



# Reformer : The efficient transformer

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Institute : Google Research

Paper : <https://arxiv.org/abs/2001.04451>

github : <https://github.com/lucidrains/reformer-pytorch>

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# Contents

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- Abstract
- Introduction
- Method
- Experiements
- Conclusion

## Reformer : The efficient transformer

### -problem

- Transformer attention structure  $O(n^2)$  complexity problem
- Feed Forward Layer memory problem -> all outputs of attention layer applied (512 inside -2048)
- N-stacked Residual connection memory problem -> gradient check point

### -Contribution

- Attend on similar pair
  - Point out that 1) high-impact word pairs are similar to each other in the embedding space, and 2) these pairs can be quickly found using Locality-Sensitive Hashing (LSH).
- Chunking data point
  - Data point chunking can reduce memory regardless feed-forward layer position
- Reversible layer
  - Residual connection can be converted as reversible (Back propagation, recover weight)

# Theoretical background

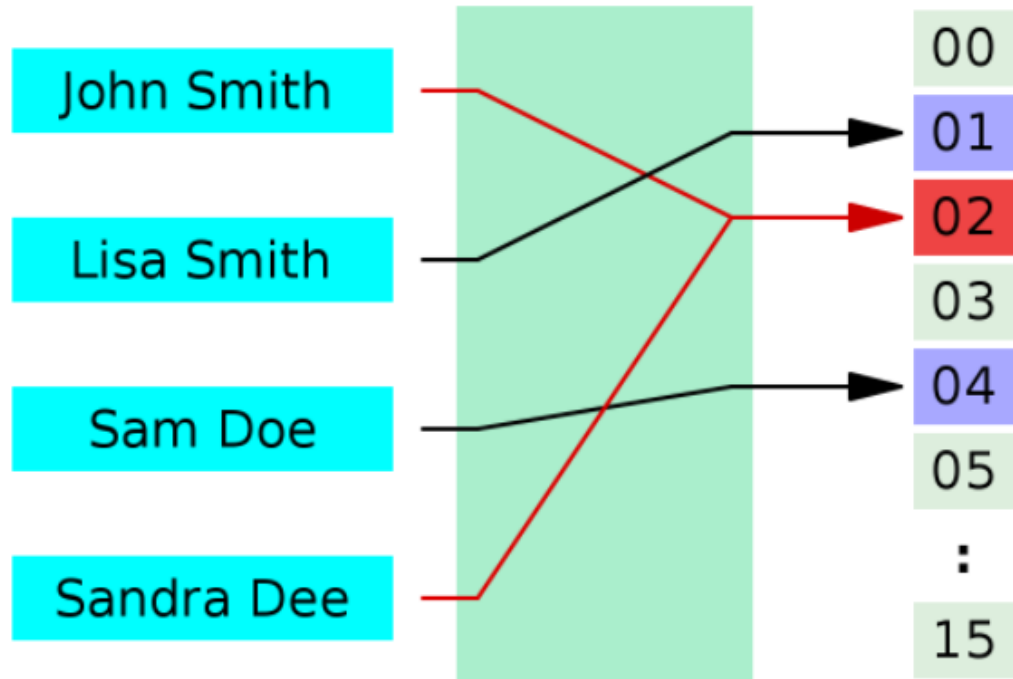
- Locality-Sensitive Hashing

**hash**

**keys**

**function**

**hashes**

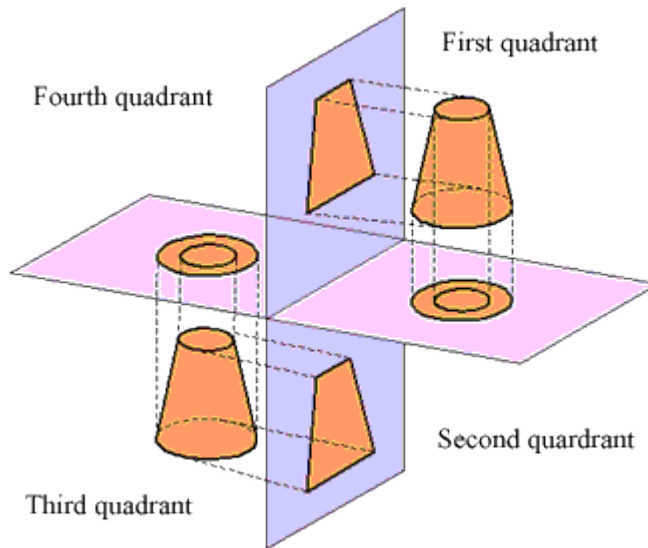


가까운 값들끼리 가까운 Hash값을 가지도록 Hashing하는 방법  
-> Locality-Sensitive Hashing

- An operation that compares actual data values is absolutely necessary.
- The comparison operation can be approximated as an operation on the hash value.

