

* Module 3: Parsing

- The program that performs syntax analysis is called the syntax analyzer or parser.
- . Parser is a program that takes ~~an~~ as input a sentence/string and if the grammar can derive ~~the~~ sentence/string Then it generates a parse tree, else it generates an error.
- . Parser has two techniques
 - Top Down (root to leaf)
 - Bottom Up (leaf to root)

Parser (Parsing techniques)

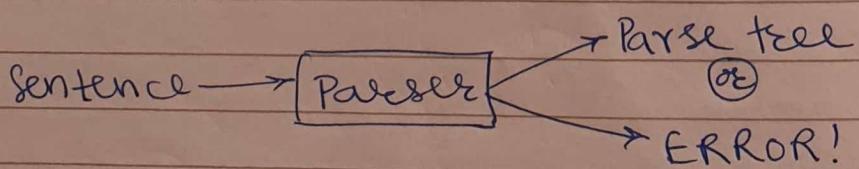
Top Down
 ↓
 Recursive Descent Parser (RDP)

$X(X)$ Predictive Parser
 ↓
 (L L (1))
 left to right LRD

Bottom Up
 ↓

Shift
 Reduce
 Parser

→ Shift Reduce Parser
 → Operator Precedence
 → Canonical parser
 → Simple LR
 → Look Ahead LR Parser (LLLR)



Top Down Parser - The parser builds the parse tree from top to bottom i.e. root to leaves.
 Bottom Up - leaves to root

1) Recursive Descent Parser

Top Down

Recursive - The parser is implemented with functions which may work recursively.

- Descent - Top down approach
- It will generate a parse tree only if the following conditions are satisfied -
 - (i) if p is completely scanned
 - (ii) the echo fn. wasn't called / no infinite loop.

Design Recursive Descent Parser :

$$S \rightarrow AB$$

$$A \rightarrow aA \mid b$$

$$B \rightarrow bB \mid a$$

• the parser will create functions for the variables (capital)

• conditions are written on terminals.

• ADVANCE() fn. checks the next input symbol.

sol. function S()

```

  {
    A();
    B();
  }
```

```

  else
  {
```

```

    if(input_symbol == 'b')
```

```
      ADVANCE();
```

```

      {
        else {
          ERROR();
        }
      }
```

function A()

```

  {
    if (input_symbol == 'a')
      ADVANCE();
      A();
  }
```

{ function B()

{ if (input_symbol == 'b')

 ADVANCE();

 B();

}

else if (input_symbol == 'a')

 ADVANCE();

}

else

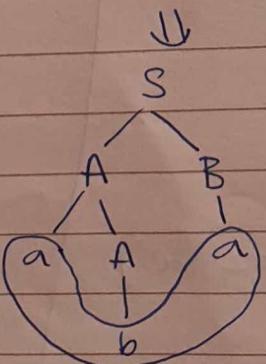
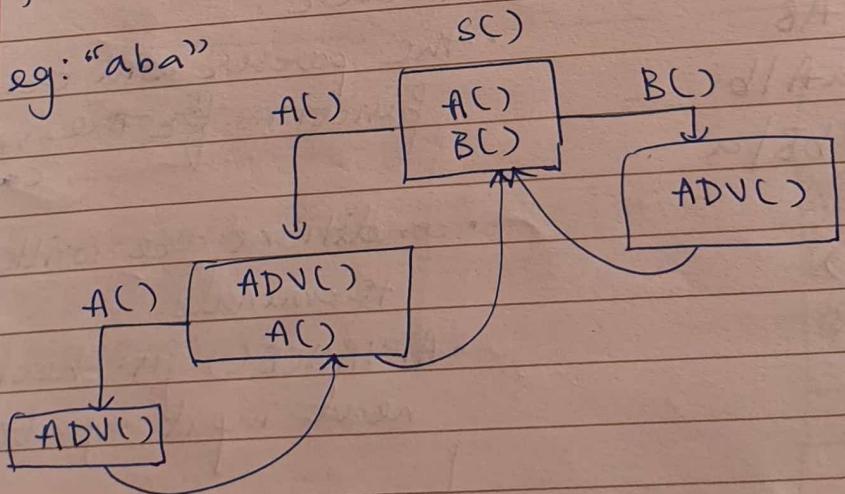
{

 ERROR();

}

}

⇒ eg: "aba"





gaya



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Q $E \rightarrow E + E \mid id$ (doesn't work ;))

to make it work

function E()

{ if (input_sym ==
E();) }

$\leftarrow \begin{cases} \text{left recursive} \\ \text{for production of} \\ \text{the form} \\ A \rightarrow A\alpha \mid \beta \end{cases}$

function E() {

{ if (input_sym == 'id')

$$\begin{aligned} A &\rightarrow \beta A' \\ A' &\rightarrow \alpha A' \mid \epsilon \end{aligned}$$

ADVANCE();

}

else

E();

ADVANCE();

{ if (input_sym == '+')

$$A \rightarrow E + E \mid id$$

becomes

$$A \rightarrow id E'$$

$$E' \rightarrow + E E' \mid \epsilon$$

ADVANCE();

E();

}

ERROR();

}

}

In the above parser (example), the parser goes into an infinite loop because the given grammar is left recursive & hence not suitable for Parser Design.

left recursive - Any production of the form

$$A \rightarrow A\alpha | \beta$$

Eliminating left recursive grammar

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' | \epsilon$$

$$\begin{aligned} \therefore E &\rightarrow id E' \\ E'' &\rightarrow + E E' | \epsilon \end{aligned}$$

function E()

{ if (input_symbol == 'id')

 ADVANCE();

 E'();

}

else

{ ERROR();

}

function E'()

{ if (input_symbol == '+')

A certain grammar / production is said to be left recursive if the left most variable of the RHS is the same as the left most variable of the LHS.

