

CSc 217 – Probability and Statistics for Computer Science

Problem Set №1

by

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Problem 1:

Each year an employee at a company will receive a salary increase. The amount an employee's salary increases each year is a random variable X . The probability distribution for an employee's salary increase is as follows:

$$P(X) = \begin{cases} 2/8 & \mapsto 1\% \\ 3/8 & \mapsto 2\% \\ 2/8 & \mapsto 3\% \\ 1/8 & \mapsto 5\% \end{cases}$$

What is the probability that after five years (five salary increases), a cumulative salary increase of $x \geq 10\%$ occurs?

Problem 2:

The Federal Reserve Bank of the United States targets an annual inflation rate of 2%. This means that for an employee's salary to purchase the same amount of goods and services next year, their salary must increase by 2% to match the 2% expansion of the money supply within the economy induced by the Federal Reserve Bank. One measure of purchasing power used by economists to mediate difference in currency exchange rates and inflationary effects of currencies is Purchasing Power Parity (PPP). Each year an employee at a company will receive an adjustment in their salary's PPP.

The amount an employee salary's PPP adjusts by each year is a random variable Y . The probability distribution for a PPP adjustment is as follows:

$$P(Y) = \begin{cases} 2/8 & \mapsto & -1\% \\ 3/8 & \mapsto & \pm 0\% \\ 2/8 & \mapsto & +1\% \\ 1/8 & \mapsto & +3\% \end{cases}$$

It is desirable for an employee's PPP to increase overtime as they accumulate skills and knowledge, commonly known as "beating inflation."

What is the probability that after five years (five PPP adjustments), a cumulative PPP adjustment x "beats inflation"; i.e. $x > 0\%$?

Problem 3:

Each year, an employee who switches employment from one company to another will receive a 10% salary increase (+8% PPP) but will not receive a raise that year. Hence, a simple strategy to maximize earning potential is to *jump* between companies with relative frequency.

Unfortunately, an employee does not always have the opportunity to switch employment each year, and instead they must *stay* with their current employer and receive the PPP adjustment Y from Problem 2. The opportunity to switch employment is a random variable S with the probability distribution:

$$P(S) = \begin{cases} 1/2 & \mapsto \text{Jump} : +8\% \text{ PPP} \\ 1/2 & \mapsto \text{Stay} : P(Y) \end{cases}$$

What is the probability an employee utilizing this “job-jumping” strategy for one year (at most one job jump) receives a PPP adjustment x which “beats inflation;” i.e $x > 0\%$?

Problem 4:

Shockingly, employees are not likely to higher employees who jump between employers frequently. The more recently an employee has jumped between employers the less likely they are to be able to find an opportunity to jump to a new employer this year. The opportunity to jump between employment is a random variable J with the probability distribution:

$$P(J) = \begin{cases} 1/6 & \text{iff } \text{Did } \textit{Jump} \text{ last year} \\ 2/6 & \text{iff } \text{No } \textit{Jump} \text{ last year} \\ 3/6 & \text{iff } \text{No } \textit{Jump} \text{ last year nor the previous year} \end{cases}$$

As with Problem 3, if an employee does not have the opportunity to *jump*, then they must *stay* with their current employer and receive the PPP adjustment Y from Problem 2.

What is the probability that after five years (five PPP adjustments), a cumulative PPP adjustment $x \geq 10\%$ occurs?

Extra Credit 5:

Which is the most preferable from these mutually exclusive options?

♡ Pursue your passion

\$ Take the money