# Deep Learning Assignment1

## v 0.1.Installation

import torch

! pip install d2l



Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/pytho Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.10/dist Requirement already satisfied: ipython-genutils in /usr/local/lib/python3 Requirement already satisfied: ipython>=5.0.0 in /usr/local/lib/python3.1 Requirement already satisfied: jupyter-client in /usr/local/lib/python3.1 Requirement already satisfied: tornado>=4.2 in /usr/local/lib/python3.10/ Requirement already satisfied: widgetsnbextension~=3.6.0 in /usr/local/li Requirement already satisfied: jupyterlab-widgets>=1.0.0 in /usr/local/li Requirement already satisfied: prompt-toolkit!=3.0.0,!=3.0.1,<3.1.0,>=2.0 Requirement already satisfied: pygments in /usr/local/lib/python3.10/dist Requirement already satisfied: lxml in /usr/local/lib/python3.10/dist-pac Requirement already satisfied: beautifulsoup4 in /usr/local/lib/python3.1 Requirement already satisfied: bleach in /usr/local/lib/python3.10/dist-p Requirement already satisfied: defusedxml in /usr/local/lib/python3.10/di Requirement already satisfied: entrypoints>=0.2.2 in /usr/local/lib/pytho Requirement already satisfied: jinja2>=3.0 in /usr/local/lib/python3.10/d Requirement already satisfied: jupyter-core>=4.7 in /usr/local/lib/python Requirement already satisfied: jupyterlab-pygments in /usr/local/lib/pyth Requirement already satisfied: MarkupSafe>=2.0 in /usr/local/lib/python3. Requirement already satisfied: mistune<2,>=0.8.1 in /usr/local/lib/python Requirement already satisfied: nbclient>=0.5.0 in /usr/local/lib/python3. Requirement already satisfied: nbformat>=5.1 in /usr/local/lib/python3.10 Requirement already satisfied: pandocfilters>=1.4.1 in /usr/local/lib/pyt Requirement already satisfied: tinycss2 in /usr/local/lib/python3.10/dist Requirement already satisfied: pyzmq<25,>=17 in /usr/local/lib/python3.10 Requirement already satisfied: argon2-cffi in /usr/local/lib/python3.10/d Requirement already satisfied: nest-asyncio>=1.5 in /usr/local/lib/python Requirement already satisfied: Send2Trash>=1.8.0 in /usr/local/lib/python Requirement already satisfied: terminado>=0.8.3 in /usr/local/lib/python3 Requirement already satisfied: prometheus-client in /usr/local/lib/python Requirement already satisfied: nbclassic>=0.4.7 in /usr/local/lib/python3 Requirement already satisfied: gtpy>=2.4.0 in /usr/local/lib/python3.10/d Requirement already satisfied: setuptools>=18.5 in /usr/local/lib/python3 Requirement already satisfied: jedi>=0.16 in /usr/local/lib/python3.10/di Requirement already satisfied: decorator in /usr/local/lib/python3.10/dis Requirement already satisfied: pickleshare in /usr/local/lib/python3.10/d Requirement already satisfied: backcall in /usr/local/lib/python3.10/dist Requirement already satisfied: pexpect>4.3 in /usr/local/lib/python3.10/d

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Requirement already satisfied: excentiongroup in /usr/local/lih/nython3.1
```

# 2.1.Data Manipulation

```
torch.zeros((2,3,4))
→ tensor([[[0., 0., 0., 0.],
              [0., 0., 0., 0.],
              [0., 0., 0., 0.]],
             [[0., 0., 0., 0.],
             [0., 0., 0., 0.]
              [0., 0., 0., 0.]]
torch.ones((2,3,4))
→ tensor([[[1., 1., 1., 1.],
              [1., 1., 1., 1.],
              [1., 1., 1., 1.]],
             [[1., 1., 1., 1.],
             [1., 1., 1., 1.],
              [1., 1., 1., 1.]])
torch.randn(3, 4)
→ tensor([[-2.2815, -0.0781, -0.6076, -1.5795],
             [2.4762, -0.2083, 1.1259, 0.1583],
            [ 1.9715, 0.0754, -1.7220,
                                          0.0183]])
K = torch.tensor([[2,1,4,3], [1,2,3,4], [4,3,2,1]])
print(K[2][3])
```

• torch를 사용하여 python에서 deeplearning 관련 프로젝트를 진행할 때 matrix를 관리할 수 있음.

 $\rightarrow$  tensor(1)

```
X[1, 2] = 17
Χ
\rightarrow tensor([[ 0., 1., 2., 3.],
             [ 4., 5., 17., 7.],
[ 8., 9., 10., 11.]])
torch.exp(x)
    tensor([1.0000e+00, 2.7183e+00, 7.3891e+00, 2.0086e+01, 5.4598e+01,
     1.4841e+02,
             2.4155e+07, 1.0966e+03, 2.9810e+03, 8.1031e+03, 2.2026e+04,
     5.9874e+04])
x = torch.tensor([1.0, 2, 4, 8])
y = torch.tensor([2, 2, 2, 2])
x + y, x - y, x * y, x / y, x ** y
    (tensor([ 3., 4., 6., 10.]),
     tensor([-1., 0., 2., 6.]),
tensor([ 2., 4., 8., 16.]),
      tensor([0.5000, 1.0000, 2.0000, 4.0000]),
      tensor([ 1., 4., 16., 64.]))
X = torch.arange(12, dtype=torch.float32).reshape((3,4))
Y = torch.tensor([[2.0, 1, 4, 3], [1, 2, 3, 4], [4, 3, 2, 1]])
print(X)
print(Y)
print(torch.cat((X, Y), dim=0))
print(torch.cat((X, Y), dim=1))
\rightarrow tensor([[ 0., 1., 2., 3.],
             [4., 5., 6., 7.],
             [8., 9., 10., 11.]])
     tensor([[2., 1., 4., 3.],
             [1., 2., 3., 4.],
             [4., 3., 2., 1.]])
                    1., 2., 3.],
     tensor([[ 0.,
             [4., 5., 6.,
             [8., 9., 10., 11.],
             [ 2., 1., 4.,
                               3.],
             [ 1.,
                          3.,
                    2.,
                               4.],
             [ 4., 3., 2.,
                               1.]])
     tensor([[ 0., 1., 2.,
                               3., 2.,
                                          1.,
                                                    3.],
             [4., 5., 6.,
                              7.,
                                    1.,
                                          2.,
                                               3.,
             [8., 9., 10., 11.,
                                    4.,
                                          3.,
```

```
print(X == Y)
print(X.sum())
→ tensor([[False, True, False, True],
             [False, False, False],
             [False, False, False, False]])
    tensor(66.)
a = torch.arange(3).reshape((3, 1))
b = torch.arange(2).reshape((1, 2))
a, b
\rightarrow (tensor([[0],
              [1],
              [2]]),
      tensor([[0, 1]]))
a + b
\rightarrow tensor([[0, 1],
             [1, 2],
             [2, 3]])
```

브로드캐스팅이 일어날 수 있는 조건은 다음과 같다.차원의 크기가 1일때 가능하다 두 배열 간의 연산에서 최소한 하나의 배열의 차원이 1이라면(0번 축이든 1번 축이든; 1행이든 1열이든) 가능하다.차원의 짝이 맞을때 가능하다 차원에 대해 축의 길이가 동일하면 브로드캐스팅이 가능하다. 출처:

https://sacko.tistory.com/16 [데이터 분석하는 문과생, 싸코:티스토리]