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ADVANCE();
AEC();
E'();

}

else
{

no-action;

}

- When we change the production to remove left recursion we should preserve the original grammar (production)
- Grammar input in a parser should be right recursive

~~XXX~~

- A production of the grammar is said to have left recursion if the left most variable of its RHS is the same as the variable in its LHS

eg.

$$A \rightarrow A\alpha \mid \beta \quad (A = \beta\alpha^*)$$

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \epsilon$$

General form: $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_n$

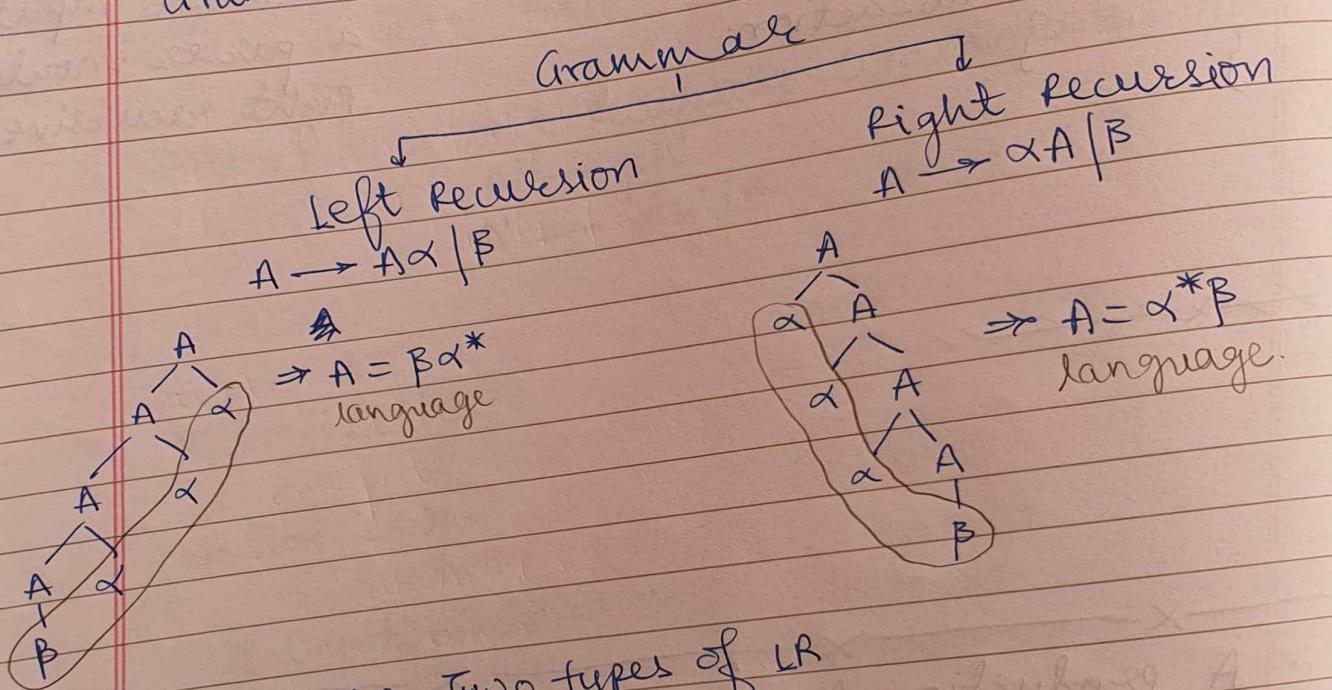
$$A \rightarrow \beta_1 \mid \beta_2 \mid \dots \mid \beta_m$$

$$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_m A'$$

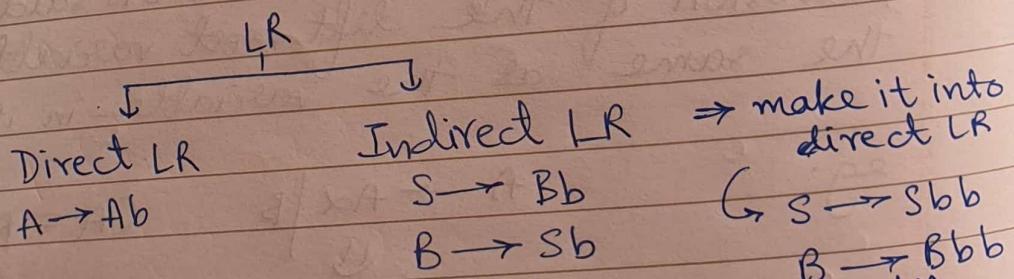
$$A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_n A' \mid \epsilon$$

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- Top down parser cannot handle grammar having left recursion because they are not suitable for parser design.
- We have to remove/eliminate left recursion but preserve the language generated by Grammar



- There are two types of LR



Q. Eliminate the LR from the following grammar:

$$E \rightarrow E + T | T$$

$$T \rightarrow T * E | F$$

$$F \rightarrow id$$

$E \rightarrow TE'$ $E' \rightarrow +TE' | \epsilon$ $T \rightarrow FT'$ $T' \rightarrow *ET' | \epsilon$ $F \rightarrow id$

function $E()$
{

 $T();$ $E'();$

}

function $E'()$
{

 if (input-symbol == '+')
{

ADVANCE();

 $T();$ $E'();$

}

 else
{

no-action;

}

}

function $T()$
{

 $F();$ $T'();$

}

function $T'()$
{

 if (input-symbol == '*')
{

$E();$
 $T'();$

}

else

{

no-action;

}

}

function $F()$
{

 if (input-symbol == 'id')
{

ADVANCE();

}

else

{

ERROR();

