

$v_d$

$v_+$

$v_-$

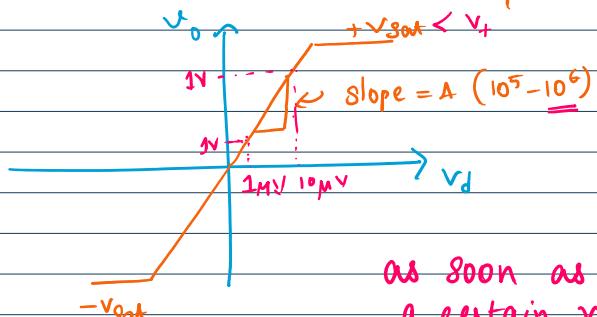
$v_{out} = Av_d$

$A \rightarrow 10^5 - 10^6$

$= 1mV \times 10^5$

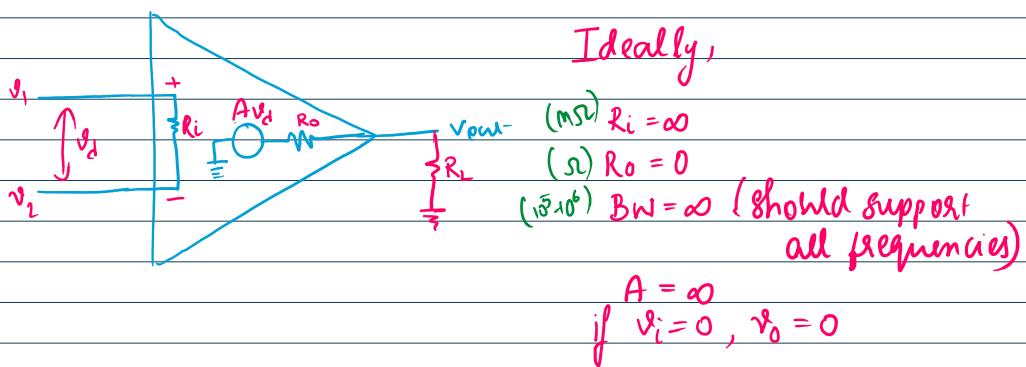
$= 100V$

{ o/p voltage lies  
b/w the biasing voltages }



as soon as i/p voltage goes beyond a certain value, the o/p will get saturated to the  $\oplus$  saturation voltage.

Similarly, as soon as i/p voltage goes beyond some threshold value, at the o/p you will get  $\ominus$  saturation voltage.



→ Slew rate - how fast op amp is able reach its final value



$$SR = \frac{dv_o}{dt} \quad \begin{matrix} \text{rate of} \\ \text{change of} \\ \text{o/p voltage} \\ \text{per unit time.} \end{matrix}$$

Ideally,  $SR = \infty$  [unit: V/μs]

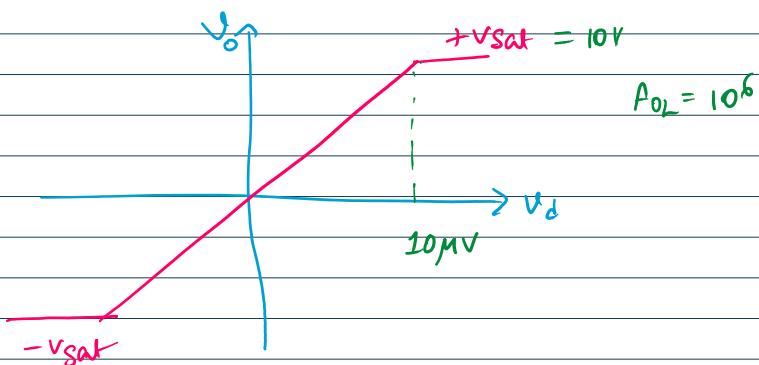
→ Common Mode Rejection Ratio: How well the op amp is able to reject the common mode voltages that are being applied to both inputs and how well it is able to amplify the diff. b/w the two voltages.

$$CMRR = \frac{A_d}{A_c} \quad \begin{matrix} \text{Ratio of differential voltage gain to} \\ \text{common mode voltage gain.} \end{matrix}$$

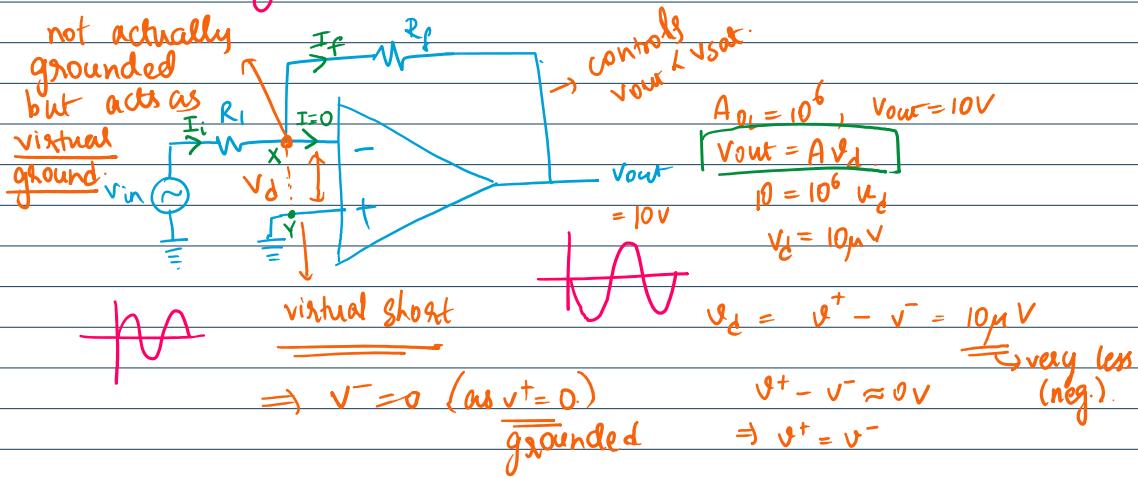
Ideally,  $CMRR = \infty$

### OP AMP 741

$R_i$	$2M\Omega$
$R_o$	$75\Omega$
$A$	$10^5$
Offset voltage	1mV
$SR$	$0.5 V/\mu s$
CMRR	70-90dB



## C1: Inverting Op Amp



$$R_{in} = \infty \Rightarrow I = 0$$

$$\rightarrow I_i = I_f$$

$$\frac{V_{in} - V_x}{R_i} = \frac{V_x - V_{out}}{R_f} \quad \left( V_x = 0 \text{ as } Y \text{ is grounded} \right)$$

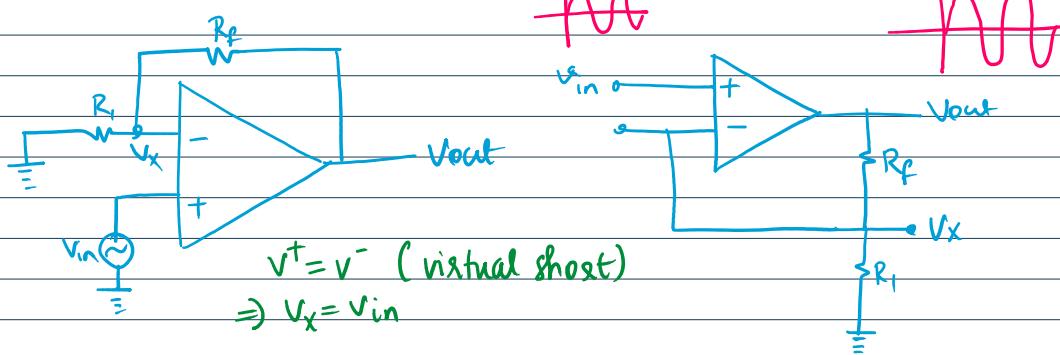
by virtual ground concept.

$$\frac{V_{in}}{R_i} = -\frac{V_{out}}{R_f}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_f}{R_i}$$

$$A_{CL} = -\frac{R_f}{R_i}$$

## C2: Non-inverting Op Amp



$$V_x = \frac{R_i}{R_i + R_f} \times V_{out}$$

$$\left. \begin{array}{l} A_{CL} = A_f \text{ (w/ feedback)} \\ A_{OL} = A \text{ (w/o feedback)} \end{array} \right\}$$

$$V_K = \frac{R_L}{R_L + R_F} \times V_{out}$$

$$V_{in} = \frac{R_1}{R_1 + R_F} \times V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{R_1 + R_F}{R_1}$$

$$A_{CL} = 1 + \frac{R_F}{R_1}$$

Advantages of NIOA over IOA

↓  
Same phase

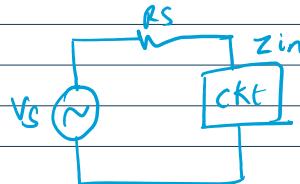
↓  
180° phase shift.

$$Z_{in} = \frac{V_{in}}{I_{in}}, I_{in} = 0$$

$$\Rightarrow Z_{in} = \infty$$

$$Z_{in} = \frac{V_{in}}{I_{in}}, I_{in} = \frac{V_{in}}{R_1}$$

$$\Rightarrow Z_{in} = R_1$$

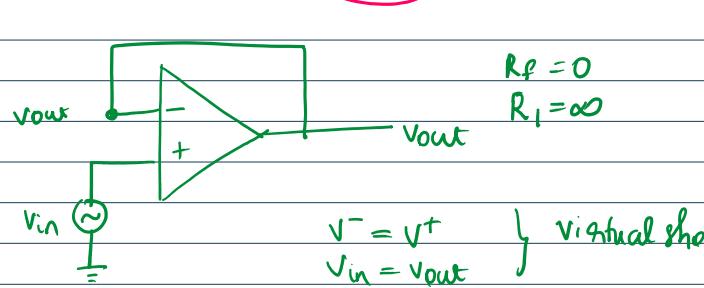


$$Z_{in} = R_S$$

$$V = \frac{R_{in}}{R_{in} + R_S} \times V_S = \frac{V_S}{2}$$

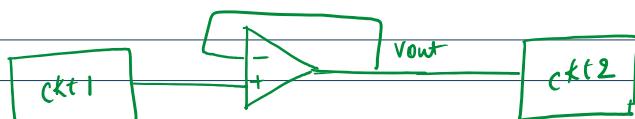
→  $Z_{in} \neq \infty$ .

