## Implicit Relation Inferring Using Knowledge Graph

### A Probabilistic Approach

#### **ABSTRACT**

In this paper, we propose an approach for detecting the implicit relations between 2 entities.

#### 1. INTRODUCTION

#### 2. RELATED WORKS

#### 3. FRAMEWORK

First,we do conceptualization Next,Judge whether the 2 entities are conceptually same Then, there are 2 cases of the CanBeExplained function:

• Explain 2 conceptually similar entity

Table 1: conceptually similar entity

entity	concept
Steve jobs	Person
Bill Gates	Person

• Explain 2 conceptually different entity

Table 2: Add caption

entity	concept
Mona Lisa	Painting
Renaissance	Period

Note that the concept here are not unique.

Last, We rank all the explanations in each step.

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# 4. PROBABILITY RECALCULATION AFTER CONCEPTUALIZATION

Given an entity e, from Probase, we can acquire its concepts' set C and for each  $c_i \in C$ , the frequency  $n(c_i, e)$  can be accordingly derived, which means how many times the e is A  $c_i$  pattern can be observed from the original corpus.

However, the concepts here has various forms as illustrated in Example 1. For our task, we only need relatively general concepts. The number of entities can be very large, but the number of top concepts and the relationship between them are limited, literally, we can find all the possible relationship between concepts instead of store all the long-tailed entities and their relations, which indicates the rationality of doing conceptualization.

EXAMPLE 1 (VARIOUS FORMS OF CONCEPTS). Take the entity Mona Lisa as example, its concepts includes painting, famous painting, world's most famous painting, with corresponding frequency 33,8,1

#### 4.1 Problem Definition

Given Probase, for each entity e, we can derive  $P(c_i|e)$ , where  $c_i \in C_{probase}$ ,

$$P(c_i|e) = \frac{n(c_i, e)}{n(e)}$$

We divide the  $C_{Probase}$  into 2 parts,  $C_{simple}$  and  $C_{long}$ , where  $C_{simple}$  only contains one word and  $C_{long}$  are the rest.  $C_{simple}$  are generated by the head modifier detection. The problem here is to recalculate the probability  $P(\gamma_i|e)$  where  $\gamma_i \in C_{simple}$ , literally, we should contribute all the counts of  $C_{long}$  to  $C_{simple}$ .

#### 4.2 Problem Solution

After head modifier detection, we have a set of  $\gamma_i \in C_{simple}$ , among all the  $c_{long_j} \in C_{long}$ , there are 2 cases in the probase determined by whether the  $c_{long_j}$  has an isA edge towards  $\gamma_i$  or not. The intuition of doing so is illustrated in the example 2:

EXAMPLE 2 (CONTRIBUTING LONG CONCEPTS). Assume that Mona Lisa is a painting and Mona Lisa is a famous painting are observed respectively 33 times and 8 times from different documents, we will get the knowledge that Mona Lisa is a painting occurs 41 times instead of 33 times. There are less chance of occurring Famous painting is a painting so that there won't be necessarily an isA edge from famous painting to painting.

Therefore, to calculate  $P(\gamma_i|e)$ , there are three cases:

- 1. e is A  $\gamma_i$ . The entity has has an is A edge towards one or more simple concept, which gives the original  $P_{original}(\gamma_i|e)$
- 2. e is A  $c_{long}$ ,  $c_{long}$  is A  $\gamma_i$ , In this case, we need to calculate the following equation

$$P(\gamma_i|e) = \sum_{c_{long}^* \in C_{long}} P(\gamma_i|c_{long}^*, e) \times P(c_{long}^*|e)$$

, where  $P(c_{long}^*|e)$  can be obtained from Probase and

$$P(\gamma_i|c_{long}, e) = \frac{n(\gamma, c_{long}, e)}{n(\gamma_i, e)}$$
(1)

We assume that the occurrence of e does not affect  $P(\gamma_i|c_{long})$  equivalently speaking,  $P(\gamma_i|c_{long})$  is independent from e, thus Eq. 1 can be simplified

$$P(\gamma_i|c_{long}, e) = P_{probase}(\gamma_i|c_{long}) = \frac{n(\gamma, c_{long})}{n(\gamma_i)}$$

which can be obtained from Probase.

3. e is A  $c_{long}$ ,  $c_{long}$  has no edge towards  $\gamma_i$ . The edge here refers to the is A relationship in Probase. Example 2 pointed out that there won't be necessarily an is A edge from famous painting  $(c_{long})$  to painting  $(\gamma_i)$ , however  $c_{long}$  obviously belongs to  $\gamma_i$ . In this case, since it's detected by the head modifier method, we assume

$$P_{head}(\gamma_i|c_{long_i})=1$$

Another reason why we do head modifier detection here is that even if the long concept  $c_{long}$  has an isA edge towards a certain concept  $\gamma_i'$ , it still sometimes not include the head concept of the long concept which is very plausible. The tradeoff of the 2 method is described in Example 3