# Theoretical background

- Locality-Sensitive Hashing
  - How to machine can make locality-sensitive hash?
  - Projection method



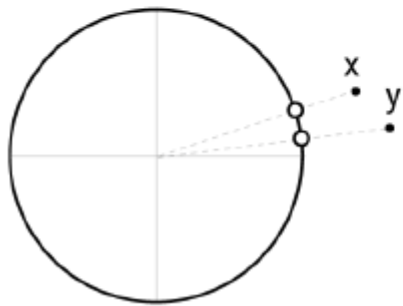
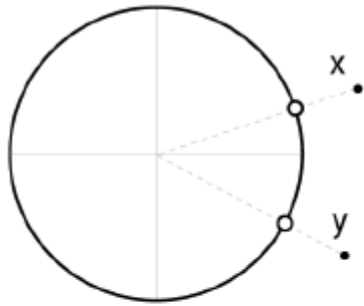
- Shared plane  $\rightarrow$  close value (+ - sign)

# Theoretical background

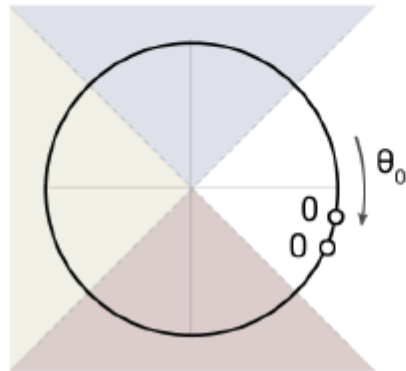
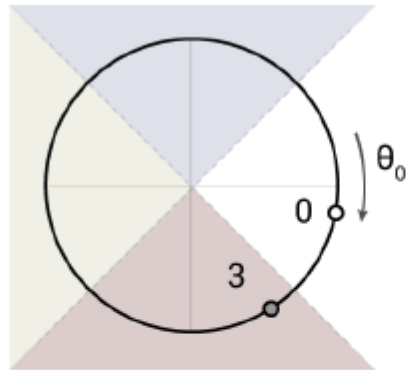
- Locality-Sensitive Hashing

- Angular LSH

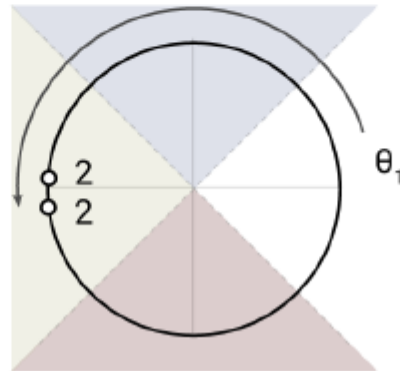
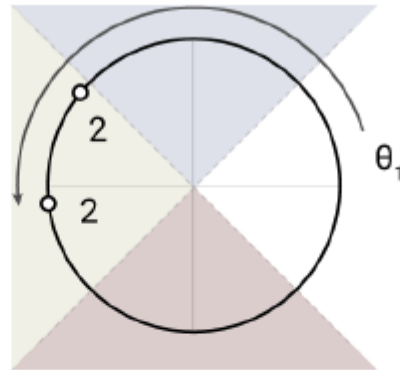
Sphere Projected Points



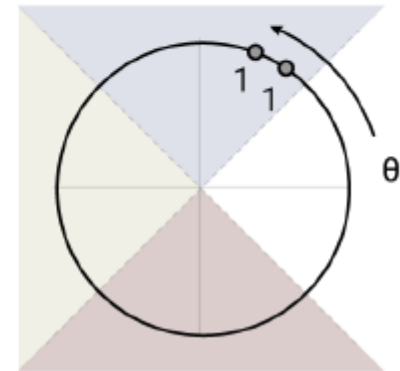
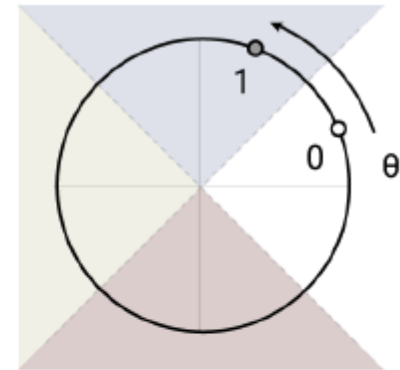
Random Rotation 0



Random Rotation 1



Random Rotation 2



x: 0 2 1

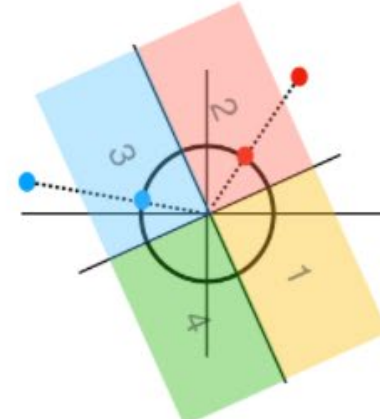
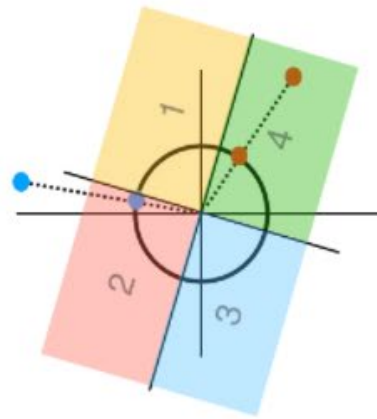
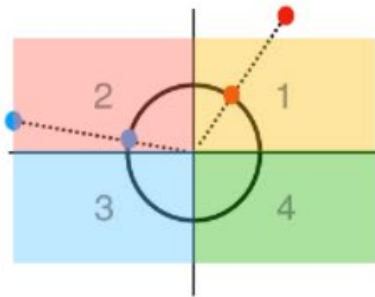
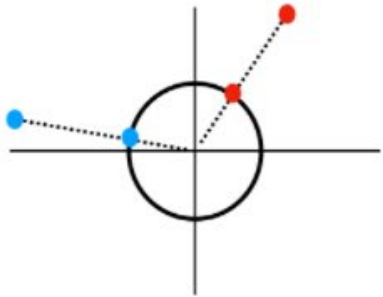
y: 3 2 0

