



VECTOR CALCULUS, LAPLACE TRANSFORM & NUMERICAL METHODS
(MA221TA)
UNIT-V

Numerical Methods

TUTORIAL SHEET-1

1. If $f(x)$ is a continuous function such that $f(a).f(b) < 0$, then the equation $f(x) = 0$, has _____ roots in the interval $[a, b]$.
2. In the method of false position for finding the root of an equation $f(x) = 0$, in the interval $[a, b]$ the curve $f(x)$ is replaced by _____.
3. In Newton-Raphson method for finding the root of an equation $f(x) = 0$, in the interval $[a, b]$ the curve $f(x)$ is replaced by _____.
4. If $f(x)$ is a continuous function such that $f(a)$ and $f(b)$ have same sign, then the equation $f(x) = 0$, has _____ roots in the interval $[a, b]$.
5. Find the positive real root of the equation $x^4 - x - 10 = 0$, which lies between 1 and 2 by method of false position correct to five places of decimal.
(Answer: 1.855584)
6. Find an approximate real root of the equation $= \frac{\cos(x)+1}{3}$, correct to four places of decimal using Regula falsi method.
(Answer: 0.6071)
7. Find a positive real root of the equation $2x - \ln(x) = 6$, correct to three places of decimal by method of chords.
(Answer: 3.257)
8. Using method of false position find a positive real root of the equation $x\sin(x) + \cos(x) = 0$ which lies between 2 and 3 correct three places of decimal.
(Answer: 2.798)



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TUTORIAL SHEET-2

1. Find the negative real root of equation $x^3 - 21x + 3500 = 0$, correct to four places of decimal using Newton-Raphson method. (Answer: -15.64385)
2. Find a positive real root of equation $x\sin(x) + \cos(x) = 0$ near $x = \pi$ using method of tangents. (Answer: 2.798)
3. Using Newton-Raphson method find the reciprocal of a non-zero positive number 'N', hence find $(1/31)$.
4. The bacteria concentration in a reservoir varies as $c = 4e^{-2t} + e^{-0.1t}$, using Newton Raphson method, calculate the time required for bacteria concentration to be 0.5 (Answer: 6.889)
5. The current 'I' in an electric circuit is given by $I = 10e^{-t}\sin(2\pi t)$, 't' in seconds, using Newton Raphson method find the value of 't' for $I = 2A$. (Answer: 0.0333)
6. Determine the root of the equation $x^2 - \ln(x) - 12 = 0$, in $(3, 4)$ using Newton's method. (Answer: 3.646044)



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TUTORIAL SHEET-3

1. Obtain the Taylor series solution of the initial value problem $y' = y \sin(x) + \cos(x)$, $y(0) = 0$, up to terms containing x^5 . Hence, find $y(0.1)$
(Answer: $y = x + \frac{x^3}{6} + \frac{x^5}{120} + \dots$, $y(0.1) = 0.10016675$)
2. Find the approximate Taylor series solution of $xy' = x - y$, $y(2) = 2$ for $x = 2.1$
(Answer: 2.00238)
3. Using the Runge-Kutta method evaluate $y(1.1)$, given $y' = 2x - y$, $y(1) = 3$, $h = 0.1$
(Answer: 2.9145)
4. Solve $y' - x^2y = x$, $y(0) = 1$ for $x = 0.1, 0.2$ by using Runge-Kutta method.
(Answer: 1.0053, 1.0227)
5. By using Milne method solve $y' = x^2 + y^2$, $y(0) = 1$ finding $y(0.1)$, $y(0.2)$ and $y(0.3)$ from the Taylor series method.
(Answer: 1.6876)