}

}

Q. $A \rightarrow Ba | Aa | \epsilon c$ \Rightarrow make it Direct LR first
 $B \rightarrow Bb | Ab | b d$

$$\begin{cases} A \rightarrow BaA' | CaA' \\ A \not\sim A' \end{cases}$$

$$\begin{cases} A \rightarrow Aba | Aa | c \\ B \rightarrow Bb | Bab | b d \end{cases}$$

$$\begin{cases} A \rightarrow cA' \\ A' \rightarrow baA' | aA' | \epsilon \\ B \rightarrow dB' \\ B' \rightarrow bB' | abB' | \epsilon \end{cases}$$

function $A()$

```
{ if (input_sym == 'c')
    ADVANCE();
    A'();
}
```

function $A'()$

```
{ if (input_sym == 'b')
    ADVANCE();
    if (input_sym == 'a')
        ADVANCE();
        A'();
}
```

```
{ else if (input_sym == 'a')
    ADVANCE();
    ERROR();
    A'();
}
```

~~else~~

{

~~ERROR(), no-action~~~~function B()~~

{

~~if (inp_sym == 'd')~~~~ADVANCE();~~~~B'();~~

{

~~else~~

{

~~ERROR();~~

{

~~function B'();~~

{

~~if (inp_sym == 'b')~~~~else~~

{

~~ADVANCE();~~~~ERROR();~~~~B'();~~

{

~~else if (inp_sym == 'a')~~~~else~~

{

~~no action;~~~~ERROR();~~~~if !LWY ADVANCE();~~

{

~~if (inp_sym == 'b')~~

{

~~ADVANCE();~~~~B'();~~

{

{ function A'()

{ if (inp-sym == 'b')

ADVANCE();

{ if (inp-sym == 'a')

ADVANCE();

A'();

}

else
{

ERROR();

}

} else if (inp-sym == 'a')

{

ADVANCE();

A'();

}

else
{

no-action;

}

}

Q $S \rightarrow Aa \mid b \Rightarrow S \rightarrow Sda \mid b$
 $A \rightarrow Ac \mid Sd \mid \epsilon \Rightarrow A \rightarrow Ac \mid Aad \mid \epsilon$

$\Rightarrow S \rightarrow bS' \Rightarrow S \rightarrow bS'$
 $S' \rightarrow daS' \mid \epsilon \Rightarrow S' \rightarrow daS' \mid \epsilon$
 $A \rightarrow A' \Rightarrow A \rightarrow cA \mid adA \mid \epsilon$
 $A' \rightarrow ca' \mid adA' \mid \epsilon$

Grammar

Deterministic

- Determined where we want to go exactly
- used in Parser

Non-Deterministic

$A \rightarrow \alpha\beta \mid \alpha\gamma$

~~left factoring -~~

There are two types of grammar - NDG.

- Deterministic Grammar determines where we want to go exactly.
- In DG, there is exactly 1 unique prefix
- In NDG, there is not exactly 1 unique prefix

$A \rightarrow \alpha\beta \mid \alpha\gamma$

The main cause of NDG is repetition of prefixes.

Due to this, the parser is unable to determine to which production it wants to go. Therefore, left factoring comes into the picture.

In left factoring, NDG is converted to DG

Any production of the form $A \rightarrow \alpha\beta \mid \alpha\gamma$
 common prefix

To eliminate (common prefix) left factoring, is used -

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 \beta_2 \dots$$

General :

~~$$A \rightarrow \alpha, \beta_1 | \alpha_1 \beta_2 | \dots | \gamma_1 | \gamma_2$$~~

~~$$\Rightarrow A' \rightarrow \alpha$$~~

~~$$A \rightarrow \alpha, \beta_1 | \alpha_1 \beta_2 | \dots | \gamma_1 | \gamma_2$$~~

~~$$\Rightarrow A \rightarrow \alpha, A' | \gamma_1 | \gamma_2$$~~

~~$$A' \rightarrow \beta_1 | \beta_2 | \dots$$~~

Q Eliminate left factoring
 (i) $S \rightarrow aSb|ab$

$$\Rightarrow S \rightarrow aS'$$

$$S' \rightarrow Sb | ab$$

$$(ii) A \rightarrow aBla | c$$

$$\Rightarrow A \rightarrow aA'$$

$$A' \rightarrow Blbc$$

$$(iii) S \rightarrow iEtS | iEtSeSa$$

$$E \rightarrow \epsilon b$$

$$\Rightarrow S \rightarrow iEtS'S' | a$$

$$S' \rightarrow eS | \epsilon$$

$$E \rightarrow b$$

$$(iv) S \rightarrow aSSbS \mid aSaSb \mid abb \mid b$$

$$\Rightarrow S \rightarrow as' \mid b$$

$$\begin{cases} S' \rightarrow SSbS \mid SaSb \mid bb \mid b \\ \downarrow \end{cases}$$

$$S \rightarrow ass' \mid as'' \mid b$$

$$S' \rightarrow$$

$$\left. \begin{array}{l} S \rightarrow as' \mid as'' \mid as''' \mid b \\ S' \rightarrow SSbS \\ S'' \rightarrow SaSb \\ S''' \rightarrow bb \end{array} \right\}$$

$$S' \rightarrow SSbS$$

$$S'' \rightarrow SaSb$$

$$S''' \rightarrow bb$$

$$S \rightarrow ass' \mid as'' \mid b$$

$$S' \rightarrow SbS \mid asb$$

$$S'' \rightarrow bb$$

$$S \rightarrow aA' \mid b$$

$$A' \rightarrow SS' \mid S''$$

$$S' \rightarrow SbS \mid asb$$

$$S'' \rightarrow bb$$

$\times \quad \quad \quad \times \quad \quad \quad \times \quad \quad \quad \times \quad \quad \quad \times$