Op Amp as a Buffer →  $Z_{in}$  of Buffer is very high !!

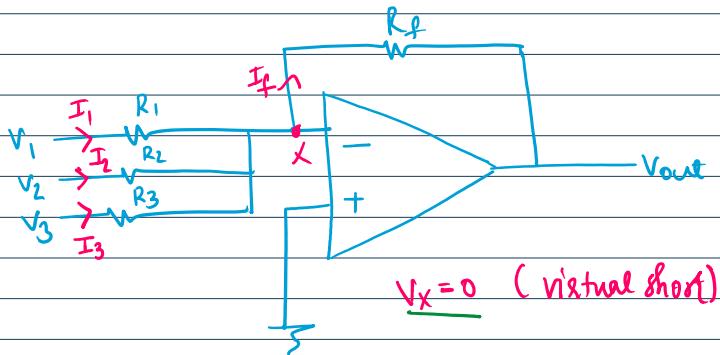


Voltage follower circuit

→ Can isolate & diff circuits.



## Inverting Summing Amplifiers:



$$I_1 + I_2 + I_3 = I_f$$

$$\frac{V_1 - 0}{R_1} + \frac{V_2 - 0}{R_2} + \frac{V_3 - 0}{R_3} = \frac{0 - V_{out}}{R_f}$$

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} = -\frac{V_{out}}{R_f}$$

$$V_{out} = -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right)$$

→ if  $R_1 = R_2 = R_3 = R$

$$V_{out} = -\frac{R_f}{R} (V_1 + V_2 + V_3)$$

if  $R_f = R$ ,

$$V_{out} = -(V_1 + V_2 + V_3)$$

→ if  $R_1 \neq R_2 \neq R_3$ ,  $\frac{R_f}{R_1} \neq \frac{R_f}{R_2} \neq \frac{R_f}{R_3}$

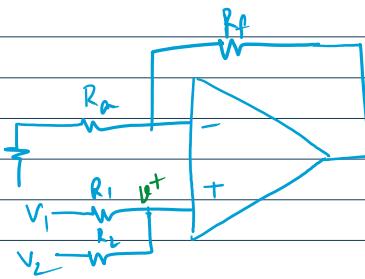
$$V_{out} = -[A V_1 + B V_2 + C V_3]$$

Can be used for → summing, scaling, averaging  
providing DC offset

Digital to analog converter

audio mixer.

## Non-Inverting Summing Amplifier



$$\rightarrow V_{out} = \left(1 + \frac{R_f}{R_a}\right) V^+$$

$$V_{out} = \left(1 + \frac{R_f}{R_a}\right) \left(\frac{R_2}{R_1+R_2} V_1 + \frac{R_1}{R_1+R_2} V_2\right)$$

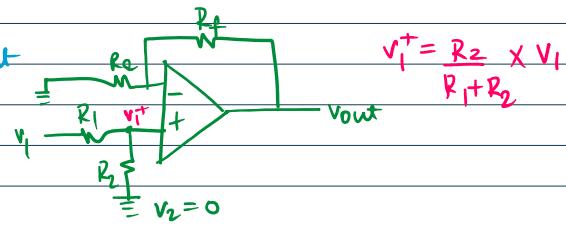
if  $R_1 = R_2$ ,

$$V_{out} = \left(1 + \frac{R_f}{R_a}\right) \left(\frac{V_1 + V_2}{2}\right)$$

if  $R_f = R_a$

$$V_{out} = V_1 + V_2$$

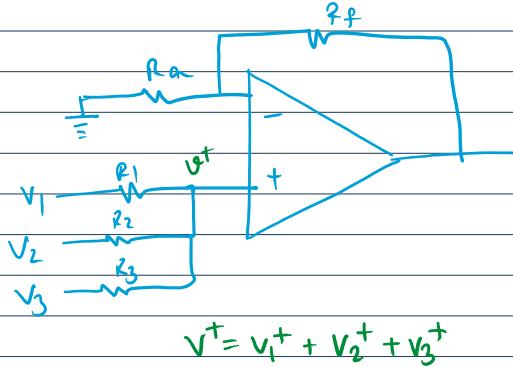
Superposition Theorem:



$$V_{out1}^+ = \frac{R_2}{R_1+R_2} V_1$$

$$V_{out2}^+ = \frac{R_1}{R_1+R_2} V_2$$

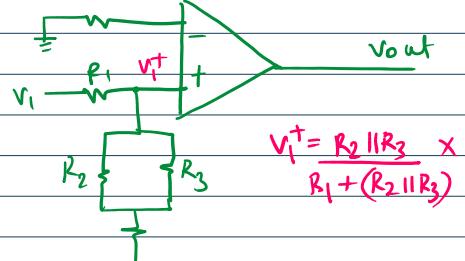
$$\begin{aligned} V^+ &= V_1^+ + V_2^+ \\ &= \frac{R_2}{R_1+R_2} V_1 + \frac{R_1}{R_1+R_2} V_2 \\ &= \frac{R_2 V_1 + R_1 V_2}{R_1+R_2} \end{aligned}$$



$$V^+ = V_1^+ + V_2^+ + V_3^+$$

$$\text{if } R_1 = R_2 = R_3, \quad V_1^+ = \frac{V_1}{3}, \quad V_2^+ = \frac{V_2}{3}, \quad V_3^+ = \frac{V_3}{3}$$

$$V^+ = \frac{V_1 + V_2 + V_3}{3}$$



$$V_{out1}^+ = \frac{R_2 || R_3}{R_1 + (R_2 || R_3)} \times V_1$$

$$\text{Similarly } V_{out2}^+ = \frac{R_1 || R_3}{R_2 + (R_1 || R_3)} \times V_2$$

$$V_{out3}^+ = \frac{R_1 || R_2}{R_3 + (R_1 || R_2)} \times V_3$$

$$\rightarrow V_{out} = \left(1 + \frac{R_f}{R_a}\right) \left(\frac{V_1 + V_2 + V_3}{3}\right)$$

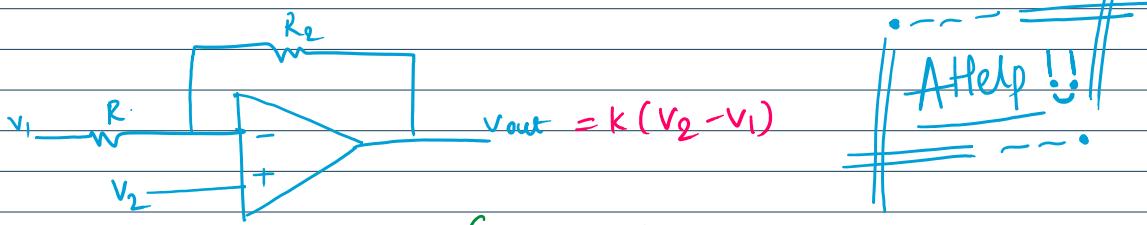
$$\text{if } 1 + \frac{R_f}{R_a} = 3, \quad V_{out} = \underline{\underline{V_1 + V_2 + V_3}}$$



## Differential Amplifier



## Differential Amplifier



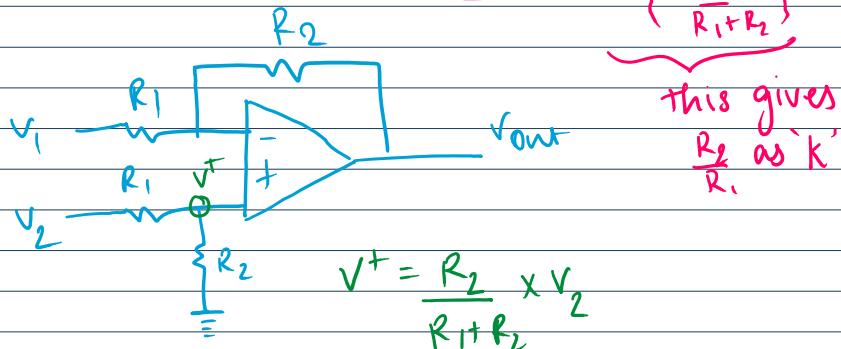
$$\left\{ \begin{array}{l} V_{o1} = \left( -\frac{R_f}{R_1} \right) V_1 \quad \text{if } V_1 \rightarrow \infty \\ V_{o2} = \left( 1 + \frac{R_f}{R_1} \right) V_2 \quad \text{if } V_2 \rightarrow \infty \end{array} \right.$$