x: 0 2 1

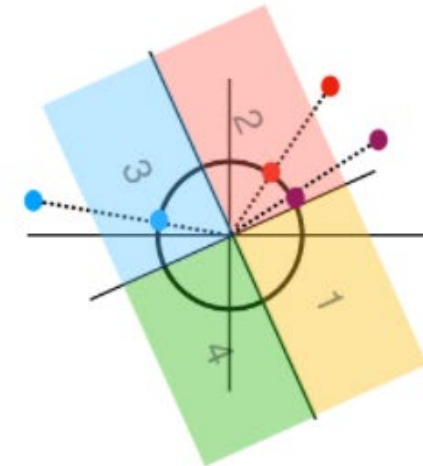
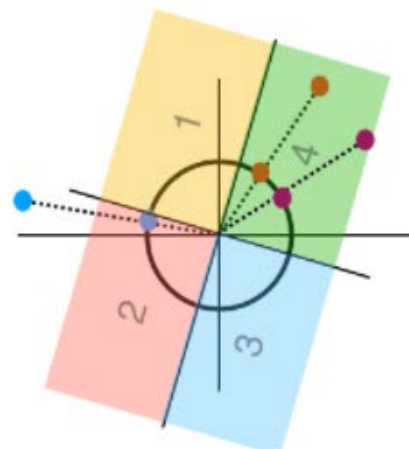
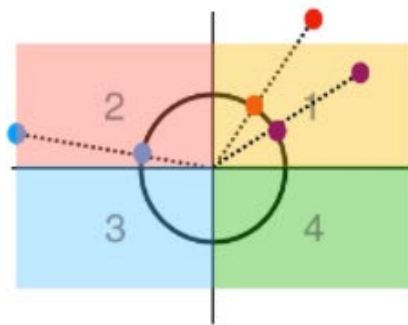
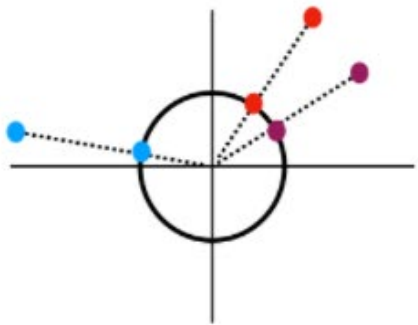
y: 0 2 1

# Theoretical background

- Locality-Sensitive Hashing



- $X1 = (3,4)$   $X2 = (-12,5)$   $X1' = (3/5, 4/5)$   $X2' = (-12/13, 5/13)$  Hash  $X1 = (1, 4, 2)$  Hash  $X2 = (2, 2, 3)$



- $Y1 = (4,3)$   $Y' = (4/5, 3/5)$  Hash  $Y1 = (1,4,2)$

Hash  $X1 = \text{Hash } Y1$

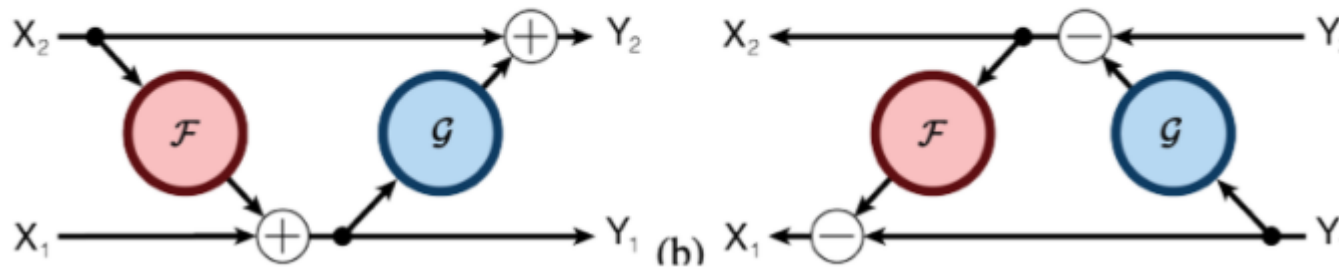
# Theoretical background

- Reversible Network
  - Residual connection (Resnet or Transformer)

$$y = x + F(x) \quad x \rightarrow y \text{ possible} \quad \text{but} \quad y \rightarrow x$$

$x = (x_1, x_2)$   $y = (y_1, y_2)$  pair representation

$$y_1 = x_1 + F(x_2), y_2 = x_2 + G(y_1)$$



$$x_2 = y_2 - G(y_1)$$

$$x_1 = y_1 - F(x_2)$$

-> reversible calculation !



