

Image Representation

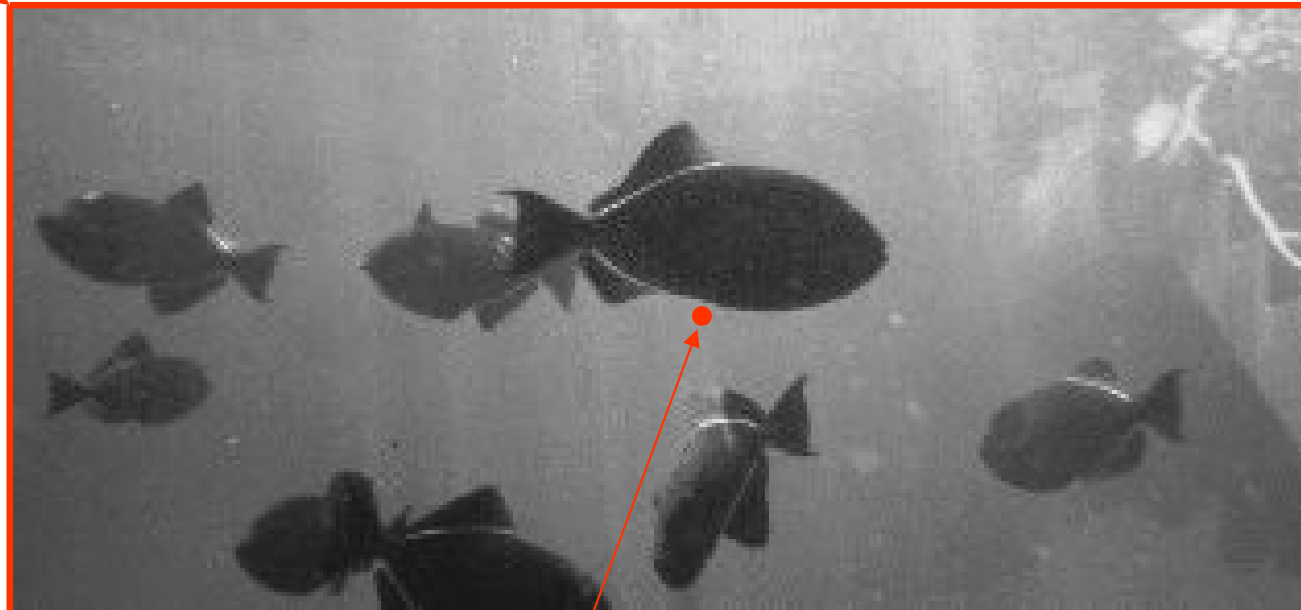
Reference:

[Gonzalez and Woods] Rafael C. Gonzalez and Richard E. Woods, Digital Image Processing, Second Edition, Prentice-Hall, Inc.

<http://www.imageprocessingplace.com/>

Image representation

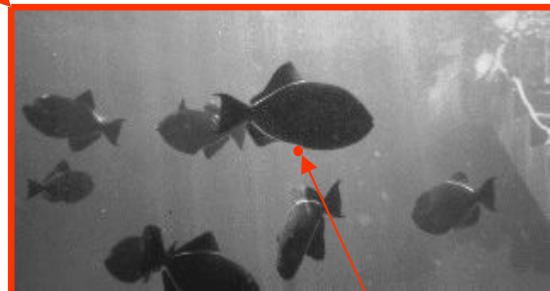
origin (0,0) in *C*, and (1,1) in MATLAB



$f(x,y)$, a 2D function representing image intensity; (x,y) represents a pair of spatial coordinates

Image representation

origin



y

- Discretized in both
 - Spatial coordinates
 - Brightness

$f(x,y)$

x

Similar to a matrix in Linear Algebra

Individual elements are called:
image elements, picture elements (pixels), (image points)

Image representation (MATLAB convention)

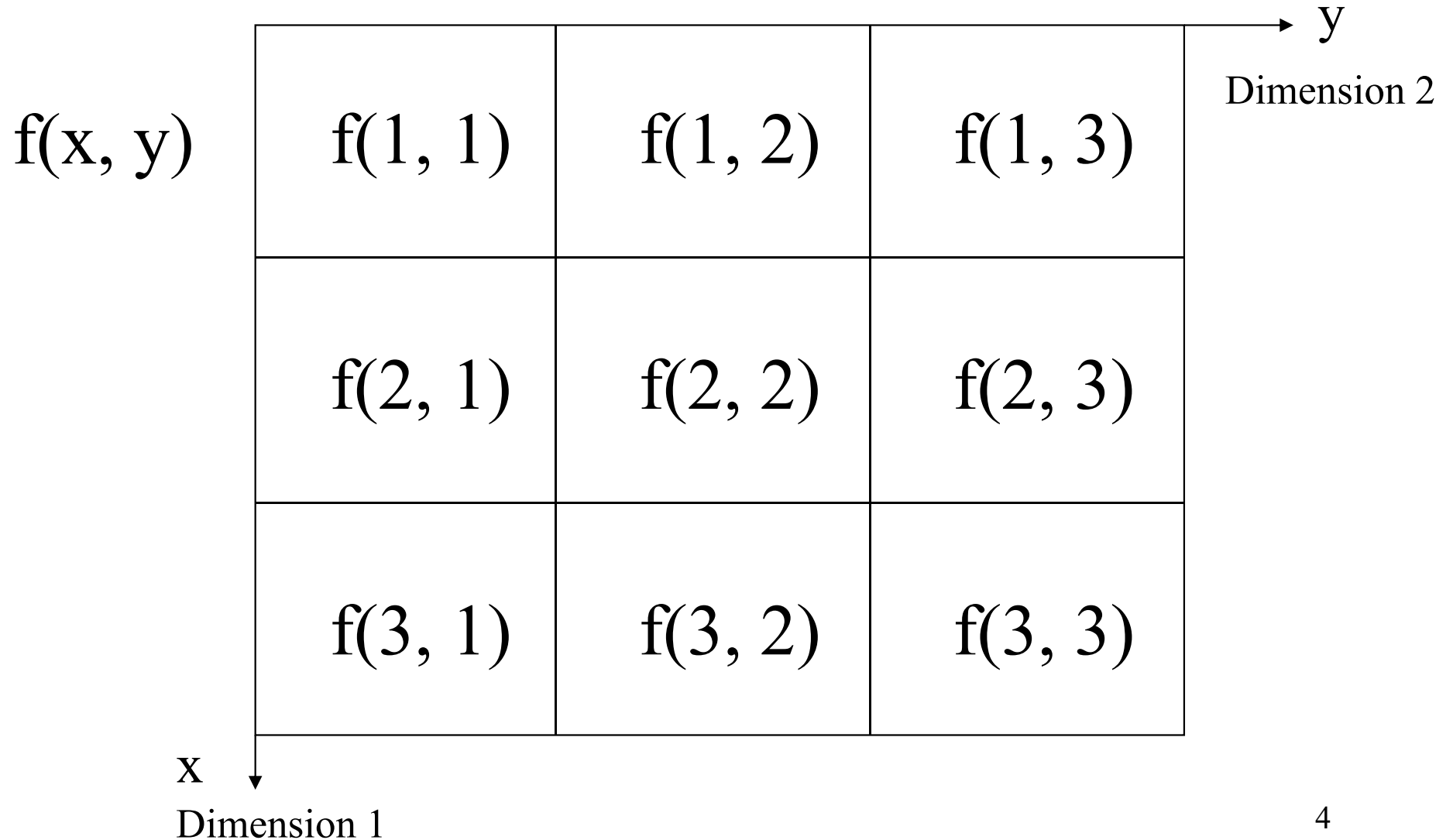
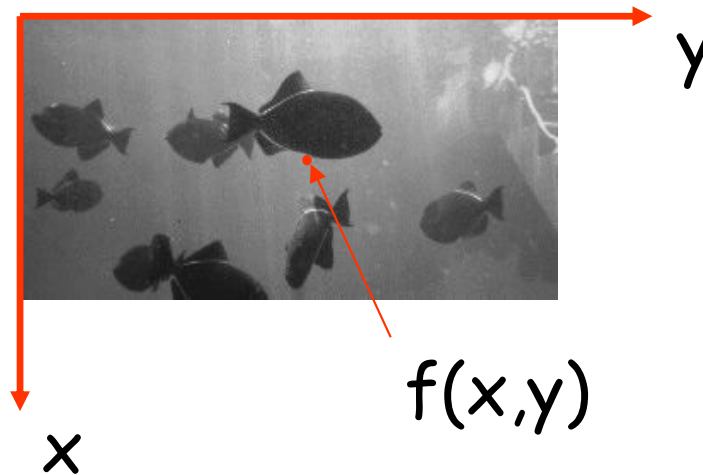


