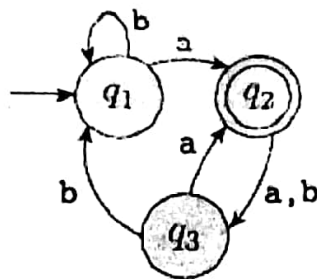


Answer the following questions.

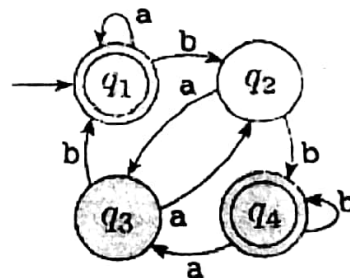
1. a. Consider the following language ( $\Sigma = \{0,1\}$ )  
 $L = \{w \mid \text{the number of zeros in } w \text{ is less than the number of ones}\}$   
 Use pumping lemma to prove that  $L$  is not regular. 5

- b. Let,  $A$  be a language and  $NoPrefix$  is an operation on  $A$  as defined below:  
 $NoPrefix(A) = \{w \in A \mid \text{no proper prefix of } w \text{ is a member of } A\}$   
 Prove that the class of regular language is closed under the operation  $NoPrefix$ . 5

2. a. Consider the following DFAs. 3+3



$M_1$

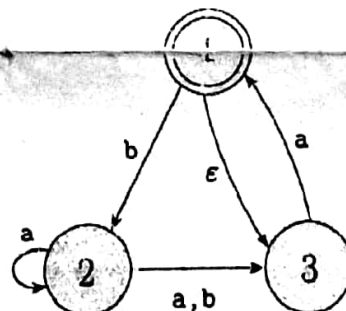


$M_2$

Draw finite state machines that accept the following languages

- i.  $L(M_2) - L(M_1)$   
 ii. The reverse language of  $L(M_2)$

- b. Consider the following NFA. 4



Draw the DFA that accepts the complement of the language accepted by the above NFA.

3. a. Draw the minimum state DFA for the following language. ( $\Sigma = \{a, b\}$ )  
 $\{w \mid w \text{ has an even number of } a\text{'s and each } a \text{ is followed by at least one } b\}$  4+2

- b. Consider the following CFG with start symbol  $E$ . 2+2

$$E \rightarrow I \mid E + E \mid E * E \mid (E)$$

$$I \rightarrow a \mid b \mid Ia \mid Ib \mid I0 \mid I1$$

Show the leftmost and rightmost derivation of the string  $(a1 * (b0 + a10))$  using the above grammar.