# Model Architecture

- Assumption

Query (Q) = Key(K)

-If dataset is enough, not decrease performance of transformer

- LSH Attention to Transformer

- Q = K (each data query)

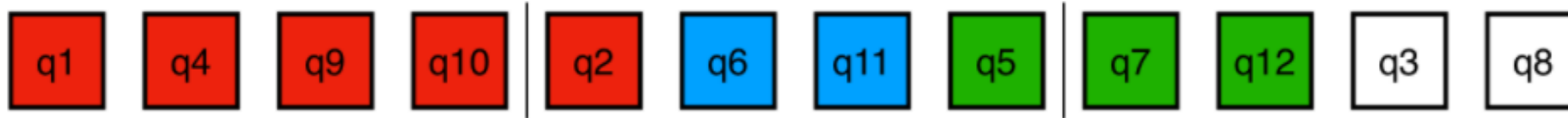


- LSH applied on each data point & Bucketing



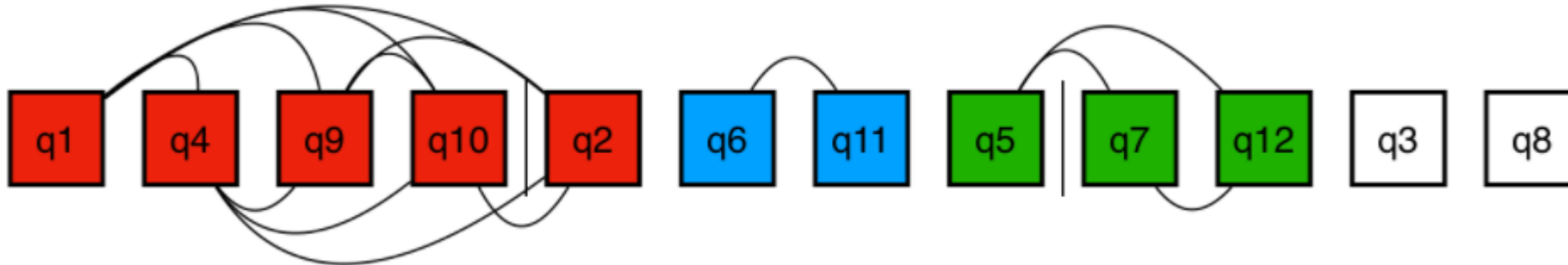
# Model Architecture

- Chunking



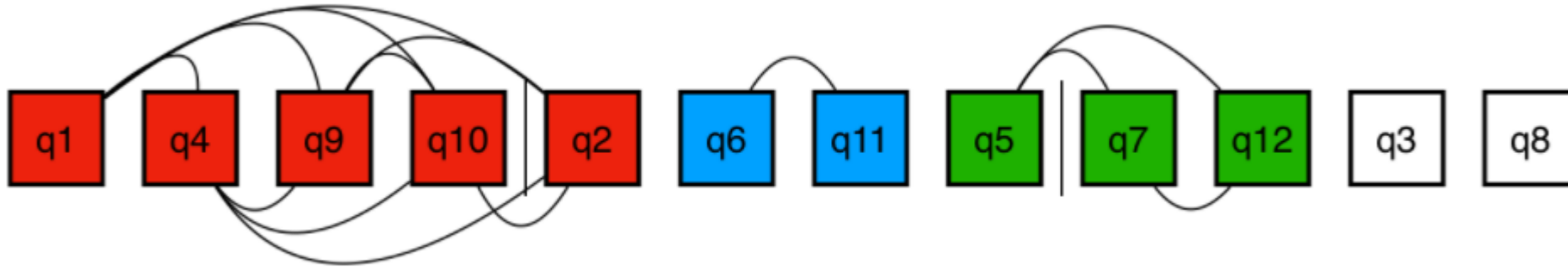
- Attention weight calculation

1. Two data point should be in same bucket (same color)
2. Two data point should be in same chunk or end point attention should be the next chunk of start point attention
3.  $Q=K \rightarrow$  Self-attention always large weight  $\rightarrow$  not allow self-attention