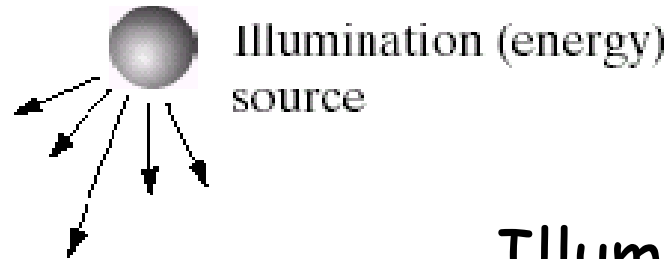
Image function, f (intensity)



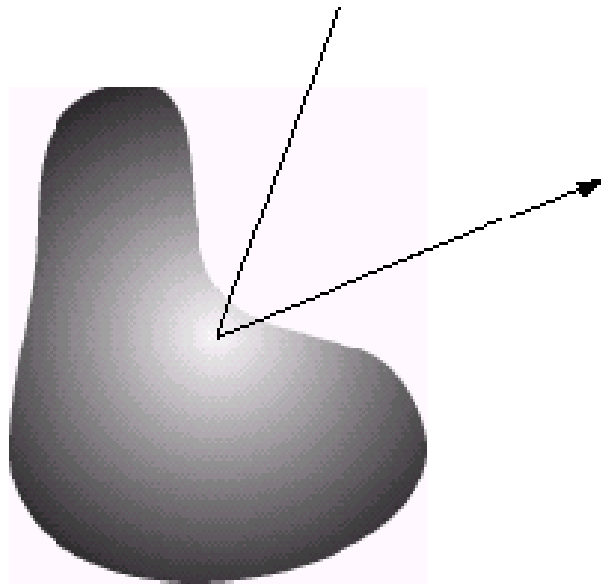
The image function (intensity/color) f can be characterized by two components:
(1) illumination (light source) and
(2) reflectance (materials).

Image intensity is depending on these two factors.

Image function, f (intensity)



Illumination: the amount of source illumination (energy) **incident** on the scene being viewed.



Scene element

Reflectance: the amount of source illumination (energy) **reflected** by the objects (or elements) in the scene.

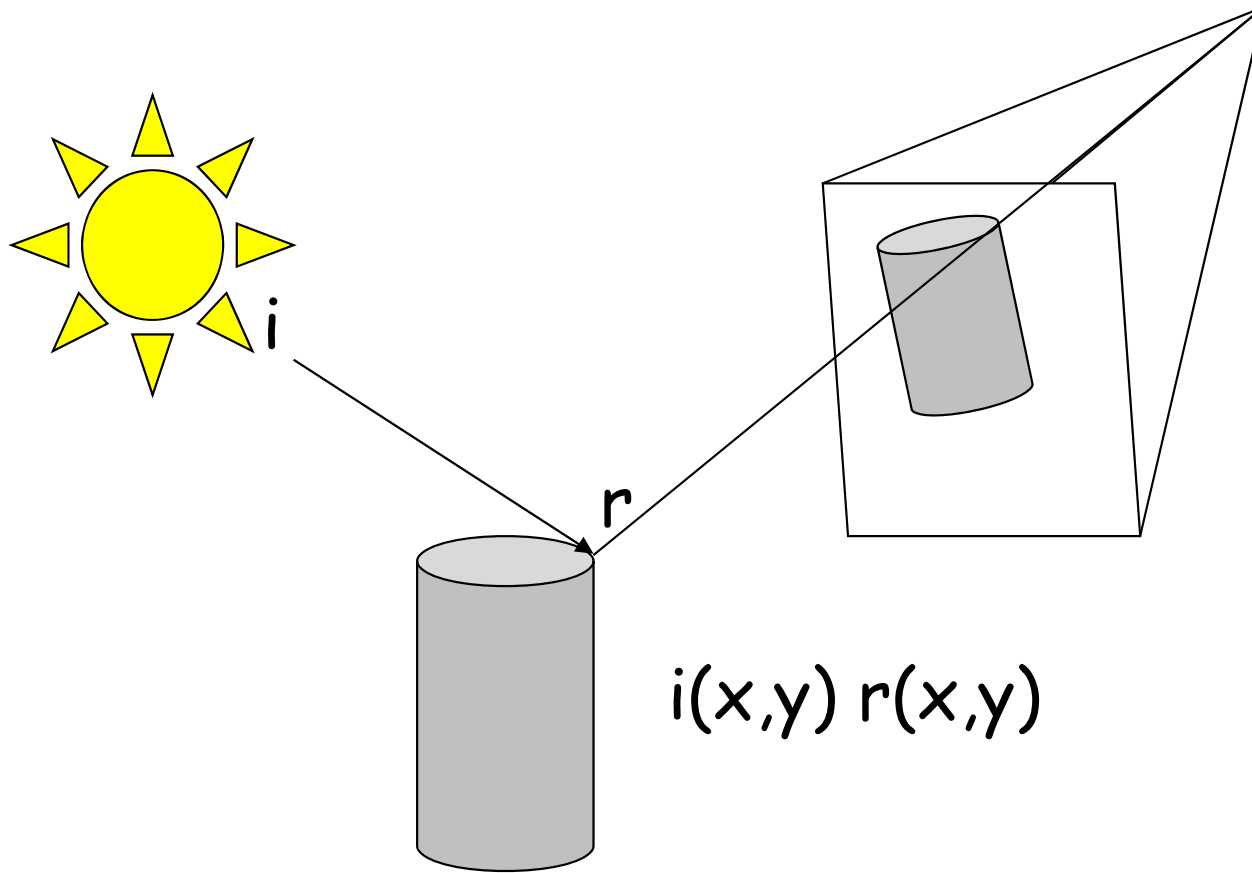
Image model

- Basic nature of $f(x,y)$ has two components:
$$f(x,y) = i(x,y) r(x,y)$$
- $i(x,y)$ is illumination component
$$0 \leq i(x,y) < +\infty$$
- $r(x,y)$ is reflectance component
$$0 \leq r(x,y) \leq 1$$

$$0 = \text{total absorption}, 1 = \text{total reflectance}.$$
- $f(x,y)$ is intensity
- $$0 \leq f(x,y) < +\infty$$