```
before = id(Y)
Y = Y + X
id(Y) == before

→ False
```

```
Z = 1 //torch.zeros_like(Y)
print(id(Y))
print('id(Z):', id(Z))
Z[:] = X + Y
print('id(Z):', id(Z))
Z += Y
print(id(Z))
→ 139141620424096
    id(Z): 139141620319152
    id(Z): 139141620319152
    139141620319152
A = X_numpy()
B = torch.from_numpy(A)
type(A), type(B)
(numpy.ndarray, torch.Tensor)
a = torch.tensor([3.5])
a, a.item(), float(a), int(a)
(tensor([3.5000]), 3.5, 3.5, 3)
  • python에서 딥러닝 학습을 위해 tensor를 사용한다.
```

- tensor를 통해 matrix를 연산을 수행, 관리할 수 있다.

# 2.2.Data Preprocessing using Panda

#### # 2.2 Data Preprocessing using panda

```
import os
os.makedirs(os.path.join('..', 'data'), exist_ok=True)
data_file = os.path.join('...', 'data', 'house_tiny.csv')
with open(data_file, 'w') as f:
    f.write('''NumRooms,RoofType,Price
NA, NA, 127500
2,NA,106000
4, Slate, 178100
NA,NA,140000''')
import pandas as pd
data = pd.read_csv(data_file)
print(data)
       NumRooms RoofType Price
            NaN
                      NaN 127500
    1
            2.0
                      NaN 106000
    2
            4.0
                    Slate 178100
    3
            NaN
                      NaN 140000
inputs, targets = data.iloc[:, 0:2], data.iloc[:, 2]
inputs = pd.get_dummies(inputs, dummy_na=True)
print(inputs)
print(targets)
```

| $\overline{\Rightarrow}$ |     | NumRooms   | RoofTy | be_Slate | RoofType_nan |
|--------------------------|-----|------------|--------|----------|--------------|
|                          | 0   | NaN        |        | False    | True         |
|                          | 1   | 2.0        |        | False    | True         |
|                          | 2   | 4.0        |        | True     | False        |
|                          | 3   | NaN        |        | False    | True         |
|                          | 0   | 127500     |        |          |              |
|                          | 1   | 106000     |        |          |              |
|                          | 2   | 178100     |        |          |              |
|                          | 3   | 140000     |        |          |              |
|                          | Nai | me: Price, | dtype: | int64    |              |

```
inputs = inputs.fillna(inputs.mean())
print(inputs)
        NumRooms RoofType_Slate RoofType_nan
\rightarrow
             3.0
                            False
                                            True
    0
             2.0
    1
                            False
                                            True
    2
             4.0
                            True
                                           False
    3
             3.0
                            False
                                            True
import torch
X = torch.tensor(inputs.to_numpy(dtype=float))
y = torch.tensor(targets.to_numpy(dtype=float))
Х, у
\rightarrow (tensor([[3., 0., 1.],
              [2., 0., 1.],
              [4., 1., 0.],
              [3., 0., 1.]], dtype=torch.float64),
      tensor([127500., 106000., 178100., 140000.], dtype=torch.float64))
```

# 2.3.Linear Algebra

```
# 2.3 Linear Algebra

x = torch.tensor(3.0)
y = torch.tensor(2.0)

x + y, x * y, x / y, x**y

→ (tensor(5.), tensor(6.), tensor(1.5000), tensor(9.))

x = torch.arange(3)
x, x[2], len(x), x.shape

→ (tensor([0, 1, 2]), tensor(2), 3, torch.Size([3]))
```

```
A = torch.arange(6).reshape(3,2)
A, A.T
\rightarrow (tensor([[0, 1],
               [2, 3],
               [4, 5]]),
      tensor([[0, 2, 4],
               [1, 3, 5]]))
A = torch.tensor([[1, 2, 3], [2, 0, 4], [3, 4, 5]])
A == A.T
→ tensor([[True, True, True],
              [True, True, True],
              [True, True, True]])
torch.arange(24).reshape(2, 3, 4)
\rightarrow tensor([[[0, 1, 2, 3],
               [ 4, 5, 6, 7], [ 8, 9, 10, 11]],
              [[12, 13, 14, 15],
               [16, 17, 18, 19],
               [20, 21, 22, 23]]])
A = torch.arange(6, dtype=torch.float32).reshape(2, 3)
B = A.clone() # Assign a copy of A to B by allocating new memory
A, A + B, A * B
\rightarrow (tensor([[0., 1., 2.],
               [3., 4., 5.]]),
      tensor([[ 0., 2., 4.],
      [ 6., 8., 10.]]),
tensor([[ 0., 1., 4.],
               [ 9., 16., 25.]]))
```

```
a = 2
X = torch.arange(24).reshape(2, 3, 4)
a + X, a * X, (a * X). shape
→ (tensor([[[ 2, 3, 4,
               [6, 7, 8, 9],
               [10, 11, 12, 13]],
              [[14, 15, 16, 17],
               [18, 19, 20, 21],
               [22, 23, 24, 25]]]),
     tensor([[[0, 2, 4, 6],
               [8, 10, 12, 14],
               [16, 18, 20, 22]],
              [[24, 26, 28, 30],
               [32, 34, 36, 38],
               [40, 42, 44, 46]]]),
      torch.Size([2, 3, 4]))
x = torch.arange(3, dtype=torch.float32)
x, x.sum()
→ (tensor([0., 1., 2.]), tensor(3.))
A.shape, A.sum()
→ (torch.Size([2, 3]), tensor(15.))
print(A,
A.shape,
A.sum(axis=0),
A.sum(axis=0).shape,
A.sum(axis=1))
\rightarrow tensor([[0., 1., 2.],
             [3., 4., 5.]]) torch.Size([2, 3]) tensor([3., 5., 7.]) torch.Size([
A.mean(), A.sum() / A.numel()
(tensor(2.5000), tensor(2.5000))
```

```
A.mean(axis=0), A.sum(axis=0) / A.shape[0]
(tensor([1.5000, 2.5000, 3.5000]), tensor([1.5000, 2.5000, 3.5000]))
sum_A = A.sum(axis=1, keepdims=True)
sum B = A.sum(axis = 1)
sum_A, sum_A.shape, sum_B, sum_B.shape
\rightarrow (tensor([[ 3.],
              [12.]]),
     torch.Size([2, 1]),
      tensor([ 3., 12.]),
      torch.Size([2]))
A / sum_A #keepdims를 했기 때문에 나누기 연산이 가능해짐.
→ tensor([[0.0000, 0.3333, 0.6667],
             [0.2500, 0.3333, 0.4167]])
A, A.cumsum(axis=0)
→ (tensor([[0., 1., 2.],
              [3., 4., 5.]]),
      tensor([[0., 1., 2.],
              [3., 5., 7.]]))
y = torch.ones(3, dtype = torch.float32)
x, y, torch.dot(x, y)
\rightarrow (tensor([0., 1., 2.]), tensor([1., 1., 1.]), tensor(3.))
torch.sum(x * y)
\rightarrow tensor(3.)
A, x, A.shape, x.shape, torch.mv(A, x), A@x
# torch.mv 는 matrix vector
→ (tensor([[0., 1., 2.],
              [3., 4., 5.]]),
      tensor([0., 1., 2.]),
      torch.Size([2, 3]),
      torch.Size([3]),
      tensor([ 5., 14.]),
      tensor([ 5., 14.]))
```