# Model Architecture

- Linear complexity



data point length :  $l$

chunk number :  $c$

chunked part length :  $l / c$

Attention number is portion of  $l \times (2l / c)^2$

if  $c$  is large then, approximation to linear complexity

# Feed Forward Network with Reversible Network

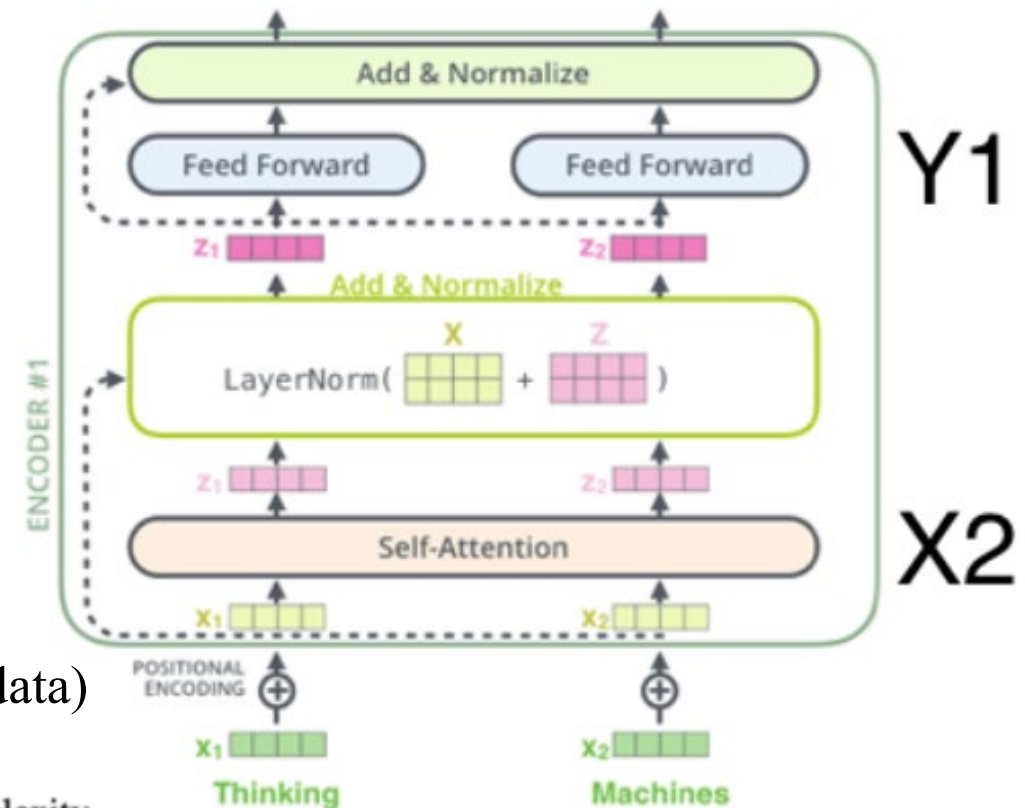
- Memory reduce from reversible network

$$y_1 = x_1 + F(x_2), y_2 = x_2 + G(y_1)$$

$$y_1 = x_1 + \text{Attention}(x_2)$$

$$y_2 = x_2 + \text{FeedForward}(y_1)$$

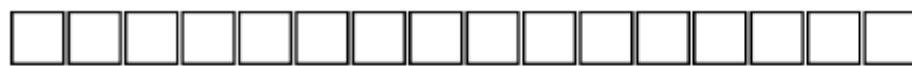
- 64K sequence -> 16K chunk ! (each chunk has 4 data)



Model Type	Memory Complexity	Time Complexity
Transformer	$\max(bld_{ff}, bn_h l^2) n_l$	$(bld_{ff} + bn_h l^2) n_l$
Reversible Transformer	$\max(bld_{ff}, bn_h l^2)$	$(bn_h l d_{ff} + bn_h l^2) n_l$
Chunked Reversible Transformer	$\max(bld_{model}, bn_h l^2)$	$(bn_h l d_{ff} + bn_h l^2) n_l$
LSH Transformer	$\max(bld_{ff}, bn_h n_r c) n_l$	$(bld_{ff} + bn_h n_r c) n_l$
Reformer	$\max(bld_{model}, bn_h n_r c)$	$(bld_{ff} + bn_h n_r c) n_l$

# Model Architecture

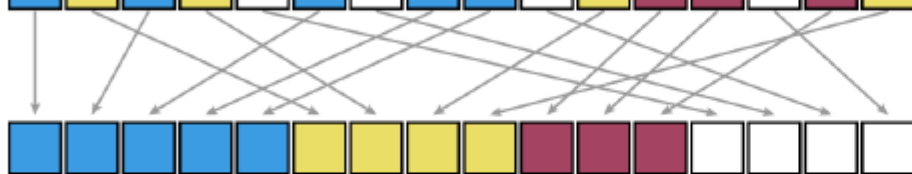
Sequence of queries=keys



LSH bucketing



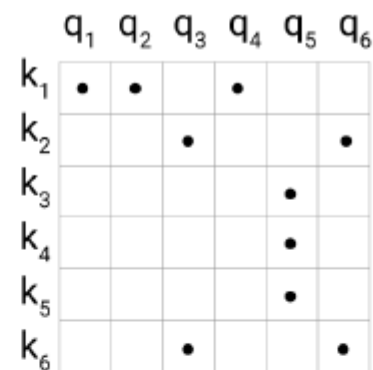
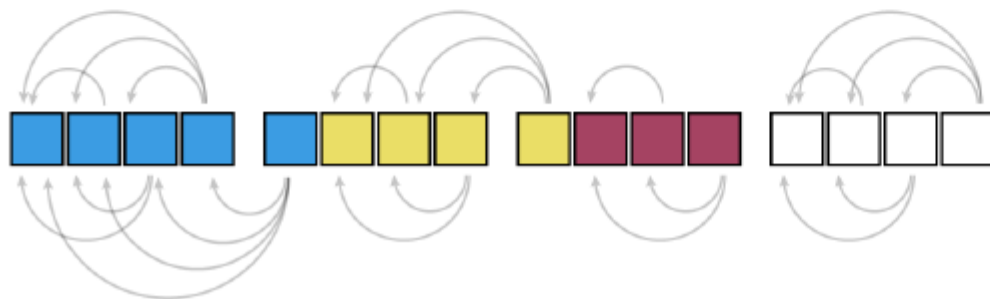
Sort by LSH bucket



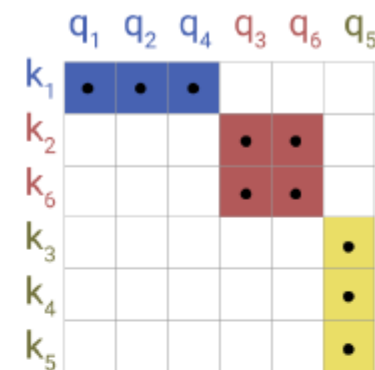
Chunk sorted sequence to parallelize



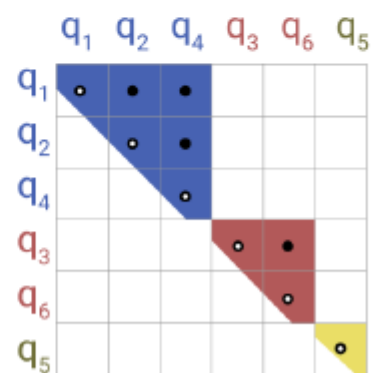
Attend within same bucket in own chunk and previous chunk