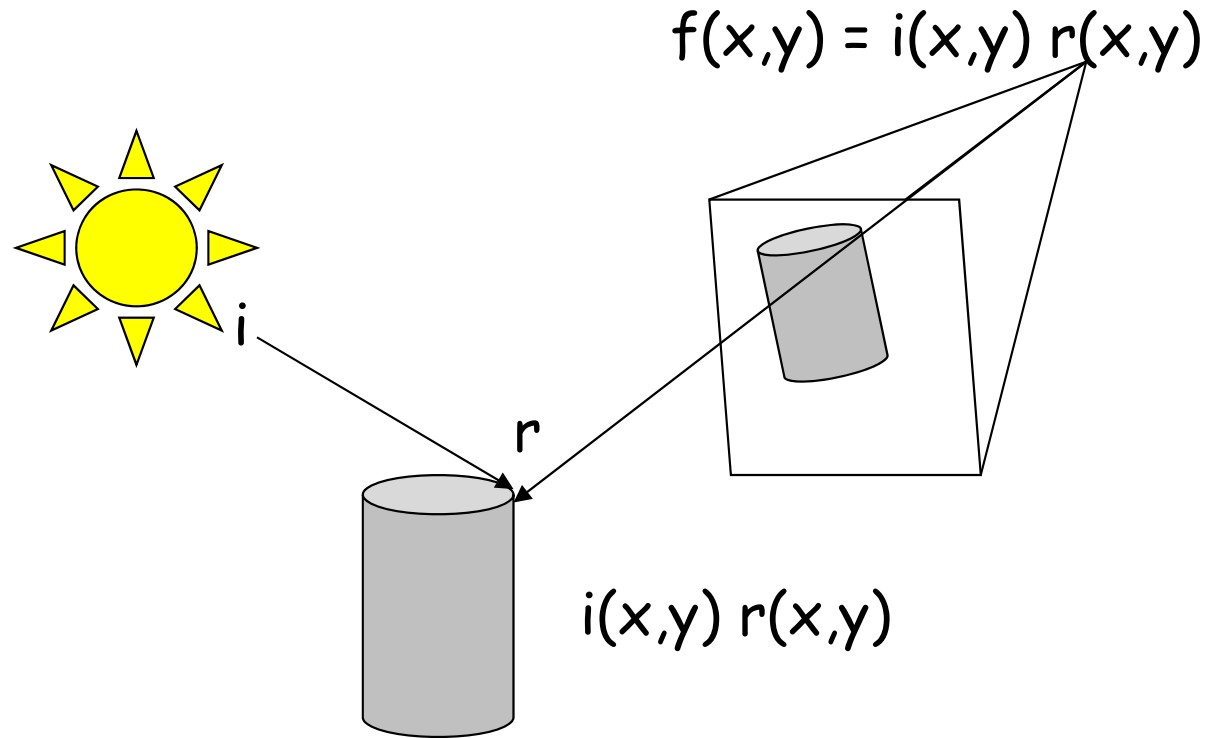
Image model

$$f(x,y) = i(x,y) r(x,y)$$



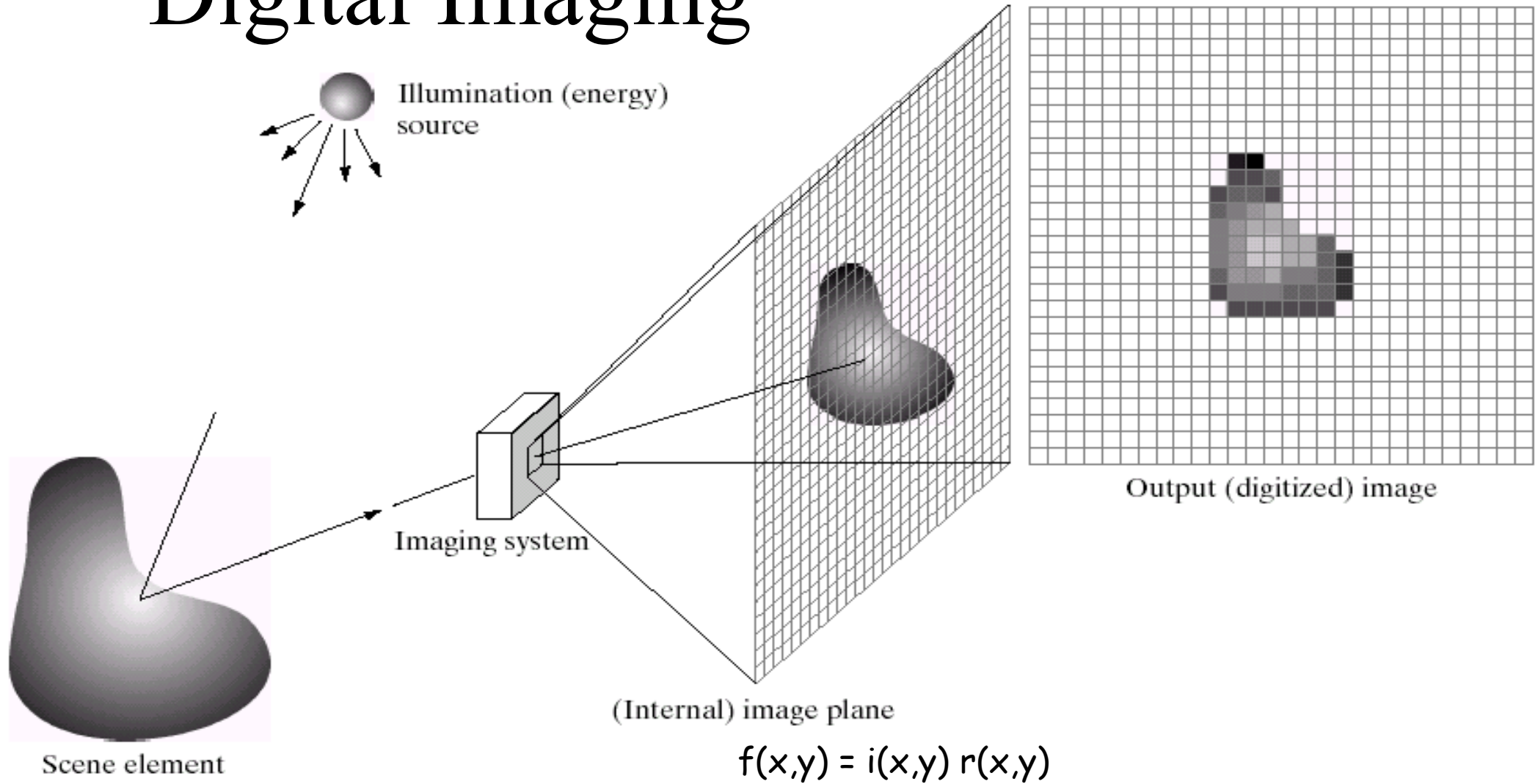
i and r are continuous functions
thus $f(x,y)$ can be continuous

