# Induction heuristics

#### **Basic heuristics**

Theorems about recursive functions are proved by induction

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Induction on argument number i of f if f is defined by recursion on argument number i

primrec itrev :: 'a list  $\Rightarrow$  'a list  $\Rightarrow$  'a list

```
primrec itrev :: 'a list \Rightarrow 'a list \Rightarrow 'a list itrev [] ys = ys | ys = ys |
```

```
primrec itrev :: 'a list \Rightarrow 'a list \Rightarrow 'a list itrev [] ys = ys | ys = itrev(x#xs) ys = itrev(x#ys)
```

```
primrec itrev :: 'a list \Rightarrow 'a list \Rightarrow 'a list itrev [] ys = ys | ys = itrev(x\#xs) ys = itrev(x\#ys) | ys = itrev(x*s) | ys = itrev(x*s
```

## Demo: first proof attempt

### Generalisation (1)

Replace constants by variables

lemma itrev xs ys = rev xs @ ys

## Demo: second proof attempt

## Generalisation (2)

Quantify free variables by ∀ (except the induction variable)

lemma  $\forall$  ys. itrev xs ys = rev xs @ ys