

let $A = \text{input}$ $B = \text{output}$

$$A'_2 = T A_2$$

$$A'_3 = T A_3$$

$$T = T(B_1 - A_1)$$

$$\vec{a} = A_2 - A_1$$

$$\vec{b} = B_2 - B_1$$

$$\alpha = \arctan\left(\frac{\vec{a}_y}{\vec{a}_x}\right)$$

$$\beta = \arctan\left(\frac{\vec{b}_y}{\vec{b}_x}\right)$$

$$R = R(\alpha - \beta)$$

$$A''_2 = R A'_2$$

$$A''_3 = R A'_3$$

$$\vec{b}_\perp = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \vec{b}$$

$$A^b_2 = M_b A''_2$$

$$A^b_3 = M_b A''_3$$

$$M_b = \begin{bmatrix} \vec{b}_x & \vec{b}_{\perp x} \\ \vec{b}_y & \vec{b}_{\perp y} \end{bmatrix}^{-1}$$

$$B^b_2 = M_b B_2$$

$$B^b_3 = M_b B_3$$

$$S_b = \frac{B^b_{2x}}{A^b_{2x}}$$

$$S_\perp = \frac{B^b_{3y}}{A^b_{3y}}$$

$$S_h = \frac{B^b_{3x} A^b_{3x} S_b}{B^b_{3y}}$$

$$S = \begin{bmatrix} S_b & S_h & 0 \\ 0 & S_\perp & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\text{Projection matrix} = P = S M_b R T$$