- * first(α) means set of words & terminals which can be derived from α .
- can be applied on all terminals & variables.
- It is defined as a set of terminals that begins with the string derived from α . α is some sentential form

$$R1] X \rightarrow \alpha \alpha$$

$$\text{FIRST}\{\star\} = \{\alpha\}$$

$$R2] X \rightarrow \epsilon$$

$$\text{FIRST}\{X\} = \{\epsilon\}$$

$$R3] \text{FIRST}\{\alpha\} = \{\alpha\}$$

where a is a terminal.

$$R4] X \rightarrow Y_1 Y_2 Y_3 \dots Y_k$$

$$\text{FIRST}\{X\} = \text{FIRST}\{Y_1\}$$

if Y_1 contains ϵ ,
 $\Rightarrow \text{FIRST}\{X\} = \text{FIRST}\{Y_j\} - \{\epsilon\}$
 $+ \text{FIRST}\{\epsilon Y_2\}$

note: if Y_j contains ϵ then
 $\text{FIRST}\{X\} = \epsilon$

where $j = [1, k]$

- FOLLOW(A) \leftarrow only for variables
- It is defined as a set of terminals that can appear on RHS of variable A.

R1] if Y is a start variable,
 $\text{FOLLOW}(Y) = \{\$\}$

R2] $X \rightarrow \alpha Y$
 $\text{FOLLOW}(Y) = \text{FOLLOW}(X)$

R3] $X \rightarrow \alpha Y \beta$
 $\text{FOLLOW}(Y) = \text{FIRST}\{\beta\}$

if $\text{FIRST}\{\beta\}$ contains ϵ then
 $\text{FOLLOW}(Y) = \text{follow}(X)$
 $\text{FOLLOW}(Y) = \text{FIRST}\{\beta\} - \{\epsilon\} + \text{FOLLOW}(X)$

14/02/2024

Q2 Find first & follow of the given grammar.

$$\begin{aligned} S &\rightarrow ABC \\ A &\rightarrow a/\epsilon \\ B &\rightarrow b \\ C &\rightarrow c/\epsilon \end{aligned}$$

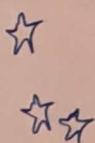
First

Q1. find first -

$$\begin{aligned} S &\rightarrow ABC \\ A &\rightarrow a/\epsilon \\ B &\rightarrow b/\epsilon \\ C &\rightarrow c/\epsilon \end{aligned}$$

$$\text{first}(S) = \epsilon$$

$$\text{first}(A) = \text{first}(B) = \text{first}(C) \neq \epsilon$$



$$\text{first}\{a\} = \{a\}$$

$$\text{first}\{b\} = \{b\}$$

$$\text{first}\{c\} = \{c\}$$

$$\text{first}\{A\} = \{a, \epsilon\}$$

$$\text{first}\{B\} = \{b, \epsilon\}$$

$$\text{first}\{C\} = \{c, \epsilon\}$$

$$\text{first}\{S\} = \{a, b, c, \epsilon\}$$

2.

$$\text{first}\{A\} = \{a, \epsilon\}$$

$$\text{first}\{B\} = \{b\}$$

$$\text{first}\{C\} = \{c, \epsilon\}$$

$$\text{first}\{a\} = \{a\}$$

$$\text{first}\{b\} = \{b\}$$

$$\text{first}\{c\} = \{c\}$$

$$\text{first}\{S\} = \{a, b, \epsilon\}$$

$$\text{follow}\{A\} = \text{follow}\{S\} = \{\$\}$$

$$\text{follow}\{B\} =$$

$$\text{follow}\{A\} = \text{first}\{B\} = \{b\}$$

$$\text{follow}\{B\} = \text{first}\{C\} = \{c, \$\}$$

$$\text{follow}\{C\} = \text{follow}\{S\} = \{\$\}$$

$$\text{follow}\{S\} = \{\$\}$$

Q3.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

$$T \rightarrow (E) | id$$

$$\text{first}\{+\} = \{+\}$$

$$\text{first}\{(E)} = \{(E)\}$$

$$\text{first}\{()\} = \{()\}$$

$$\text{first}\{id\} = \{id\}$$

$$\text{first } \{ E T \} = \{ (, \text{id} \}$$

$$\text{first } \{ E' \} = \{ +, \epsilon \}$$

$$\text{first } \{ E \} = \{ (, \text{id} \}$$

$$\text{follow } \{ E \} = \{ \$,) \}$$

$$\text{follow } \{ E' \} = \text{follow } \{ E \} = \{ \$,) \}$$

$$\text{follow } \{ T \} = \text{First } \{ E' \} = \{ +, \$ \}$$

* look at all instances of the variable being in RHS

$$\text{follow } \{ E \} = \{ \$ \} + \text{first } \{) \} = \{ \$,) \}$$

$$\text{follow } \{ E' \} = \text{follow } \{ E \} + \text{follow } \{ E' \} = \{ \$,) \}$$

$$\text{follow } (T) = \text{first } \{ E' \} \\ \text{follow } \{ E' \} =$$

{ not completed }

Q

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

$$T \rightarrow FT'$$

$$F \rightarrow *FT' | \epsilon$$

$$F \rightarrow (E) | \text{id}$$

variable/term. first

+

+

*

*

(

(

)

)

id

id

$$\text{first } \{ F \} = \{ (, \text{id} \}$$

$$\text{first } \{ T' \} = \{ *, \epsilon \}$$

$$\text{first } \{ T \} = \text{first } \{ F \} = \{ (, \text{id} \}$$

$$\text{first } \{ E' \} = \{ +, \epsilon \}$$

$$\text{first } \{ E \} = \text{first } \{ T \} = \{ (, \text{id} \}$$

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- LR(0)
- first & follow of variables
- parse table
- Algorithm
- example

