730 Group Project

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2024-11-30

Amani's Model: weighted linear regression

```
newdata <- read_csv("FreqCategories.csv") %>% mutate(Weight = Freq / sum(Freq))
## New names:
## Rows: 5462 Columns: 9
## -- Column specification
## ----- Delimiter: "," chr
## (2): AgeCat, EduCat dbl (7): ...1, y, REGION, SEX, RACENEW, POORYN, Freq
## i Use 'spec()' to retrieve the full column specification for this data. i
## Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## * '' -> '...1'
newdata <-mutate (newdata, weight.var=1/Freq) %% mutate (REGION=as.factor(REGION)) %% mutate (AgeCat=as.f
#converting y's into factor variable, changing range from 0-8 to 1-9 to match with model output
newdata1<-mutate(newdata, y=y+1) %>% mutate(y, factor(y, ordered=TRUE))
modA <- brm(
 y | weights(Weight) ~ (1 | REGION + AgeCat + SEX + RACENEW + EduCat + POORYN),
 family = gaussian(),
 data = newdata1,
 iter = 1000,
 chains = 4,
 cores = getOption("mc.cores", 4),
 seed = 12345
## Compiling Stan program...
## Start sampling
summary(modA)
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: y | weights(Weight) ~ (1 | REGION + AgeCat + SEX + RACENEW + EduCat + POORYN)
```

```
##
     Data: newdata1 (Number of observations: 5462)
##
    Draws: 4 chains, each with iter = 1000; warmup = 500; thin = 1;
           total post-warmup draws = 2000
##
##
## Multilevel Hyperparameters:
## ~AgeCat (Number of levels: 3)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
                                                               2338
## sd(Intercept)
                               2.35
                                       0.08
                     2.46
                                                 8.39 1.00
                                                                          992
##
## ~EduCat (Number of levels: 4)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                               2.12
                                       0.09
                                                 7.93 1.00
## sd(Intercept)
                     2.39
                                                               1998
                                                                        1179
## ~POORYN (Number of levels: 2)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)
                     2.55
                               2.36
                                        0.12
                                                 8.83 1.00
                                                               1689
                                                                         1088
##
## ~RACENEW (Number of levels: 6)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)
                     2.48
                               2.31
                                       0.08
                                                 8.55 1.00
                                                               2080
##
## ~REGION (Number of levels: 4)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
##
                     2.32
                               2.26
                                       0.07
                                                 7.90 1.00
## sd(Intercept)
                                                             1739
##
## ~SEX (Number of levels: 2)
                Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                     2.50
                               2.46
                                        0.10
                                                 8.54 1.00
## sd(Intercept)
                                                               2590
##
## Regression Coefficients:
##
             Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept
                 3.67
                           3.67
                                   -3.94
                                            10.73 1.00
                                                           2520
                                                                     1185
## Further Distributional Parameters:
         Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma
                      4.21
                                1.87
                                        14.78 1.00
            5.89
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

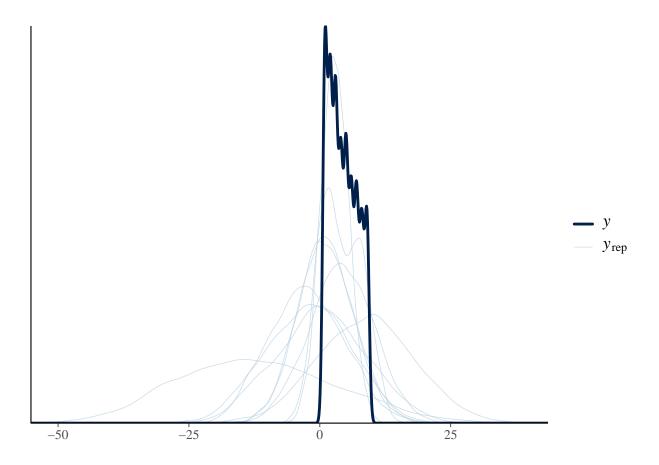
prior_summary(modA)

##	prior			class	coef	group	resp	dpar	nlpar	1b	ub
##	student_t(3,	4,	3)	Intercept							
##	student_t(3,	Ο,	3)	sd						0	
##	student_t(3,	Ο,	3)	sd		AgeCat				0	
##	student_t(3,	Ο,	3)	sd	Intercept	AgeCat				0	
##	student_t(3,	Ο,	3)	sd		EduCat				0	
##	student_t(3,	Ο,	3)	sd	Intercept	EduCat				0	
##	student_t(3,	Ο,	3)	sd		POORYN				0	
##	student_t(3,	Ο,	3)	sd	Intercept	POORYN				0	
##	student_t(3,	Ο,	3)	sd		RACENEW				0	
##	student_t(3,	Ο,	3)	sd	Intercept	RACENEW				0	

```
student_t(3, 0, 3)
                                              REGION
                                                                       0
##
                               sd
##
    student_t(3, 0, 3)
                                              REGION
                                                                       0
                               sd Intercept
##
    student_t(3, 0, 3)
                                                 SEX
                                                                       0
##
    student_t(3, 0, 3)
                               sd Intercept
                                                 SEX
                                                                       0
                                                                       0
##
    student_t(3, 0, 3)
                            sigma
##
          source
##
         default
         default
##
##
    (vectorized)
##
    (vectorized)
    (vectorized)
    (vectorized)
##
##
    (vectorized)
##
    (vectorized)
##
    (vectorized)
##
    (vectorized)
##
    (vectorized)
    (vectorized)
##
    (vectorized)
##
    (vectorized)
##
         default
##
```

pp_check(modA)

Using 10 posterior draws for ppc type 'dens_overlay' by default.



Analysis with Amani's Model

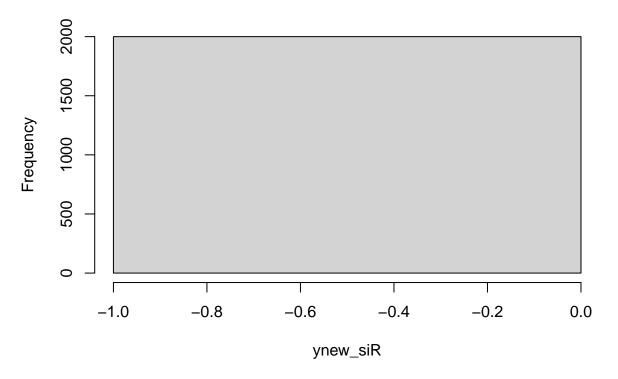
```
observed_counts <- select(newdata1, c(y, Freq))
total_freq<-group_by(observed_counts, y) %>% summarise(total=sum(Freq))
observed_props<-mutate(total_freq, observed=total/sum(total)) %>% mutate(y=as.factor(y))

get_sum_stat<-function(y, row){(sum(y==5))/nrow(row)}

tobs<-observed_props[5,3]

predicted_catsR<-as.data.frame(posterior_predict(modA))
ynew_siR<-apply(predicted_catsR, 1, get_sum_stat, newdata)
#ppc for proportion of observations in category 5
hist(ynew_siR)
abline(v = tobs)</pre>
```

Histogram of ynew_siR



```
#ppc for all categories
#formatting for ggplot
posterior_preds_longR <- predicted_catsR %>%
    pivot_longer(cols = everything(), names_to = "chain", values_to = "predicted_category")
posterior_preds_longR$predicted_category <- as.factor(posterior_preds_longR$predicted_category)</pre>
```

Warning: Removed 9 rows containing missing values or values outside the scale range
('geom_bar()').

Mental Health Category Proportions for Observed and Predicted Data