Sampling and quantization are affecting the image quality.



i and r are continuous functions
thus $f(x,y)$ can be continuous

Digital Imaging



a b c d e

FIGURE 2.15 An example of the digital image acquisition process. (a) Energy (“illumination”) source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

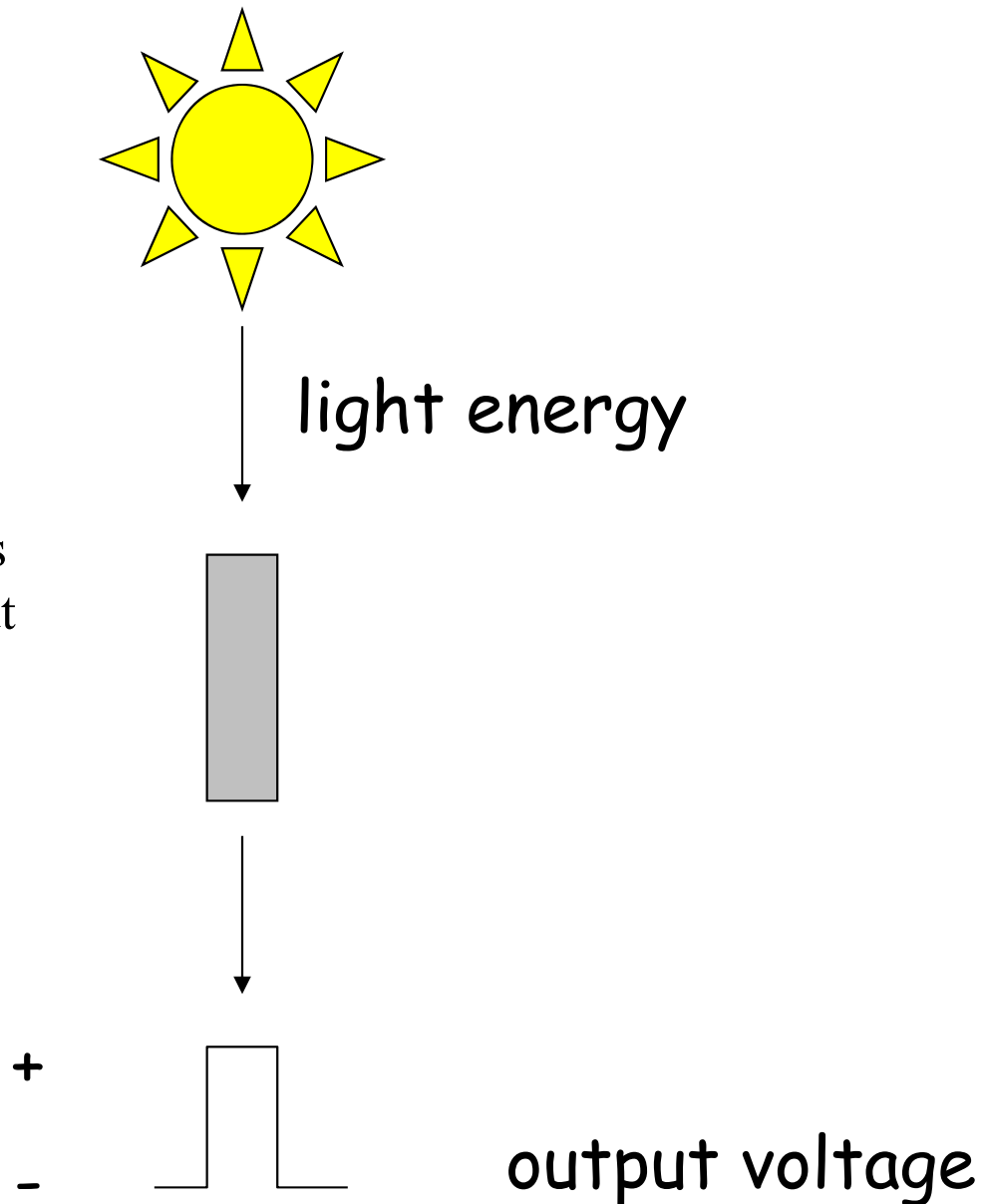
Digital Imaging

- Charged-Coupled Device (CCD)
 - consists of photosites
 - silicon imaging elements that give a voltage output proportional to the intensity of the incident light
 - linear array (scanner)
 - area array (Camera CCD)
- http://en.wikipedia.org/wiki/Charge-coupled_device