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$$\text{Follow}(F) = \text{first}\{T'\} + \text{Follow}(T)$$

$$= \{\ast, +, \$,)\}$$

$$\text{Follow}(T) = \text{first}\{E'\} + \text{Follow}(E)$$

$$= \{+, \$,)\}$$

$$\text{Follow}(E) = \{\$\} + \text{first}\{)\}$$

$$= \{\$,)\}$$

$$\text{Follow}(T') = \text{Follow}(T) = \{\$,)\}$$

$$= \{+, \$,)\}$$

$$\text{Follow}(E') = \text{Follow}(E)$$

$$= \{\$,)\}$$

14/02/24

Module 3 / Process

Q. Design predictive parser for the following grammar

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' | \epsilon$$

$$T \rightarrow (E) | \text{id}$$

(i) Elimination of LR & LRF

$$\text{first}\{E\} = \{ (, \text{id} \}$$

$$\text{follow}(E) = \{\$,)\}$$

$$\text{first}\{E'\} = \{ +, \epsilon \}$$

$$\text{follow}(E') = \{\$,)\}$$

$$\text{first}\{T\} = \{ (, \text{id} \}$$

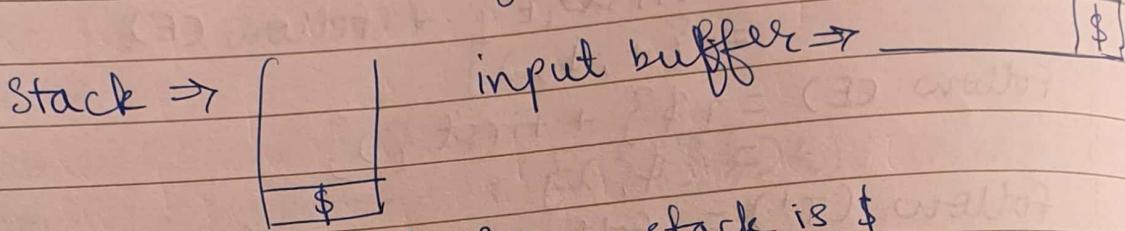
$$\text{follow}(T) = \{ +, \$,)\}$$

(ii) Predictive parser table

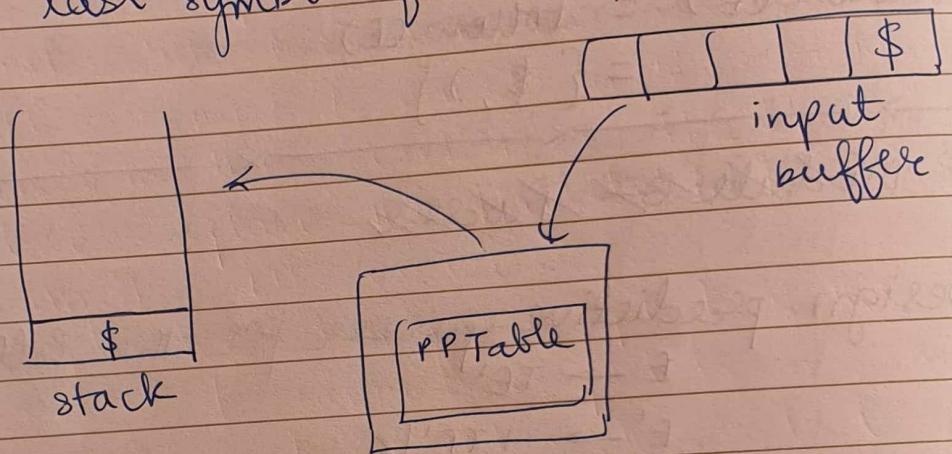
\sqrt{T}	id	+	$\ast($)	\$	$\text{follow}(E')$
E	$E \rightarrow TE'$		$E \rightarrow TE'$			contains \$,)
$E' \Rightarrow E'$		$E' \rightarrow +TE'$		$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$	ϵ
T	$T \rightarrow \text{id}$		$T \rightarrow (E)$			writes the E' production of E' in) & \$

* Since each entry of the PP table consists of a single production, this is an LL(1) parser

(iv) Predictive Parser algorithm



- * the bottom symbol of the stack is \$
- * the last symbol of the input buffer is \$



- (i) let 'x' be a stack top symbol & 'a' be the input symbol
- (ii) if $x = a = \$$ then accept & break
- (iii) if $x = a \neq \$$ then pop x & remove a
- (iv) if $M[x, a] x \rightarrow y_1 y_2 \dots y_k$ then pop x & push $y_k y_{k-1} \dots y_1$
- (v) else ERROR()

Q. Test if the following grammar is LL(1) or not

$$S \rightarrow AaAb \mid Babb$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

(i) LR(LF)

$$S \rightarrow$$

(i) LR(LF) ✓

$$\text{first } \{B\} = \{\epsilon\} \quad \text{follow}(A) = \{a, b\}$$

$$\text{First } \{A\} = \{\epsilon\} \quad \text{follow}(B) = \{a, b\}$$

$$\text{first } \{S\} = \{A, B\} \quad \text{follow}(S) = \{\$\}$$

$$\text{first } \{S\} = \{a, b\}$$

(iii) Table

\sqrt{T}	a	b	\$	
A	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$		* Not an LL(1) Parser
B	$B \rightarrow \epsilon$	$B \rightarrow \epsilon$		
S	$S \rightarrow AaAb$	$S \rightarrow Babb$		

16/2/24 Shift Reduce Parser

Handle, Handle pruning, Actions in SR parser, algorithm

Q Design the following grammar using shift reduce parser method.