~~At help !!~~

$$V_{out} = V_{o1} + V_{o2}$$

$$= \left( -\frac{R_f}{R_1} \right) V_1 + \left( 1 + \frac{R_f}{R_1} \right) V_2$$

$$\times \left( \frac{R_2}{R_1 + R_2} \right)$$



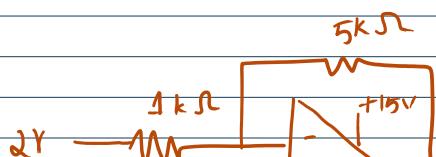
this gives  
 $\frac{R_2}{R_1}$  as 'K'

$$\begin{aligned} V_{o2} &= \left( 1 + \frac{R_2}{R_1} \right) V^+ \\ &= \left( \frac{R_1 + R_2}{R_1} \right) \left( \frac{R_2}{R_1 + R_2} \right) V_2 \\ &= \frac{R_2}{R_1} V_2 \end{aligned}$$

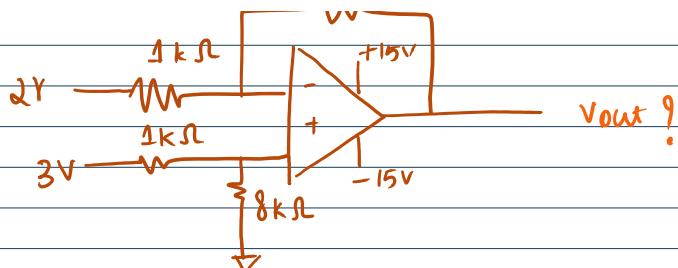
$$\begin{aligned} V_{out} &= V_{o1} + V_{o2} \\ &= \left( -\frac{R_2}{R_1} \right) V_1 + \left( \frac{R_2}{R_1} \right) V_2 \end{aligned}$$

$$V_{out} = \frac{R_2}{R_1} (V_2 - V_1)$$

e.g



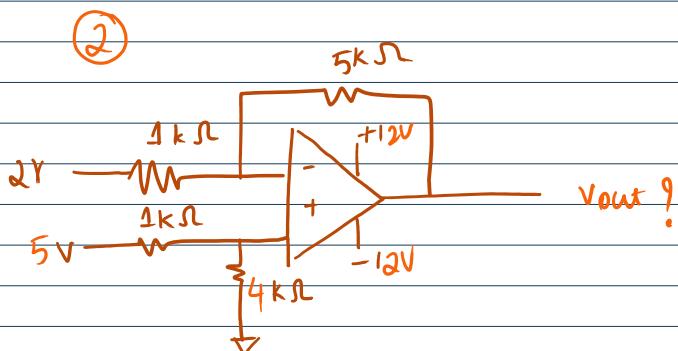
$$V_1 = 2V$$



$$\begin{aligned}V_1 &= 2V \\V_2 &= 3V \\R_1 &= 1k\Omega \\R_2 &= 5k\Omega \\R_3 &= 8k\Omega\end{aligned}$$

$$\begin{aligned}
 V_{out} &= V_{O1} + V_{O2} \\
 &= \left( \frac{-R_2}{R_1} \right) V_1 + \left( 1 + \frac{R_2}{R_1} \right) V^+ \\
 &= \frac{-5k \times 2}{1k} + \left( 1 + \frac{5k}{1k} \right) \left( \frac{8k}{1k+8k} \times 3 \right) \\
 &= -10 + 16 \\
 V_{out} &= 6V
 \end{aligned}$$

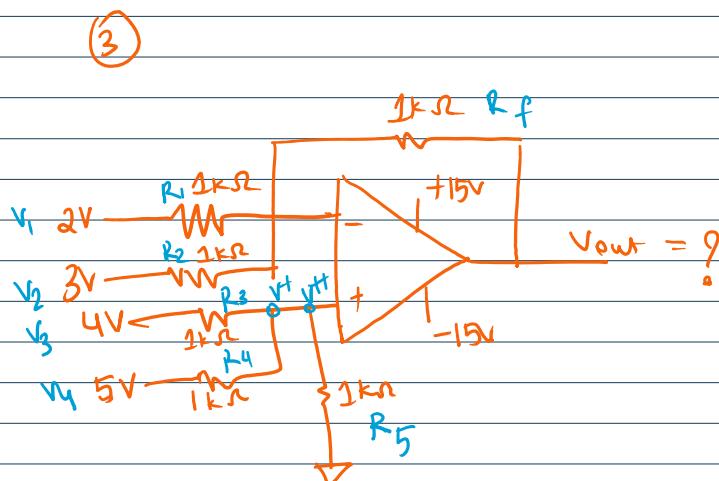
lies b/w  $\underbrace{-15V \text{ to } +15V}$   
 biasing voltages



$$V_{out} = 14V \times$$

but +12 is max 93

$$V_{out} = 12V$$



see

$$V_{01} = - R_F \left( \frac{V_1 + V_2}{R_1 + R_2} \right)$$

$$V_{01} = -5V$$

Let  $R_3 = R_4 = R$

$$V_{O2} = \left(1 + \frac{R_2}{R_{II}}\right) V^+$$

here,  $R_2 \parallel R_{II}$

$$V_{O2} = \left(1 + \frac{1k}{0.5k}\right) 3$$

$$V_{O2} = 9V$$

$$V_{OUT} = V_{O1} + V_{O2}$$

$$= -5 + 9$$

$$\underline{\underline{V_{OUT} = 4V}}$$

$$V^+ = \frac{R_S \times V^+}{R_S + R_{II}}$$

$$\left. \begin{aligned} R_{II} &= \frac{R \times R}{R + R} \\ &= \frac{R}{2} \\ R_{II} &= 0.5k\Omega \end{aligned} \right\}$$

$$V^+ = \frac{R_4 \times V_3 + R_2 \times V_4}{R_3 + R_4}$$

$$= \frac{R \times V_3 + R \times V_4}{R + R}$$

$$= \frac{4}{2} + \frac{5}{2}$$

$$= 2 + 2.5$$

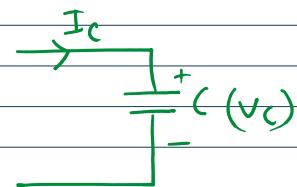
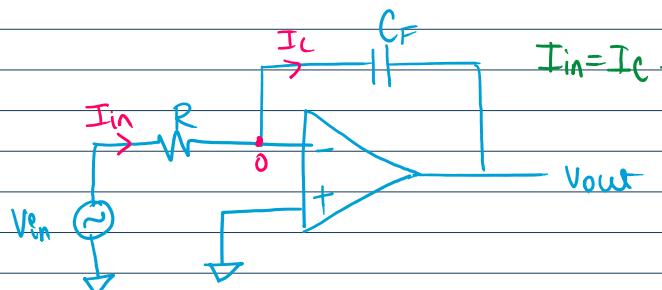
$$V^+ = 4.5$$

$$V^{++} = \frac{1k}{1k + 0.5k} \times 4.5$$

$$= 3V$$



## Op Amp Integrator



$$Q = CV$$

$$I_C = \frac{dQ}{dt}$$

$$I_C = C \frac{dV_C}{dt}$$

$$\frac{V_{in} - 0}{R} = I_C$$

$$\frac{V_{in}}{R} = C_F \frac{dV_C}{dt} \quad [V_C = 0 - V_{out}]$$

$$\frac{V_{in}}{R} = C_F \frac{d(0 - V_{out})}{dt}$$

$$\frac{V_{in}}{R} = -C_F \frac{dV_{out}}{dt}$$

$$\frac{dV_{out}}{dt} = -\frac{1}{RC_F} \times V_{in}(t)$$

$$V_{out} = -\frac{1}{RC_F} \int V_{in}(t) dt + V_{out}(0^+)$$





$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

$$V_{out} = -\frac{X_C}{R} \times V_{in}$$

$$A_V = -\frac{X_C}{R} = \frac{1}{2\pi \times R \times C \times f}$$

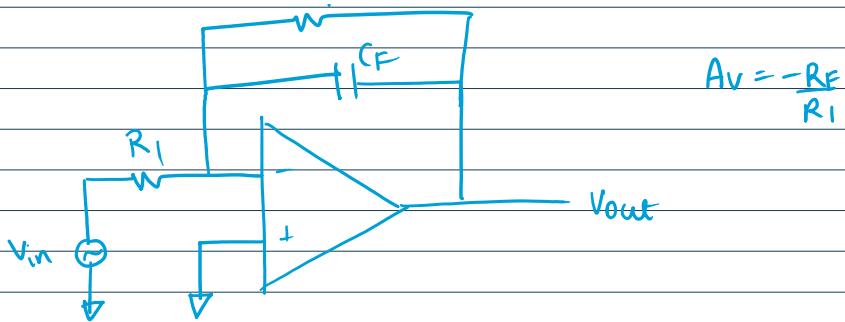
Frequency response of Ideal Integrator.



