# SOAP FILM SIMULATION

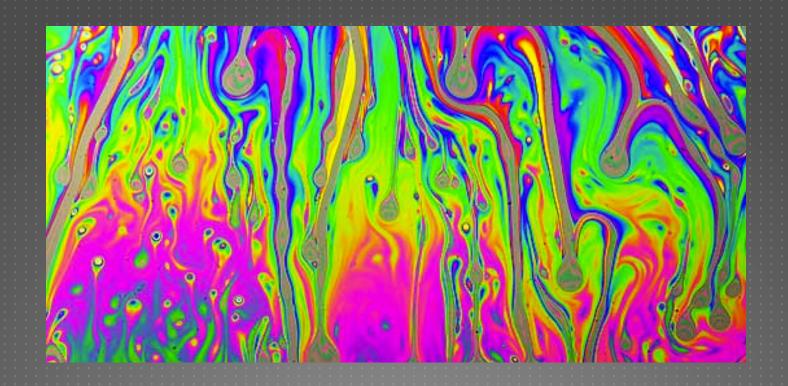
PH 235 Physics Simulation

Rebecca Poch

### **OVERVIEW**

- ► Background Information and Past Work
- ► Goals
- Solution Approach
- ▶ Results and Evaluation
- ▶ PH 235 Topics
- ► Reflections Challenges and Changes

# WHAT ARE SOAP FILMS

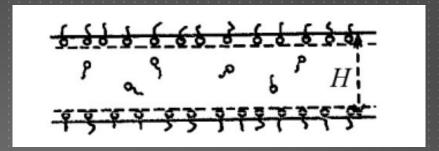


https://people.rit.edu/andpph/text-figures/soap/soap-film-9959A.jpg

# BACKGROUND

### WHY SOAP FILMS?

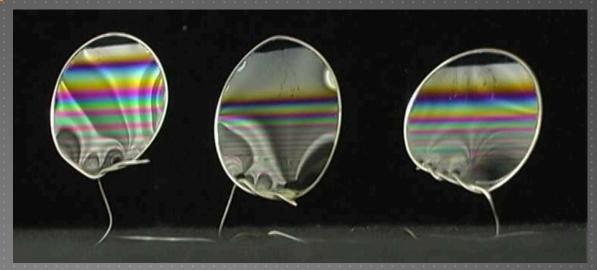
- Microscopic level
  - Intermolecular forces
- Macroscopic level
  - Minimum surface
  - Stability
  - Surface Tension
  - Gravity
- Mysels et al. 1959



[1] Brasz, Frederik

### **EXAMPLES**

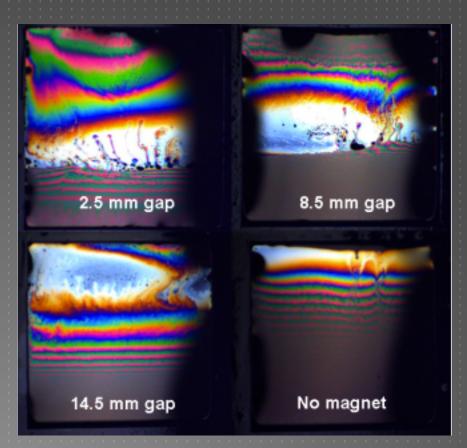
- ► <u>Video Visualization</u>
- ► Minimal Surface Example
- ▶ Draining



http://www.animations.physics.unsw.edu.au/jw/light/soap-bubbles.htm

### MOULTON ET AL.

- Draining soap film with ferrofluid
- Derived equations from experimental result
- Used MATLAB to solve system of ODEs



[2] Moulton, D.E. and Pelesko, J.A.

# GOALS

# **GOALS**

- ▶ Reproduce results of Moulton et al.
- Vary parameters
  - Magnetic field strength
  - Initial profile

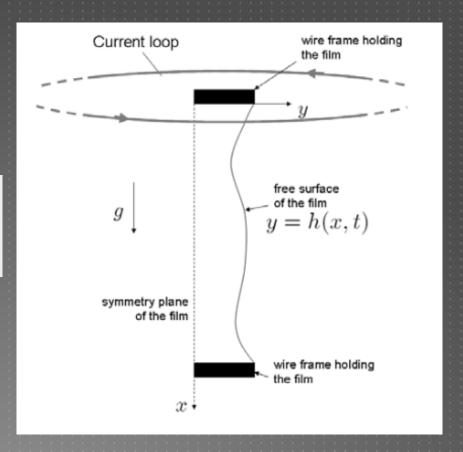
# SOLUTION APPROACH

### MAGNETIC DRAINING EQUATION

$$\frac{\partial \mathbf{h}}{\partial \mathbf{t}} = -\frac{\partial Q}{\partial x}$$

