

Theory of Computation Assignment No. 3

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Q1) Find the language generated by the grammar on $\{a, b\}^*$ and provide a proof?

Grammar:

$$\begin{aligned} S &\rightarrow aAb \mid AB \\ A &\rightarrow aAb \mid B \mid a \\ B &\rightarrow bBa \mid a \end{aligned}$$

Sol: The language(L) generated is the union of set of languages,

$$L = \cup_{i=0}^{13} L_i$$

$$\begin{aligned} L_1 &= \{a^n b^n, n \geq 1\} & L_2 &= \{a^{n+1} b^n, n \geq 1\} \\ L_3 &= \{a^n b^{n+1}, n \geq 1\} & L_4 &= \{a^n b^{n+2}\} \\ L_5 &= \{b^{n+2} a^n, n \geq 1\} & L_6 &= \{ab^{n+1} a^n, n \geq 1\} \\ L_7 &= \{b^{n+1} a^n b^{m+1} a^m; m, n \geq 1\} & L_8 &= \{a^n b^{m+1} a^m b^m; m, n \geq 1\} \\ L_9 &= \{b^{n+1} a^n b, n \geq 1\} & L_{10} &= \{a^{n+1} b^{m+n+1} a^m; m, n \geq 1\} \\ L_{11} &= \{a^n b^{m+1} a^m b^{n+1}; m, n \geq 1\} & L_{12} &= \{a^n b^{m+1} a^m b^{n+l+2} a^l; l, m, n \geq 1\} \end{aligned}$$

L_1 is derived by the following derivations:

$$\begin{aligned} S &\rightarrow AB \\ A &\rightarrow aAb \\ B &\rightarrow b \end{aligned}$$

only ab can be derived by,

$$\begin{aligned} S &\rightarrow AB \\ A &\rightarrow a \\ B &\rightarrow b \end{aligned}$$

L_2 is derived by the following derivations:

$$\begin{aligned} S &\rightarrow aAb \\ A &\rightarrow aAb \mid a \end{aligned}$$

L_3 is derived by the following derivations:

$$\begin{aligned} S &\rightarrow aAb \\ A &\rightarrow aAb \end{aligned}$$

after reaching upto n a'^s and b'^s then,
 $A \rightarrow B$ and $B \rightarrow b$

L_4 is derived by the following derivations:

$$\begin{array}{l} S \rightarrow AB \\ A \rightarrow aAb \end{array}$$

after reaching upto n a'^s and b'^s then,
 $A \rightarrow B$ and $B \rightarrow b$
 and the right-most $B \rightarrow b$

L_5 is derived by the following derivations:

$$\begin{array}{l} S \rightarrow AB \\ A \rightarrow B \end{array}$$

after reaching upto n b'^s and a'^s then,
 $A \rightarrow B(B \rightarrow b)$ and
 right-most B derives,

$$B \rightarrow bBa$$

and then b.