Practical Integrator using OP AMPS

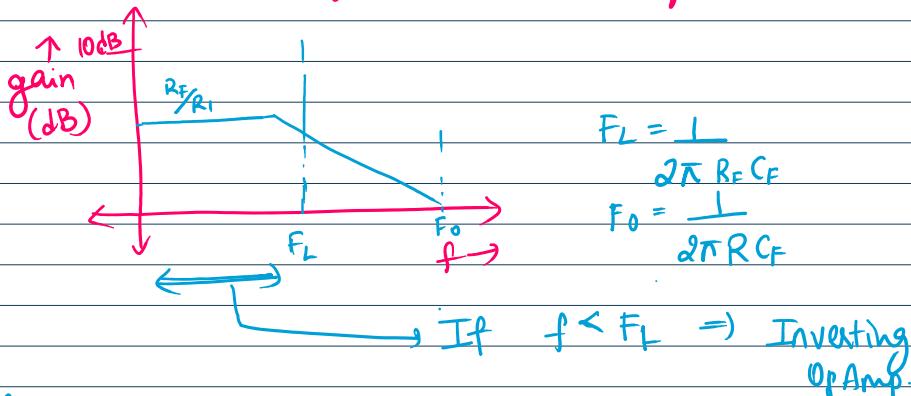


$$A_V = -\frac{R_F}{R}$$



$$A_V = -\frac{R_F}{R_1}$$

## Frequency response of Practical Integrator

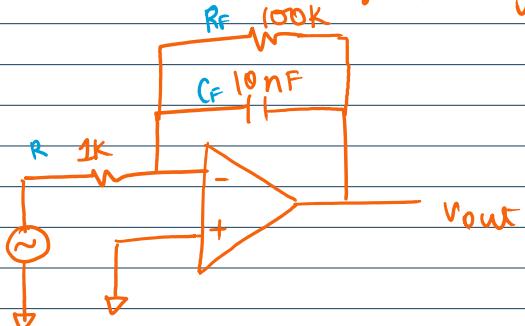


for it to act as integrator opamp,

$$[f > f_L] \quad \text{X}$$

$f_s > 10f_L$  for proper integration

eg: ① find lower frequency limit of integration for the circuit.

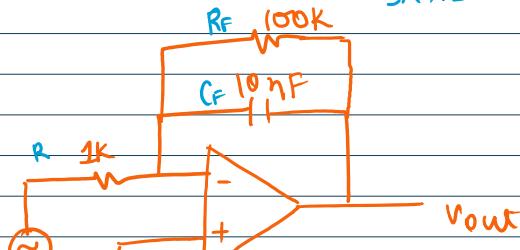


$$f_L = \frac{1}{2\pi R_F C_F} = \frac{1}{2(3.14)(100k)(10n)}$$

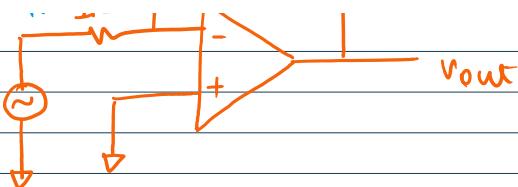
$$f_L = 159 \text{ Hz}$$

i/p signal must be  $> 159 \text{ Hz}$  for integration  
and  $> 1590 \text{ Hz}$  for proper integration  
 $(10 \times f_L)$

②  $V_{in} = 8 \sin(2\pi \times 5000t)$   $\frac{5 \text{ kHz}}{}$



$$f_L = \frac{1}{2\pi R_F C_F} = \frac{1}{2(3.14)(100k)(10n)}$$



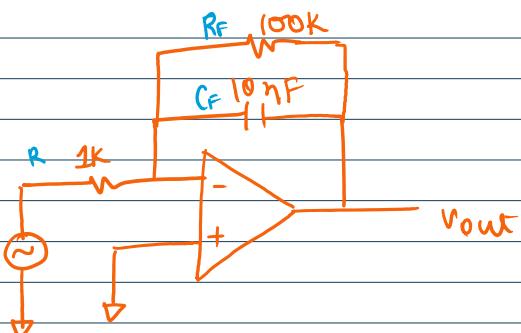
$$2(3.14)(100\text{Hz})(10\text{n})$$

$$F_L = 159 \text{ Hz}$$

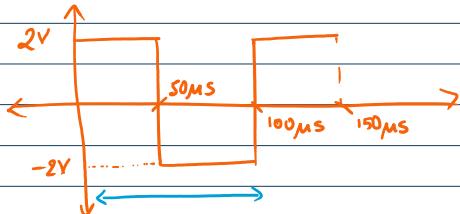
$$F_S = 10F_L = 1.59 \text{ kHz}$$

$$\begin{aligned} V_{out} &= -\frac{1}{RC_F} \int v_{in}(t) dt \\ &= -\frac{1}{(1\text{K})(10\text{n})} \int \sin(2\pi \times 5000t) dt \\ &= -\frac{10^5}{2\pi \times 5000} -\cos(2\pi \times 5000t) \\ V_{out} &= 3.18 \cos(2\pi \times 5000t) \end{aligned}$$

③



i/p signal  $\Rightarrow$



$$T = 100 \mu\text{s}$$

$$F = 10 \text{ kHz}$$

$$F_L = 19.5 \text{ Hz}$$

$$F_S = 1.59 \text{ kHz}$$

$$v_1(t) = 2V ; 0 < t < 50$$

$$v_2(t) = -2V ; 50 < t < 100$$

$$v_{o1} = -\frac{1}{RC_F} \int v_1(t) dt$$

$$= -10^5 \int_0^{50\mu\text{s}} 2 dt$$

$$= -10^5 \times 2 \times 50\mu\text{s}$$

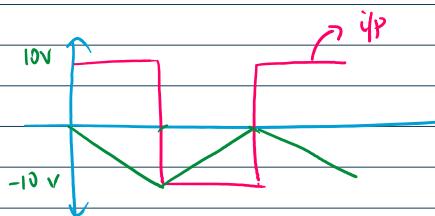
$$v_{o1} = -10V$$

$$v_{o2} = -\frac{1}{RC_F} \int v_2(t) dt$$

$$= -10^5 \int_{50\mu\text{s}}^{100\mu\text{s}} -2 dt$$

$$= -10^5 \times -2 \times (100\mu\text{s} - 50\mu\text{s})$$

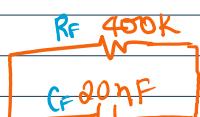
$$v_{o2} = +10V$$



**WRONG! O/P !!**

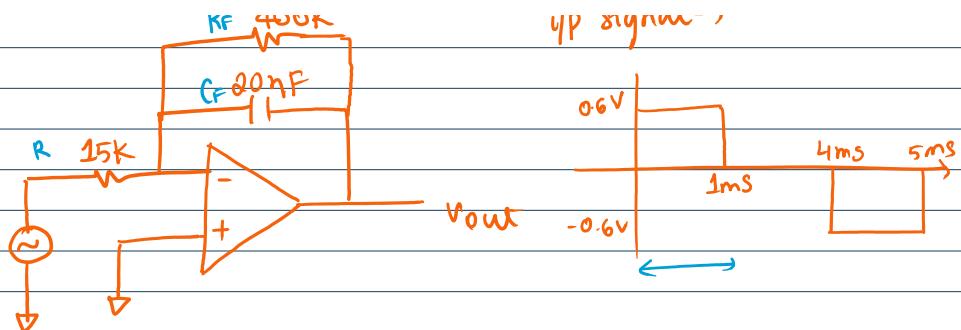
$$-10^5 \times 2 \times 50\mu\text{s}$$

④



i/p signal  $\Rightarrow$

$$0.6V$$



$$F_L = \frac{1}{2\pi R_F C_F}$$

$$= \frac{1}{2(3.14)(1000\text{K})(20\text{n})}$$

$$F_L = 19.89 \text{ Hz}$$

**DOUBT**

$$F_S = 198.9 \text{ Hz}$$

$$= 0.199 \text{ kHz}$$

$$V_{O1} = \frac{-L}{R C_F} \int_0^{1\text{ms}} 0.6 \, dt$$

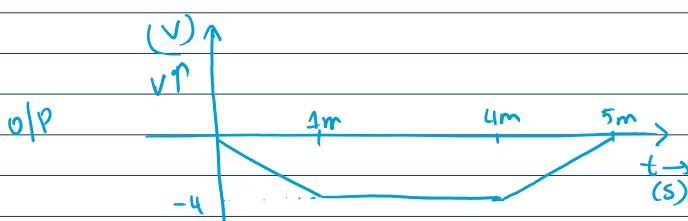
$$= \frac{-1}{(15\text{k})(20\text{n})} \times 0.6 (1\text{m} - 0)$$