```
B = torch.ones(3, 4)
A, B, torch.mm(A, B), A@B
# torch.mm 은 matrix multiplication
\rightarrow (tensor([[0., 1., 2.],
              [3., 4., 5.]]),
      tensor([[1., 1., 1., 1.],
              [1., 1., 1., 1.],
               [1., 1., 1., 1.]]),
      tensor([[ 3., 3., 3., 3.],
              [12., 12., 12., 12.]]),
      tensor([[ 3., 3., 3., 3.],
               [12., 12., 12., 12.]]))
u = torch.tensor([3.0, -4.0])
torch.norm(u)
\rightarrow tensor(5.)
torch.abs(u).sum() # 절대값 하고 다 더함
\rightarrow tensor(7.)
torch.norm(torch.ones((4, 9)))
\rightarrow tensor(6.)
```

# 2.5.Automatic Differentiation

```
# 2.5 Automatic Differentation
import torch

x = torch.arange(4.0)
x

tensor([0., 1., 2., 3.])

# Can also create x = torch.arange(4.0, requires_grad=True)
x.requires_grad_(True)
x.grad # The gradient is None by default
```

```
y = 2 * torch.dot(x, x)
У
tensor(28., grad_fn=<MulBackward0>)
y backward()
x.grad
→ tensor([ 0., 4., 8., 12.])
x.grad == 4 * x
tensor([True, True, True, True])
x.grad.zero_() # Reset the gradient
y = x_sum()
print(y)
y.backward()
x.grad
tensor(6., grad_fn=<SumBackward0>)
    tensor([1., 1., 1., 1.])
x.grad.zero_()
y = x * x
y.backward(gradient = torch.ones(len(y))) # faster : y.sum().backward()
x.grad
\rightarrow tensor([0., 2., 4., 6.])
이 경우에는 y가 vector값이 되어 수행됨.
def f(a):
    b = a * 2
    while b.norm() < 1000:
        b = b * 2
    if b.sum() > 0:
        c = b
    else:
        c = 100 * b
    return c
```

```
a = torch.randn(size=(), requires_grad=True)
print(a)
d = f(a)
d.backward()

→ tensor(-1.5992, requires_grad=True)

a.grad == d / a

→ tensor(False)
```

# → 3.1.Linear Regression

```
# 3.1 Linear Regression
```

```
%matplotlib inline
import math
import time
import numpy as np
import torch
from d2l import torch as d2l
n = 10000
a = torch.ones(n)
b = torch.ones(n)
n = 10000
a = torch.ones(n)
b = torch.ones(n)
c = torch.zeros(n)
t = time.time()
for i in range(n):
    c[i] = a[i] + b[i]
f'{time.time() - t:.5f} sec'
'0.26414 sec'
```

```
t = time.time()
d = a + b
f'{time.time() - t:.5f} sec'
    '0.00028 sec'
def normal(x, mu, sigma):
    p = 1 / math.sqrt(2 * math.pi * sigma**2)
    return p * np.exp(-0.5 * (x - mu)**2 / sigma**2)
# Use NumPy again for visualization
x = np.arange(-7, 7, 0.01)
# Mean and standard deviation pairs
params = [(0, 1), (0, 2), (3, 1)]
d2l.plot(x, [normal(x, mu, sigma) for mu, sigma in params], xlabel='x',
         ylabel='p(x)', figsize=(4.5, 2.5),
         legend = [f'mean \{mu\}, std \{sigma\}' for mu, sigma in params])
\rightarrow
        0.4
                  mean 0, std 1
                  mean 0, std 2
        0.3
                  mean 3, std 1
     ⊗ 0.2
        0.1
        0.0
```

# 3.2.Object-Oriented Design for Implementation

0

2

4

6

**-**2

-4

#### # 3.2 Object-Oriented Design for Implementation

```
import time
import numpy as np
import torch
from torch import nn
from d2l import torch as d2l
```

-6

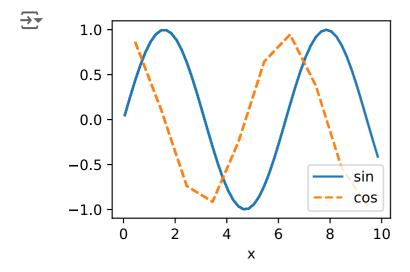
```
"@save" 주석은 허용되지 않습니다. 허용되는
def add_to_class(Class): #@save
                                            값은 다음과 같습니다. [@param, @title,
    """Register functions as methods in
                                            @markdown]
    def wrapper(obj):
        setattr(Class, obj.__name__, ok
    return wrapper
                                            "@save" 주석은 허용되지 않습니다. 허용되는
class HyperParameters: #@save
                                            값은 다음과 같습니다. [@param, @title,
    """The base class of hyperparameter
                                            @markdown]
    def save_hyperparameters(self, igno
        raise NotImplemented
class A:
    def __init__(self):
        self.b = 1
a = A()
@add_to_class(A)
def do(self):
    print('Class attribute "b" is', self.b)
a.do()
→ Class attribute "b" is 1
# Call the fully implemented HyperParameters class saved in d2l
class B(d2l.HyperParameters):
    def __init__(self, a, b, c):
        self.save_hyperparameters(ignore=['c'])
        print('self.a =', self.a, 'self.b =', self.b)
        print('There is no self.c =', not hasattr(self, 'c'))
b = B(a=1, b=2, c=3)
\rightarrow \rightarrow self.a = 1 self.b = 2
    There is no self.c = True
```

"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]



def draw(self, x, y, label, every\_r
 raise NotImplemented

```
board = d2l.ProgressBoard('x')
for x in np.arange(0, 10, 0.1):
    board.draw(x, np.sin(x), 'sin', every_n=2)
    board.draw(x, np.cos(x), 'cos', every_n=10)
```



```
class Module(nn.Module, d2l.HyperParame
    """The base class of models."""
    def __init__(self, plot_train_per_{
        super().__init__()
        self.save_hyperparameters()
        self.board = ProgressBoard()
    def loss(self, y_hat, y):
        raise NotImplementedError
    def forward(self, X):
        assert hasattr(self, 'net'), 'N
        return self.net(X)
    def plot(self, key, value, train):
        """Plot a point in animation.""
        assert hasattr(self, 'trainer')
        self.board.xlabel = 'epoch'
        if train:
            x = self.trainer.train_bate
                self.trainer.num_train_
            n = self.trainer.num train
                self.plot_train_per_epc
        else:
            x = self.trainer.epoch + 1
            n = self.trainer.num_val_ba
                self.plot_valid_per_epc
        self.board.draw(x, value.to(d2)
                        ('train_' if to
                        every_n=int(n))
    def training_step(self, batch):
        l = self.loss(self(*batch[:-1])
        self.plot('loss', l, train=True
        return l
    def validation_step(self, batch):
        l = self.loss(self(*batch[:-1])
        self.plot('loss', l, train=Fals
    def configure_optimizers(self):
        raise NotImplementedError
```

"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]