Notice that the boundary between case 2 and case 3 are not strict, there are such edges that have low observation in Example 3. So that if we consider them as a whole, we can derive:

$$P(\gamma_i|c_{long}) = \lambda P_{head}(\gamma_i|c_{long}) + (1 - \lambda)P_{probase}(\gamma_i|c_{long})$$

where  $\lambda$  is a parameter principle: related to plausibility, number of occurrence, varies for different  $c_{long}$  should it be derived from learning? since we assume  $P_{head}(\gamma_i|c_{long})$  to be 1, Eq. 2 is simplified to:

$$P(\gamma_i|c_{long}) = \lambda + (1 - \lambda)P_{probase}(\gamma_i|c_{long})$$

Example 3 (Head concepts VS Original concepts). Again take famous painting as example, whose concepts image, treasure are reasonable but implausible, since their occurrence are twice and once respectively. However, the most plausible concept painting is not among the concepts. On the other hand, there exists several concepts that have also reasonable. For example topax(a kind of yellow gemstone) has the concept precious stones, and precious stones has an edge towards material which is reasonable.

Finally  $P(\gamma_i|e)$  is calculated using the following equation:

$$P(\gamma_i|e) = P_{original}(\gamma_i|e) + \sum_{\substack{c_{long}^* \in C_{long}}} [\lambda_i^* + (1 - \lambda_i^*)P(\gamma_i|c_{long}^*)] \times P(c_{long}^*|e)$$
(3)

The process of calculation is illustrated in the example 4

Example 4 (Calculating  $P(\gamma_i|e)$ ). As illustrated in Fig. 4.2, the process of calculating the typicality a concept is as follows, where painting is  $\gamma_i$  and Mona Lisa is e P(painting|MonaLisa) consists of 2 parts, the direct edge  $P_{original}(\gamma_i|e) = 0.23$ , and the second part

$$\sum_{c_{long}^* \in C_{long}} [\lambda_i^* + (\alpha_i^*) P(\gamma_i | c_{long}^*)] \times P(c_{long}^* | e)$$

 $(\alpha_i^* + \gamma_i^* = 1)$  Thus we get

$$P = 0.007 \times \lambda_{i2} + 0.05 \times \lambda_{i1} + 0.04 \times (\lambda_{i3} + 0.65\alpha_{i3})$$

For piece, it is the similar process. The relation here is only part of the whole graph.

We consider only 2 layers of is A relationship for 2 reasons. The first one is that more layers will lead to noisy concepts such as issue, factor, element, which are concepts for almost eveything, Secondly, discussing the transitive relation between concepts is beyond the scope of this paper.

#### 5. FIND ALIAS FOR ATTRIBUTES

For a pair (Sherlock holmes, United Kindom), country is a merely-ok attribute, on the contrary, residence, deathPlace are better since they are more specific and more seemingly plausible to be an attribute. We argue that for each pair of entity, there is a selectional preference for attribute.

#### **5.1 Problem Definition**

Given a set of concept pairs  $(\gamma_1, \gamma_2)$ , where  $\gamma_1 \in C_1$  and  $\gamma_2 \in C_2$ , we want to find a set of attributes A, where for each  $a \in A$ : we can form a  $(\gamma_1, a, \gamma_2)$  pair which best describe the relationship between  $\gamma_1$  and  $\gamma_2$ .

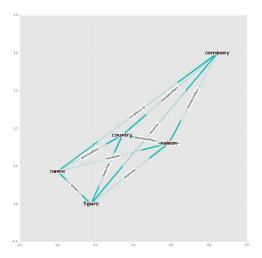


Figure 2: Subgraph of Entity Attribute Graph

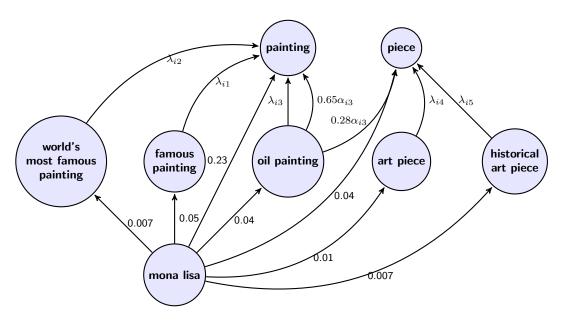


Figure 1: calculating  $P(\gamma_i|MonaLisa)$ 

#### 5.2 Problem Solution

#### 5.2.1 Entity Attribute Graph Construction

For any  $(entity_1, attribute, entity_2)$  tuple, later denoted as  $(e_1, a, e_2)$ , where  $e_1$  and  $e_2$  are also referred to as domain and range of the attribute. We can conceptualize  $e_1$  and  $e_2$  using the method in section 4, and get a set of concept  $C_1, C_2$ , accompanied with a set of probabilities  $P(\gamma_1|e_{1i})$ ,  $P(\gamma_2|e_2)$ , where  $\gamma_1 \in C_1$ ,  $\gamma_2 \in C_2$ .

