Title: Neural field

URL: https://en.wikipedia.org/wiki/Neural\_field

PageID: 80384572

Categories: Category:Artificial neural networks, Category:Deep learning, Category:Neural network

architectures, Category: Neural networks

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Supervised learning

Unsupervised learning

Semi-supervised learning

Self-supervised learning

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Decision trees
Ensembles Bagging Boosting Random forest
Bagging
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Linear regression
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Logistic regression
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Mean shift
Factor analysis
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ICA
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NMF
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Graphical models Bayes net Conditional random field Hidden Markov
Bayes net
Conditional random field
Hidden Markov
RANSAC
k -NN

Local outlier factor
Isolation forest
Autoencoder
Deep learning
Feedforward neural network
Recurrent neural network LSTM GRU ESN reservoir computing
LSTM
GRU
ESN
reservoir computing
Boltzmann machine Restricted
Restricted
GAN
Diffusion model
SOM
Convolutional neural network U-Net LeNet AlexNet DeepDream
U-Net
LeNet
AlexNet
DeepDream
Neural field Neural radiance field Physics-informed neural networks
Neural radiance field
Physics-informed neural networks
Transformer Vision
Vision
Mamba
Spiking neural network
Memtransistor
Electrochemical RAM (ECRAM)
Q-learning
Policy gradient
SARSA
Temporal difference (TD)
Multi-agent Self-play
Self-play
Active learning
Crowdsourcing
Human-in-the-loop

Mechanistic interpretability **RLHF** Coefficient of determination Confusion matrix Learning curve **ROC** curve Kernel machines Bias-variance tradeoff Computational learning theory Empirical risk minimization Occam learning **PAC** learning Statistical learning VC theory Topological deep learning **AAAI ECML PKDD NeurIPS ICML ICLR IJCAI** ML **JMLR** Glossary of artificial intelligence List of datasets for machine-learning research List of datasets in computer vision and image processing List of datasets in computer vision and image processing Outline of machine learning ٧ t In machine learning, a neural field (also known as implicit neural representation, neural implicit, or coordinate-based neural network), is a mathematical field that is fully or partially parametrized by a neural network . Initially developed to tackle visual computing tasks, such as rendering or reconstruction (e.g., neural radiance fields), neural fields emerged as a promising strategy to deal with a wider range of problems, including surrogate modelling of partial differential equations, such as in physics-informed neural networks . [1]

Differently from traditional machine learning algorithms, such as feed-forward neural networks , convolutional neural networks , or transformers , neural fields do not work with discrete data (e.g. sequences , images , tokens), but map continuous inputs (e.g., spatial coordinates , time ) to continuous outputs (i.e., scalars , vectors , etc.). This makes neural fields not only discretization

independent, but also easily differentiable. Moreover, dealing with continuous data allows for a significant reduction in space complexity, which translates to a much more lightweight network. [1]

### Formulation and training

According to the universal approximation theorem, provided adequate learning, sufficient number of hidden units, and the presence of a deterministic relationship between the input and the output, a neural network can approximate any function to any degree of accuracy. [2]

Hence, in mathematical terms, given a field  $y = \Phi$  ( x ) {\textstyle {\boldsymbol {y}}=\Phi ({\boldsymbol {x}})} , with  $x \in R$  n {\displaystyle {\boldsymbol {x}}\in \mathbb {R} ^{n}} and  $y \in R$  m {\displaystyle {\boldsymbol {y}}\in \mathbb {R} ^{m}} , a neural field  $\Psi$  0 {\displaystyle \Psi \_{\text{\text{theta }}} , with parameters 0 {\displaystyle {\boldsymbol {\text{\text{theta }}}} , is such that: [ 1 ]  $\Psi$  0 ( x ) = y ^ x y {\displaystyle \Psi \_{\text{\text{\text{theta }}}}} - {\text{\text{\text{\text{theta }}}}} - {\text{\

#### **Training**

For supervised tasks, given N {\displaystyle N} examples in the training dataset (i.e., ( x i , y i )  $\in$  D t r a i n , i = 1 , ..., N {\displaystyle ({\boldsymbol {x\_{i}}}},{\boldsymbol {y\_{i}}})\in {\mathcal {D\_{train}}},i=1,\dots ,N} ), the neural field parameters can be learned by minimizing a loss function L {\displaystyle {\mathcal {L}}} (e.g., mean squared error ). The parameters  $\theta \sim$  {\displaystyle {\tilde {\theta }}} that satisfy the optimization problem are found as: [ 1 ] [ 3 ] [ 4 ]  $\theta \sim$  = argmin  $\theta$  1 N  $\Sigma$  ( x i , y i )  $\in$  D t r a i n L (  $\Psi$   $\theta$  ( x i ) , y i ) {\displaystyle {\tilde {\boldsymbol {\theta }}}-{\text{underset {\boldsymbol {\theta }}}-{\text{underset {\theta }}-{\text{underset {\theta }}}-{\text{underset {\theta }}-{\text{underset {\theta }}}-{\text{underset {\theta }}-{\text{underset {\theta

