BRI509: Introduction to Brain Signal Processing Assignment No. 2

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(a) Draw the Bode diagrams of Do(C4), Mi(E4), Sol(G4) and their chord(C4+E4+G4).

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Source Code
1 % BRI509 (Introduction to Brain Signal Processing)
2 % Assignment # 3
3 % Author: Raymart Jay E. Canoy
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6 % Notes:
_{7} % "The frequencies 440 Hz and 880 Hz both correspond to the
     musical note A,
8 % but one octave apart. In the western musical scale, there
     are 12 notes in
9 % every octave. These notes are evenly distributed (
     geometrically), so the
_{10} % next note above A, which is B flat, has frequency (440 x
     beta), where
11 % beta is the twelfth root of two."
12 % Source: https://ptolemy.berkeley.edu/eecs20/week8/scale.html
14 %% Draw the Bode diagrams of:
15 % (a) Do(C4)
    (b) Mi(E4)
17 % (c) Sol(G4)
18 % (d) Chord(C4+E4+G4)
20 % (00) Initialization
21 clear; clc;
23 \text{ fs} = 1200;
24 T = 1/fs;
25 dur = 1;
26 L = dur*fs;
_{27} t = (0:L-1)*T;
29 % (01) Sinusoid signal
30 beta = 2^(1/12);
31 beta_exponents = [-9, -7, -5, -4, -2, 0, 2, 3];
32 note = @(index) sin(2*pi*(440*(beta^(index)))*t);
```

```
34 % C major
35 musical_scale_keys = {'C4', 'D4', 'E4', 'F4', 'G4', 'A4', 'B4'
36 musical_scale_values = cell(length(musical_scale_keys), 1);
38 for ind = 1 : length(musical_scale_keys)
      musical_scale_values{ind} = note(beta_exponents(ind));
39
40 end
42 % (02) Sofege for C major
43 music_octave = containers.Map(musical_scale_keys,
     musical_scale_values);
45 %% (03) Bode Diagram
46 assignment = {'C4', 'E4', 'G4'};
47 beta_exponents_assigment = [-9, -5, -2];