$$V_{O1} = -4 \text{ V}$$

$$V_{O2} = \frac{-L}{R C_F} \int_{4\text{m}}^{5\text{m}} -0.6 \, dt$$

$$= \frac{-1}{(15\text{k})(20\text{n})} \times -0.6 (5\text{m} - 4\text{m})$$

$$V_{O2} = +4 \text{ V}$$

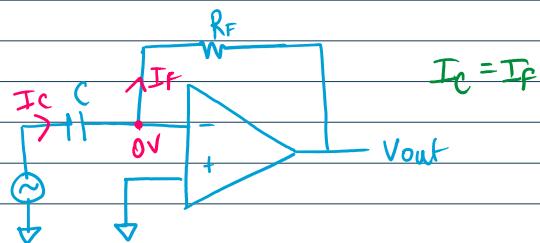
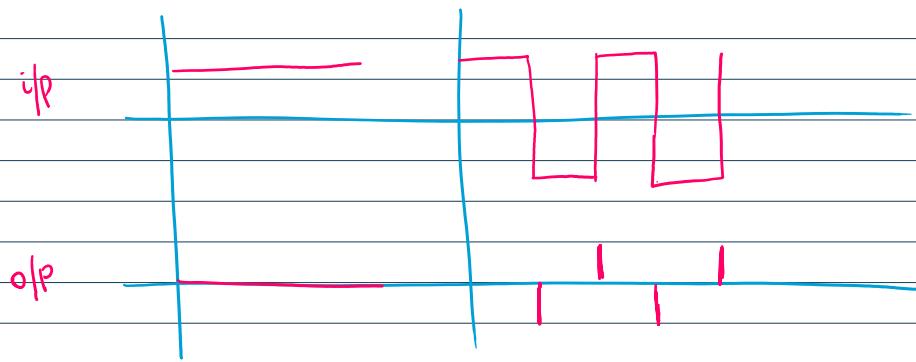


Differentiator Op Amps

82 37 60

1 hrs





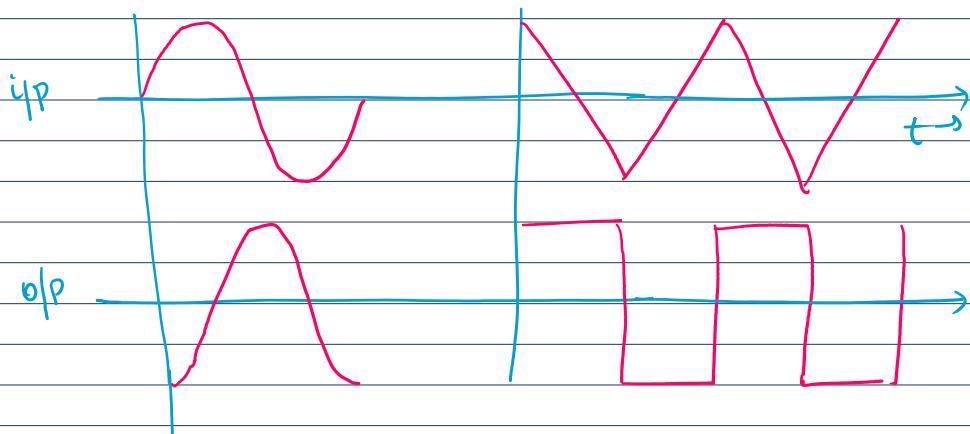
Applying KCL

$$I_C = I_F$$

$$C \frac{dV_C}{dt} = \frac{0 - V_{out}}{R_F}$$

$$C \frac{dV_{in}}{dt} = -\frac{V_{out}}{R_F}$$

$$V_{out} = -R_F C \frac{dV_{in}}{dt}$$

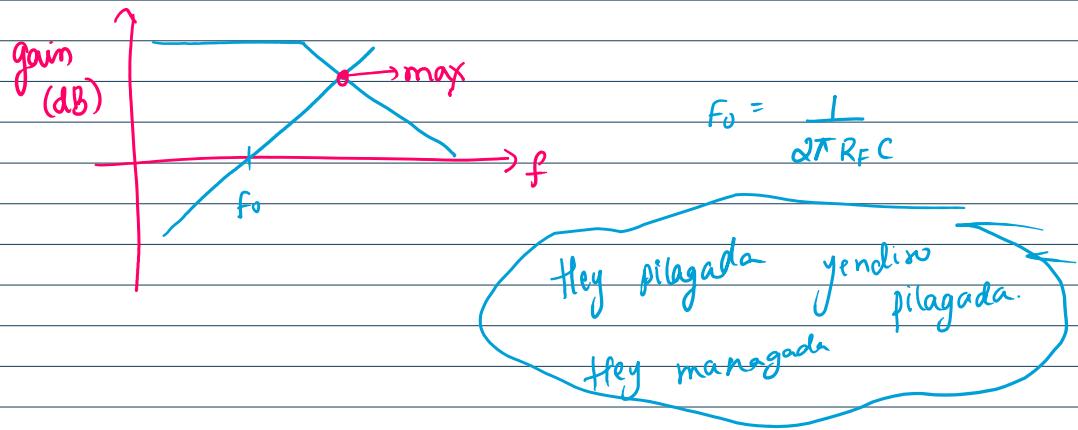


$$V_{out} = -\frac{R_F}{X_C} \times V_{in}$$

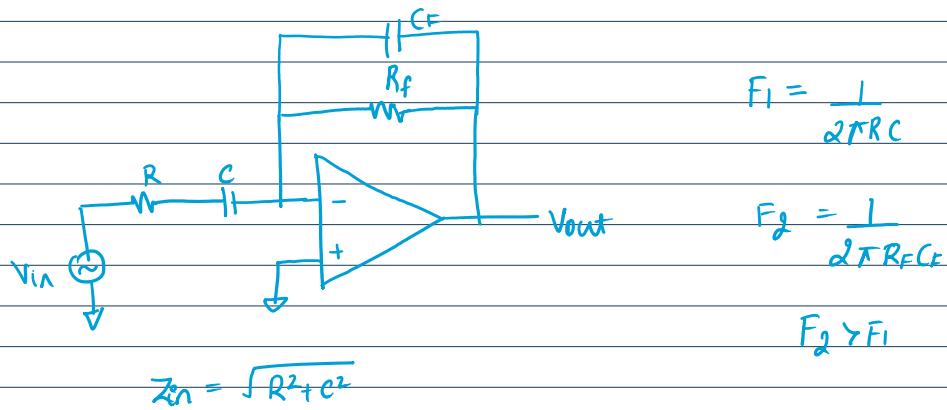
$$A = -\frac{R_F}{X_C}$$

$$A = -R_F \times 2\pi f C$$

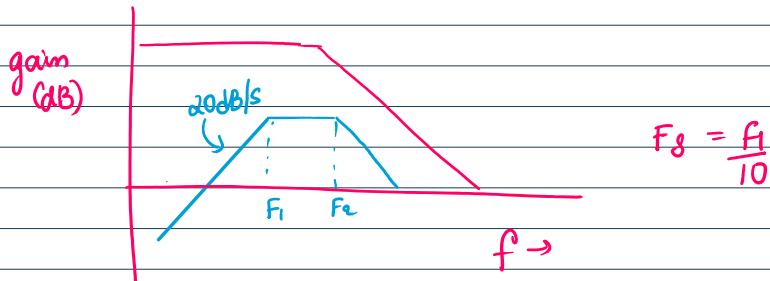
freq. response



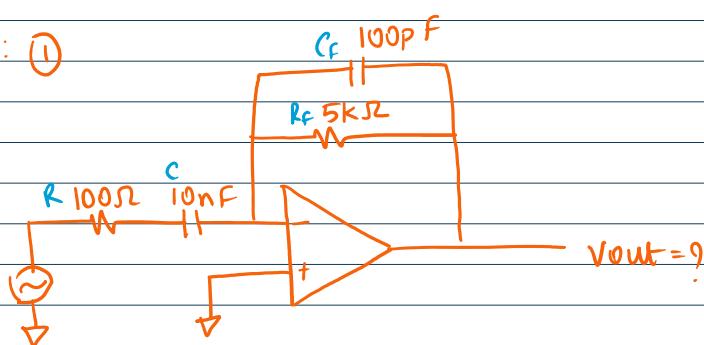
## Practical Differentiator:



$$Z_{in} > R$$



eg : ①



$$F_1 = \frac{1}{2\pi RC}$$

$$F_1 = \frac{1}{2(3.14)(100)(10n)}$$

$$F_1 = 159.2 \text{ kHz}$$

$$F_2 = \frac{1}{2\pi R_F C_F}$$

$$= \frac{1}{2(3.14)(5k)(100p)}$$

$$F_2 = 318.3 \text{ kHz}$$

$$f_1 = \frac{1}{2(3\pi)(100)(10n)} \\ f_1 = 159.2 \text{ kHz}$$

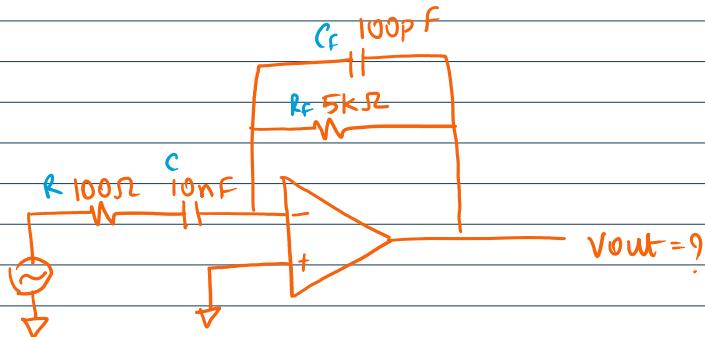
$$f_2 = \frac{1}{2(3\pi)(5k)(100p)} \\ f_2 = 318.3 \text{ kHz}$$

$$f_s < f_2$$

$$f_s < f_1$$

$$f_s = \frac{f_1}{10} \rightarrow \text{for proper differentiator.}$$

②  $v_{in}(t) = 28 \sin(2\pi \times 3000t)$



$$f_1 = 159.2 \text{ kHz} \quad f_s < \frac{159.2}{10}$$

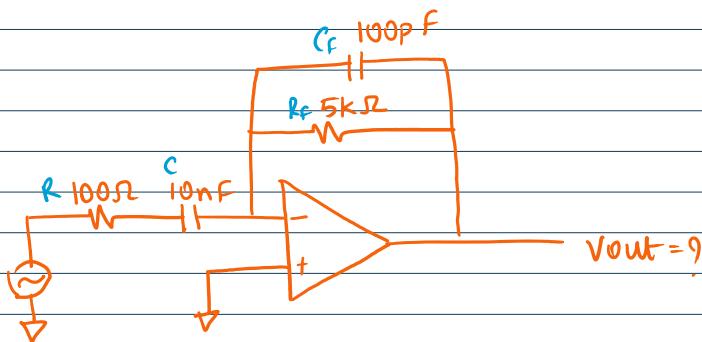
$$f_s = 3 \text{ kHz}$$

$$V_{out} = -R_f C \frac{d v_{in}}{dt} \\ = -5k \times 10n \times \frac{d}{dt} (\sin(2\pi \times 3000t))$$

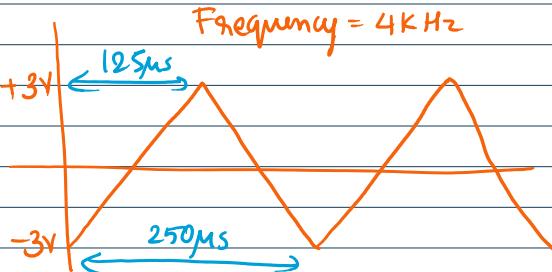
$$= -5 \times 10^{-4} \times 2\pi \times 3000 \times \cos(2\pi \times 3000t)$$

$$= -1.885 \times \cos(2\pi \times 3000t)$$

③



i/p signal  $\Rightarrow$



$$f_1 = 159.2 \text{ kHz}$$

$$T = \frac{1}{f_1} = \frac{1}{159.2 \text{ kHz}} = 250 \mu\text{s}$$

$$f_1 = 159.2 \text{ kHz}$$

$$f_2 = 4 \text{ kHz}$$

$$T = \frac{1}{f} = \frac{1}{4\text{K}} = 250 \mu\text{s}$$

$$\text{slope} = \frac{6}{125\text{M}} = 48000 \text{ V/s}$$

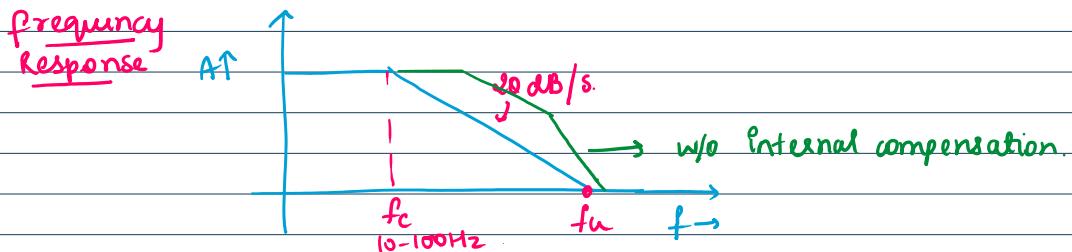
$$V_{out} = -R_f C \frac{dV_{in}}{dt}$$

$$= -(5\text{k})(10\text{n}) (48000)$$

$$V_{out} = -2.4 \text{ V} \quad (\text{for first } 125\mu\text{s})$$



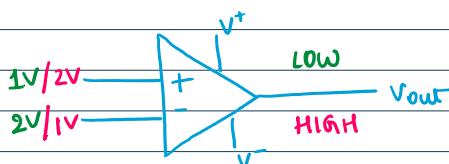
Gain Bandwidth Product.



Later ...



comparator



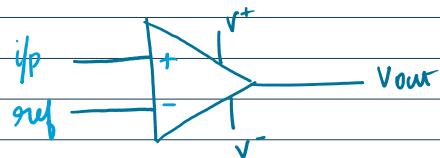
$V_+(+ > -) \Rightarrow \text{HIGH}$   
 $\text{else} \Rightarrow \text{LOW}$

$$V_o = A_{OL} \times V_{id} \quad (V_2 - V_1 = V_{id})$$

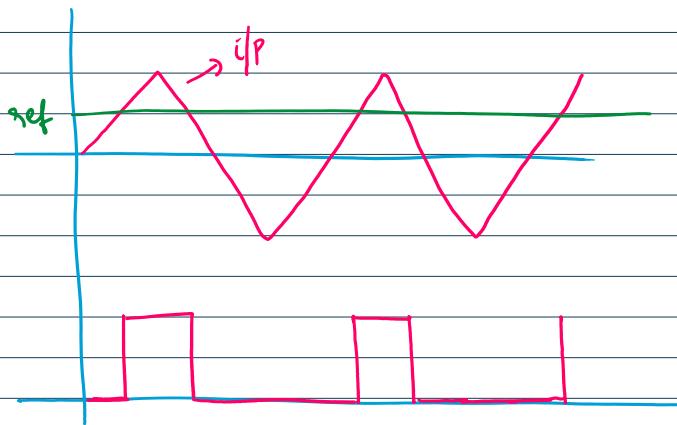
$$V_o = +V_{sat} ; V^+ > V^-$$

$$V_o = -V_{sat} ; V^+ < V^-$$

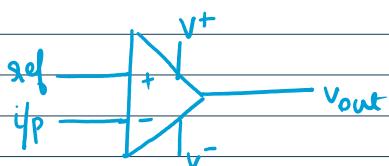
**Comparator**  
 → have low propagation delay  
 and fast rise and fall time      → designed for linear  
 applications