```
class DataModule(d2l.HyperParameters):
    """The base class of data."""
    def __init__(self, root='../data',
        self.save hyperparameters()
    def get_dataloader(self, train):
        raise NotImplementedError
    def train_dataloader(self):
        return self.get_dataloader(trai
    def val dataloader(self):
        return self.get_dataloader(trai
class Trainer(d2l.HyperParameters): #@
    """The base class for training mode
    def __init__(self, max_epochs, num_
        self.save hyperparameters()
        assert num_gpus == 0, 'No GPU s
    def prepare_data(self, data):
        self.train_dataloader = data.tr
        self.val_dataloader = data.val_
        self_num_train_batches = len(se
        self.num val batches = (len(se)
                                 if sel1
    def prepare model(self, model):
        model.trainer = self
        model.board.xlim = [0, self.ma>
        self.model = model
    def fit(self, model, data):
        self.prepare_data(data)
        self.prepare model(model)
        self.optim = model.configure_or
        self.epoch = 0
        self.train\ batch\ idx = 0
        self.val_batch_idx = 0
        for self.epoch in range(self.ma
            self.fit_epoch()
    def fit epoch(self):
        raise NotImplementedError
```

"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]

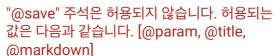
"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]

# 3.4.Linear Regression Implementation from Scratch

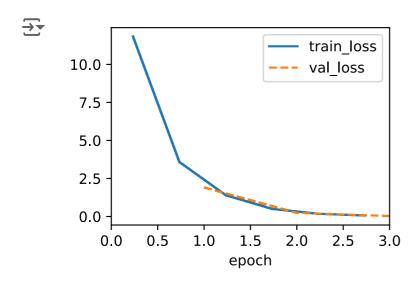
```
%matplotlib inline
import torch
from d2l import torch as d2l
                                           "@save" 주석은 허용되지 않습니다. 허용되는
class LinearRegressionScratch(d2l.Modul
                                           값은 다음과 같습니다. [@param, @title,
    def __init__(self, num_inputs, lr,
                                           @markdown]
        super().__init__()
        self.save hyperparameters()
        self.w = torch.normal(0, sigma,
        self.b = torch.zeros(1, require
                                           "@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(LinearRegressionScrat
                                           값은 다음과 같습니다. [@param, @title,
def forward(self, X):
                                           @markdown]
    return torch.matmul(X, self.w) + se
                                           "@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add to class(LinearRegressionScrat
                                           값은 다음과 같습니다. [@param, @title,
def loss(self, y_hat, y):
                                           @markdown]
    l = (y_hat - y) ** 2 / 2
    return l.mean()
                                           "@save" 주석은 허용되지 않습니다. 허용되는
class SGD(d2l.HyperParameters): #@save
                                           값은 다음과 같습니다. [@param, @title,
    """Minibatch stochastic gradient de
                                           @markdown]
    def __init__(self, params, lr):
        self.save_hyperparameters()
    def step(self):
        for param in self.params:
            param -= self.lr * param.gr
    def zero_grad(self):
        for param in self.params:
            if param.grad is not None:
                param.grad.zero_()
                                           "@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(LinearRegressionScrat
                                           값은 다음과 같습니다. [@param, @title,
def configure_optimizers(self):
                                           @markdown]
    return SGD([self.w, self.b], self.]
```

```
@d2l.add_to_class(d2l.Trainer)
                                 #@save
def prepare_batch(self, batch):
    return batch
@d2l.add_to_class(d2l.Trainer)
                                 #@save
def fit_epoch(self):
    self.model.train()
    for batch in self.train dataloader:
        loss = self.model.training_ster
        self.optim.zero_grad()
        with torch.no grad():
            loss.backward()
            if self.gradient_clip_val >
                self.clip_gradients(se)
            self.optim.step()
        self.train_batch_idx += 1
    if self.val dataloader is None:
        return
    self.model.eval()
    for batch in self.val_dataloader:
        with torch.no_grad():
            self.model.validation step(
        self.val_batch_idx += 1
```

"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]



model = LinearRegressionScratch(2, lr=0.03)
data = d2l.SyntheticRegressionData(w=torch.tensor([2, -3.4]), b=4.2)
trainer = d2l.Trainer(max\_epochs=3)
trainer.fit(model, data)



# 4.1.Softmax Regression

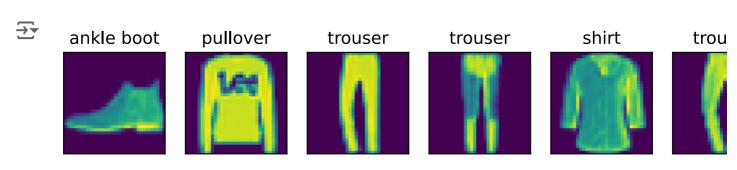
코딩을 시작하거나 AI로 코드를 생성하세요.

# 4.2.The Image Classification Dataset

```
%matplotlib inline
import time
import torch
import torchvision
from torchvision import transforms
from d2l import torch as d2l
d2l_use_svg_display()
class FashionMNIST(d2l.DataModule):
    """The Fashion-MNIST dataset."""
    def __init__(self, batch_size=64, )
        super(). init ()
        self.save_hyperparameters()
        trans = transforms.Compose([tra
        self.train = torchvision.datase
            root=self.root, train=True,
        self.val = torchvision.datasets
            root=self.root, train=False
data = FashionMNIST(resize=(32, 32))
len(data.train), len(data.val)
→ (60000, 10000)
data.train[0][0].shape
→ torch.Size([1, 32, 32])
```

"@save" 주석은 허용되지 않습니다. 허용되는 값은 다음과 같습니다. [@param, @title, @markdown]

```
"@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(FashionMNIST) #@save
                                           값은 다음과 같습니다. [@param, @title,
def text_labels(self, indices):
                                           @markdown]
    """Return text labels."""
    labels = ['t-shirt', 'trouser', 'pu
              'sandal', 'shirt', 'sneak
    return [labels[int(i)] for i in inc
                                           |'@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(FashionMNIST) #@save
                                           값은 다음과 같습니다. [@param, @title,
def get_dataloader(self, train):
    data = self.train if train else self.va @markdown]
    return torch.utils.data.DataLoader(data
                                        num
X, y = next(iter(data.train_dataloader()))
print(X.shape, X.dtype, y.shape, y.dtype)
→ /usr/local/lib/python3.10/dist-packages/torch/utils/data/dataloader.py:557:
      warnings.warn(_create_warning_msg(
    torch.Size([64, 1, 32, 32]) torch.float32 torch.Size([64]) torch.int64
tic = time.time()
for X, y in data.train_dataloader():
    continue
f'{time.time() - tic:.2f} sec'
    '11.83 sec'
                                           "@save" 주석은 허용되지 않습니다. 허용되는
def show_images(imgs, num_rows, num_cols,
                                           값은 다음과 같습니다. [@param, @title,
    """Plot a list of images."""
                                           @markdown]
    raise NotImplementedError
```



# 4.3.The Base Classification Model