Moreover, neural fields can be used in unsupervised settings, with training objectives that depend on the specific task. For example, physics-informed neural networks may be trained on just the residual . [4]

### Spectral bias

As for any artificial neural network, neural fields may be characterized by a spectral bias (i.e., the tendency to preferably learn the low frequency content of a field), possibly leading to a poor representation of the ground truth . [5] In order to overcome this limitation, several strategies have been developed. For example, SIREN uses sinusoidal activations, [6] while the Fourier-features approach embeds the input through sines and cosines. [7]

## Conditional neural fields

In many real-world cases, however, learning a single field is not enough. For example, when reconstructing 3D vehicle shapes from Lidar data, it is desirable to have a machine learning model that can work with arbitrary shapes (e.g., a car , a bicycle , a truck , etc.). The solution is to include additional parameters, the latent variables (or latent code)  $z \in R$  d {\displaystyle {\boldsymbol {z}}\in \mathbb {R} \gamma{d}}, to vary the field and adapt it to diverse tasks. [1]

## Latent code production

When dealing with conditional neural fields, the first design choice is represented by the way in which the latent code is produced. Specifically, two main strategies can be identified: [1]

Encoder: the latent code is the output of a second neural network, acting as an encoder. During training, the loss function is the objective used to learn the parameters of both the neural field and the encoder. [8]

Auto-decoding: each training example has its own latent code, jointly trained with the neural field parameters. When the model has to process new examples (i.e., not originally present in the training dataset), a small optimization problem is solved, keeping the network parameters fixed and only learning the new latent variables. [9]

Since the latter strategy requires additional optimization steps at inference time, it sacrifices speed, but keeps the overall model smaller. Moreover, despite being simpler to implement, an encoder may harm the generalization capabilities of the model. [ 1 ] For example, when dealing with a physical scalar field  $f: R 2 \to R$  {\displaystyle f:\mathbb {R} ^{2}\rightarrow \mathbb {R} } (e.g., the pressure of a 2D fluid ), an auto-decoder-based conditional neural field can map a single point to the corresponding value of the field, following a learned latent code z {\displaystyle {\boldsymbol {z}}} . [ 10 ] However, if the latent variables were produced by an encoder, it would require access to the entire set of points and corresponding values (e.g. as a regular grid or a mesh graph ), leading to a less robust model. [ 1 ]

### Global and local conditioning

In a neural field with global conditioning, the latent code does not depend on the input and, hence, it offers a global representation (e.g., the overall shape of a vehicle). However, depending on the task, it may be more useful to divide the domain of  $x \in \{boldsymbol \in x\}\}\$  in several subdomains, and learn different latent codes for each of them (e.g., splitting a large and complex scene in sub-scenes for a more efficient rendering). This is called local conditioning. [1]

#### Conditioning strategies

There are several strategies to include the conditioning information in the neural field. In the general mathematical framework, conditioning the neural field with the latent variables is equivalent to mapping them to a subset  $\theta * \{\text{boldsymbol }\{\text{boldsymbol }\{\text{boldsymbol$ 

Concatenation: the neural field receives, as input, the concatenation of the original input x {\displaystyle {\boldsymbol {z}}} with the latent codes z {\displaystyle {\boldsymbol {z}}} . For feed-forward neural networks, this is equivalent to setting  $\theta * {\displaystyle {\boldsymbol {z}}})} as the bias of the first layer and <math display="inline">\Gamma$  ( z ) {\displaystyle \Gamma ({\boldsymbol {z}})} as an affine transformation . [ 1 ]

Hypernetworks: a hypernetwork is a neural network that outputs the parameters of another neural network. [ 11 ] Specifically, it consists of approximating  $\Gamma$  ( z ) {\displaystyle \Gamma ({\boldsymbol \{z}})} with a neural network  $\Gamma \wedge \gamma$  ( z ) {\displaystyle {\hat {\Gamma }}\_{\quad \text{qamma }} ({\boldsymbol \{z}})} , where  $\gamma$  {\displaystyle {\boldsymbol \{\gamma }}} are the trainable parameters of the hypernetwork. This approach is the most general, as it allows to learn the optimal mapping from latent codes to neural field parameters. However, hypernetworks are associated to larger computational and memory complexity, due to the large number of trainable parameters. Hence, leaner approaches have been developed. For example, in the Feature-wise Linear Modulation (FiLM), the hypernetwork only produces scale and bias coefficients for the neural field layers. [ 1 ] [ 12 ]