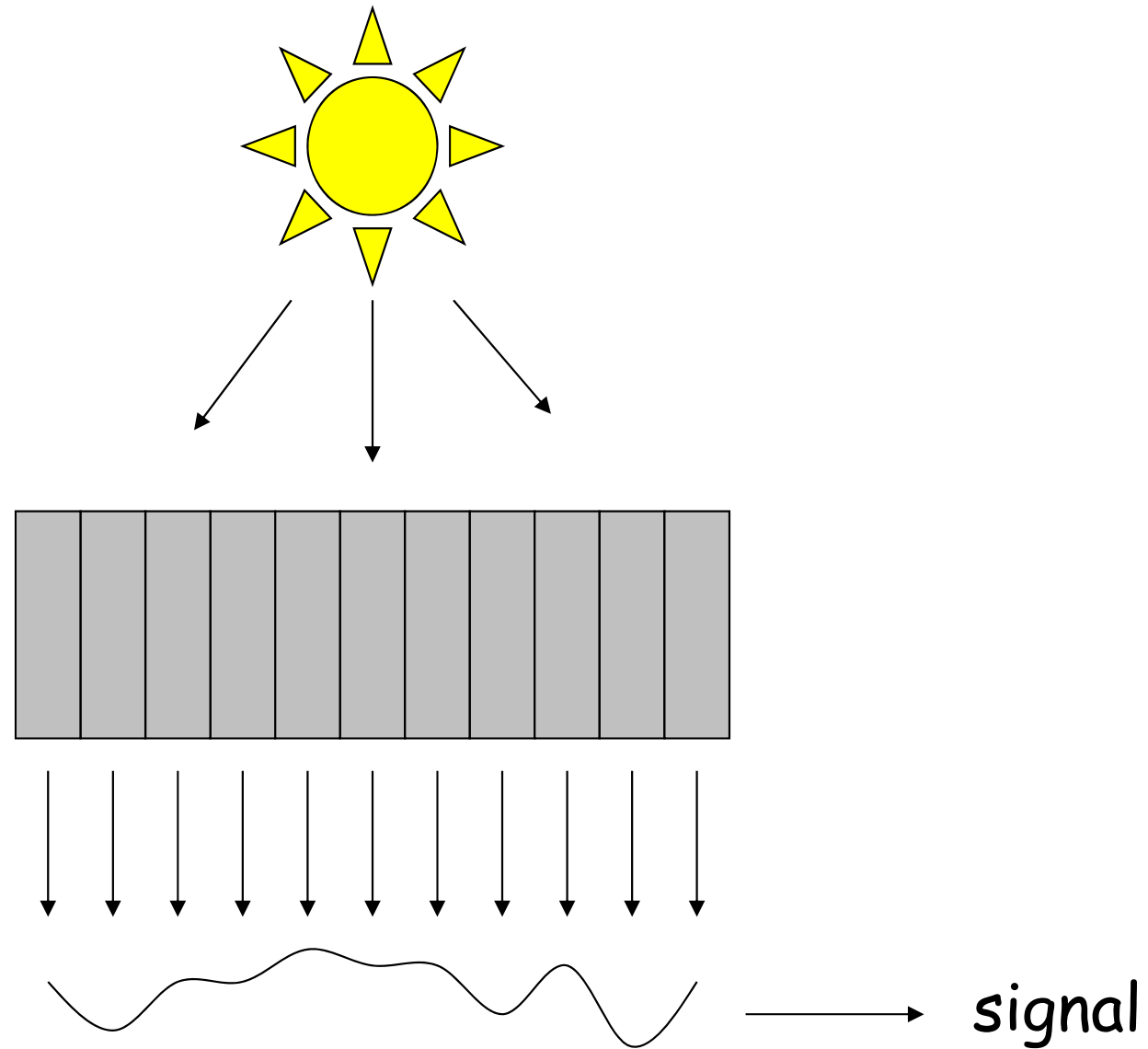
Photosites

CCD consists of photosites

- silicon imaging elements that give a voltage output proportional to the intensity of the incident light