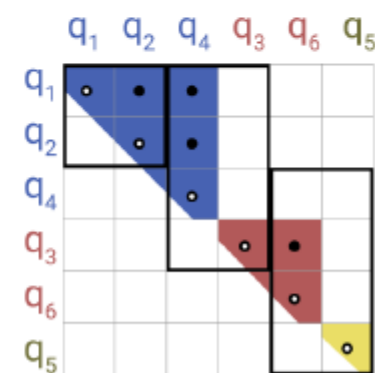
(a) Normal



(b) Bucketed



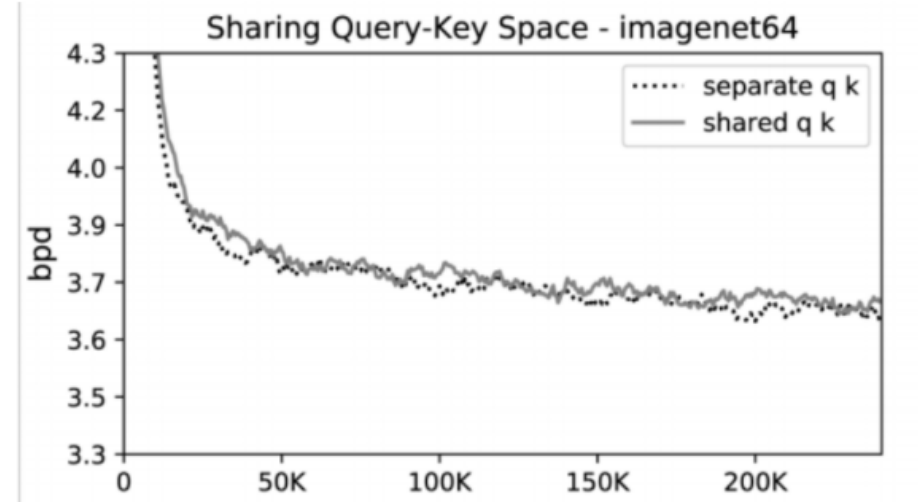
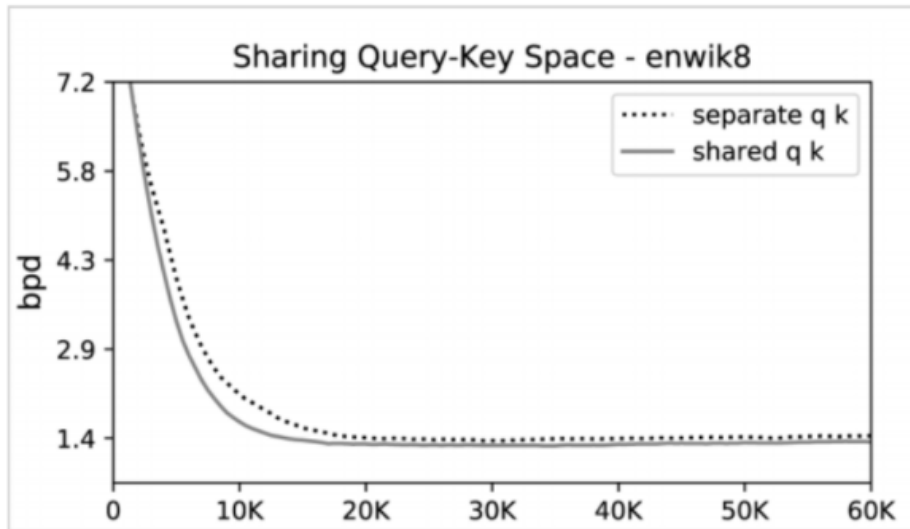
(c) Q = K



