# @MPRA package vignette

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## 1 Introduction

The analysis toolset for MPRA data (@MPRA) includes functions for simulating and analyzing MPRA data, and for power calculations of MPRA experiments. This tutorial briefly introduces the functions provided by the @MPRA package, using the example data included in the package.

We can load the library using:

```
library(atMPRA)
## Warning: package 'DESeq2' was built under R version 3.5.2
## Warning: package 'BiocParallel' was built under R version 3.5.2
We can do a quick power calculation:
nsim = 10
ntag = 10
result = getPower(nsim = nsim, ntag = ntag, nrepIn = 3, nrepOut = 3,
    slope = c(rep(1, ntag * nsim), rep(2, ntag * nsim)), method = c("MW",
        "mpra_lm"), scenario = "fixTotalDepth")
## Warning in getPower(nsim = nsim, ntag = ntag, nrepIn = 3, nrepOut = 3, slope = c(rep(1, : The input
## [1] 0.6
result$Power
## [1] 0.6
```

# 2 Data available in the package

The estimated distributional parameters of the MPRA data (GSE70531 in GEO database) was obtained using the estimateMPRA function in this package. The basic parameters include \ inputProp: The proportion of counts per tag among all tags in the library\ transEff: The distribution of transfection efficiencies (normalized RNA/DNA ratio) across tags\ dispFunc\_input: The dispersion function of the input tag counts across replicates as a function of the mean \ dispFunc\_output: The dispersion function of the output tag counts across replicates as a function of the mean \ The estimation was done using DESeq2. This distribution will be the default distribution for simulating MPRA data in this package if not specified otherwise. The data is loaded with the package automatically.

#### GSE70531\_params

```
## $dispFunc_input
## function (means)
## exp(predict(fit, data.frame(logMeans = log(means))))
## <bytecode: 0x7fa235a5c418>
## <environment: 0x7fa247392ff8>
## attr(,"fitType")
## [1] "local"
## attr(,"varLogDispEsts")
## [1] 0.4812829
## attr(,"dispPriorVar")
## [1] 0.25
##
## $dispFunc_output
## function (q)
## coefs[1] + coefs[2]/q
## <bytecode: 0x7fa235a079e8>
## <environment: 0x7fa235a41638>
## attr(,"coefficients")
## asymptDisp extraPois
## 0.5183263 12.7233435
## attr(,"fitType")
## [1] "parametric"
## attr(,"varLogDispEsts")
## [1] 0.8172103
## attr(,"dispPriorVar")
## [1] 0.3268525
##
## $inputProp
## function (v)
## .approxfun(x, y, v, method, yleft, yright, f)
## <bytecode: 0x7fa235a04c60>
## <environment: 0x7fa235a08270>
##
## $transEff
## function (v)
## .approxfun(x, y, v, method, yleft, yright, f)
## <bytecode: 0x7fa233e60e78>
## <environment: 0x7fa235a056a8>
##
## $sizeFactor_input
## K562_minP_DNA1 K562_minP_DNA2
        1.2060454
##
                       0.8291562
##
## $sizeFactor output
## K562_CTRL_minP_RNA1 K562_CTRL_minP_RNA2 K562_CTRL_minP_RNA3
##
             0.6613516
                                  0.4404059
                                                      1.4904598
## K562_CTRL_minP_RNA4 K562_CTRL_minP_RNA5 K562_CTRL_minP_RNA6
```

**##** 1.2337356 1.8488591 1.3372992

# 3 Functions

#### 3.1 Simulating MPRA data

There are multiple ways to simulate MPRA data in this package:\ 1. Simulating MPRA data using default distribution.\ 2. Simulating MPRA data using estimated distributions from observed data\ 3. Simulating MPRA data by specifying parameters in the model.\

The parameters for simulating a MPRA dataset includes:\ 1. number of SNPs in the data (nsim)\ 2. number of tags per SNP (ntag)\ 3. number of replicates in the input and output (nrepIn, nrepOut)\ 4. RNA/DNA ratio for all tags (slope)\ 5. Total depth for one replicate (fixTotalD) or mean depth per tag (fixMeanD)\