```
import torch
from d2l import torch as d2l
                                           "@save" 주석은 허용되지 않습니다. 허용되는
class Classifier(d2l.Module): #@save
                                           값은 다음과 같습니다. [@param, @title,
    """The base class of classification
                                           @markdown]
    def validation_step(self, batch):
        Y_hat = self(*batch[:-1])
        self.plot('loss', self.loss(Y_/)
        self.plot('acc', self.accuracy)
                                           "@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(d2l.Module) #@save
                                           값은 다음과 같습니다. [@param, @title,
def configure_optimizers(self):
                                           @markdown]
    return torch.optim.SGD(self.paramet
                                           "@save" 주석은 허용되지 않습니다. 허용되는
@d2l.add_to_class(Classifier) #@save
                                           값은 다음과 같습니다. [@param, @title,
def accuracy(self, Y_hat, Y, averaged=]
                                           @markdown]
    """Compute the number of correct pi
    Y_hat = Y_hat.reshape((-1, Y_hat.sh
```

preds = Y\_hat.argmax(axis=1).type()
compare = (preds == Y.reshape(-1)).
return compare.mean() if averaged @

# 4.4.Softmax Regression Implementation from Scratch

```
import torch
from d2l import torch as d2l
X = torch.tensor([[1.0, 2.0, 3.0], [4.0, 5.0, 6.0]])
X.sum(0, keepdims=True), X.sum(1, keepdims=True)
→ (tensor([[5., 7., 9.]]),
     tensor([[ 6.],
              [15.]]))
def softmax(X):
    X_{exp} = torch_{exp}(X)
    partition = X exp.sum(1, keepdims=True)
    return X_exp / partition # The broadcasting mechanism is applied here
X = torch.rand((2, 5))
X \text{ prob} = \text{softmax}(X)
X_prob, X_prob.sum(1)
→ (tensor([[0.2307, 0.2722, 0.2010, 0.1581, 0.1379],
              [0.1445, 0.2203, 0.1927, 0.2963, 0.1462]]),
     tensor([1.0000, 1.0000]))
class SoftmaxRegressionScratch(d2l.Classifier):
    def __init__(self, num_inputs, num_outputs, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
        self.W = torch.normal(0, sigma, size=(num_inputs, num_outputs),
                               requires grad=True)
        self.b = torch.zeros(num_outputs, requires_grad=True)
    def parameters(self):
        return [self.W, self.b]
@d2l.add_to_class(SoftmaxRegressionScratch)
def forward(self, X):
    X = X.reshape((-1, self.W.shape[0]))
    return softmax(torch.matmul(X, self.W) + self.b)
```

```
y = torch.tensor([0, 2])
y_hat = torch.tensor([[0.1, 0.3, 0.6], [0.3, 0.2, 0.5]])
y_hat[[0, 1], y]

ightarrow tensor([0.1000, 0.5000])

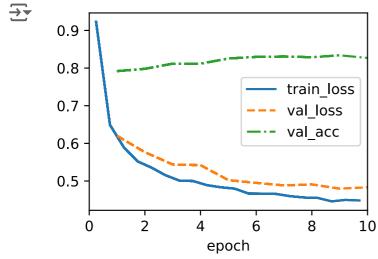
def cross_entropy(y_hat, y):
    return -torch.log(y_hat[list(range(len(y_hat))), y]).mean()

cross_entropy(y_hat, y)

ightarrow tensor(1.4979)

@d2l.add_to_class(SoftmaxRegressionScratch)
def loss(self, y_hat, y):
    return cross_entropy(y_hat, y)

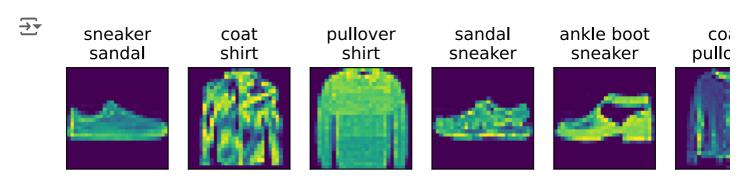
data = d2l.FashionMNIST(batch_size=256)
model = SoftmaxRegressionScratch(num_inputs=784, num_outputs=10, lr=0.1)
trainer = d2l.Trainer(max_epochs=10)
trainer.fit(model, data)
```



```
X, y = next(iter(data.val_dataloader()))
preds = model(X).argmax(axis=1)
preds.shape
```

→ torch.Size([256])

```
wrong = preds.type(y.dtype) != y
X, y, preds = X[wrong], y[wrong], preds[wrong]
labels = [a+'\n'+b for a, b in zip(
         data.text_labels(y), data.text_labels(preds))]
data.visualize([X, y], labels=labels)
```

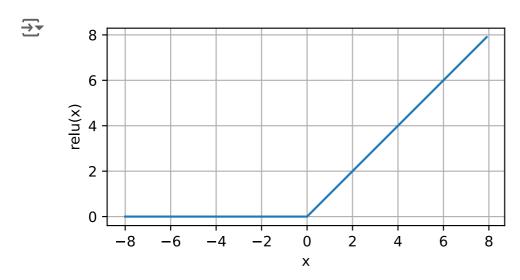


# √ 5.1.Multilayer Perceptrons

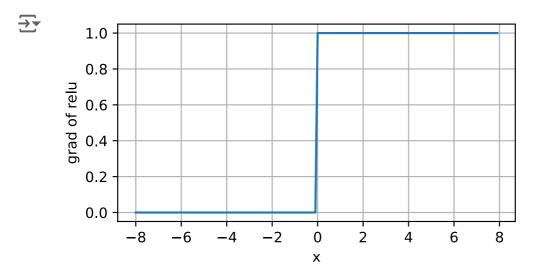
%matplotlib inline
import torch
from d2l import torch as d2l

$$ReLU(x) = max(x, 0)$$

