References

[BBG+04] Vieri Benci, C. Bonanno, Stefano Galatolo, G. Menconi, and M. Virgilio. Dynamical systems and computable information. *Discrete & Continuous Dynamical Systems - B*, 4(4):935, 2004.

In this paper, the authors examine the connections between information theory and dynamical systems. Particular attention is payed to the concept of *entropy*, paticularly in the contexts of *strings in a measure space* and the *relative entropy of a measure* (defined by the Kullback-Leibler divergence of an ergodic measure with respect to the standard Lebesgue measure). The authors then prove that certain conditions on the entropy of the measure can be used to obtain bounds on the amount of information required to describe orbits of the dynamical system.

This paper provides an interesting second perspective on how classical ideas in computing intersect with dynamical systems. In some ways the analysis appears to be more tractable than that appearing in the papers we have read that examine the dynamics of turing machines. However, it is likely that our paper will not emphasize the ideas in this paper as much.

[DKB04] Jean-Charles Delvenne, Petr Kurka, and Vincent Blondel. Decidability and Universality in Symbolic Dynamical Systems. *arXiv*, Apr 2004.

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[Kůr97] Petr Kůrka. On topological dynamics of Turing machines. *Theoretical Computer Science*, 174(1):203–216, Mar 1997.

This paper defines two dynamical systems based on the motion of the Turing Machine head and analyzes their behavior. It is interesting because it analyzes Turing Machines as dynamical systems, just like the Siegelmann paper analyzes dynamical systems as models of computation.

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This paper analyzes the decidability of questions about three-dimensional dynamical systems. It is interesting because it examines the complexity of questions we might want to ask about dynamical systems.

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