ARTICLE TITLE

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ABSTRACT

In this report, we are going to try several configurations and with Simgrid, we will evaluate our programs and compare the sequential algorithms with the parralel algorithms. The topology I used for this is a clique. The platform file and the hostfile were generated using a modification of the script that was given to us during TPs and was originally meant to generate a ring topology. I precise that I will not use ring topology because I think it is not necessary (there is no interest to run a graph algorithm on a ring). Moreover, I find it too bad that I one link is broken, the network can not work.

We are going to separate the analysis of the Kruskal's algorithm and Prim's algorithm. To do the analysis, we will test several cases. First I note G = (V, E) our graph and n = |V| and m = |E|. We will test three cases for m:

•
$$m = 2 \times n$$
 (linear)

•
$$m = \frac{n^{\frac{3}{2}}}{2}$$

And I will test those configurations for n=500 (my laptop can not handle bigger graphs). I will test this with 4 cores and 10 cores. I will take 500 for the maximum weight. Indeed, this value should not have a lot of consequences on the speed of the algorithm. I will also test a latency of 1µs and 100µs. I will call the linear graph (with $m=2\times n$) the linear graph and the graph with $m=\frac{n^{\frac{3}{2}}}{2}$ the $\frac{3}{2}$ graph.

2 RESULTS OF THE TESTS

2.1 Sequential algorithms

Table 1: Speed of the sequential algorithms (in seconds)

| | Linear | 3/2 |
|---------|---------------------|-----------------------|
| Prim | 5× 10 ⁻³ | 5.3× 10 ⁻³ |
| Kruskal | 2×10^{-3} | 3.4× 10 ⁻³ |

2.2 Parallel Prim's algorithm

Table 2: Speed of the parallel Prim's algorithm (in seconds)

| | 1μs/4 cores | 1μs/8 cores | 100µs/4 cores | 100µs/8 cores |
|--------|---------------------|---------------------|---------------------|---------------------|
| Linear | 3× 10 ⁻³ | 4× 10 ⁻³ | 3× 10 ⁻¹ | 4× 10 ⁻¹ |
| 3/2 | 3× 10 ⁻³ | 4× 10 ⁻³ | 3× 10 ⁻¹ | 4× 10 ⁻¹ |

2.3 Parallel Kruskal's algorithm

Table 3: Speed of the parallel Kruskal's algorithm (in seconds)

| | 1µs/4 cores | 1μs/8 cores | 100µs/4 cores | 100µs/8 cores |
|--------|-----------------------|-----------------------|-----------------------|-----------------------|
| Linear | 9× 10 ⁻⁶ | 1.3× 10 ⁻⁵ | 8.6×10^{-4} | 1.3× 10 ⁻³ |
| 3/2 | 9.3× 10 ⁻⁶ | 1.4× 10 ⁻⁵ | 8.5× 10 ⁻⁴ | 1.2×10^{-3} |

First, we can see that there is little different between the linear graph and the 3/2 graph. That could be expected because in every cases, because the graph is represented by a matrix, the complexity will always depends on n^2 and not on m. This is why we do not have a lot of differences between the linear graph and the 3/2 graph, the number of edges has little effect on the number of steps that the algorithm will do.

Moreover, we see that when running the parallel algorithms on 8 cores, it is a bit slower that on 4 cores. I think this comes from the fact that my processor has only 4 cores and when running the algorithms on 8 cores, I do not computation time but I loose time in communications between the "virtual" processors. Now we will compare the sequential algorithms. I will just study the linear graph because we saw that the results were similar with the 3/2 graph. I will only study the case with 4 cores because this is when my computer is the more efficient.

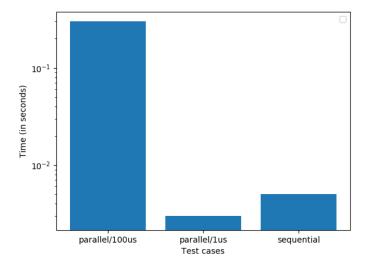


Figure 1: Comparison of sequential Prim's algorithm and parallel Prim's algorithm

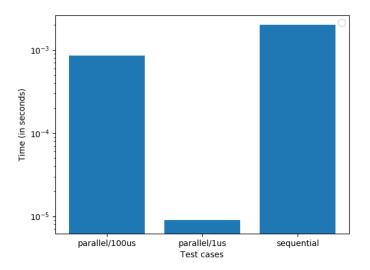


Figure 2: Comparison of sequential Kruskal's algorithm and parallel Kruskal's algorithm

COMPARISON BETWEEN SEQUENTIAL AND PARALLEL 3 **ALGORITHMS**

Sequential Prim VS Parallel Prim

As we can see on figure 1 the sequential algorithm is a little worst than the parallel one with a latency of $1\mu s$ but a lot better than the parallel one with a latency of 100μ (please note that the scale is logarithmic). One can conclude that the latency has a lot of influence on the efficiency of the parallel Prim's algorithm. This is probably due to the fact that when all the processors have their candidates, they have to send it the processor o that has to handle a lot of communications at one time, and during this time the other processor are not working.

3.2 Sequential Kruskal VS Parallel Kruskal

As we can see on figure 2, for a latency of 1µs, the parallel algorithm is a lot better than the sequential one. For a latency of 100µs, the parallel algorithm is a little better than the sequential one. First conclusion, the efficiency of the parallel algorithm is a lot better. I think we can explain this because in the parallel Kruskal, a processor wait little for another one. Indeed a processor do some computations send or receive informations and then continue working but is does not need to wait for an answer of the processor it communicated with. Also, the algorithm is a lot less "centralized". There is no processor that have to regularly get informations from everyone, a processor only work with one close neighbor. I think this is why the parallel algorithm is a lot better.