```
x = torch.arange(-8.0, 8.0, 0.1, requires_grad=True)
y = torch.relu(x)
d2l.plot(x.detach(), y.detach(), 'x', 'relu(x)', figsize=(5, 2.5))
```

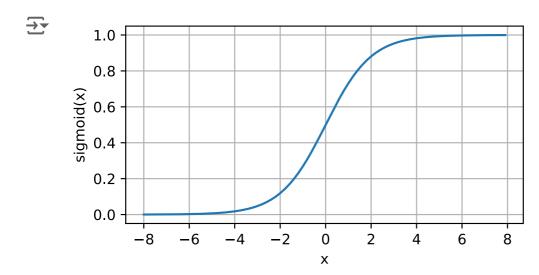


y.backward(torch.ones\_like(x), retain\_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of relu', figsize=(5, 2.5))



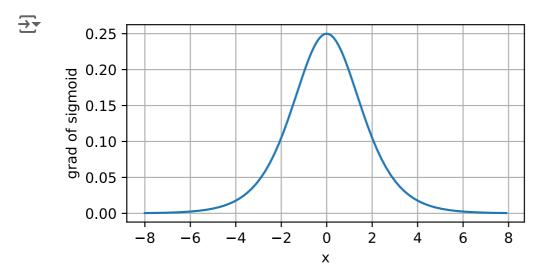
$$sigmoid(x) = \frac{1}{1 + exp(-x)}$$

y = torch.sigmoid(x)
d2l.plot(x.detach(), y.detach(), 'x', 'sigmoid(x)', figsize=(5, 2.5))



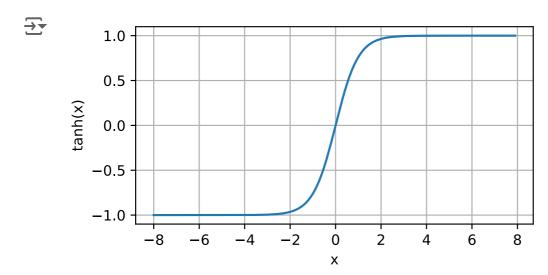
$$\frac{d}{dx}\operatorname{sigmoid}(x) = \frac{\exp(-x)}{(1 + \exp(-x))^2} = \operatorname{sigmoid}(x)(1 - \operatorname{sigmoid}(x))$$

# Clear out previous gradients
x.grad.data.zero\_()
y.backward(torch.ones\_like(x),retain\_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of sigmoid', figsize=(5, 2.5))



$$tanh(x) = \frac{1 - exp(-2x)}{1 + exp(-2x)}$$

y = torch.tanh(x)
d2l.plot(x.detach(), y.detach(), 'x', 'tanh(x)', figsize=(5, 2.5))



$$\frac{d}{dx}\tanh(x) = 1 - \tanh^2(x)$$

```
# Clear out previous gradients
x.grad.data.zero_()
y.backward(torch.ones_like(x),retain_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of tanh', figsize=(5, 2.5))

1.0
0.8
0.4
0.2
0.0
```

0

2

6

# 5.2.Implementation of Multilayer Perceptrons

**-**2

-6

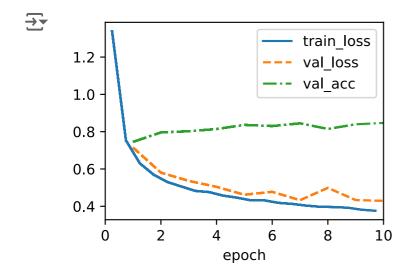
```
import torch
from torch import nn
from d2l import torch as d2l

class MLPScratch(d2l.Classifier):
    def __init__(self, num_inputs, num_outputs, num_hiddens, lr, sigma=0.01):
        super().__init__()
        self.save_hyperparameters()
        self.W1 = nn.Parameter(torch.randn(num_inputs, num_hiddens) * sigma)
        self.b1 = nn.Parameter(torch.zeros(num_hiddens))
        self.W2 = nn.Parameter(torch.randn(num_hiddens, num_outputs) * sigma)
        self.b2 = nn.Parameter(torch.zeros(num_outputs))

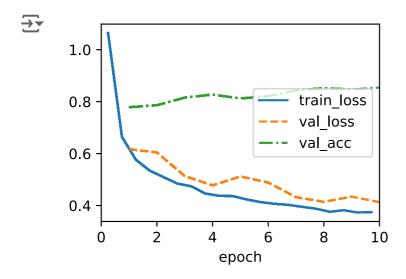
def relu(X):
    a = torch.zeros_like(X)
    return torch.max(X, a)
```

```
@d2l.add_to_class(MLPScratch)
def forward(self, X):
    X = X.reshape((-1, self.num_inputs))
    H = relu(torch.matmul(X, self.W1) + self.b1)
    return torch.matmul(H, self.W2) + self.b2