#### 3.1.1 Simulating MPRA data using estimated distributions from observed data

We have simulated the MPRA using defulat settings above. Now we want to demonstrate how to simulate MPRA using estimated distribution from observed data. Here we will use the parameters we estimated for GSE70531.

```
totalDepth = 2e+05
ntag = 10
nsim = 10
nrepIn = 5
nrepOut = 5
inputProp = GSE70531_params[[3]](runif(ntag * nsim * 2))
slopel = GSE70531_params[[4]](runif(nsim * 2))
inputDispFunc = GSE70531_params[[1]]
outputDispFunc = GSE70531_params[[2]]
slope = rep(slopel, each = ntag)
datt = sim_fixDepth(inputProp, ntag, nsim, nrepIn, nrepOut, slope, inputDispFunc = inputDispFunc, outputDispFunc = outputDispFunc, sampleDepth = totalDepth)
datt[1:10, ]
```

##		allele	$\mathtt{sim} \mathtt{N}$	input_rep1	input_rep2	input_rep3	input_rep4	input_rep5
##	1	Ref	1	1195	1278	1109	1034	1114
##	2	Ref	1	141	179	133	173	164
##	3	Ref	1	145	100	109	109	85
##	4	Ref	1	1047	1085	1101	1109	1263
##	5	Ref	1	17	14	17	9	16
##	6	Ref	1	3717	3950	4016	4150	3790

##	7	Ref :	242	240	223	262	293
##	8	Ref :	l 13	10	17	8	14
##	9	Ref :	100	113	109	107	84
##	10	Ref :	190	203	260	237	214
##		output_rep:	l output_rep2	output_rep3	$\verb"output_rep4"$	output_rep5	
##	1	1338	591	344	294	722	
##	2	268	3 27	39	15	12	
##	3	100	) 55	46	38	49	
##	4	1579	175	5217	1677	1173	
##	5	(	0	29	3	32	
##	6	3022	3828	3105	2027	2712	
##	7	140	328	188	218	511	
##	8	2	2 73	17	16	1	
##	9	34	1 33	35	55	50	
##	10	72	2 267	90	194	195	

If we would like to simulate data based on an observed MPRA dataset, we can estimate the parameters using the function estimateMPRA.

```
rnaCol=8
new_params=estimateMPRA(datt, nrepIn, rnaCol, nrepOut, nsim, ntag)
new_params
## $dispFunc_input
## function (q)
## coefs[1] + coefs[2]/q
## <bytecode: 0x7fa24568a830>
## <environment: 0x7fa24568aec0>
## attr(,"coefficients")
## asymptDisp extraPois
## 0.001355058 2.835324647
## attr(,"fitType")
## [1] "parametric"
## attr(,"varLogDispEsts")
## [1] 0.7014079
## attr(,"dispPriorVar")
## [1] 0.25
##
## $dispFunc_output
## function (q)
## coefs[1] + coefs[2]/q
## <bytecode: 0x7fa24568a830>
## <environment: 0x7fa247dc43f0>
## attr(,"coefficients")
## asymptDisp extraPois
## 0.5755493 12.1054886
## attr(,"fitType")
## [1] "parametric"
## attr(,"varLogDispEsts")
## [1] 1.199697
## attr(,"dispPriorVar")
## [1] 0.5547631
##
```

```
## $inputProp
## function (v)
  .approxfun(x, y, v, method, yleft, yright, f)
## <bytecode: 0x7fa24ea423a0>
   <environment: 0x7fa2343e3f68>
##
## $transEff
## function (v)
  .approxfun(x, y, v, method, yleft, yright, f)
## <bytecode: 0x7fa24ea423a0>
   <environment: 0x7fa23525e350>
##
## $sizeFactor_input
   input_rep1 input_rep2 input_rep3 input_rep4 input_rep5
    0.9894536 1.0039159 1.0005035 1.0093590 1.0007959
##
## $sizeFactor_output
  output_rep1 output_rep2 output_rep3 output_rep4 output_rep5
                               0.9246672
     1.1236062
                  1.0737031
                                            1.0506186
                                                         1.0670299
Then we can simulate new MPRA data using these parameters:
datt = sim_fixDepth(inputProp = new_params[[3]](runif(ntag * nsim * 2)),
    ntag, nsim, nrepIn, nrepOut, slope, inputDispFunc = new_params[[1]],
    outputDispFunc = new_params[[2]], sampleDepth = totalDepth)
datt[1:10, ]
##
      allele simN input_rep1 input_rep2 input_rep3 input_rep4 input_rep5
         Ref
## 1
                           351
                                       438
                                                  464
                                                              510
                                                                          402
                 1
## 2
         Ref
                 1
                          1266
                                      1245
                                                  1234
                                                             1342
                                                                         1303
## 3
         Ref
                 1
                          1116
                                      1137
                                                 1384
                                                             1108
                                                                         1199
## 4
         Ref
                           204
                                      227
                                                  244
                                                              272
                                                                          242
## 5
                                      1058
                                                 1177
                                                             1285
         Ref
                          1249
                                                                         1143
                 1
## 6
                          3260
                                                 3399
                                                             3084
                                                                         2873
         Ref
                 1
                                      3444
## 7
         Ref
                 1
                          1194
                                      1300
                                                 1119
                                                             1257
                                                                         1243
## 8
         Ref
                 1
                           860
                                       947
                                                  928
                                                              800
                                                                          869
## 9
                          1122
                                      1175
                                                             1277
         Ref
                 1
                                                 1117
                                                                         1184
## 10
                                                              254
                                                                          283
         Ref
                 1
                           218
                                       236
                                                  284
##
      output_rep1 output_rep2 output_rep3 output_rep4 output_rep5
## 1
               123
                             52
                                          34
                                                       77
                                                                   872
## 2
              1384
                            313
                                         350
                                                     2381
                                                                   371
## 3
               106
                            106
                                         367
                                                      230
                                                                  1540
## 4
               170
                             57
                                         126
                                                      158
                                                                   245
## 5
                            537
                                                                   914
               819
                                        1219
                                                     1009
## 6
              1189
                           1877
                                        6407
                                                     5602
                                                                   748
## 7
              1056
                            180
                                         476
                                                                   435
                                                      310
## 8
               666
                            992
                                         487
                                                     1664
                                                                   699
## 9
              1427
                           1111
                                         842
                                                      426
                                                                   793
## 10
                73
                            367
                                          21
                                                      471
                                                                   133
```