48 chord = music_octave('C4') + music_octave('E4') + music_octave
     ('G4');
49
50 \text{ for } i = 1 : 4
      % Fourier Transform
      n = 256*2^(nextpow2(L));
52
      if i < 4
          x = music_octave(assignment{i});
54
55
56
          x = chord;
57
      end
      X = fftshift(fft(x, n, 2));
58
60
      f = [0: fs/n : fs/2 - fs/n];
      PdB = 20*log10(2*abs(X(end/2+1:end)./L));
61
      phase = rad2deg(angle(X(end/2+1:end)));
62
63
64
      A = [ones(size(f, 2), 1), [1:1:size(f, 2)]'];
      theta = pinv(A'*A)*(A'*f');
65
66
      if i < 4
67
          f_center_index = round((440*(beta^(
68
     beta_exponents_assigment(i))) - theta(1))/theta(2));
```

```
else
69
70
          f_center_index = 144017;
71
      end
      figure,
72
      p1 = plot([0: fs/n : fs/2 - fs/n], 2*abs(X(end/2+1:end)./L
     ), 'k')
      grid on
74
      xlim([0 fs/2])
      ylim([0 1])
76
      xlabel('Frequency, $f$ ($Hz$)', 'Interpreter', 'Latex', '
77
     FontSize', 16)
      ylabel('$|X(f)|$', 'Interpreter', 'Latex', 'FontSize', 16)
      if i < 4
80
          title(sprintf('Single-sided spectrum of %s (f = %2f Hz
     )', assignment{i}, 440*(beta^(beta_exponents_assignent(i)))
     ))
      else
          title('Single-sided spectrum of chord (C4+E4+G4)')
82
83
      saveas(gcf, sprintf('FFT_Prob%02d.png', i))
84
85
86
      figure;
      ax1 = axes();
87
      plot(ax1, f, PdB, 'k');
88
89
      hold on
      if i < 4
90
          plot(ax1, f(f_center_index - 5000)*ones(1200, 1),
91
     linspace(min(PdB), max(PdB), 1200), 'r', 'LineWidth', 1);
          plot(ax1, f(f_center_index + 5000)*ones(1200, 1),
92
     linspace(min(PdB), max(PdB), 1200), 'r', 'LineWidth', 1);
      else
93
          plot(ax1, f(f_center_index - 35000)*ones(1200, 1),