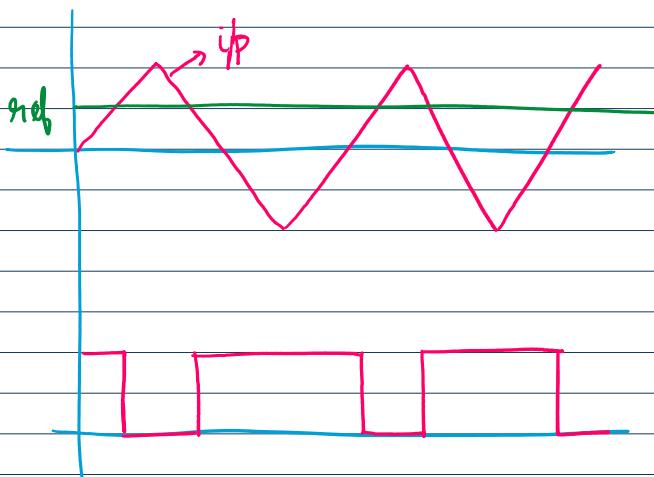
Non-inverting comparator

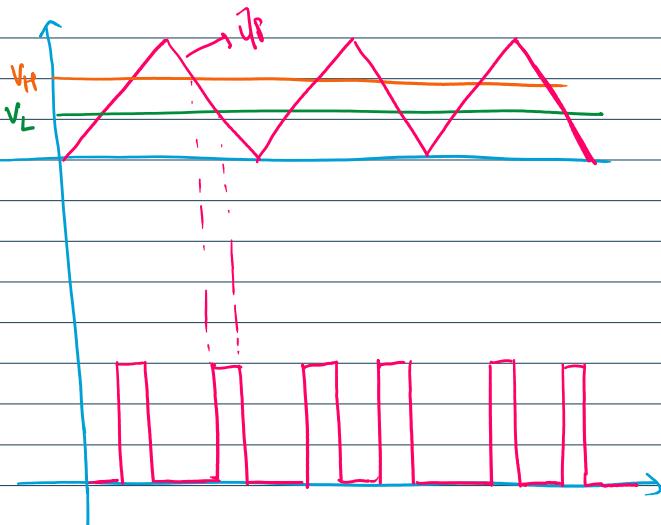
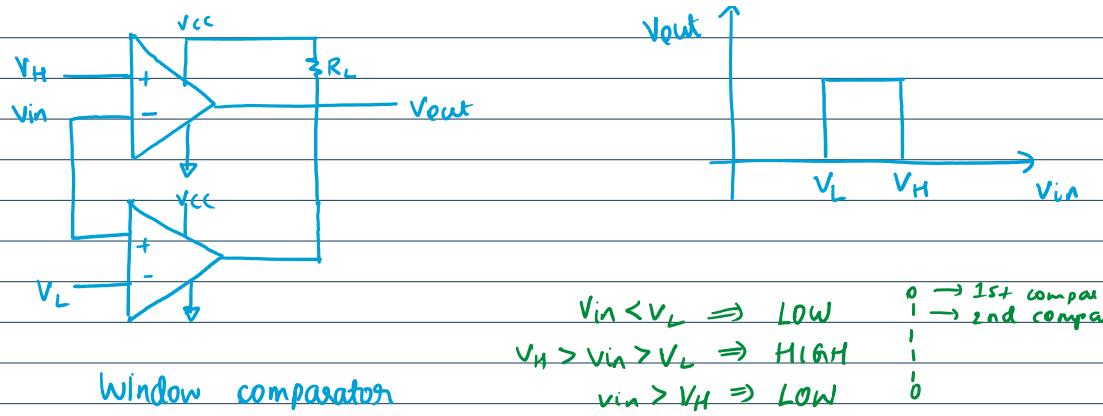


Non-inverting. → o/p ↑ only when  $i/p > \text{ref}$ .



Inverting comparator.





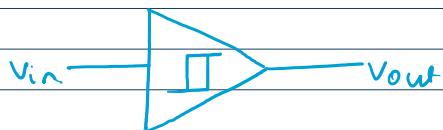
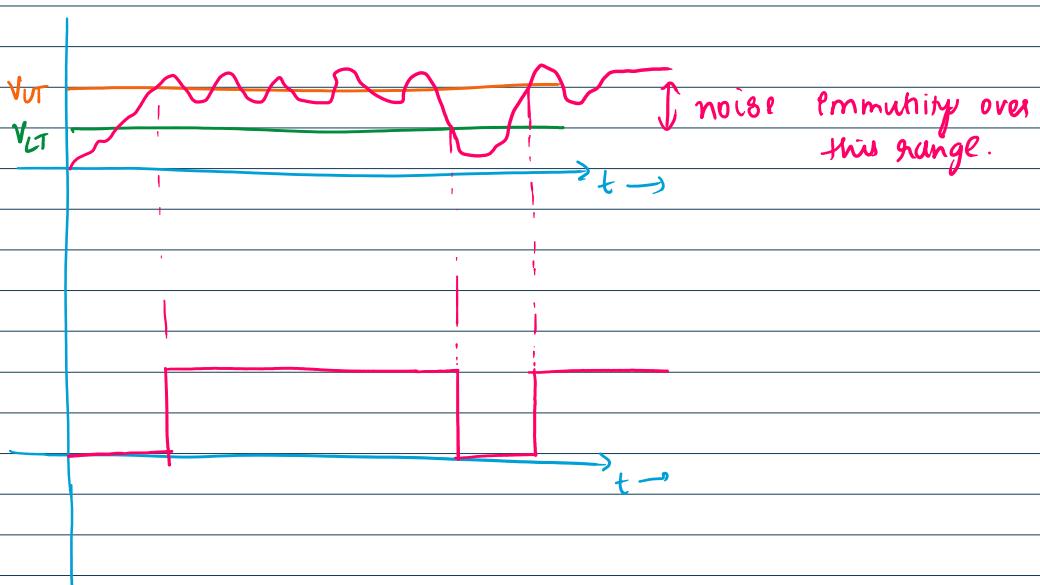
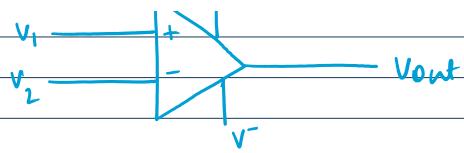
To make comparators immune to noise,

+ve feedback is provided to this comparator ckt.  
 $\Rightarrow$  schmitt trigger



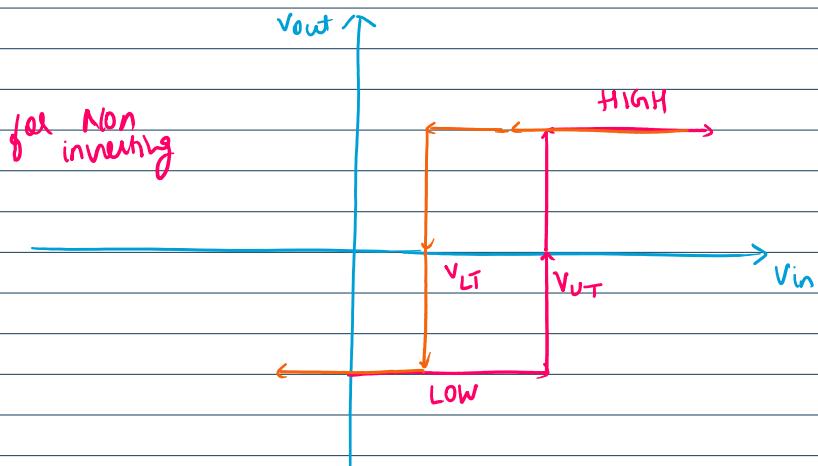
Schmitt Trigger



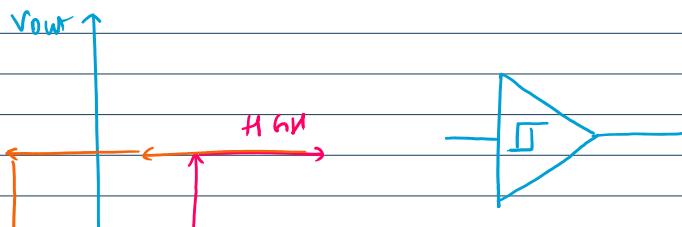


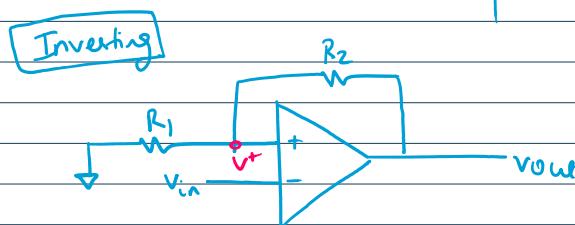
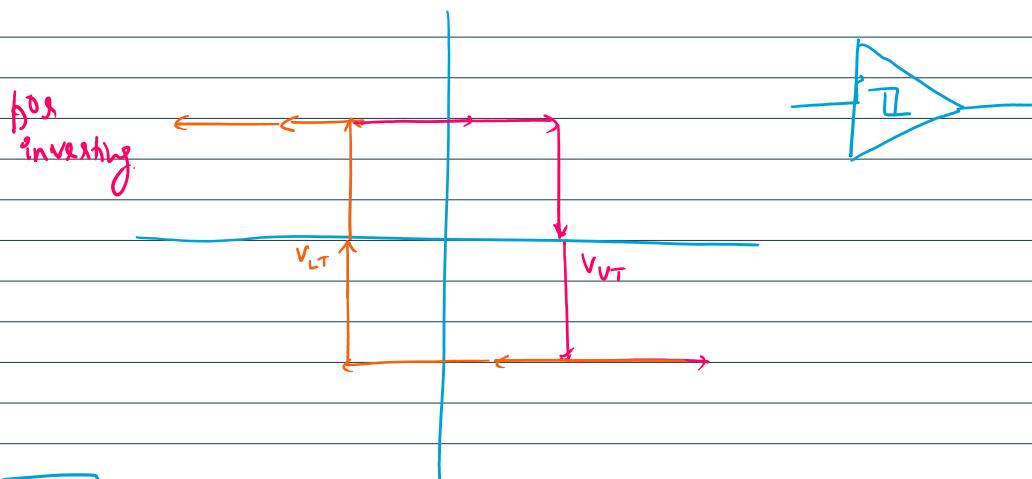
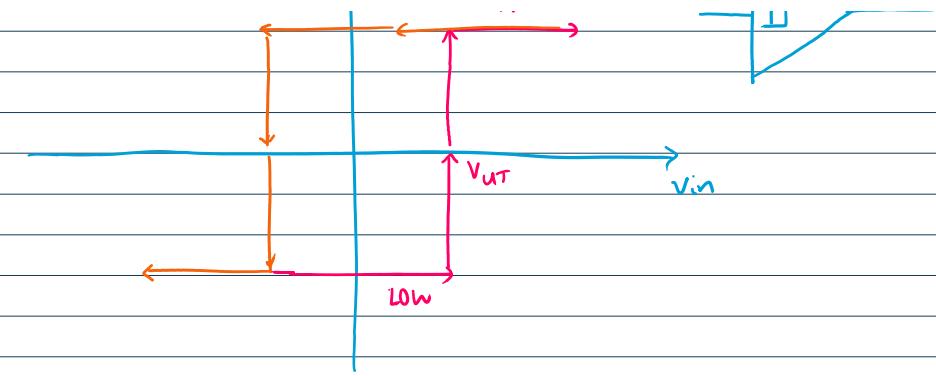
upper threshold voltage  $\rightarrow$  Low to High  
lower threshold voltage  $\rightarrow$  High to Low