$$E \rightarrow E+E \mid E * E \mid id$$

stack

\$

\$ id

\$ E

\$ E +

\$ E id

\$ E+E

\$ E

input

id+id\$

+id\$

+id\$

id\$

\$

\$

\$

action

shift id

reduce using $E \rightarrow id$

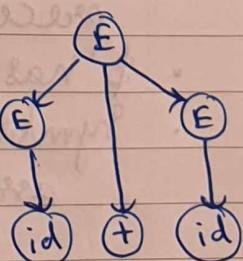
shift +

shift id

reduce using $E \rightarrow id$

reduce using $E \rightarrow E+E$

accept



- * Handle is a string on the RHS of a production which can be reduced by replacing it with the LHS variable in a process called pruning to get to the start variable.
- * Handle pruning is a process used to reduce a handle by replacing it with the LHS of the production.
- * Actions in LR parser -
 - (i) Shift - till the string in the stack is a handle.
 - (ii) Reduce - replace the handle in the stack with its LHS variable
 - (iii) Accept - the string is accepted if the input gets scanned completely and the stack only has the start variable (and the \$ ofc). The string is then valid
 - (iv) Reject - the string is invalid.

* Operator Precedence Parser

- An identifier is always given higher precedence than other symbols
- \$ has the lowest precedence
- Symbols with the same precedence follow associativity

Symbol	Precedence	Associativity
\$	lowest	-
+, -	-	Left
*, /	-	Left
^	-	Right
id	Highest	-

operator grammar is a CFG that satisfies -

- (i) no null production is present
- (ii) no two variables are present together

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* Steps to design Operator Precedence Parser.

(i) Design Operator Precedence Relation Table (?)

(ii) Algorithm

(a) if input has been completely scanned and the stack only has the start variable + (\$), accept & break

(b) else

 if let $a = \text{topmost stack terminal}$

$b = \text{input symbol}$

 if $a \neq b$ or $a = b$ (precedence)

$\rightarrow \text{SHIFT}$

 else if ($a \geq b$)

$\rightarrow \text{REDUCE}$

 else ERROR()

(iii) example

$E \rightarrow E+E | E*E | id$

eg: id+id

stack

\$

\$id

\$E

\$E+

input

id id \$

+ id \$

id \$

id \$

action

shift

reduce

shift (?)

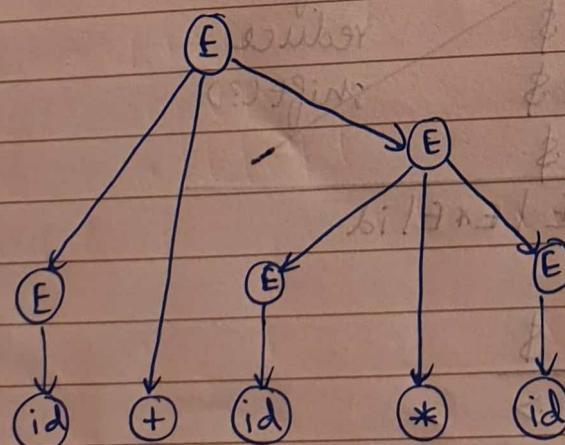
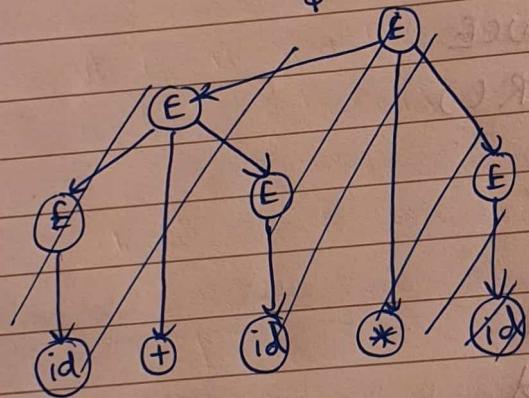
eg: $E \rightarrow E+E | E*E | id$

Step 1:

	id	+	*	\$
id	-	>	>	>
+	<	>	<	>
*	<	>	>	>
\$	<	<	<	Accept

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Stack	Input	top most stack term	input term	Action
\$	a		b	shift id
\$id	id + id * id \$	\$	id	reduce E → id
\$E	+ id * id \$	id	+	shift +
\$E +	+ id * id \$	\$	+	shift id
\$E + id	id * id \$	id	*	reduce E → id
\$E + E	* id \$	id	*	shift *
\$E + E *	* id \$	*	id	shift id
\$E + E * id	id \$	id	\$	reduce E → id
\$E + E * E	\$	*	\$	reduce E → E * E
\$E + E E	\$	*	+	reduce E → E + E
\$E	\$	\$	\$	Accept



E₁ - missing operator (for id id)

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Q.

$$E \rightarrow E+E \mid E*E \mid E \uparrow E \mid id$$

input = id + id * id + id + id

whether enter (available) plus valid for eval (ii)

step'	id	*	+	\$
id	-	>	>	>
*	<	<	>	>
+	<	<	<	>
\$	<	<	<	<

0/8dK/2d2d2 ← 3 ←

stack

input \$

action

\$ shift id

\$id Reduce id

\$ E shift ↑

\$ E↑ id shift id

\$ E↑ E Reduce E↑ id

0/1T+T ← T

0/0/1/0 ← V

b*c*d+r : b*c*d+r of print

\$	*	+	1	,))	d	r	0
<	<	<	-	-	-	-	-	-	↑
<	<	<	-	-	-	-	-	-	d
<	<	<	-	-	-	-	-	-	c
<	<	<	-	-	-	-	-	-	b
<	<	<	-	-	-	-	-	-	a
<	<	<	-	-	-	-	-	-	*
<	<	<	-	-	-	-	-	-	+
<	<	<	-	-	-	-	-	-	1
<	<	<	-	-	-	-	-	-	,
<	<	<	-	-	-	-	-	-	0

- * Operator Grammar is a CFG that
- contains no null productions
 - does not contain any productions where variables occur together

Q Converting Grammar to Operator Grammar

(i) $S \rightarrow \$SAS|ba$
 $A \rightarrow bSb|b$

$\Rightarrow S \rightarrow SbSbS|SbS|a$

* since A is unreachable from the start variable
 it is useless, do not write it

(ii) $S \rightarrow SES$ $E \rightarrow +|-|*$
 $\Rightarrow S \rightarrow +S+S|S*S$

Q With the help of following grammar, explain the role of operator precedence parser.

