

# FUNCTIONS (P1)

(10 MARKS)

FUNCTIONS  
ALONE

WITH  
QUADRATICS

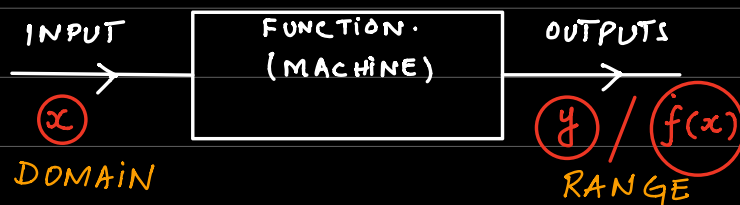
WITH  
TRIG

WITH  
DIFFERENTIATION

VERY LONG BUT EASY CHAPTER.

MEMORIZE EVERY DETAIL!

FUNCTIONS ARE NUMBER MACHINES.



$$f(x) = 2x + 3$$

↙ Name of function  
↘ value of input ( $x$ )

$$g(x) = x^2 - 5$$

$$f(1) = 2(1) + 3 = 5$$

$$f(4) = 2(4) + 3 = 11$$

$$g(3) = (3)^2 - 5 = 4$$

$$f(k) = 2k + 3$$

$$g(t-1) = (t-1)^2 - 5$$

## INVERSE OF A FUNCTION:

(2 MARKS in O LEVELS) (3 MARKS in A LEVELS)

THERE ARE ADDITIONAL STEPS. BE CAREFUL!

$$f(x) = 2x - 5$$

STEP 1:

$$f(x) = y$$

$$y = 2x - 5$$

$$y + 5 = 2x$$

$$f(x) = y$$

STEP 2:

$$x = \frac{y + 5}{2}$$

$$f^{-1}(y) = x$$

STEP 3:

$$f^{-1}(y) = x$$

STEP 4:

$$f^{-1}(y) = \frac{y + 5}{2}$$

$$f^{-1}(x) = \frac{x + 5}{2}$$

Q.

$$f(x) = 2x + 8$$

$$f(x) = y$$

$$y = 2x + 8$$

$$y - 8 = 2x$$

$$x = \frac{y - 8}{2}$$

$$f^{-1}(y) = x$$

$$f^{-1}(y) = \frac{y - 8}{2}$$

$$f^{-1}(x) = \frac{x - 8}{2}$$

Q.

$$g(x) = x^3 - 8$$

$$g(x) = y$$

$$y = x^3 - 8$$

$$y + 8 = x^3$$

$$x^3 = y + 8$$

$$x = \sqrt[3]{y + 8}$$

$$g^{-1}(y) = x$$

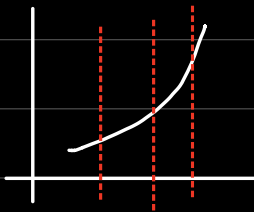
$$g^{-1}(y) = \sqrt[3]{y + 8}$$

$$g^{-1}(x) = \sqrt[3]{x + 8}$$

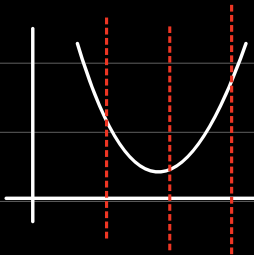
# TEST

## VERTICAL LINE TEST

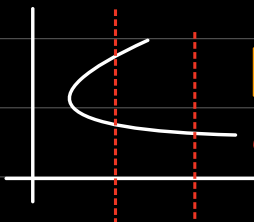
CHECKS WHETHER A GRAPH IS A FUNCTION OR NOT?



**PASS** IT IS FUNCTION  
ONE-ONE FUNCTION



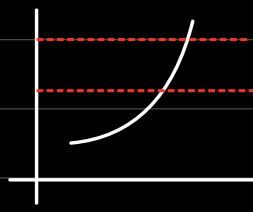
**PASS** IT IS FUNCTION  
MANY-ONE FUNCTION



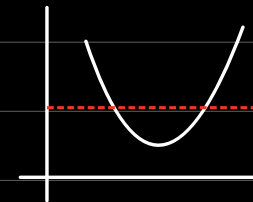
**FAIL** NOT A FUNCTION  
ONE-MANY.