Line scan sensor



Area scan sensor

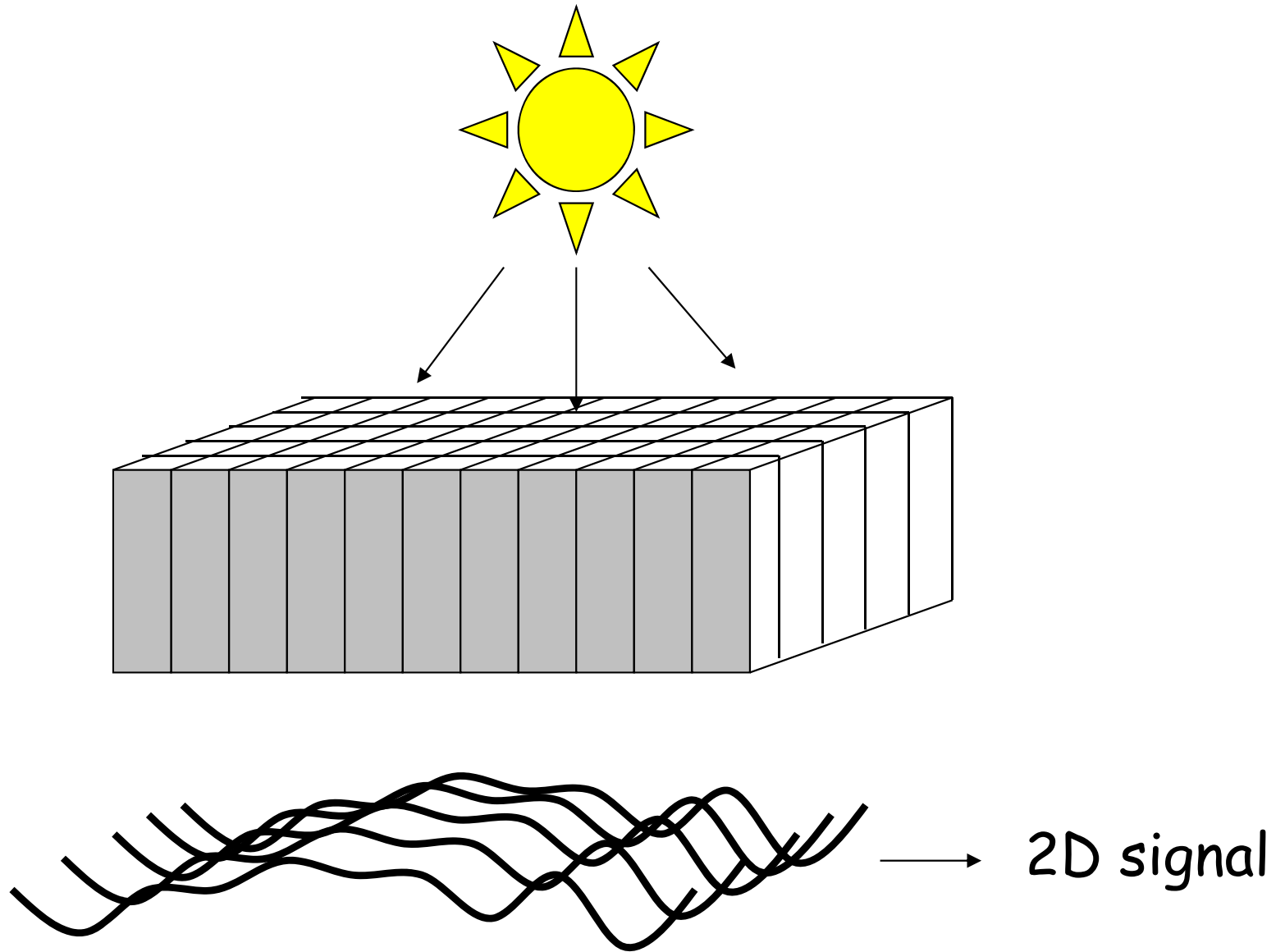
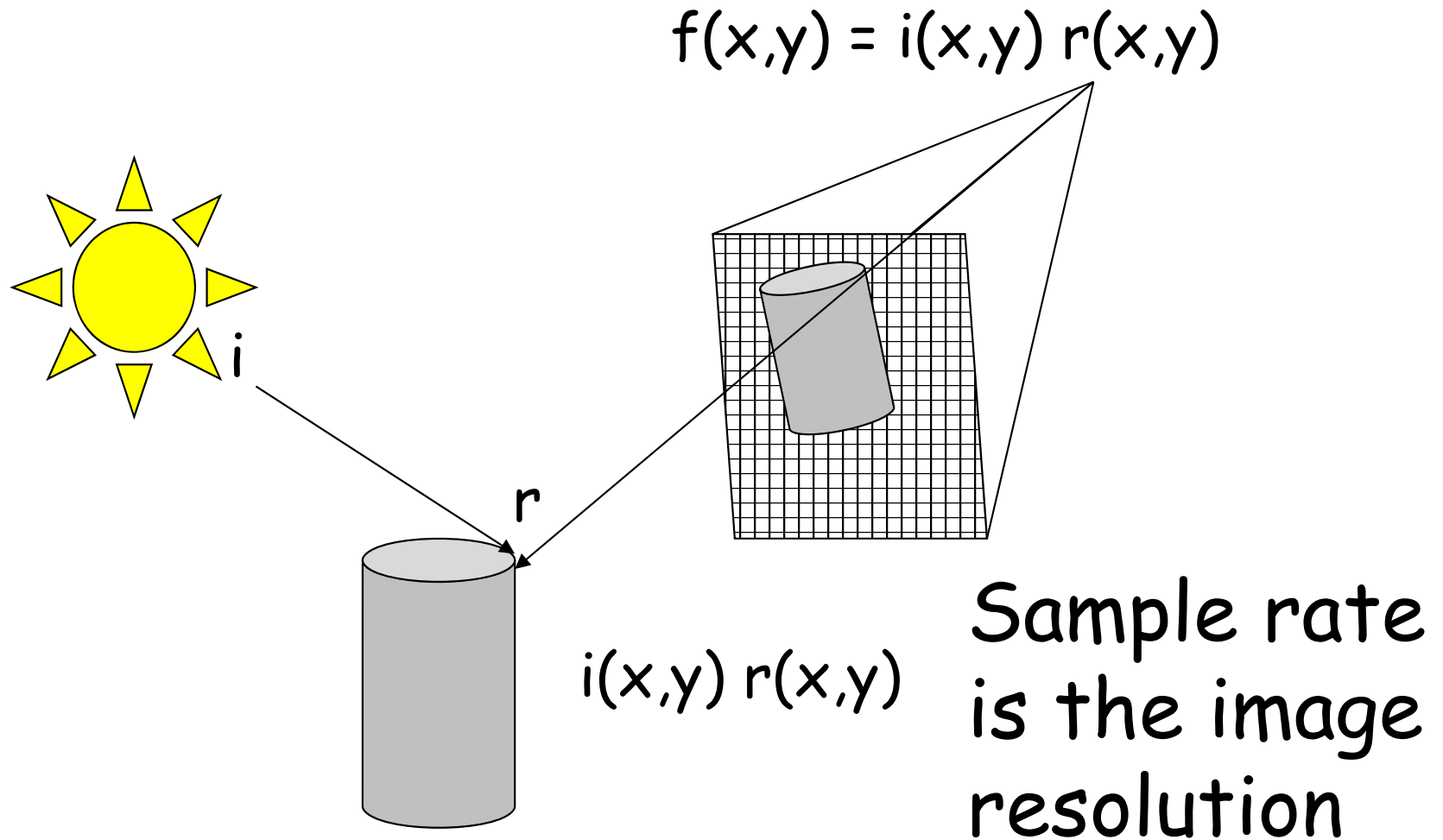
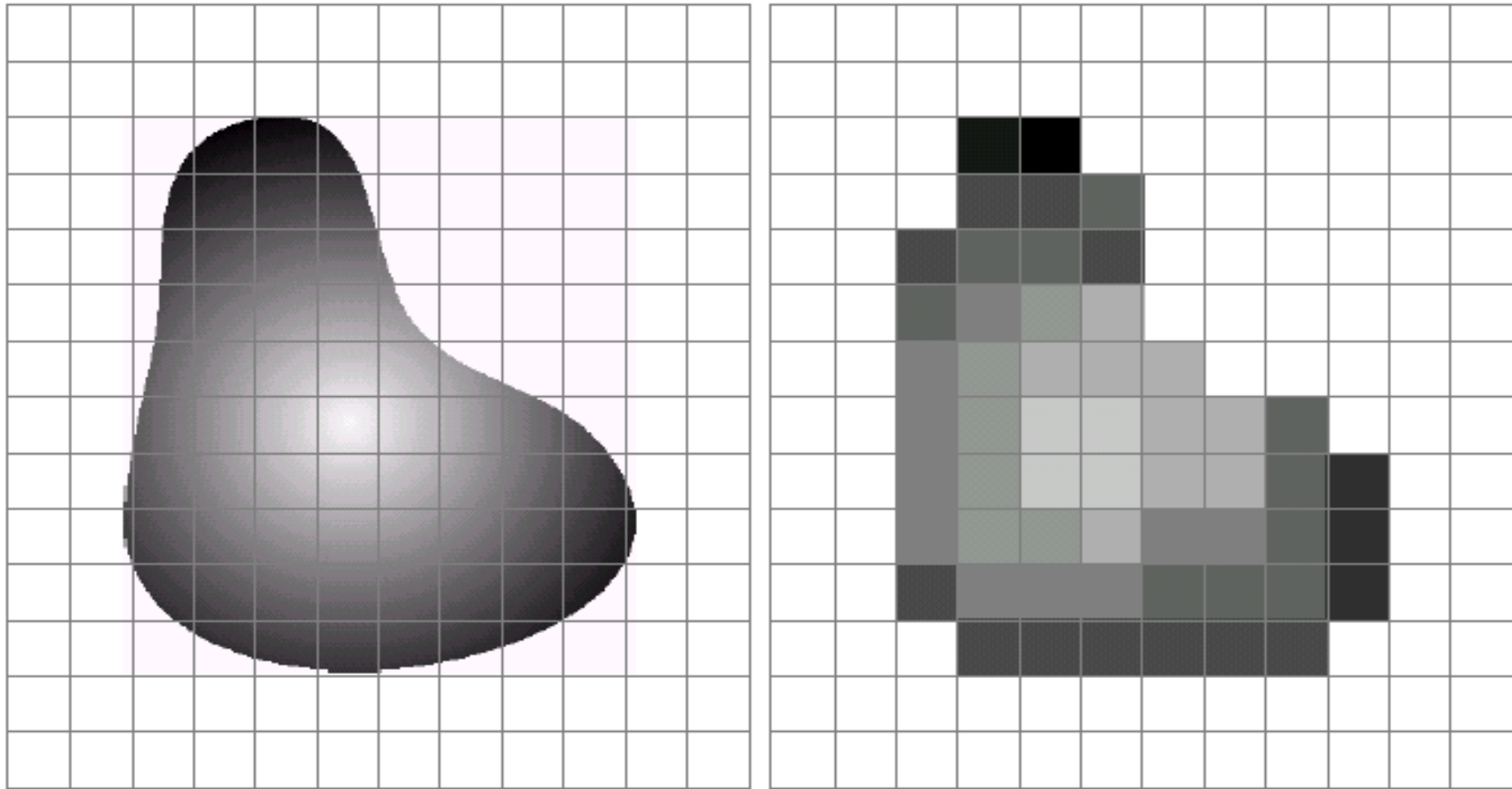


Image sampling/resolution



Spatially discretized



a b

FIGURE 2.17 (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

A digital image is discrete

$$f(x,y) \sim \begin{pmatrix} f(0,0) & f(0,1) & . & . & . & f(0,m-1) \\ f(1,0) & f(1,1) & . & . & . & f(1,m-1) \\ . & . & . & . & . & . \\ . & . & . & . & . & . \\ f(n-1,0) & f(n-1,1) & . & . & . & f(n-1,m-1) \end{pmatrix}$$

A digital image is discrete
(MATLAB convention)

$$f(x,y) \sim \begin{pmatrix} f(1,1) & f(1,2) & . & . & . & f(1,m) \\ f(2,1) & f(2,2) & . & . & . & f(2,m) \\ . & . & . & . & . & . \\ . & . & . & . & . & . \\ f(n,1) & f(n,2) & . & . & . & f(n,m) \end{pmatrix}$$