$E \rightarrow E+T|ET$

$T \rightarrow T*V|V$

$V \rightarrow a|b|c|d$

String to be parsed: $a+b*c*d$

Sol.

	a	b	c	d	+	*	\$
a	-	-	-	-	>	>	>
b	-	-	-	-	>	>	>
c	-	-	-	-	>	>	>
d	-	-	-	-	>	>	>
+	<	<	<	<	>	>	>
*	<	<	<	<	>	<	>
\$	<	<	<	<	>	>	>

Accept

$E \rightarrow T \rightarrow V \rightarrow a b | c | d | E * E | E + E$

$E \rightarrow E + E | E * E | a b | c | d$

 ϵ

Stack

 $\$$ $\$ab$ $\$E$ $\$E +$ $\$E + b$ $\$E + E$ $\$E + E *$ $\$E + E * c$ $\$E + E * E$ $\$E + E$ $\$E + E *$ $\$E + E * d$ $\$E + E * E$ $\$E + E$ $\$ E$

Input

a b c d

Action

shift a

Reduce $E \rightarrow a$

shift +

shift b

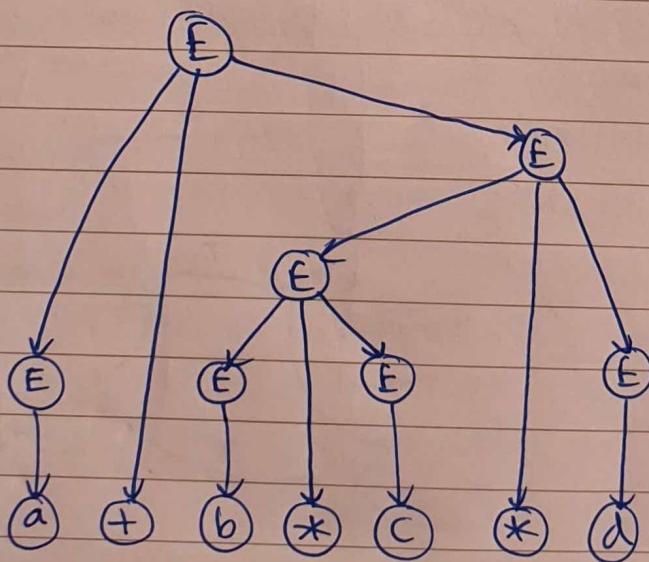
Reduce $E \rightarrow b$

shift *

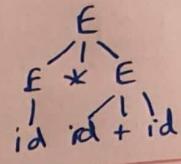
shift c

Reduce $E \rightarrow c$ shift *
~~reduce~~shift *
~~reduce~~shift *d
~~reduce~~shift *d
~~reduce~~shift *d
~~reduce~~shift *d
~~reduce~~shift *d
~~reduce~~shift *d
~~reduce~~

Accept



$\$(a+b)+c\$$



Q

$E \rightarrow E+E \mid E * E \mid (E) \mid id$
 input = $E \leftarrow (E+E \mid id * (id+id))$

stack

\$

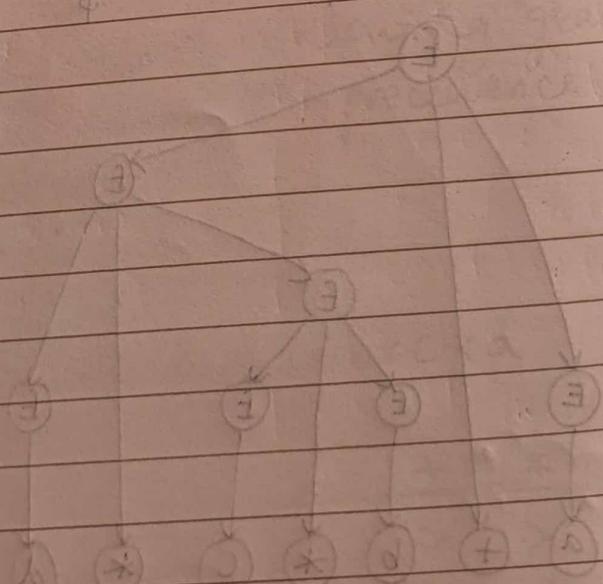
\$ id

+ \$ E

\$ E *

input	a	b	Action
$id * (id+id) * \$$	id		shift id
$* (id+id) \$$	*		reduce $E \rightarrow$
$* (id+id) \$$	*		shift *
$(id+id) \$$	(shift (

	id	+	*	()	*	\$
id	E_1	*	>	E_1	>	>	
+	<	*	>	<	<	>	
*	<	>	>	<	>	>	
(<	*	<	<	=	E_2	
)	E_1	>	>	E_1	>	>	
\$	<	<	*	<	E_2	Accept	



* SLR

Apply SLR parsing technique and construct SLR parse table for the following grammar.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

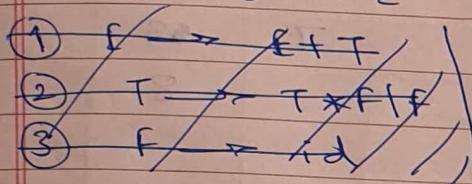
$$F \rightarrow id$$

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{ closure }
 { LR(0) }
 { complete item }

