

Given $h(t) = h_0 + a \cos(\Omega t) + b \sin(\Omega t)$

then $h'(t) = -a\Omega \sin(\Omega t) + b\Omega \cos(\Omega t)$.

To find the maximum and minimum points,
we set $h'(t) = 0$:

$$-a\Omega \sin(\Omega t) + b\Omega \cos(\Omega t) = 0$$

$$\div \Omega \Rightarrow -a \sin(\Omega t) + b \cos(\Omega t) = 0$$

$$\Rightarrow a \sin(\Omega t) = b \cos(\Omega t)$$

$$\Rightarrow \frac{\sin(\Omega t)}{\cos(\Omega t)} = \frac{b}{a} \Rightarrow \tan(\Omega t) = \frac{b}{a}$$

$$\Rightarrow \Omega t = \arctan\left(\frac{b}{a}\right) + 180n, n \in \mathbb{N}$$

(arctan in degrees)

$$\Rightarrow t = \frac{1}{\Omega} \arctan\left(\frac{b}{a}\right) + 180n.$$

And to determine whether $h(t)$ is a high or low tide:

$$h''(t) = -a\Omega^2 \cos(\Omega t) - b\Omega^2 \sin(\Omega t)$$

$$h''(t) > 0 \Rightarrow \text{minimum} \Rightarrow \text{low tide}$$

$$h''(t) < 0 \Rightarrow \text{maximum} \Rightarrow \text{high tide}$$