(d) Chunked

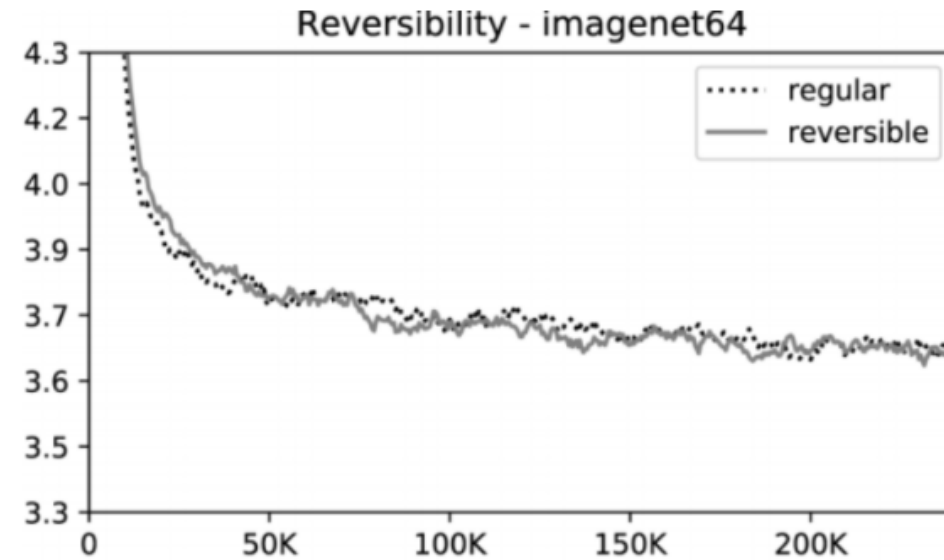
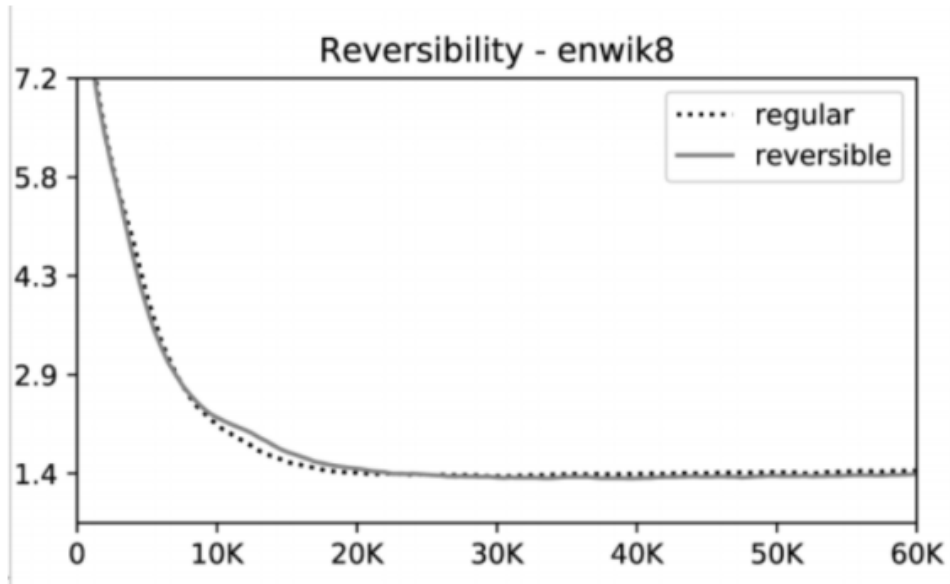
# Assumption prove

- Three main assumption
  1. Reformer structure  $Q = K$
  2. Reformer attention block  $\rightarrow$  reversible layer
  3. LSH attention  $\rightarrow$  not decrease performance of transformer & Linear complexity
- Assumption 1 :  $O = K$