model = MLPScratch(num_inputs=784, num_outputs=10, num_hiddens=256, lr=0.1)
data = d2l.FashionMNIST(batch_size=256)
trainer = d2l.Trainer(max_epochs=10)
trainer.fit(model, data)
```



model = MLP(num\_outputs=10, num\_hiddens=256, lr=0.1)
trainer.fit(model, data)



# 5.3.Forward Propagation, Backward Propagation, and Computational Graphs

# Discussions & Exercises

## 2.1.3.Discussions

tensor를 concat 할 수 잇는데, dim에 따라서 행으로 옆에 붙일지 열로 밑으로 붙일지를 정할 수 있다. dim = 0 을 하면, 열의 개수가 유지되며 밑으로 붙이고 dim = 1 을 하면, 행의 개수가 유지되어 옆으로 붙인다.

#### 2.2.2.Discussions

iloc[a:b, c:d] <- a<=x<b index에 대하여 c<=y<=d label 출력

## 2.3.6.Discussions

sum을 수행할 때, axis = 0 or 1 에 따라서 각각 행, 열에 대한 합을 도출한다. axis = 0,1로 하면 행, 열에 대한 합을 모두 수행하기 때문에 전체 합이 도출된다.

#### 2.3.7.Discussions

keepdims가 의마하는 것은? -> 브로드캐스팅을 위해 차원을 유지하는 것 질문? 왜 keepdims를 제거했을 때 shape에서 torch.Size([1,2])가 되지 않을까?

#### 2.5.1.1.Discussions

requires\_grad = True 를 통해서 x의 gradient를 구할 준비를 하고, y를 backward()한 뒤, x.grad를 하면 gradient 값을 구할 수 있다.

•  $2x^2$ 를 미분하면 4x

#### 2.5.1.2.Discussions

x0, x1, x2, x3에 대해 미분한 값임.

• y = x0 + x1 + x2 + x3 인데 각각 xn에 대하여 미분하면 y=1이므로 [1,1,1,1]이 들어가게 됨.

#### 2.5.Discussions

딥러닝에서는 학습에 있어서 파라미터들의 전파 역전파에 대한 정보를 얻기 위해 gradient값을 아는 것이 중요한데, 이를 grad를 통해서 쉽게 관리 하고 구할 수 있다. 이때, y가 갖는 값이 scalar 인지 vector인지 구분하는 것 또한 중요함.

#### 3.1.Discussions

normal distribution을 통해서 linear regression을 연관지을 수 있다. (x - sigma)^2에 (y-wtx -b)^2을 넣어 loss에 대한 normal distribution을 만들고 이를 통해 maximum likelihood를 구할 수 있다.

#### 3.2.Discussions

**Model Definition (Module)** Moudle 클래스의 서브클래스에서 모델 구조를 정의하고, forward propagation 및 최적화 설정 과 같은 메서드를 사용. 이를 통해 모델 구성 요소의 정의와 재사용이 간편해 짐.

**Data Handling (DataModule)** DataModule 클래스는 데이터 다운로드, 전처리 및 학습과 검증을 위이한 데이터 로더를 제공하는 기본 클래스. 이를 통해 일관되고 재사용 가능한 데이터 처리가 가능.

**Training(Trainier)** Trainer 클래스는 데이터 배치 반복, gradient 계산, 모델 파라미터 업데이트 등의 전체 훈련 루프를 담당. 이를 통해 epoch같은 훈련 세부 사항을 관리할 수 있음.

#### 3.4.2.Discussions

**Loss Function** 

$$L = \frac{(\hat{y} - y)^2}{2}$$

#### 3.4.4.Discussions

## Training

1. Initialize parameters

$$(\mathbf{w}, b)$$

- 2. Repeat until done
  - Compute gradient

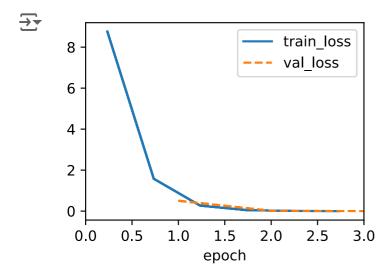
$$\mathbf{g} \leftarrow \partial_{(\mathbf{w},b)} \frac{1}{|B|} \sum_{i \in B} l(\mathbf{x}^{(i)}, y^{(i)}, \mathbf{w}, b)$$

Update parameters

$$(\mathbf{w}, b) \leftarrow (\mathbf{w}, b) - \eta \mathbf{g}$$

3.4.4.Exercises\_Changing LearningRate

model = LinearRegressionScratch(2, lr=0.05)
data = d2l.SyntheticRegressionData(w=torch.tensor([2, -3.4]), b=4.2)
trainer = d2l.Trainer(max\_epochs=3)
trainer.fit(model, data)



#### 4.1.Discussions

#### Softmax?

classfication과 같은 것에서 각 x값들의 합을 1로 하고 범위가 0~1이 되도록 수치를 조종

$$O = XW + b$$

$$\hat{\mathbf{y}} = \text{softmax}(\mathbf{o}) \quad \text{where} \quad \hat{y}_i = \frac{\exp(o_i)}{\sum_i \exp(o_j)}$$

큰 값이 큰 값으로 유지됨.

#### Log-Likelihood?

$$P(\mathbf{Y} \mid \mathbf{X}) = \prod_{i=1}^{n} P(y^{(i)} \mid \mathbf{x}^{(i)}).$$

$$-\log P(\mathbf{Y} \mid \mathbf{X}) = \sum_{i=1}^{n} -\log P(y^{(i)} \mid \mathbf{x}^{(i)}) = \sum_{i=1}^{n} l(y^{(i)}, \hat{\mathbf{y}}^{(i)}),$$

$$l(\mathbf{y}, \hat{\mathbf{y}}) = -\sum_{i=1}^{q} y_{i} \log \hat{y}_{j}.$$

흔히 cross-entropy loss라고 불림.

#### **Entropy?**

$$H[P] = \sum_{j} -P(j) \log P(j).$$

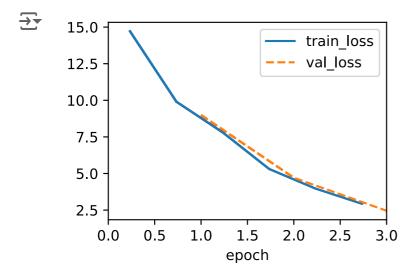
## 4.2.Discussions

FashoinMNIST 이미지 데이터셋을 통해 분류하는 classfier를 만들어 보았고 몇개의 예시가 분류되는 것을 보았음.

## 4.2.1. Memo

Fashion-MNIST consists of images from 10 categories, each represented by 6000 images in the training and by 1000 in the test dataeset. -> 60000, 10000.

model = LinearRegressionScratch(2, lr=0.01)
data = d2l.SyntheticRegressionData(w=torch.tensor([2, -3.4]), b=4.2)
trainer = d2l.Trainer(max\_epochs=3)
trainer.fit(model, data)



#### 4.3. Discussions

정확도는 예측된 값인  $\hat{y}$  과 label 값인  $\hat{y}$ 를 비교하여 계산된다. 이때,  $\hat{y}$ 의 '==' 비교는 data type에 민감하므로 data type을 맞추어준 뒤 0, 1로 비교하여 나타낸다.

#### **4.4.MEMO**

- 28 x 28 pixel image를 flatten 하여 784길이의 벡터값으로 변환한다.
- 결과가 class의 개수인 10개로 나와야 하기 때문에 weight vector가 784 x 10 에 bias 1 x 10 으로 하였음.
- W 를 Gaussian noise로 정함.
- bias는 0으로 초기화.

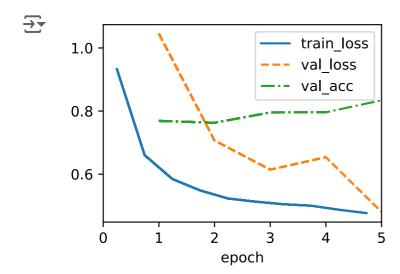
## 4.4.2.Discussions

reshape의 첫번째 인자 -1은 나머지를 통해 적절한 차원의 크기로 자동으로 저장해 주는 기능임. self.W.shape[0]인 W의 첫번째 차원의 크기가 784 이므로 28 x 28 이 1 x 784가 됨.

## 4.4.5.Exercise

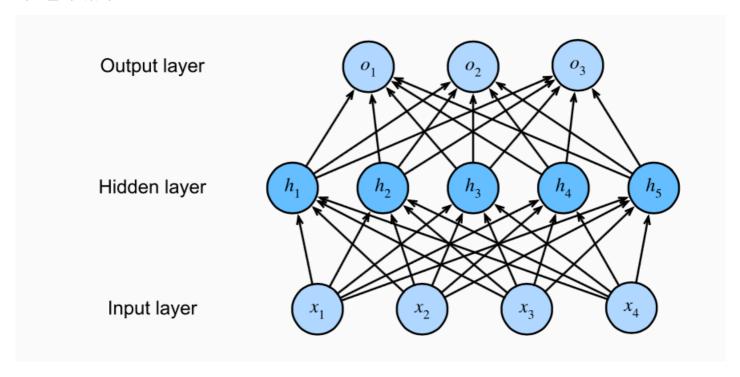
기존 에제에서 10 epoch 가량에 train\_loss가 줄어들지만 val\_loss가 늘어나는 overfitting이 생겼음. 또한 val\_lossdml 기울기가 매우 완만하여 epoch를 5로 줄이고 Ir을 0.2f로 늘려서 진행하여봄.