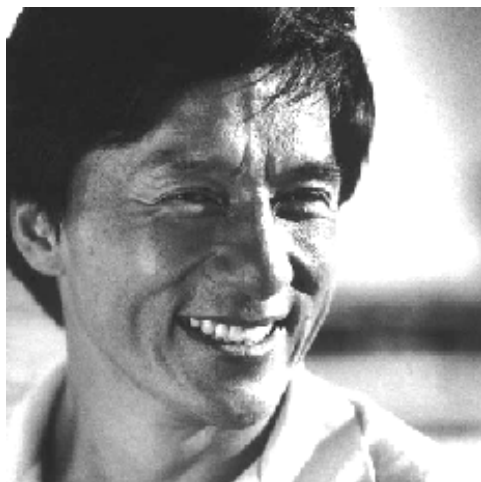
Effects of spatial resolution



a	b	c
d	e	f

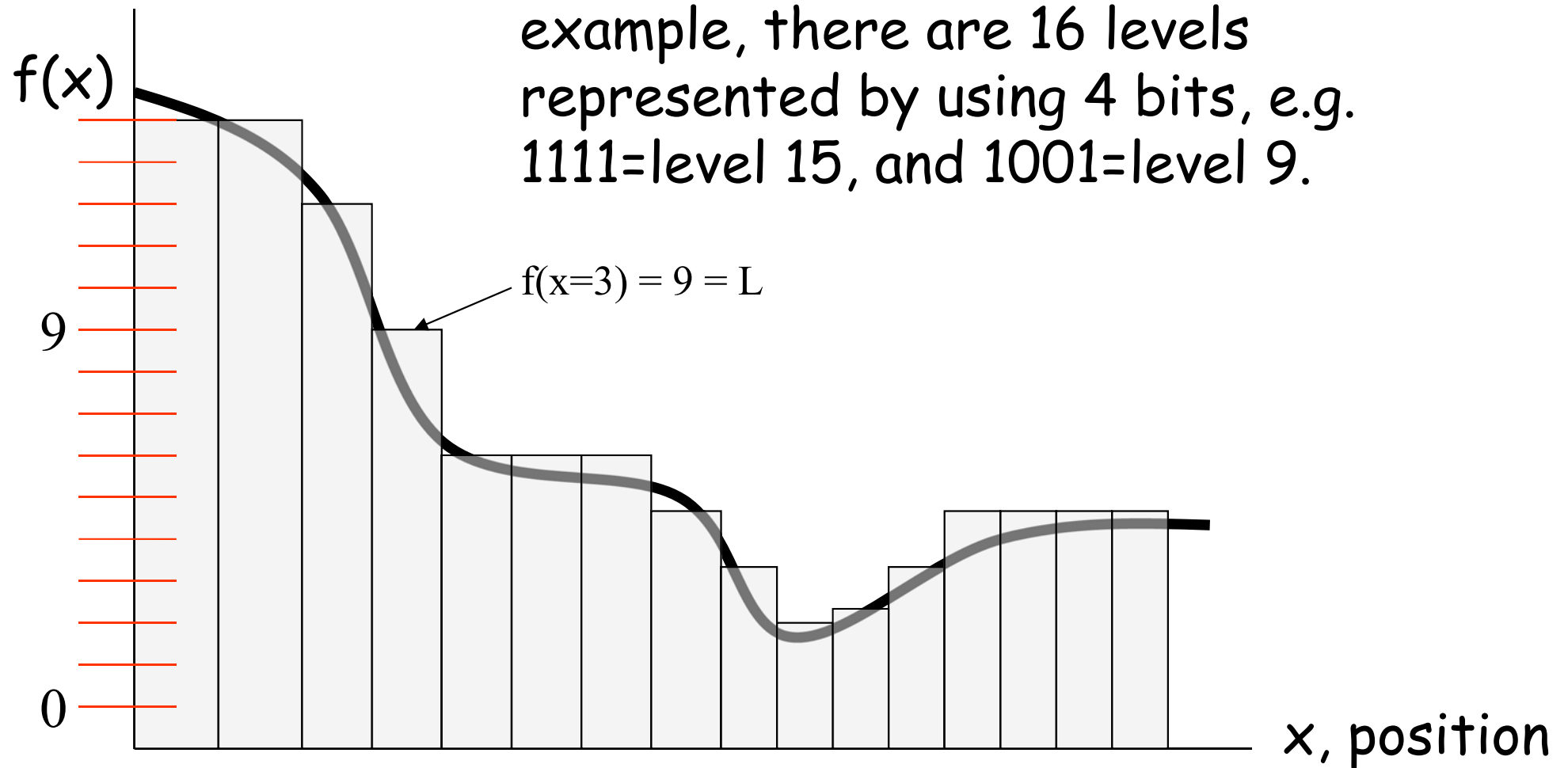
FIGURE 2.20 (a) 1024×1024 , 8-bit image. (b) 512×512 image resampled into 1024×1024 pixels by row and column duplication. (c) through (f) 256×256 , 128×128 , 64×64 , and 32×32 images resampled into 1024×1024 pixels.

Effects of spatial resolution



Intensity quantization

We will call intensity of a monochrome image, its grey level (L). In this example, there are 16 levels represented by using 4 bits, e.g. 1111=level 15, and 1001=level 9.



Effects of intensity quantization

e f
g h

FIGURE 2.21

(Continued)

(e)–(h) Image displayed in 16, 8, 4, and 2 gray levels. (Original courtesy of Dr. David R. Pickens, Department of Radiology & Radiological Sciences, Vanderbilt University Medical Center.)

