

# **DISTRIBUTED DATABASE SYSTEMS**

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# COM\_MIN Algorithm

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- **Given:** a relation  $R$  and a set of simple predicates  $p_r$
- **Output:** a complete and minimal set of simple predicates  $P_r$  for  $P_r$
- **Rule 1:** a relation or fragment is partitioned into at least two parts which are accessed differently by at least one application.

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**Algorithm 3.1:** COM\_MIN Algorithm

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**Input:**  $R$ : relation;  $Pr$ : set of simple predicates

**Output:**  $Pr'$ : set of simple predicates

**Declare:**  $F$ : set of minterm fragments

**begin**

find  $p_i \in Pr$  such that  $p_i$  partitions  $R$  according to *Rule 1* ;

$$Pr' \leftarrow p_i;$$
$$Pr \leftarrow Pr - p_i;$$
$$F \leftarrow f_i \quad \{f_i \text{ is the minterm fragment according to } p_i\} ;$$

**repeat**

find a  $p_j \in Pr$  such that  $p_j$  partitions some  $f_k$  of  $Pr'$  according to *Rule 1*

;

$$Pr' \leftarrow Pr' \cup p_j;$$
$$Pr \leftarrow Pr - p_j;$$
$$F \leftarrow F \cup f_j;$$

**if  $\exists p_k \in Pr'$  which is not relevant then**

$$Pr' \leftarrow Pr' - p_k ;$$
$$F \leftarrow F - f_k ;$$

**until**  $Pr'$  *is complete* ;

end

# PHORIZONTAL Algorithm

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## Algorithm 3.2: PHORIZONTAL Algorithm

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**Input:**  $R$ : relation;  $Pr$ : set of simple predicates

**Output:**  $M$ : set of minterm fragments

**begin**

$Pr' \leftarrow \text{COM\_MIN}(R, Pr)$  ;

    determine the set  $M$  of minterm predicates ;

    determine the set  $I$  of implications among  $p_i \in Pr'$  ;

**foreach**  $m_i \in M$  **do**

**if**  $m_i$  is contradictory according to  $I$  **then**

$M \leftarrow M - m_i$

**end**

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# PHF – Example

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- Two candidate relations : PAY and PROJ.
- Fragmentation of relation PAY
  - Application: Check the salary info and determine raise.
  - Employee records kept at two sites □ application run at two sites
  - Simple predicates
    - $p1 : SAL \leq 30000$
    - $p2 : SAL > 30000$
    - $Pr = \{p1, p2\}$  which is complete and minimal  $Pr' = Pr$
  - Minterm predicates
    - $m1 : (SAL \leq 30000)$
    - $m2 : NOT(SAL \leq 30000) = (SAL > 30000)$

# PHF – Example

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PAY<sub>1</sub>

TITLE	SAL
Mech. Eng.	27000
Programmer	24000

PAY<sub>2</sub>

TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000

# PHF – Example

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- Fragmentation of relation PROJ
  - Applications:
    - Find the name and budget of projects given their no.
      - Issued at three sites
    - Access project information according to budget
      - one site accesses  $\leq 200000$  other accesses  $> 200000$

# PHF – Example

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- Fragmentation of relation PROJ

- Simple predicates

- For application (1)

- $p1 : \text{LOC} = \text{“Montreal”}$
    - $p2 : \text{LOC} = \text{“New York”}$
    - $p3 : \text{LOC} = \text{“Paris”}$

- For application (2)

- $p4 : \text{BUDGET} \leq 200000$
    - $p5 : \text{BUDGET} > 200000$

- $P_r = P_{\hat{r}} = \{p1, p2, p3, p4, p5\}$



# PHF – Example

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- Fragmentation of relation PROJ continued
  - Minterm fragments left after elimination
    - $m1 : (LOC = \text{“Montreal”}) \wedge (BUDGET \leq 200000)$
    - $m2 : (LOC = \text{“Montreal”}) \wedge (BUDGET > 200000)$
    - $m3 : (LOC = \text{“New York”}) \wedge (BUDGET \leq 200000)$
    - $m4 : (LOC = \text{“New York”}) \wedge (BUDGET > 200000)$
    - $m5 : (LOC = \text{“Paris”}) \wedge (BUDGET \leq 200000)$
    - $m6 : (LOC = \text{“Paris”}) \wedge (BUDGET > 200000)$

# PHF – Example

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PROJ<sub>1</sub>

PNO	PNAME	BUDGET	LOC
P1	Instrumentation	150000	Montreal

PROJ<sub>3</sub>

PNO	PNAME	BUDGET	LOC
P2	Database Develop.	135000	New York

PROJ<sub>4</sub>

PNO	PNAME	BUDGET	LOC
P3	CAD/CAM	255000	New York

PROJ<sub>6</sub>

PNO	PNAME	BUDGET	LOC
P4	Maintenance	310000	Paris

# PHF – Correctness

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- Completeness
  - Since  $P_{\tilde{r}}$  is complete and minimal, the selection predicates are complete
- Reconstruction
  - If relation  $R$  is fragmented into  $F_R = \{R_1, R_2, \dots, R_r\}$ 
    - $R = \bigcup_{R_i \in F_R} R_i$
- Disjointness
  - Minterm predicates that form the basis of fragmentation should be mutually exclusive.