## HORIZONTAL LINE TEST

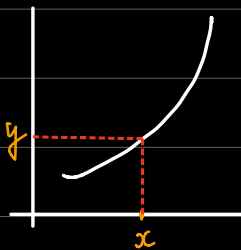
CHECKS IF THE INVERSE OF A FUNCTION EXISTS OR NOT?



**PASS** INVERSE EXISTS  
ONE-ONE FUNCTION

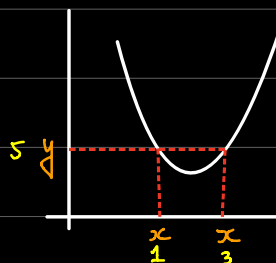


**FAIL** INVERSE DOES NOT EXIST.  
MANY-ONE FUNCTION



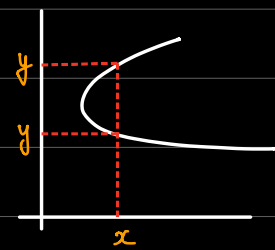
ONE-ONE FUNCTION

For one input you will get one output.



MANY TO ONE FUNCTION

For Many inputs you can get one output.



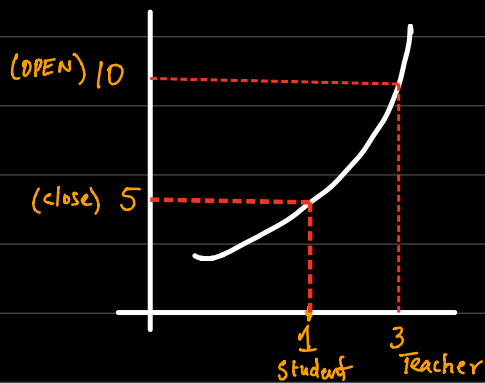
ONE TO MANY

one input can get you many outputs.

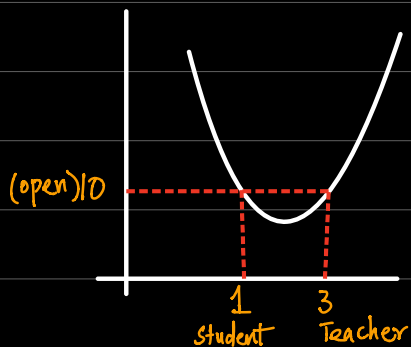
## ACCESS POINTS

INPUT = 1 (STUDENT)  
= 3 (TEACHER)

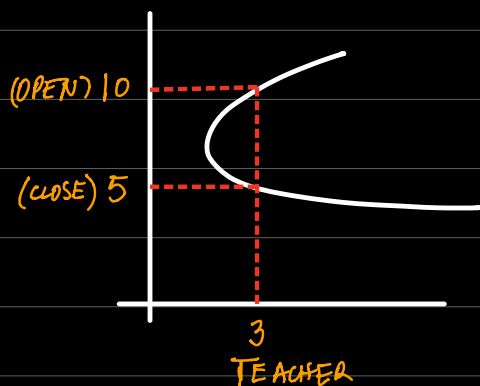
OUTPUT = 5 (CLOSE)  
= 10 (OPEN)



→ This would be useful at  
STAFF ROOM DOOR.



→ THIS WOULD BE USEFUL  
AT SCHOOL MAIN GATE  
etc.



→ THIS IS NOT A USEFUL  
MACHINE.

ONE-TO-MANY IS  
NOT A FUNCTION.

## FOR TOMORROW

### PRE REQUISITES

- 1) MEMORIZE TODAY'S WORK.
- 2) STRONG COMMAND ON QUADRATICS.

↓  
Youtube Marathon.