#### 3.1.2 Simulating MPRA data by specifying parameters in the model.

We can also simulate MPRA data by specifying parameters. For example, we may want to specify different mean input counts across tags for allele A and allele B. We can check if methods are biased by the allelic

imbalance in the input distribution later using this simulated data.

```
inputDist = GSE70531_params[[3]](runif(nsim * ntag * 2))
datt = sim_fixInputMean(mean_A = 10, mean_B = 100, ntag = ntag, nsim = nsim,
    nrepIn = nrepIn, nrepOut = nrepOut, slope = slope, inputDist = inputDist,
    inputDispFunc = inputDispFunc, outputDispFunc = outputDispFunc)
## converting counts to integer mode
## converting counts to integer mode
datt[c(1:5, 101:105), ]
##
       allele simN input_rep1 input_rep2 input_rep3 input_rep4 input_rep5
## 1
          Ref
                             3
                                        19
                                                    7
                                                               13
                                                                           16
## 2
                            15
                                        28
                                                   13
                                                               27
          Ref
                  1
                                                                           23
## 3
          Ref
                  1
                            21
                                        16
                                                   14
                                                               18
                                                                           18
                             0
## 4
          Ref
                  1
                                         0
                                                    1
                                                                0
                                                                            0
## 5
                             4
                                         1
                                                    1
                                                                8
                                                                            3
          Ref
                  1
## 101
          Mut
                           273
                                       284
                                                  249
                                                              210
                                                                          183
```

##	104	Mut 1	0	5	0	7
##	105	Mut 1	136	128	89	101
##		output_rep1	output_rep2	output_rep3	output_rep4	output_rep5
##	1	1	22	7	17	23
##	2	12	10	15	8	76
##	3	7	15	10	5	8
##	4	0	0	0	0	0
##	5	1	1	1	0	7
##	101	393	254	123	378	157
##	102	3	30	0	0	0
##	103	8	14	2	30	9
##	104	0	0	0	1	0
##	105	101	116	194	95	169

Note the distribution of counts are very different between the two alleles Ref and Mut.

## 3.2 Analyze MPRA data

## 102

## 103

Mut

We provide a list of methods to analyze MPRA data. The input MPRA data frame should have nsim\*ntag\*2 rows and 2+nrepIn+nrepOut columns. The first column should be named 'allele', and the second column should be named 'simN'. The 'allele' columns should contain only two possible values 'Ref' and 'Mut' to refer to the two versions of alleles for each SNP.