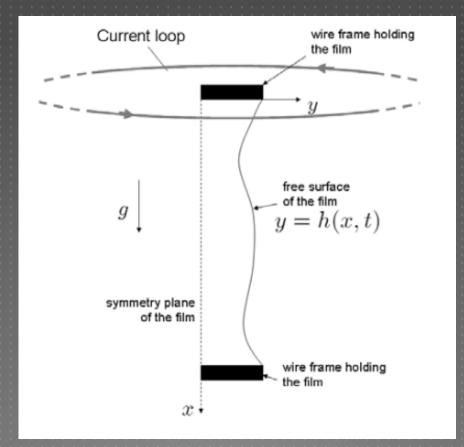
$$Q(x) = \frac{h^3}{3} [\sigma h_{xxx} + 1 + \lambda f(x)]$$

$$f(x) = \frac{-3\eta^2 x}{(1+\eta^2 x^2)^4}$$



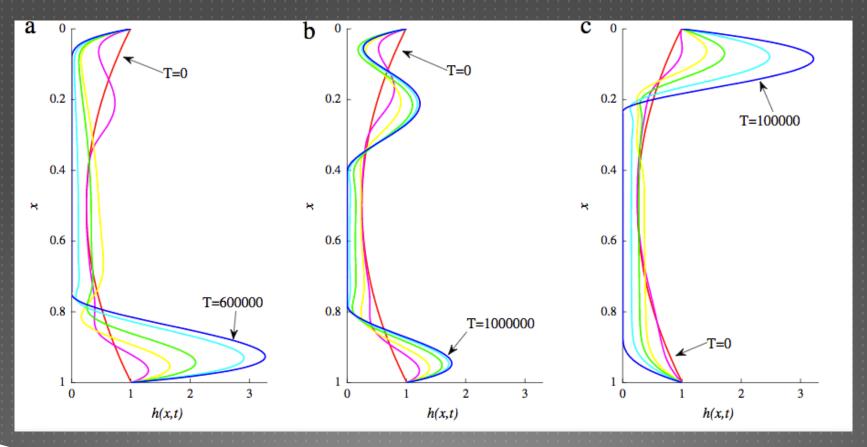
[2] Moulton, D.E. and Pelesko, J.A.

### **DIAGRAM**



[2] Moulton, D.E. and Pelesko, J.A.

### MOULTON ET AL. TIME EVOLUTION



[3] Moulton, D.E. and Lega, J.

#### FIRST ATTEMPTS

- ► Tried to reproduce results in paper by using a python equivalent for MATLAB's ODE15 solver
- Searching online found that scipy.integrate ode solver solution
- Couldn't get it to work with my code

#### SOLUTION APPROACH

Forward propagation for finding the h<sub>xxx</sub> term

$$Q(x) = \frac{h^3}{3} [\sigma h_{xxx} + 1 + \lambda f(x)]$$

Adams-Bashforth Method

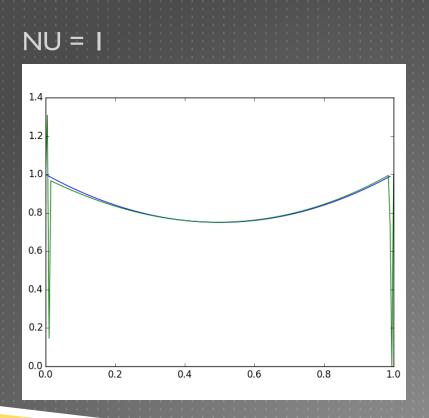
$$\frac{d\mathbf{h}}{dt} = \frac{Q_{i+1/2} - Q_{i-1/2}}{\mathbf{d}}$$

# RESULTS

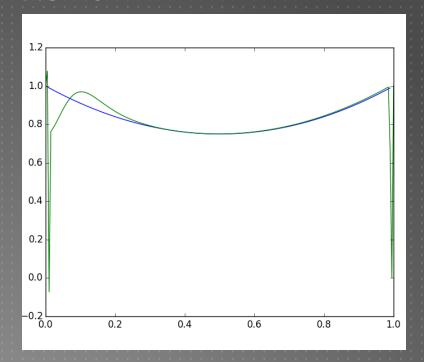
#### RESULTS

- First three timesteps produce plots within range
- After fourth step, the solution highly diverges at the endpoints
- NU is a relative measure of magnetic field strength
  - ▶ I is weak, 5 is strong

