

- A. Which, if any, of the following algorithms, bubble-sort, heap-sort, insertion sort, merge-sort, and quick-sort, are stable? Briefly justify your answer.

A sorting algorithm is stable if it does not change the order of the element with the same values

Example :bubble sort ,insertion sort ,merge sort are stable

Selection sort is unstable and heap sort also unstable

Sample for selection sort;

If arr=[4,4,2,1]

Using selection sort

4,4,2,1. Find the mini

4,4,2,1 swap

1,4,2,4 find mini

1,4,2,4 swap

1,2,4,4. So that here the order of 4 is changes the first 4 comes before the second 4 this is unstable;

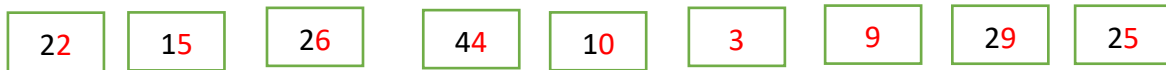
Out of the not inplace sort algorithm radix sort ,bucket sort are stable and PQ sort is unstable because of the bubble down and bubble up it may interchange their order of the same values;

- B. Is the bucket-sort algorithm in-place? Why or why not?

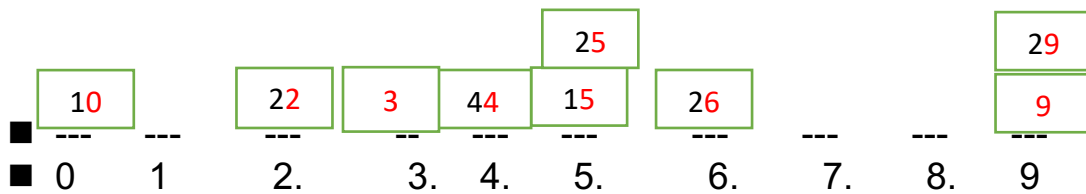
Not in place because this sorting technique uses extra memory to sort the elements so that this is not in place sorting algorithm

- C. Illustrate the performance of the radix-sort algorithm on the following input sequence

(22, 15, 26, 44, 10, 3, 9, 13, 29, 25).



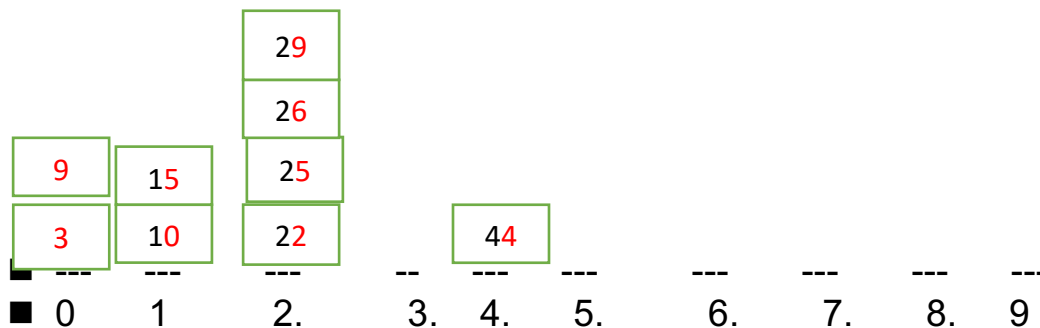
Step 1:



Step 2



Then compared the second digit



Finally it will be sorted



Result will be **[3,9,10,15,22,25,26,29,44]**

E. What can you conclude about the different sort algorithms?

Generally bubble sort, shell sort, selection sort, heap sort, insertion sort are in-place sorting algorithm techniques that means they do not use extra memory to do sorting and PQ, radix, bucket sort are generally not in-place they use extra memory's to do sorting

For almost sorted elements and few elements insertion sort is better than the other techniques

But overall heap sort has better efficiency than the other in-place sorting algorithm

Generally, to compare all the sorting algorithm based on their time complexity and space complexity is

Radix sort are more efficient than the other not in place sorting algorithm

In place sorting algorithm					
Sorting Algorithm	Time complexity			Space complexity	
	best case	average case	worst case	worse case	stable
Bubble sort	$O(N^2)$	$O(N^2)$	$O(N^2)$	$O(1)$	yes
Selection sort	$O(N^2)$	$O(N^2)$	$O(N^2)$	$O(1)$	no
Insertion sort	$O(N)$	$O(N^2)$	$O(N^2)$	$O(1)$	yes
Heap sort	$O(N \log N)$	$O(N \log N)$	$O(N \log N)$	$O(1)$	no
Quick sort	?	?	?	?	?
not In place sorting algorithm					
Sorting Algorithm	Time complexity			Space complexity	
	best case	average case	worst case	worse case	stable
Bucket sort	$O(N+k)$	$O(N+k)$	$O(N^2)$	$O(N)$	yes
Radix Sort	$O(N \cdot k)$	$O(N \cdot k)$	$O(N \cdot k)$	$O(N)$	yes
PQ sort	$O(N \log N)$	$O(N \log N)$	$O(N \log N)$	$O(N)$	no
Merge sort	?	?	?	?	?

Algorithm theSameSet(A,B)

If A.length!=B.length	1
return false;	1
PQSort(A)	nlogn
PqSort(B)	nlogn
for i:=0 to A.length do n	
if A[i]!=B[i]	n
return false	1
return true;	1

Big O of this is $O(n\log n + n)$

```
function theSameSet(A,B){
    if(A.length!==B.length) return false;
    let sort=new Sorts.ArraySorter();
    sort.PQSort(A)
    sort.PQSort(B)
    for(let i=0;i<A.length;i++){
        if(A[i]!=B[i])
            return false
    }
    return true
}

let A= [1,4,3]
let B= [4,1,3]
console.log("expected true: "+ theSameSet(A,B))
let C=[9,1,3]
let D=[9,1,2]
console.log("expected false: "+ theSameSet(C,D))
```