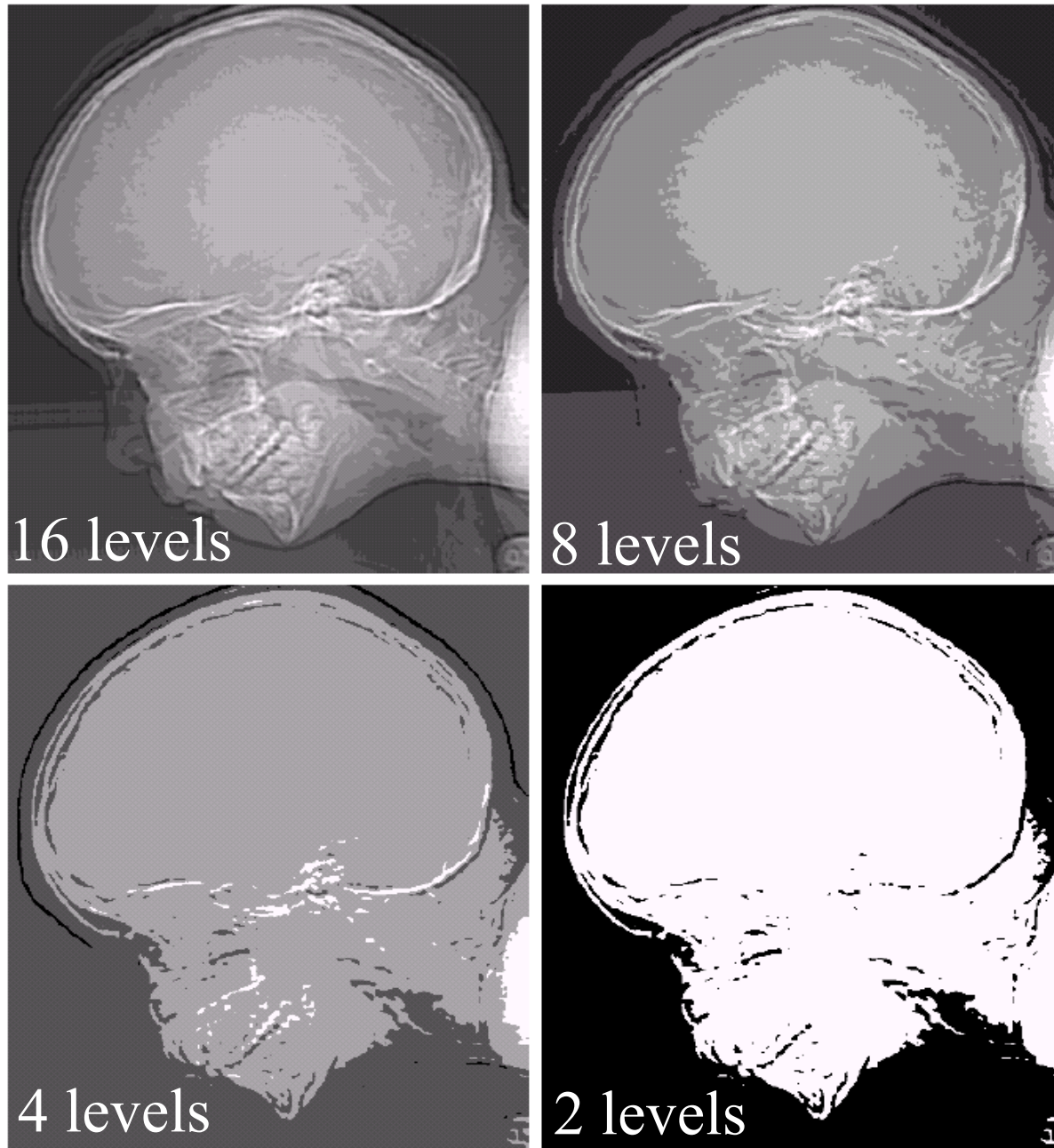
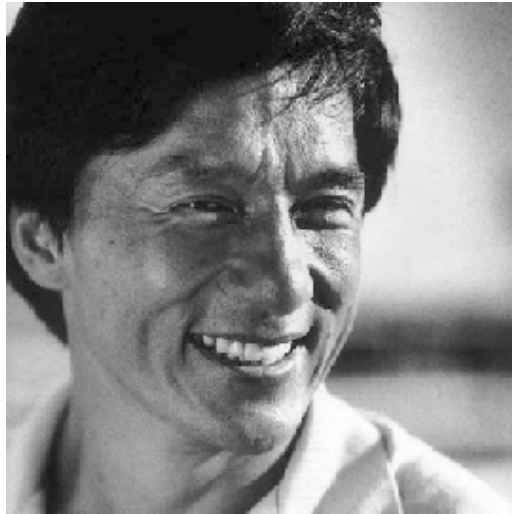


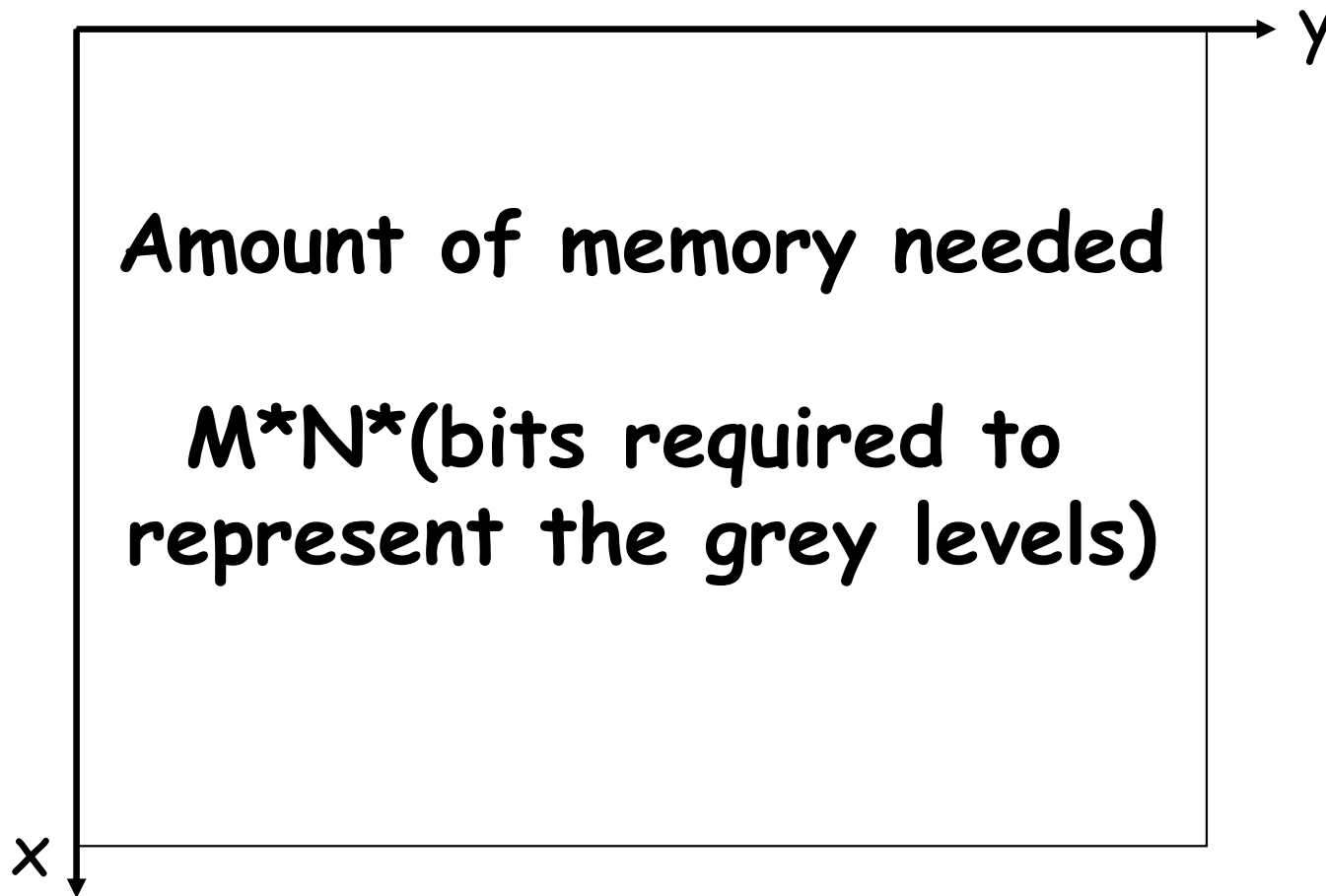
Image resolution is fixed but the number of gray levels decreases.

Effects of intensity quantization



Storage requirements

M = number of columns,
"Width" in MATLAB



N = number of rows, "height" in MATLAB