### Meta-learning

Instead of relying on the latent code to adapt the neural field to a specific task, it is also possible to exploit gradient-based meta-learning . In this case, the neural field is seen as the specialization of an underlying meta-neural-field, whose parameters are modified to fit the specific task, through a few steps of gradient descent . [ 13 ] [ 14 ] An extension of this meta-learning framework is the CAVIA algorithm, that splits the trainable parameters in context-specific and shared groups, improving parallelization and interpretability , while reducing meta- overfitting . This strategy is similar to the auto-decoding conditional neural field, but the training procedure is substantially different. [ 15 ]

# **Applications**

Thanks to the possibility of efficiently modelling diverse mathematical fields with neural networks, neural fields have been applied to a wide range of problems:

3D scene reconstruction: neural fields can be used to model the properties of 3D scenes (i.e., geometry, appearance, materials, and lighting), in both static and dynamic cases. [1] For example, a neural field can learn signed distance functions (SDFs) [9] or occupancy functions, [16] which provide an efficient and continuous representation of the geometry. Another example is

represented by neural radiance fields (NeRFs), that learn to render 3D scenes, by mapping coordinates and viewing angles to the corresponding radiance and density. [17]

Digital humans: neural fields can be used to model human shape and appearance and can include information on the complex movements of a human body. [1]

Generative modelling: by leveraging conditioning, neural fields can also work as deep generative models. [1]

Image processing: with respect to convolutional neural networks, neural fields offer a continuous representation of the image and, hence, are not limited to the original pixel discretization. [1]

Robotics: the strengths of neural fields in scene reconstruction are also useful in robotics, as navigation requires reconstructing the surroundings from sensor data. Moreover, neural fields can be used for planning and control. [1]

Lossy data compression [1]

Signal processing [1]

Scientific computing: scientific machine learning (SciML) recently emerged as the combination of physics-based and data-driven models, to numerically solve differential equations. [4] In this context, the ability of neural fields to model input and solution in a continuous and differentiable manner is invaluable. For example, physics-informed neural networks (PINNs) use neural fields to include, in the training objective, the residual computed via automatic differentiation. [18] Instead, encode-process-decode architectures (e.g. CORAL), built on conditional neural fields, have been explored as an alternative operator-learning technique. [19] [10]

See also

Artificial intelligence

Machine learning

Neural network (machine learning)

Neural radiance field

Neural operators

References

External links

Brown University's database of neural-field architectures

Neural Radiance Fields: visual computing applications

GitHub-Awesome list of Implicit Neural Representations

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History timeline

timeline

Companies

**Projects** 

Parameter Hyperparameter

Hyperparameter

Loss functions

Regression Bias-variance tradeoff Double descent Overfitting

Bias-variance tradeoff	
Double descent	
Overfitting	
Clustering	
Gradient descent SGD Quasi-Newton method Conjugate gradient method	
SGD	
Quasi-Newton method	
Conjugate gradient method	
Backpropagation	
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Convolution	
Normalization Batchnorm	
Batchnorm	
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Recursive self-improvement	

Hallucination Word embedding Vibe coding Machine learning In-context learning In-context learning Artificial neural network Deep learning Deep learning Language model Large language model NMT Large language model **NMT** Reasoning language model Model Context Protocol Intelligent agent Artificial human companion Humanity's Last Exam Artificial general intelligence (AGI) AlexNet WaveNet Human image synthesis **HWR** OCR Computer vision Speech synthesis 15.ai ElevenLabs 15.ai ElevenLabs Speech recognition Whisper Whisper Facial recognition AlphaFold Text-to-image models Aurora DALL-E Firefly Flux Ideogram Imagen Midjourney Recraft Stable Diffusion Aurora DALL-E Firefly Flux Ideogram Imagen Midjourney

Recraft
Stable Diffusion
Text-to-video models Dream Machine Runway Gen Hailuo Al Kling Sora Veo
Dream Machine
Runway Gen
Hailuo Al
Kling
Sora
Veo
Music generation Riffusion Suno Al Udio
Riffusion
Suno Al
Udio
Word2vec
Seq2seq
GloVe
BERT
T5
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Chinchilla Al
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GPT 1 2 3 J ChatGPT 4 4o o1 o3 4.5 4.1 o4-mini 5
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Claude
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Gemini (language model)

Grok
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Neural Turing machine

Differentiable neural computer

Transformer Vision transformer (ViT)

Vision transformer (ViT)

Recurrent neural network (RNN)

Long short-term memory (LSTM)

Gated recurrent unit (GRU)

Echo state network

Multilayer perceptron (MLP)

Convolutional neural network (CNN)

Residual neural network (RNN)

Highway network

Mamba

Autoencoder

Variational autoencoder (VAE)

Generative adversarial network (GAN)

Graph neural network (GNN)

Category