A list of the methods that are available is here:

Test	singleReplicate	OptionName
Mann-Whitney	YES	MW
Matching	YES	Matching
Adaptive	YES	Adaptive
QuASAR-MPRA	YES	QuASAR
Fisher's Exact Test	YES	Fisher
T-test	NO	T-test
mpralm using mean	NO	mpralm

Test	${\rm single Replicate}$	OptionName
mpralm using sum	NO	mpralm
edgeR	NO	edgeR
DESeq2	NO	DESeq2

To analyze a formmated MPRA data:

```
datt[1:10, ]
```

```
##
       allele simN input_rep1 input_rep2 input_rep3 input_rep4 input_rep5
## 1
                                3
          Ref
                                            19
                                                          7
                                                                      13
                                                                                    16
## 2
                                                                                    23
          Ref
                   1
                               15
                                            28
                                                         13
                                                                      27
## 3
          Ref
                   1
                               21
                                            16
                                                         14
                                                                      18
                                                                                    18
## 4
          Ref
                                0
                                             0
                                                          1
                                                                        0
                                                                                     0
                   1
## 5
          Ref
                                4
                                             1
                                                          1
                                                                        8
                                                                                     3
## 6
                                                                        3
                                                                                     0
          Ref
                                0
                                             0
                                                          \cap
                   1
## 7
          Ref
                                2
                                             8
                                                         10
                                                                        6
                                                                                     4
                               18
                                                          3
                                                                      21
                                                                                     9
## 8
          Ref
                   1
                                            13
## 9
          Ref
                               33
                                            10
                                                         14
                                                                      15
                                                                                    27
## 10
                                9
                                            10
                                                          2
          Ref
                                                                                     1
                   1
##
       output_rep1 output_rep2 output_rep3 output_rep4 output_rep5
## 1
                   1
                                22
                                               7
                                                             17
                                                                           23
## 2
                  12
                                              15
                                                              8
                                                                           76
                                10
## 3
                   7
                                15
                                              10
                                                              5
                                                                            8
                                                                            0
## 4
                   0
                                 0
                                                0
                                                              0
                                                                            7
## 5
                                                              0
                   1
                                 1
                                                1
## 6
                   0
                                 0
                                                0
                                                                            0
                                                              1
                   2
                                 7
                                               9
## 7
                                                              4
                                                                           15
## 8
                   0
                                 1
                                              10
                                                              0
                                                                            8
## 9
                   0
                                23
                                                8
                                                              8
                                                                            1
## 10
                   0
                                 3
                                                0
```

```
results = analyzeMPRA(datt, nrepIn, rnaCol, nrepOut, nsim, ntag, method = c("MW", "Adaptive", "QuASAR", "T-test", "mpralm", "DESeq2"), cutoff = 0, cutoffo = 0)
```

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred results

```
resMW resMatching resAdaptive
##
      simN
              resInput
                                                                QuASAR
## 1
         1 0.446967893 0.133300136
                                      0.7850000 0.133300136 0.70556915
##
  2
         2 0.011655012 0.965400612
                                      0.8000000 0.800000000 0.21797602
                                      0.5555556 0.555555556 0.39468110
## 3
         3 0.015220074 0.742986425
## 4
         4 0.002997003 0.093406593
                                      1.0000000 1.000000000 0.75114684
## 5
         5 0.015540016 0.408245349
                                      0.9375000 0.937500000 0.91195738
##
  6
         6 0.094719522 0.315378120
                                      1.0000000 0.315378120 0.24724308
## 7
         7 0.954645355 0.004795205
                                      0.0200000 0.004795205 0.49637433
         8 0.015540016 0.572603867
                                      1.0000000 1.000000000 0.27658795
## 8
## 9
         9 0.002756067 0.931427396
                                      0.6000000 0.600000000 0.65749897
## 10
        10 0.002879473 0.853428305
                                      0.8400000 0.840000000 0.06888803
##
      ttest paired
                        ttest mpralm mean mpralm sum
        0.49600889 0.44695352 0.13947732 0.17692214 0.41145687
## 1
## 2
        0.62283991 0.60933897 0.74079292 0.58523620 0.54655056
```

```
0.67165489 0.57520972 0.87891246 0.21255610 0.56512818
## 3
## 4
       0.15584428 0.08185680 0.05774892 0.06173449 0.02402666
## 5
        0.12586559 0.14520206 0.40745486 0.08727867 0.06398433
        0.12791239 0.16463032 0.65767993 0.39718596 0.24811849
## 6
##
        0.18530027 0.18304483 0.03245511 0.26855007 0.08682319
## 8
       0.03619947 0.02659521 0.41057972 0.07743880 0.03366014
## 9
        0.83524321 0.83505842 0.28909495 0.36536318 0.80565785
## 10
       0.66773593  0.65763577  0.32731427  0.84686548  0.65469411
```