Thus for any attribute a, given a pair of entity  $(e_{1i}, e_{2j})$ , we can define: should i use joint ratio here?

$$P_{(e_{1i},e_{2j})}((\gamma_{1},\gamma_{2})|a) = P_{before}(\gamma_{1}|a) \times P_{after}(\gamma_{2}|a)$$

$$= P(\gamma_{1}|e_{1i})P(e_{1i}|a) \times P(\gamma_{2}|e_{2j})P(e_{2j}|a)$$
(4)

where we use  $P_{(e_{1i},e_{2j})}((\gamma_1,\gamma_2)|a)$  to denote observing a single pair  $(e_{1i},e_{2j})$ , how likely is a combination of  $(\gamma_1,a,\gamma_2)$  to occur.

Consequently,

$$P((\gamma_1, \gamma_2)|a) = \sum_{e_{1i} \in E_1, e_{2j} \in E_2} P_{(e_{1i}, e_{2j})}((\gamma_1, \gamma_2)|a)$$
 (5)

where  $E_1$ ,  $E_2$  denoting the whole set of domain entity and range entity, The  $P(e_{1i}|a)$  and  $P(e_{2j}|a)$  here has only 2 values 1 and 0, depending on whether  $e_1$  occurs before a or  $e_2$  occurs after a. Apparently, only  $(e_{1i}, a, e_{2j})$  occurs will give the equation a non-zero value, therefore, Eq. 5 is finally equal to Eq. 6.

$$P((\gamma_{1}, \gamma_{2})|a) = \sum_{(e_{1i}, a, e_{2j}) \in KB} P_{(e_{1i}, e_{2j})}((\gamma_{1}, \gamma_{2})|a)$$

$$= \sum_{(e_{1i}, a, e_{2j}) \in KB} P(\gamma_{1}|e_{1i}) \times P(\gamma_{2}|e_{2j})$$
(6)

The process of calculating is demonstrated in Example. 5

Example 5 (Calculating  $P((\gamma_1, \gamma_2)|a)$ ). As illustrated in Fig. 3, the process of calculating  $P((\gamma_1, \gamma_2)|a)$  is as follows

insert a graph

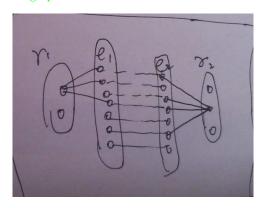


Figure 3: Calculating  $P((\gamma_1, \gamma_2)|a$  for

To Construct the Entity Attribute Graph, we calculate  $P((\gamma_1, \gamma_2)|a)$  for each attribute.

Note that we only consider the attributes whose range is an entity, and ignore those numerical values or date-and-time values such as (MonaLisa, Year, 1503).

For each  $(\gamma_1, a, \gamma_2)$  tuple, we can calculate  $P((\gamma_1, \gamma_2)|a)$  for each

#### **5.3** Find the best alias

We then Use an arg max model to solve the problem. Given  $(e_1, e_2)$ , our goal is to find the best attribute for it. We denote it as:

Normalize and get topK, K trough case study is around 5, so we here set K=10

Add edge $\ddot{i}$ jŽC1->C2 with label: attr, score to the alias graph

#### 6. EXPERIMENT

#### 6.1 Head Concept Vs Original Concept

#### 6.2 Find alias

#### 6.2.1 compare

Compare  $P((\gamma_{1i}, \gamma_{2i}|a))P(\gamma_{1i}|a) \times P(\gamma_{2i}|a)$ 

#### 6.2.2 Sense Disambiguation

We can solve the problem of sense disambiguation problem well by applying this method since there are many entities belongs to the same concept and we only consider topK  $(\gamma_1, \gamma_2)$  pairs that has high typicality  $P((\gamma_1, \gamma_2)|a)$ , so that the weird  $(\gamma_1, \gamma_2)$  patterns as manifest in Example. 6 can be easily filtered.

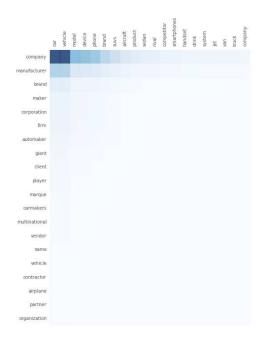


Figure 4:  $\gamma_1, \gamma_2$ ) plot for attribute Manufacturer

Example 6 (Sense Disambiguation). Consider the following (e1, a, e2) tuple (iphone, manufacturer, apple). Suppose it is our query, where apple's sense can either be a kind of fruit or a company. Fig. 4 is a heatmap for all the concepts pairs  $(\gamma_1, \gamma_2)$  of attributes manufacturer. The horizontal axis represents the  $e_1$  and the vertical axis stands for  $e_2$ . The darker the blue is, the higher typicality it will be. In Fig. 4, We can observe that the top concepts of  $e_2$  in the heatmap are company, manufacturer,... and top 10 pairs also does not include fruit. The intuition for this is that there exists thousands of (e1, a, e2) tuple such as (BMW\_Z4,manufacturer,BMW), (PlayStation\_4,manufacturer,Sony) other than (iphone, manufacturer, apple) tuple, which results in a reasonable distribution.

#### **6.3** Selectional Preference

#### 6.4 Evaluation

#### 7. CONCLUSION