundary to separate the data into

two or more categories ("classes").

SVM Support vector machine.

Tail(s) Highest and lowest-value parts of a distribution.

Test data/test set Portion of the data used to assess the effectiveness of a model once

built.

Threshold A value that denotes the difference between something happening or

not happening. For example, if "whenever p is greater than 0.15, we include the corresponding variable in a regression model" then 0.15 would be the "threshold" value of p that differentiates between

including and not including the variable.

Time series data

Data that records the same attribute/response at multiple points in

time (often at equal time intervals).

Training data/training set Portion of the data to build/fit a model. Normally, most of the data is

used for training.

Transformation A mapping of points from one space to another.

Transition matrix Matrix of transition probabilities.

Transition probability Probability of moving from current state i to next state j, often

denoted p_{ij} .

Tree Iterative split (branching) of a data set into more-specific subsets that

each are modeled separately. Often used for classification, regression, and decision-making. Also can be used to solve optimization problems.

Trend Increase or decrease in data values over time.

Triple exponential smoothing

Three-parameter exponential smoothing technique that incorporates

trend and seasonality; also called Winters' method or Holt-Winters.

True negative (TN) Data point that a model correctly classifies as not being in a certain

category. ("Negative" means the model classified it as not being in the category, and "True" means the model's classification is correct.)

Sometimes abbreviated as "TN".

True negative rate Fraction of data points not in a certain category that are correctly

classified by a model; equal to $\frac{TN}{TN+FP}$; also called specificity.

True positive (TP)

Data point that a model correctly classifies as being in a certain

category. ("Positive" means the model classified it as being in the category, and "True" means the model's classification is correct.)

Sometimes abbreviated as "TP".

True positive rate Fraction of data points in a certain category that are correctly classified

	by a model; equal to $\frac{TP}{TP+FN}$; also called sensitivity, hit rate, and recall.
Uncertainty	Lack of knowledge about a data value, parameter value, outcome, etc.
Unstructured data	Data that is not very well organized for analysis – for example, a list of free responses to the question "What do you like about analytics?"
Unsupervised learning	Machine learning where the "correct" answer is not known for the data points in the training set.
Upper tail	Highest-value part of a distribution
Validation	Measuring a model's effectiveness on data that was not used to build/train/fit the model. If there is a large difference between a model's effectiveness on a validation set of data and its effectiveness on the training set of data, it is evidence that the model may be overfit.
Validation (of simulation)	Making sure that simulation results are similar-enough to those of the real system being simulated, so the simulation can be used to analyze the real system.
Validation data/validation set	Portion of the data used for validation of a model and compare between models.
Variable (optimization sense)	A decision that an optimization model suggests a value for.
Variable (statistics sense)	An attribute whose value can differ for different data points.
Variable selection	Process of selecting the best subset of predictors to explain variance in data; involves eliminating unnecessary or redundant or less-important variables from a potential set of predictors.
Vertex	Location in a network. In a network model, there is a constraint for each vertex to ensure that the incoming flow equals the outgoing flow. Also called a node.
Voronoi diagram	Graphical representation of splitting a plane with two or more special points into regions with one special point each, where each region's points are closer to the region's special point than to any other special point.
Weibull distribution	Continuous probability distribution that is often used to model the
	time until failure of a device, component, etc.: $f(x) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} e^{-\left(\frac{x}{\lambda}\right)^k}$
	for $x \ge 0$.
Wilcoxon signed rank test (one sample)	Nonparametric test for a single response, to determining whether the median is different from a specific value.

Definitions in this document are meant to be in the context of ISYE 6501 only. Some of these terms have other definitions beyond the scope of this course. Many of these terms have precise mathematical definitions not included here (or even glossed over here), because they are beyond the scope of the course.

where the output is quantitative.

Nonparametric test for comparing the medians of paired samples

Wilcoxon signed rank test

(paired samples)

Zero-sum game

A game where the total gain and loss of all participants is zero. Some participants might benefit and others might lose, but the total of all benefits is equal to the total of all losses.