```
data = d2l.FashionMNIST(batch_size=256)
model = SoftmaxRegressionScratch(num_inputs=784, num_outputs=10, lr=0.2)
trainer = d2l.Trainer(max_epochs=5)
trainer.fit(model, data)
```



## 5.1.1.Discussions

선형성으로 모든 문제를 해결할 수 없음. 예를 들어 고양이와 개의 이미지를 분류할 때, 단순 한 픽셀의 밝기에 대하여 선형 모델을 사용하는 것은 실패할 가능성이 크다. 이를 신경망을 사용하여 hidden layer을 통해학습할 수 있다.

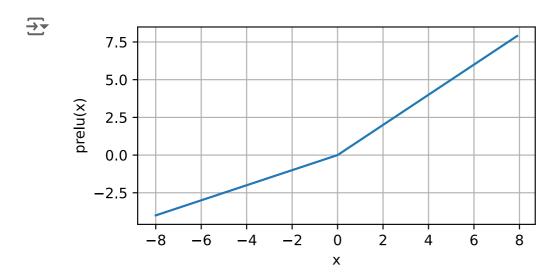


$$H = XW + b$$
$$O = HW + b$$

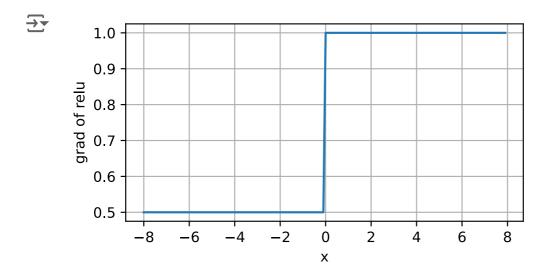
## √ 5.1.2.1. Exercises

$$pReLU(x) = max(0, x) + \alpha min(0, x)$$

alpha = 0.5 x = torch.arange(-8.0, 8.0, 0.1, requires\_grad=True) y = torch.where(x > 0, x, alpha \* x) # torch.where 사용해 요소별로 조건 적용 d2l.plot(x.detach(), y.detach(), 'x', 'prelu(x)', figsize=(5, 2.5))



y.backward(torch.ones\_like(x), retain\_graph=True)
d2l.plot(x.detach(), x.grad, 'x', 'grad of relu', figsize=(5, 2.5))

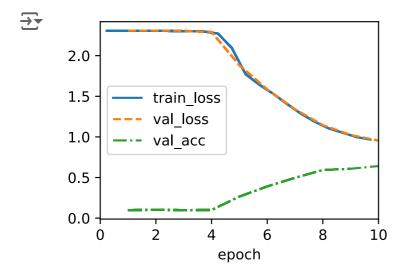


## → 5.2.Exercises

Activate Function, LearningRate 혹은 hiddenlayer의 개수를 바꾸어서 실행해보았음.

```
class MLPScratchEx(d2l.Classifier):
    def __init__(self, num_inputs, num_outputs, num_hiddens1, num_hiddens2, lr,
        super().__init__()
        self.save hyperparameters()
        self.W1 = nn.Parameter(torch.randn(num_inputs, num_hiddens1) * sigma)
        self.b1 = nn.Parameter(torch.zeros(num_hiddens1))
        self.W2 = nn.Parameter(torch.randn(num hiddens1, num hiddens2) * sigma)
        self.b2 = nn.Parameter(torch.zeros(num_hiddens2))
        self.W3 = nn.Parameter(torch.randn(num_hiddens2, num_outputs) * sigma)
        self.b3 = nn.Parameter(torch.zeros(num_outputs))
def relu(X):
    a = torch.zeros_like(X)
    return torch.max(X, a)
def sigmoid(X):
    return 1 / (1 + torch.exp(-X))
@d2l.add_to_class(MLPScratchEx)
def forward(self, X):
    X = X.reshape((-1, self.num_inputs))
    # 첫 번째 hidden layer: W1, b1
    H1 = sigmoid(torch.matmul(X, self.W1) + self.b1)
    # 두 번째 hidden layer 추가: W2, b2
    H2 = sigmoid(torch.matmul(H1, self.W2) + self.b2)
    # 출력 layer: W3, b3 (기존 W2, b2에서 W3, b3로 변경)
    return torch.matmul(H2, self.W3) + self.b3
```

model = MLPScratchEx(num\_inputs=784, num\_outputs=10, num\_hiddens1=256, num\_hidd



## 5.3.1.Discussions

#### Forward propagation

$$\mathbf{z} = \mathbf{W}^{(1)}\mathbf{x}$$

$$\mathbf{h} = \phi(\mathbf{z})$$

$$\mathbf{o} = \mathbf{W}^{(2)}\mathbf{h}$$

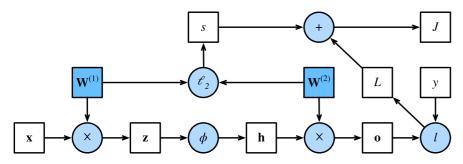
$$L = l(\mathbf{o}, \mathbf{y})$$

$$s = \frac{\lambda}{2} (\|\mathbf{W}^{(1)}\|_F^2 + \|\mathbf{W}^{(2)}\|_F^2)$$

$$J = L + s$$

input 데이터에 대하여 가중치를 곱한 뒤 activation 함수 넣음. 그 결과에 대한 가중치를 또 곱하여 output 만들어냄. output과 실제 label간의 Loss를 구한다. reqularization을 통해 구한 값과 Loss값을 구하여 모델의 regularized loss를 구한다.

## Computational Graph of Forward Propagation



#### → 5.3.2.Discussions

#### Back propagation

$$\frac{\partial J}{\partial L} = 1 \quad \text{and} \quad \frac{\partial J}{\partial s} = 1$$

$$\frac{\partial J}{\partial \mathbf{o}} = \operatorname{prod}\left(\frac{\partial J}{\partial L}, \frac{\partial L}{\partial \mathbf{o}}\right) = \frac{\partial L}{\partial \mathbf{o}} \in \mathbb{R}^{q}$$

$$\frac{\partial s}{\partial \mathbf{W}^{(1)}} = \lambda \mathbf{W}^{(1)} \quad \text{and} \quad \frac{\partial s}{\partial \mathbf{W}^{(2)}} = \lambda \mathbf{W}^{(2)}$$

$$\frac{\partial J}{\partial \mathbf{W}^{(2)}} = \operatorname{prod}\left(\frac{\partial J}{\partial \mathbf{o}}, \frac{\partial \mathbf{o}}{\partial \mathbf{W}^{(2)}}\right) + \operatorname{prod}\left(\frac{\partial J}{\partial s}, \frac{\partial s}{\partial \mathbf{W}^{(2)}}\right) = \frac{\partial J}{\partial \mathbf{o}} \mathbf{h}^{\mathsf{T}} + \lambda \mathbf{W}^{(2)}$$

$$\frac{\partial J}{\partial \mathbf{h}} = \operatorname{prod}\left(\frac{\partial J}{\partial \mathbf{o}}, \frac{\partial \mathbf{o}}{\partial \mathbf{h}}\right) = \mathbf{W}^{(2)\mathsf{T}} \frac{\partial J}{\partial \mathbf{o}}$$

$$\frac{\partial J}{\partial \mathbf{z}} = \operatorname{prod}\left(\frac{\partial J}{\partial \mathbf{h}}, \frac{\partial \mathbf{h}}{\partial \mathbf{z}}\right) = \frac{\partial J}{\partial \mathbf{h}} \odot \phi'(\mathbf{z})$$

$$\frac{\partial J}{\partial \mathbf{W}^{(1)}} = \operatorname{prod}\left(\frac{\partial J}{\partial \mathbf{z}}, \frac{\partial \mathbf{z}}{\partial \mathbf{W}^{(1)}}\right) + \operatorname{prod}\left(\frac{\partial J}{\partial s}, \frac{\partial s}{\partial \mathbf{W}^{(1)}}\right) = \frac{\partial J}{\partial \mathbf{z}} \mathbf{x}^{\mathsf{T}} + \lambda \mathbf{W}^{(1)}$$

코딩을 시작하거나 AI로 코드를 생성하세요.