     linspace(min(PdB), max(PdB), 1200), 'r', 'LineWidth', 1);
95
          plot(ax1, f(f_center_index + 35000)*ones(1200, 1),
     linspace(min(PdB), max(PdB), 1200), 'r', 'LineWidth', 1);
96
      end
      set(gca, 'xscale', 'log')
97
      grid on
98
      xlim([min(f) max(f)])
99
```

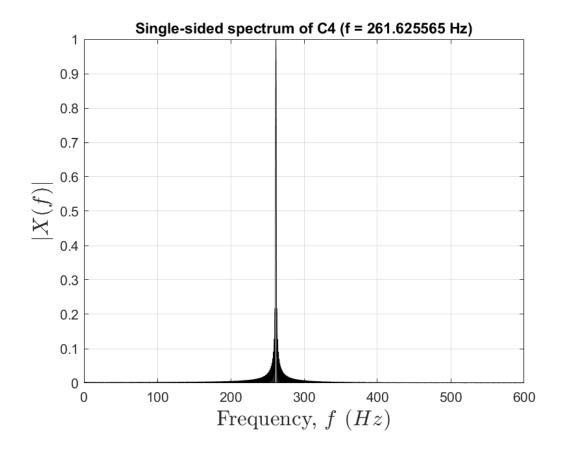
```
ylim([min(PdB) max(PdB)])
100
101
      xlabel('$\omega / 2\pi$', 'Interpreter', 'Latex', '
     FontSize', 16)
      ylabel('$|X(f)|_{dB}$', 'Interpreter', 'Latex', 'FontSize'
102
      , 16)
      if i < 4
           title(sprintf('Bode Diagram of %s (f = %2f Hz) [
104
     Amplitude]', assignment{i}, 440*(beta^(
     beta_exponents_assigment(i))))
105
           title('Bode Diagram of chord (C4+E4+G4) [Amplitude]')
06
      end
107
      ax2 = axes('Position', [0.2 0.5 0.3 0.3]);
109
      ax2.XColor = 'red';
      ax2.YColor = 'red';
      if i < 4
111
          plot(ax2, f(f_center_index - 5000:f_center_index+5000)
112
      , PdB(f_center_index - 5000:f_center_index+5000), 'k')
113
14
          plot(ax2, f(f_center_index - 35000:f_center_index
     +35000), PdB(f_center_index - 35000:f_center_index+35000),
      'k')
      end
      set(gca, 'xscale', 'log', 'XColor', 'red', 'YColor', 'red'
116
17
      grid on
      ylim([min(PdB) max(PdB)])
18
      saveas(gcf, sprintf('Bode_diagram%02d.png', i))
19
20
121
      figure;
      ax1 = axes();
122
      plot(ax1, f, phase, 'k');
124
      hold on
125
      if i < 4
          plot(ax1, f(f_center_index - 5000)*ones(1200, 1),
126
     linspace(min(phase), max(phase), 1200), 'r', 'LineWidth',
          plot(ax1, f(f_center_index + 5000)*ones(1200, 1),
     linspace(min(phase), max(phase), 1200), 'r', 'LineWidth',
```