S1. Augment the Grammar & list the follows

$$E' \rightarrow E$$



$$\textcircled{1} \quad E \rightarrow E + T$$

$$\textcircled{2} \quad E \rightarrow T$$

$$\textcircled{3} \quad T \rightarrow T * F$$

$$\textcircled{4} \quad T \rightarrow F$$

$$\textcircled{5} \quad F \rightarrow id$$

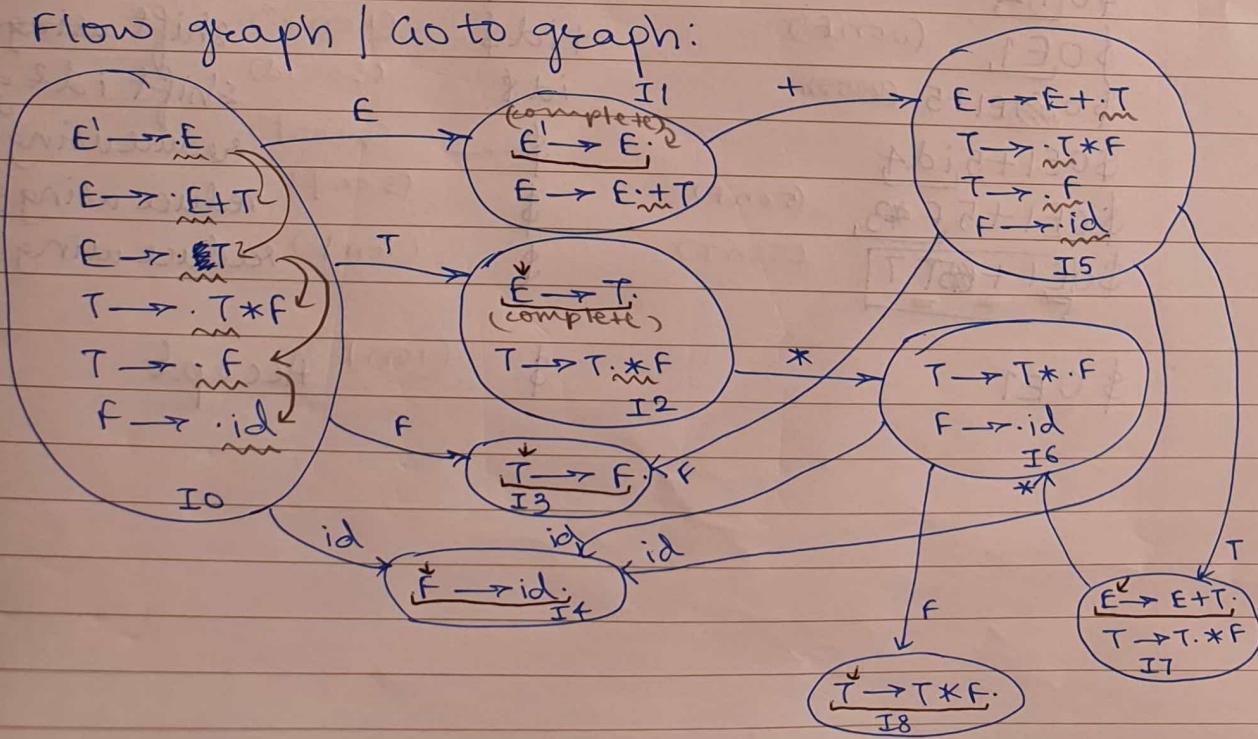
$$\text{follow}(E') = \{ \$ \}$$

$$\text{follow}(E) = \{ \$, + \}$$

$$\text{follow}(T) = \{ \$, +, * \}$$

$$\text{follow}(F) = \{ \$, +, * \}$$

S2 Flow graph / Ato graph:



S3 LR(0) Parser Table

States	Actions			goto			
	id	+	*	\$	E	T	F
0	S4					1	
1		S5				2	
2				Accept			
3							
4							
5	S4						
6	S4						
7							
8							

FOLLOW(E)
 $r_2 \rightarrow 2$
 FOLLOW(T)
 $r_4 \rightarrow 3$
 FOLLOW(F)
 $r_5 \rightarrow 4$
 FOLLOW(CE)
 $r_1 \rightarrow 7$
 FOLLOW(CT)
 $r_3 \rightarrow 8$

S4 eg: id+id

stack

 $\$ 0$ state $\$ 0 id4$ $\$ 0 F3$ (0 on F) $\$ 0 T2$ (0 on T) $\$ 0 E1$ (0 on E) $\$ 0 E1 + 5$ (0 on +) $\$ 0 E1 + 5 id4$ $\$ 0 E1 + 5 F43$ $\$ 0 E1 + 5 T7$ $\$ 0 E1$

input

input

shift id & goto + (0 on id)

reduce using ⑤ $F \rightarrow id$ (4 on +)reduce using ④ $T \rightarrow F$ (3 on +)reduce using ③ $E \rightarrow T$ (2 on +)

shift using + & goto \$ (1 on +)

shift id & goto + (5 on id)

reduce using ⑤ $F \rightarrow id$ (0 on \$)reduce using ④ $T \rightarrow F$ (3 on \$)reduce using ① $E \rightarrow id$ (7 on \$)

Accept



Q

compute LR(0) item (the flow diagram) for the following production $S \rightarrow XYZ$

$S \rightarrow \cdot S \times$ not required for single production

$S \rightarrow \cdot XYZ$

$S \rightarrow X \cdot YZ$

$S \rightarrow XY \cdot Z$

$S \rightarrow XYZ \cdot$

Q

Apply SLR parsing techniques and construct SLR parser table for the following grammar -

$$S \rightarrow (S)S$$

$$S \rightarrow \epsilon$$