You can remove tags with mean counts less than the cutoffs specified for the input and output.

#### 3.3 Power calculation

We can compute power based on simulated MPRA data specified using the options described above. Addition parameters here include the correction method for multiple testing, and the significance level to be used.

```
nrepIn = 2
nrepOut = 2
slopel = GSE70531_params[[4]](runif(nsim))
slopel = c(slopel, slopel + 1)
slope = rep(slopel, each = ntag)
result2 = getPower(nsim, ntag, nrepIn, nrepOut, slope, scenario = "fixInputDist",
    method = c("MW", "T-test", "mpralm", "edgeR", "DESeq2"),
    fixInput = c(20, 100), inputDist = inputDist, inputDispFunc = inputDispFunc,
    outputDispFunc = outputDispFunc, cutoff = -1, cutoffo = -1)
##
          resMW ttest_paired
                                            mpralm_mean
                                     ttest
                                                           mpralm_sum
##
            0.1
                          0.0
                                       0.0
                                                     0.2
                                                                  0.0
##
                      DESeq2
          edgeR
##
            0.5
                          0.5
result2$Power
##
          resMW ttest_paired
                                     ttest
                                            mpralm_mean
                                                           mpralm_sum
##
            0.1
                          0.0
                                       0.0
                                                     0.2
                                                                  0.0
##
                      DESeq2
          edgeR
##
                          0.5
            0.5
result3 = getPower(nsim, ntag, nrepIn, nrepOut, slope = 1, scenario = "fixTotalDepth",
    method = c("MW", "Matching", "Adaptive", "Fisher", "QuASAR", "T-test",
        "mpralm", "edgeR", "DESeq2"), fixTotalD = 2e+05, inputDist = inputDist,
    inputDispFunc = inputDispFunc, outputDispFunc = outputDispFunc, cutoff = -1,
    cutoffo = -1)
##
                                                  QuASAR fisherPvalue
          resMW
                 resMatching resAdaptive
##
            0.0
                          0.0
                                       0.0
                                                     0.0
                                                                  0.9
##
  ttest_paired
                        ttest
                               mpralm_mean
                                             mpralm_sum
                                                                edgeR
##
                          0.0
                                       0.0
                                                     0.0
                                                                  0.0
            0.0
         DESeq2
##
            0.0
##
result3$Power
##
          resMW
                                                  QuASAR fisherPvalue
                 resMatching
                              resAdaptive
##
            0.0
                          0.0
                                                     0.0
                                                                  0.9
## ttest paired
                              mpralm mean
                                                                edgeR
                       ttest
                                             mpralm sum
##
            0.0
                          0.0
                                       0.0
                                                     0.0
                                                                  0.0
```

```
## DESeq2
## 0.0
```

## 3.4.Other methods included

calEnrichment: This function uses hypergeometric tests to compute enrichment in SNPs with significant allelic DNA imbalance among the SNPs with significant allele-specific effect defined by each method.

```
calEnrichment(results)
```

## Compute enrichment in allele-imbalanced SNPs among significant results...

```
##
           method q m
                        enrichP
## 1
            resMW 0 1 1.0000000
## 2
      resMatching 0 1 1.0000000
      resAdaptive 0 1 1.0000000
## 3
## 4
           QuASAR 0 0 1.000000
## 5 ttest_paired 1 1 0.7000000
## 6
            ttest 1 1 0.7000000
## 7
      mpralm_mean 0 1 1.0000000
       mpralm_sum 0 0 1.0000000
## 8
## 9
           DESeq2 2 2 0.4666667
```