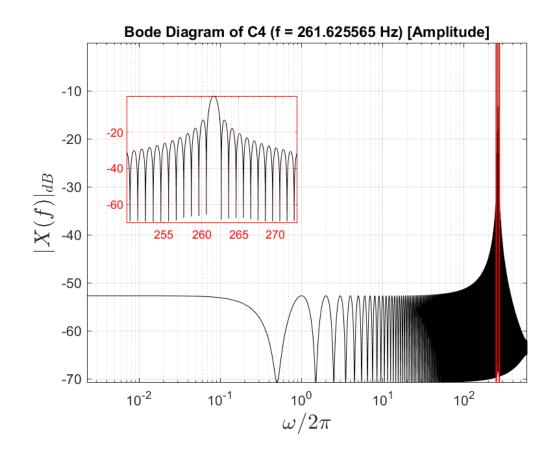
```
1);
          plot(ax1, f(f_center_index - 35000)*ones(1200, 1),
129
     linspace(min(phase), max(phase), 1200), 'r', 'LineWidth',
          plot(ax1, f(f_center_index + 35000)*ones(1200, 1),
     linspace(min(phase), max(phase), 1200), 'r', 'LineWidth',
     1);
      end
      set(gca, 'xscale', 'log')
132
      grid on
      xlim([min(f) max(f)])
134
      ylim([min(phase) max(phase)])
136
      xlabel('$\omega / 2\pi$', 'Interpreter', 'Latex', '
     FontSize', 16)
      ylabel('$\angle X(f)$ (deg)', 'Interpreter', 'Latex', '
     FontSize', 16)
      if i < 4
          title(sprintf('Bode Diagram of %s (f = %2f Hz) [Phase]
39
      , assignment{i}, 440*(beta^(beta_exponents_assignent(i))))
40
      else
          title('Bode Diagram of chord (C4+E4+G4) [Phase]')
41
142
      ax2 = axes('Position', [0.177 0.16 0.3 0.3]);
      ax2.XColor = 'red';
44
      ax2.YColor = 'red';
45
      if i < 4</pre>
46
          plot(ax2, f(f_center_index - 5000:f_center_index+5000)
47
      , phase(f_center_index - 5000:f_center_index+5000), 'k')
48
          plot(ax2, f(f_center_index - 35000:f_center_index
     +35000), phase(f_center_index - 35000:f_center_index+35000)
     , 'k')
      end
150
      set(gca, 'xscale', 'log', 'XColor', 'red', 'YColor', 'red'
      grid on
152
      ylim([min(phase) max(phase)])
```

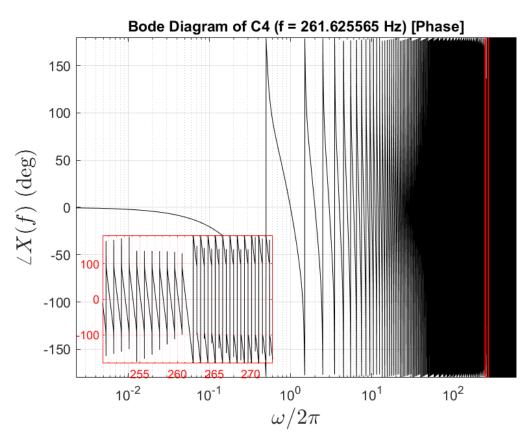
```
saveas(gcf, sprintf('Bode_diagram_phase%02d.png', i))
155 end
156
158 %% (04) Audio Files
159 % (00) Initialization
160 clear; clc;
161
62 \text{ fs} = 48000;
_{63} T = 1/fs;
64 dur = 1;
65 L = dur*fs;
66 t = (0:L-1)*T;
68 % (01) Sinusoid signal
_{69} beta = 2^{(1/12)};
[70 \text{ beta_exponents} = [-9, -7, -5, -4, -2, 0, 2, 3];