# **DERIVED HORIZONTAL FRAGMENTATION**

# Derived Horizontal Fragmentation

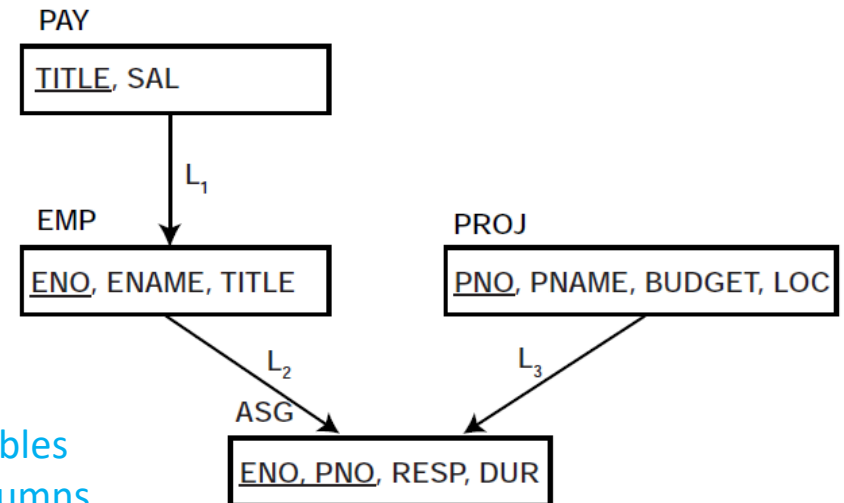
- Defined on a member relation of a link according to a selection operation specified on its owner.
- Each link is an equijoin.
- Equijoin can be implemented by means of semijoins.

links between database objects (i.e., relations in our case)

Link owner: The relation at the tail of a link

Link member: relation at the head

equijoin is a type of join that combines tables based on matching values in specified columns.



# DHF – Definition

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- Given a link  $L$  where  $owner(L) = S$  and  $member(L) = R$ , the derived horizontal fragments of  $R$  are defined as

$$R_i = R \bowtie S_i, 1 \leq i \leq w$$

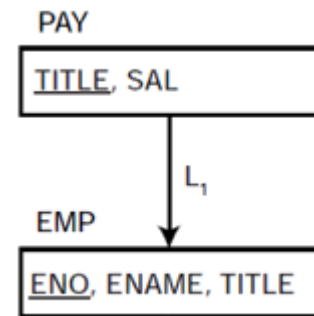
- where  $w$  is the maximum number of fragments that will be defined on  $R$  and

$$S_i = \sigma_{F_i}(S)$$

- where  $F_i$  is the formula according to which the primary horizontal fragment  $S_i$  is defined.

# DHF – Example

- Given link  $L_1$  where
  - $owner(L_1) = PAY$
  - $member(L_1) = EMP$



EMP		
ENO	ENAME	TITLE
E1	J. Doe	Elect. Eng
E2	M. Smith	Syst. Anal.
E3	A. Lee	Mech. Eng.
E4	J. Miller	Programmer
E5	B. Casey	Syst. Anal.
E6	L. Chu	Elect. Eng.
E7	R. Davis	Mech. Eng.
E8	J. Jones	Syst. Anal.

- Then we can group engineers into two groups according to their salary

- $EMP_1 = EMP \bowtie PAY_1$
- $EMP_2 = EMP \bowtie PAY_2$

- Where

- $PAY_1 = \sigma_{SAL \leq 30000}(PAY)$
- $PAY_2 = \sigma_{SAL > 30000}(PAY)$

PAY	
TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000
Mech. Eng.	27000
Programmer	24000

EMP <sub>1</sub>		
ENO	ENAME	TITLE
E3	A. Lee	Mech. Eng.
E4	J. Miller	Programmer
E7	R. Davis	Mech. Eng.

EMP <sub>2</sub>		
ENO	ENAME	TITLE
E1	J. Doe	Elect. Eng.
E2	M. Smith	Syst. Anal.
E5	B. Casey	Syst. Anal.
E6	L. Chu	Elect. Eng.
E8	J. Jones	Syst. Anal.

PAY <sub>1</sub>	
TITLE	SAL
Mech. Eng.	27000
Programmer	24000

PAY <sub>2</sub>	
TITLE	SAL
Elect. Eng.	40000
Syst. Anal.	34000

# DHF – Correctness

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- Completeness

- Referential integrity

- Let  $R$  be the member relation of a link whose owner is relation  $S$  which is fragmented as

$$F_S = \{S_1, S_2, \dots, S_n\}$$

- Furthermore, let  $A$  be the join attribute between  $R$  and  $S$ . Then, for each tuple  $t$  of  $R$ , there should be a tuple  $t'$  of  $S$  such that

$$t[A] = t'[A]$$

- Reconstruction

- Same as primary horizontal fragmentation.

- Disjointness

- disjointness is guaranteed as long as the minterm predicates determining the fragmentation are mutually exclusive.



# **VERTICAL FRAGMENTATION**

# Vertical fragmentation

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- Vertical fragmentation (VF) will group the columns of a table into fragments.
- VF must be done in such a way that the original table can be reconstructed from the fragments.
- This fragmentation requirement is called “reconstructiveness.”
- each VF fragment must contain the primary key column(s) of the table.
  - Because each fragment contains a subset of the total set of columns in the table
- To create a vertical fragment from a table:
  - a select statement is used in which “Column\_list” is a list of columns from R that includes the primary key.