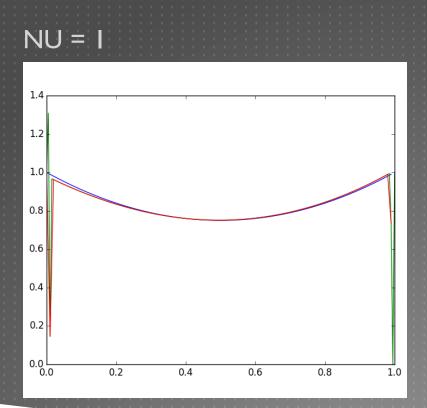
### I STEP



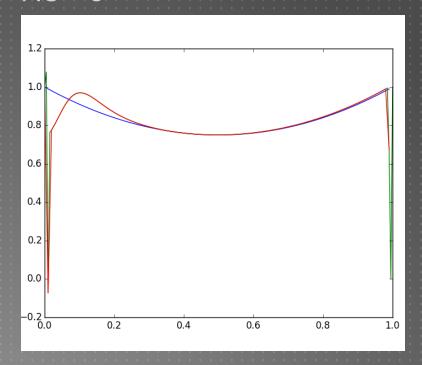




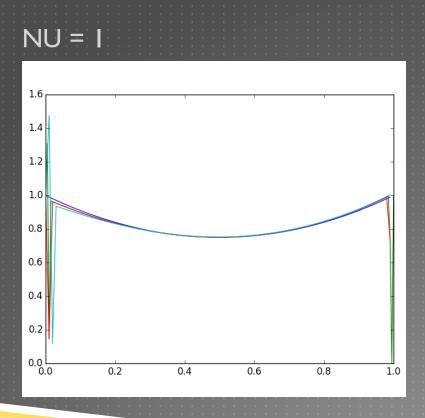
# 2 STEPS



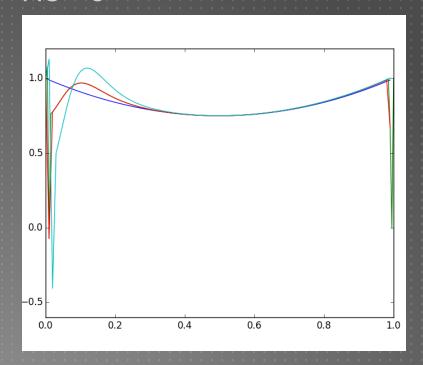




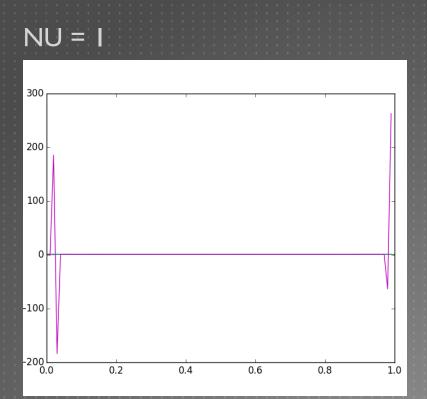
### 3 STEPS



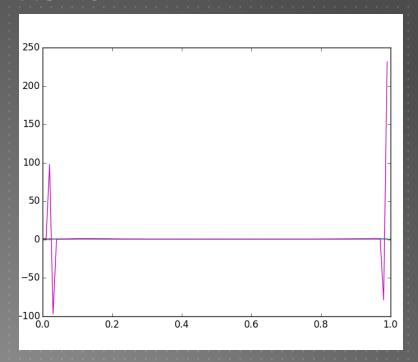




### 4 STEPS







### POSSIBLE PROBLEMS

- ► Error with boundary points
- Change mesh
- Parameters
- Method itself isn't suited well
  - ► Higher order Adams-Bashforth
  - ▶ Try different method

# PH 235 TOPICS

### PH 235 TOPICS

- Python Basics
- Accuracy and Error
- Derivatives and Ordinary Differential Equations
  - Linear multistep methods

# REFLECTIONS

#### REFLECTIONS

- Understanding the paper
- Starting small and scaling up
- Schedule estimations
- Knowing when to revise plan and move along
  - Decided to focus on time evolution, not equilibrium analysis
  - Did not have time to produce visualization
- Trying other methods for solving

### **SUMMARY**

- Soap film studies
- ► Preliminary Simulation
- Forward Propagation and Adams-Bashforth
- ► Time step results
- ▶ PH 235 Topics
- Reflections

#### REFERENCES

- ► [1] Brasz, Frederik. "Statics and Dynamics." Princeton University, 8 Jan. 2010. Web.
- ▶ [2] Moulton, D. E., and Pelesko, J.A. "Reverse Draining of a Magnetic Soap Film." *Physical Review E Phys. Rev. E* 81.4 (2010) Web.
- [3] Moulton, D. E., and Lega, J. "Reverse Draining of a Magnetic Soap Film Analysis and Simulation of a Thin Film Equation with Non-Uniform Forcing." Physica D, 28 Aug. 2009. Web. 05 Nov. 2015.

# QUESTIONS?