71 note = @(index) sin(2*pi*(440*(beta^(index)))*t);
173 % C major
musical_scale_keys = \{'C4', 'D4', 'E4', 'F4', 'G4', 'A4', 'B4'\}
     , 'C5'};
75 musical_scale_values = cell(length(musical_scale_keys), 1);
for ind = 1 : length(musical_scale_keys)
      musical_scale_values{ind} = note(beta_exponents(ind));
179 end
81 % (02) Sofege for C major
82 music_octave = containers.Map(musical_scale_keys,
     musical_scale_values);
84 \text{ assignment} = \{'C4', 'E4', 'G4'\};
test chord = music_octave('C4') + music_octave('E4') + music_octave
      ('G4');
187 \text{ for } i = 1 : 4
188
     if i < 4
           mp3_file = [zeros(1, 100) music_octave(assignment{i})
```

```
zeros(1, 100)]';
    audiowrite(sprintf('
    Assigment3_2020021376_CanoyRaymartJay_%s.mp4', assignment{i
}), mp3_file, fs)
else
    mp3_file = [zeros(1, 100) chord zeros(1, 100) zeros(1,
    100)]';
    audiowrite(sprintf('
    Assigment3_2020021376_CanoyRaymartJay_%s.mp4', 'chord'),
    mp3_file, fs)
end
end
```

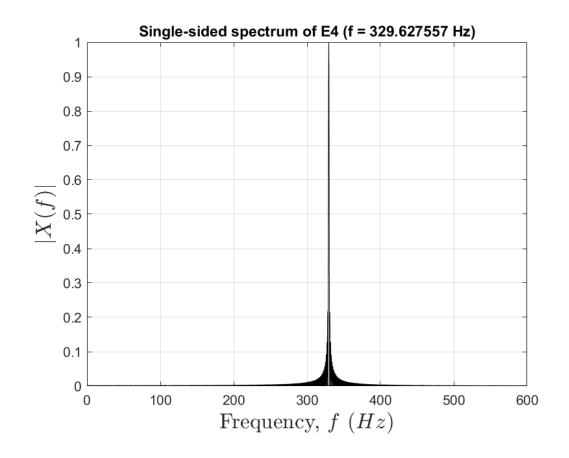
(b) Bode diagram of C4

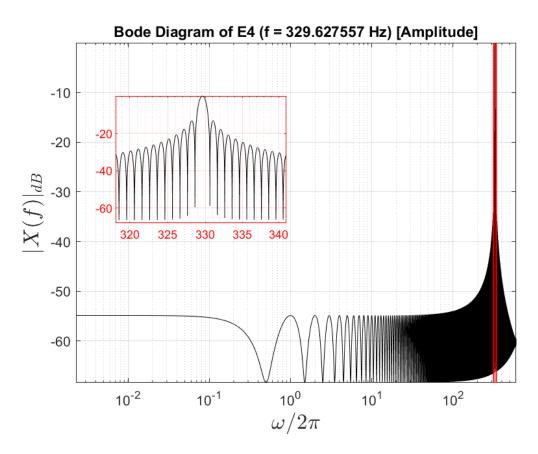


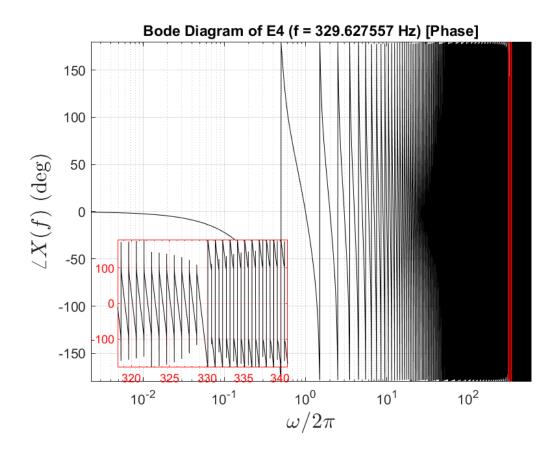




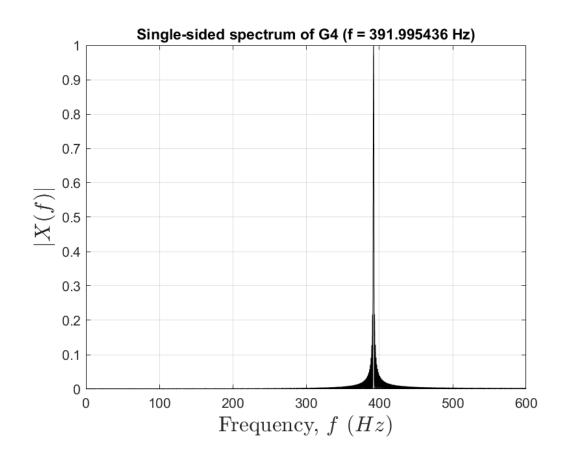
(c) Bode diagram of E4

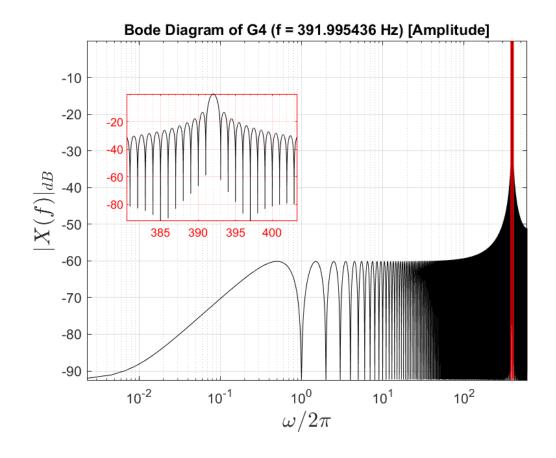


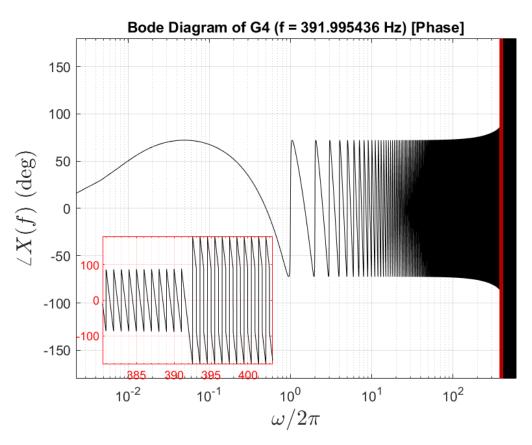




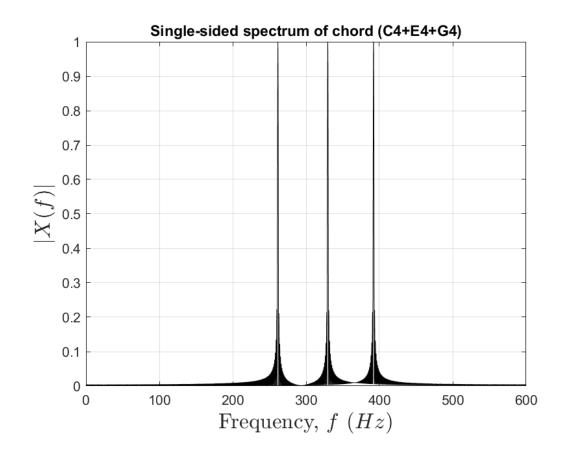
(d) Bode diagram of G4

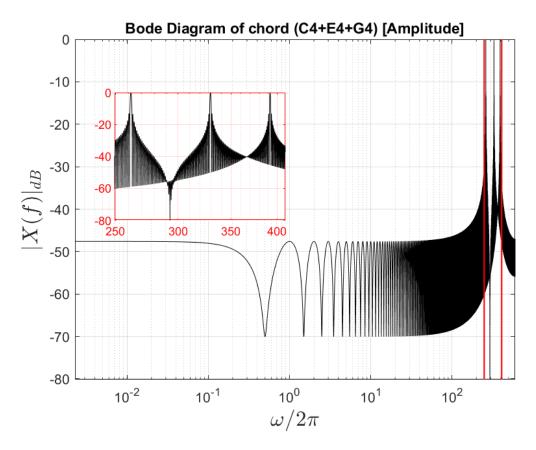


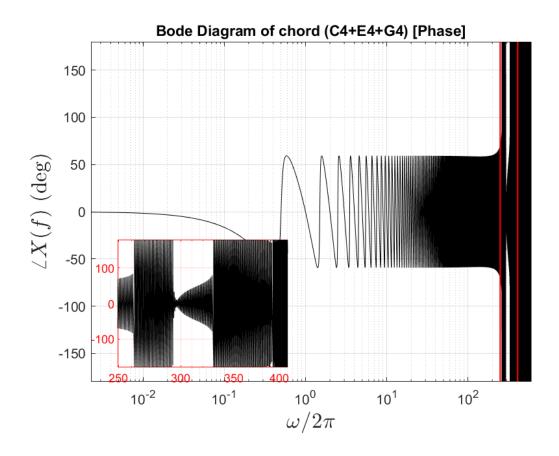




(e) Bode diagram of C4+E4+G4







Note: All the files were uploaded on GitHub

All the files in this document were uploaded on Github, and can be accessed at:

https://github.com/rjcanoy03/BRI509/tree/Assignment%233

If there are errors in the solution or codes kindly email, recanoy@korea.ac.kr.