### Transfer Characteristics of Schmitt Trigger.



if  $V_H, V_L$  equal with opp polarity





KCL,

$$\frac{V^+ - 0}{R_1} + \frac{V^+ - V_{out}}{R_2} = 0$$

$V_{in} > V^+ \Rightarrow$  O/P LOW  
 $V_{in} < V^+ \Rightarrow$  HIGH

$$\frac{V^+}{R_1} + \frac{V^+}{R_2} - \frac{V_{out}}{R_2} = 0$$

$$V^+ \frac{R_1 + R_2}{R_1 R_2} = \frac{V_{out}}{R_2}$$

$$V^+ = \frac{R_1 \times V_{out}}{R_1 + R_2}$$

$$\rightarrow V_1 = V_{UT} = \frac{R_1}{R_1 + R_2} \times V_H$$

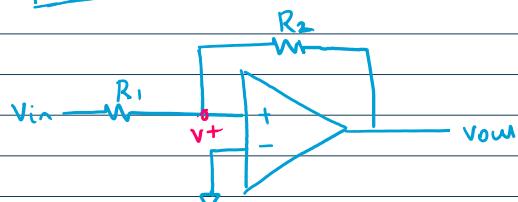
[when  $V_{in} < V^+$ ]

$$V_2 = V_{LT} = \frac{R_1}{R_1 + R_2} \times V_L$$

[when  $V_{in} > V^+$ ]

→ Hysteresis :  $V_{UT} - V_{LT}$

**Non-inverting**



KCL,

$$\frac{V^+ - V_{in}}{R_1} + \frac{V^+ - V_{out}}{R_2} = 0$$

$$\frac{V^+}{R_1} + \frac{V^+}{R_2} = \frac{V_{in}}{R_1} + \frac{V_{out}}{R_2}$$

$$V^+ = R_2 \times V_{in} + R_1 \times V_{out}$$

↙ ↘

$$\frac{V_+}{R_1} + \frac{V_-}{R_2} = \frac{V_{in}}{R_1} + \frac{V_{out}}{R_2}$$

$$V^+ = \frac{R_2}{R_1+R_2} \times V_{in} + \frac{R_L}{R_1+R_2} \times V_{out}$$

→  $V^+ < 0 \Rightarrow V_{out} = LOW$

→  $V^+ > 0 \Rightarrow V_{out} = HIGH$

$$V_1 = \frac{R_2}{R_1+R_2} \times V_{in} + \frac{R_L}{R_1+R_2} \times V_L$$

if  $V_1 > 0 \Rightarrow V_{out} = HIGH$

$$V_2 = \frac{R_2}{R_1+R_2} \times V_{in} + \frac{R_L}{R_1+R_2} \times V_H$$

if  $V_2 < 0 \Rightarrow V_{out} = LOW$

$$So \quad \frac{R_2}{R_1+R_2} \times V_{in} > -\frac{R_L}{R_1+R_2} \times V_L$$

$$V_{in} > -\frac{R_L}{R_2} \times V_L$$

$$V_{out} = -\frac{R_1}{R_2} \times V_L$$

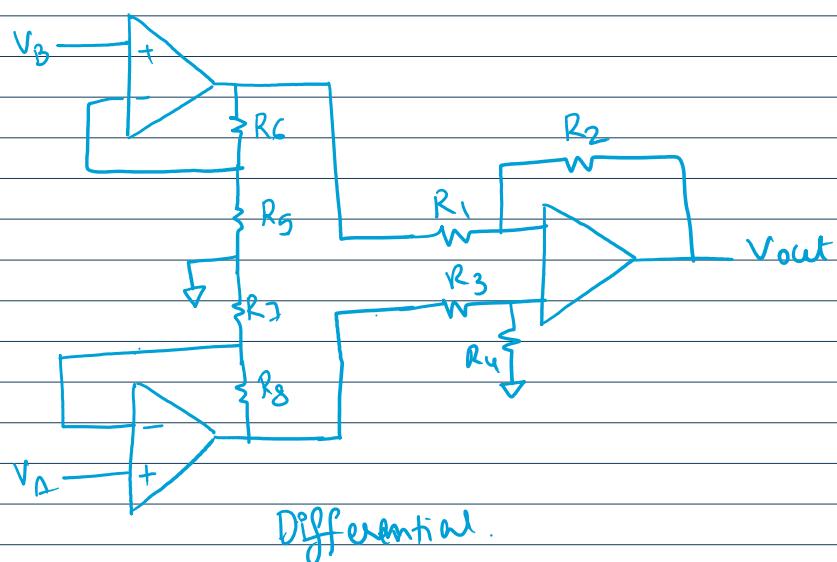
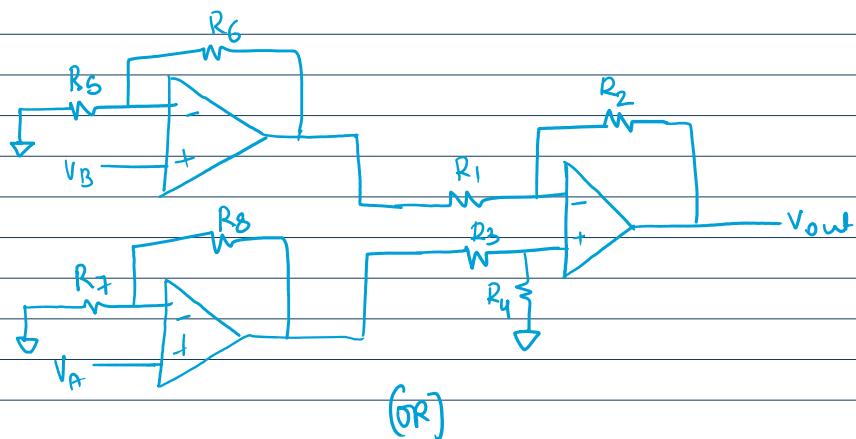
$$\frac{R_2}{R_1+R_2} \times V_{in} < -\frac{R_L}{R_1+R_2} \times V_H$$

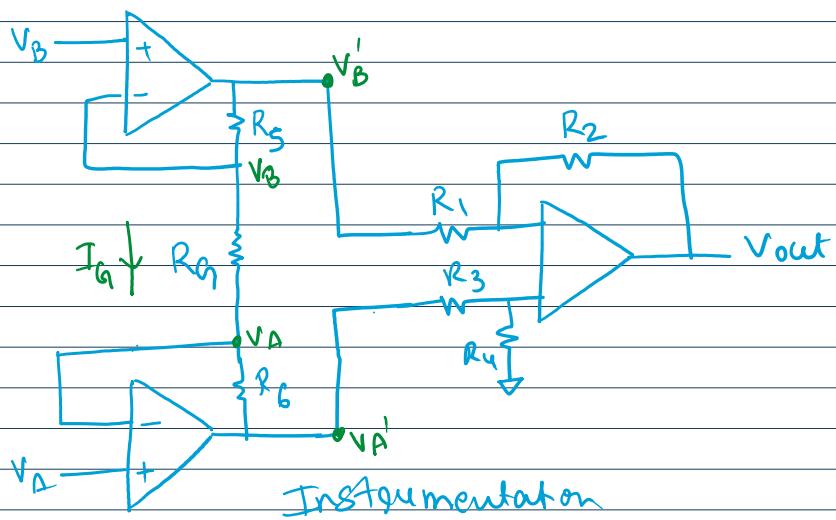
$$V_{in} < -\frac{R_L}{R_2} \times V_H$$

$$V_{out} = -\frac{R_1}{R_2} \times V_H$$



## Instrumentation op-Amps.





$$V_o = \left(1 + \frac{2R_5}{R_6}\right) \left(\frac{R_2}{R_1}\right) \times (V_A - V_B)$$

$$R_5 = R_6 \quad \& \quad \frac{R_4}{R_3} = \frac{R_2}{R_1}$$

$$\Rightarrow V_o = \frac{R_2}{R_1} (V_A' - V_B')$$

$$I_{G1} = \frac{V_B - V_A}{R_6}$$

$$V_B' - V_A' = I_{G1} (R_5 + R_6 + R_G)$$

$$\begin{aligned} V_B' - V_A' &= I_{G1} (2R_5 + R_6) \\ &= (V_B - V_A) \left(1 + \frac{2R_5}{R_6}\right) \end{aligned}$$

$$V_A' - V_B' = (V_A - V_B) \left(1 + \frac{2R_5}{R_6}\right)$$

$$V_o = \left(\frac{R_2}{R_1}\right) \left(1 + \frac{2R_5}{R_6}\right) (V_A - V_B)$$