None of the problems on this assignment are graded. Instead, after completing it, please fill out the associated Google form. That form is the only graded component.

Exercise 1. Use the seive of Eratosthenes to find all of the prime numbers from 0 to 100. This might seem daunting, but you will soon realize that it wont take too long.

Exercise 2. Fundamental theorem of arithmetic: find the prime factors of all of the following:

- 10
- 26
- 96
- 60
- 1890

Exercise 3. Determine if the following numbers are or aren't prime using Wilson's theorem (they may seem abvious, but show them with wilson's theorem specifically):

- 5
- 9
- 11

See why I chose such small numbers?

Exercise 4. Determine if the following numbers are or aren't prime using Fermat's little theorem.

- 17
- 19
- 21

**Exercise 5.** Determine the Euler totient function  $\varphi(n)$  for the following numbers:

- 12
- 26
- *35*

**Exercise 6.** For the following choices of a and n show that Euler's theorem holds, and if it doesn't explain why.

## Exercise 7.

$$a = 3, n = 5$$
  
 $a = 2, n = 7$   
 $a = 14, n = 21$   
 $a = 1, n \in \mathbb{Z}$  (n is any integer)

## Bonus

**Exercise 8.** To find all of the prime numbers between 0 and some integer n,