# Assumption prove

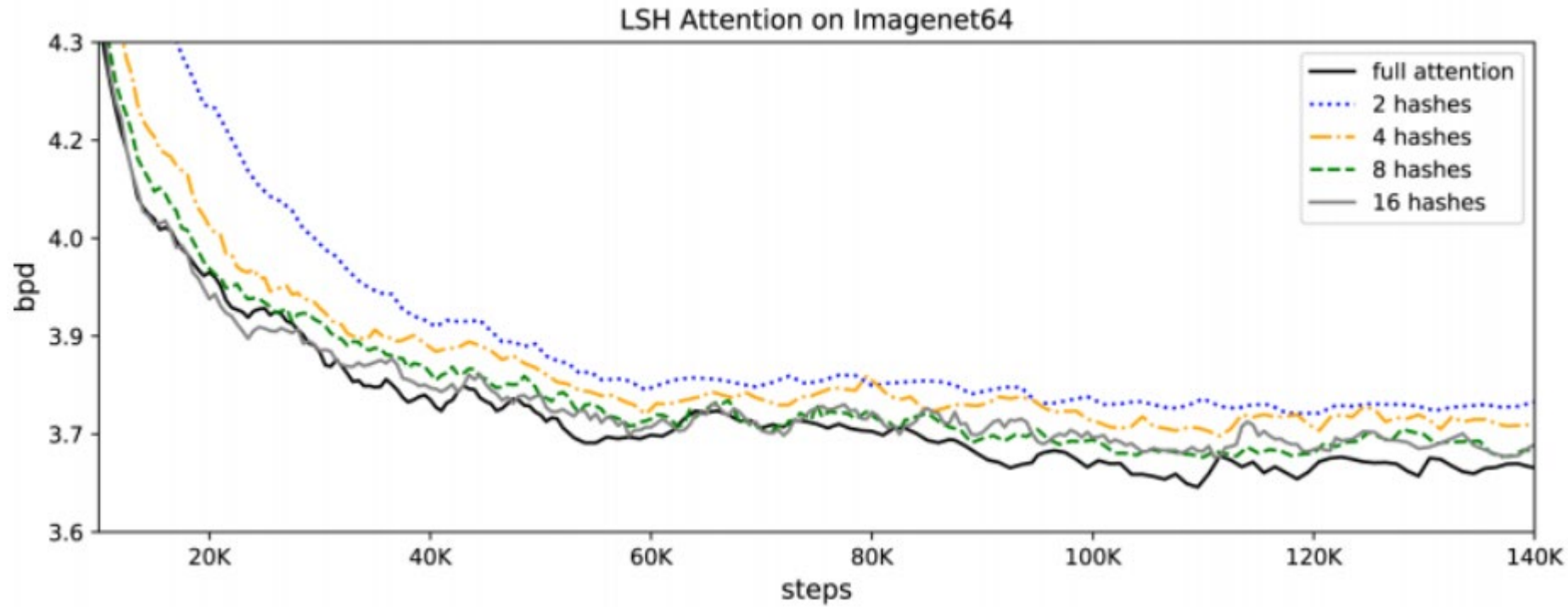
- Assumption 2: Reversible layer



- No significant difference

# Assumption prove

- Assumption 3: LSH attention

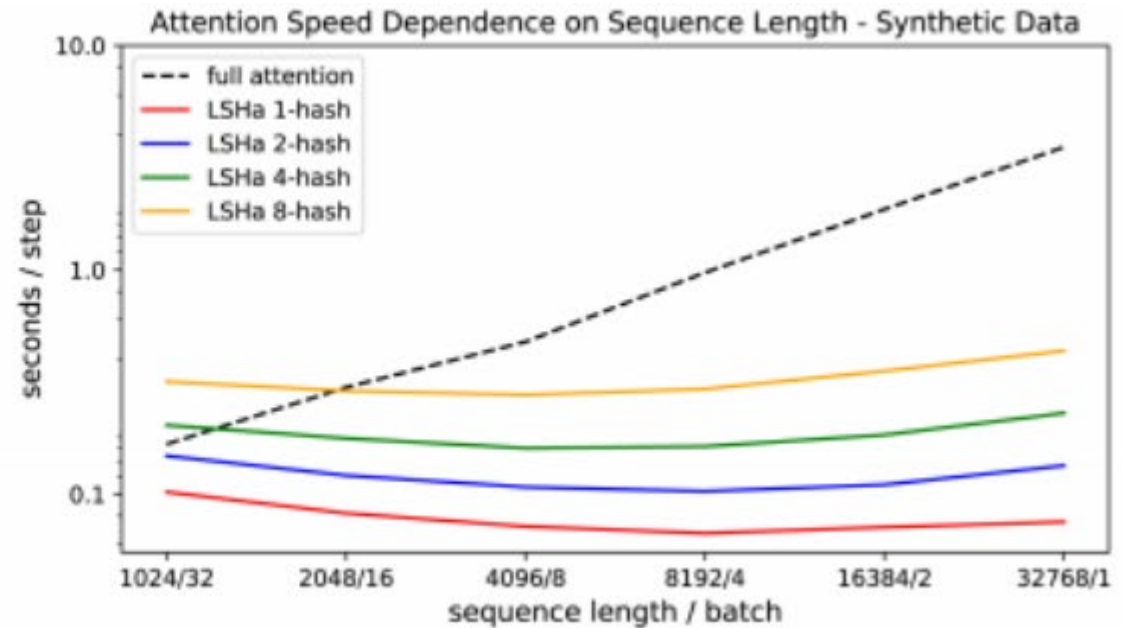
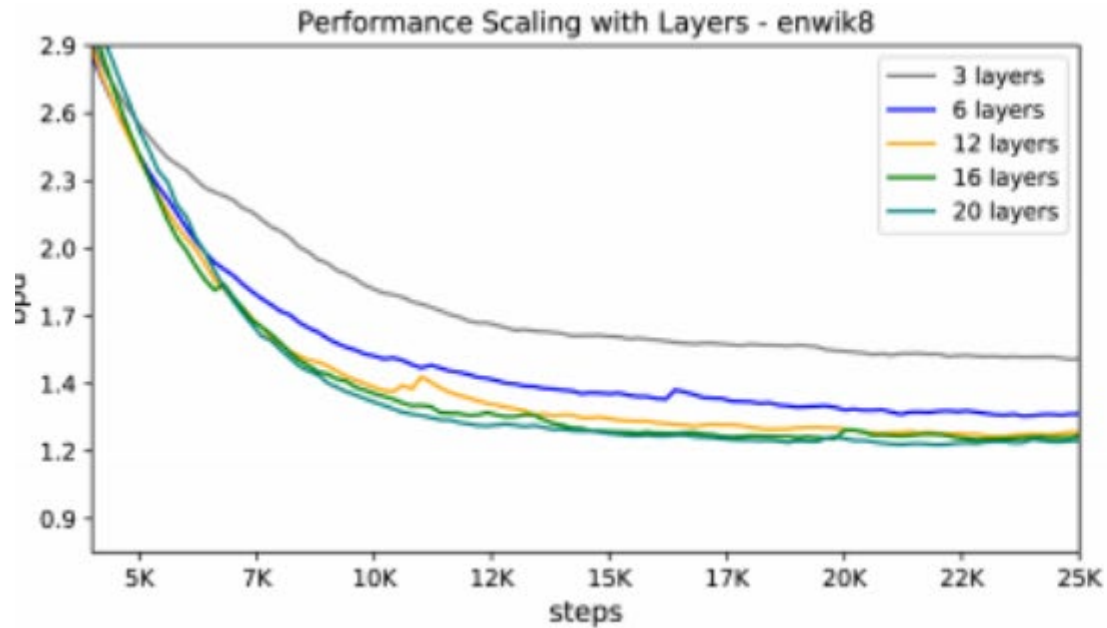


More parallel hashes -> lower gap from full attention



# Assumption prove

- Assumption 3: LSH attention



- Performance (bits per dimension)
- Consistent speed on length

# Appendix

- Angular LSH
  - Magnitude / norm
  - Angular LSH -> Transformer Layer normalization (scale is not important)
  - cosine similiarity -> Comparison between Euclidean space and Spherical space
- LSH validty

Train \ Eval					
	Full Attention	LSH-8	LSH-4	LSH-2	LSH-1
Full Attention	100%	94.8%	92.5%	76.9%	52.5%
LSH-4	0.8%	100%	99.9%	99.4%	91.9%
LSH-2	0.8%	100%	99.9%	98.1%	86.8%
LSH-1	0.8%	99.9%	99.6%	94.8%	77.9%



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**End of presentation**