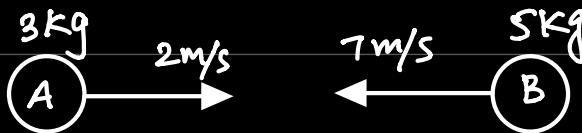


MOMENTUM = PRODUCT OF MASS AND VELOCITY.

$$P = mv$$

$$\text{Units} = \text{kg}\cdot\text{m/s} \quad \text{or} \quad \text{kgms}^{-1}$$

IMP: DIRECTION WITH VELOCITY.

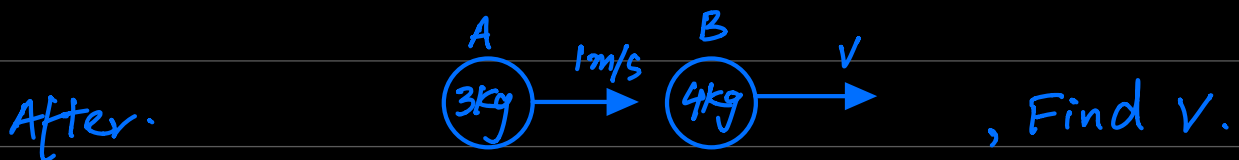
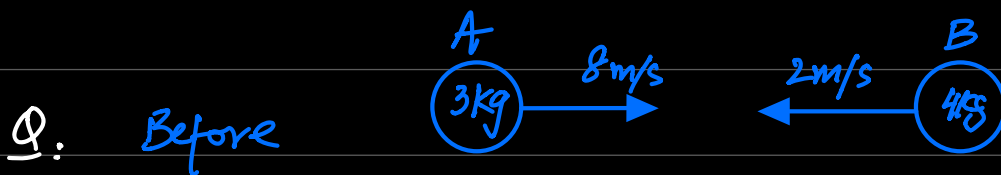


$$p_A = (3)(2) \\ = 6 \text{ kgms}^{-1}$$

$$p_B = (5)(-7) \\ = -35 \text{ kgms}^{-1}$$

## COLLISIONS

$$\begin{array}{ccc} \text{TOTAL MOMENTUM} & = & \text{TOTAL MOMENTUM} \\ \text{BEFORE COLLISION} & & \text{AFTER COLLISION} \end{array}$$



$$\text{TOTAL MOMENTUM BEFORE} = \text{TOTAL MOMENTUM AFTER}$$

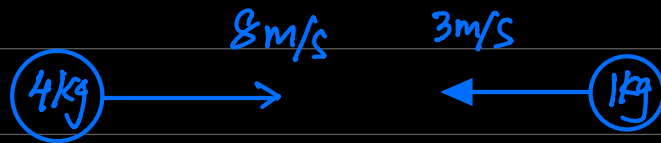
$$(3)(8) + (4)(-2) = (3)(1) + (4)(v)$$

$$24 - 8 = 3 + 4v$$

$$16 - 3 = 4v$$

$$v = 3.25$$

Q:



After the collision, Both boxes coalesce.

Coalesce = Join together



TOTAL MOMENTUM BEFORE = TOTAL MOMENTUM AFTER.

$$(4)(8) + (1)(-3) = (4+1)(v)$$

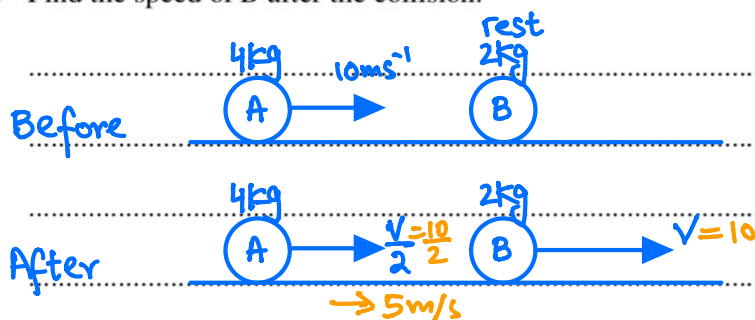
$$32 - 3 = 5v$$

$$v = 5.8$$

- 4 Small smooth spheres  $A$  and  $B$ , of equal radii and of masses  $4\text{ kg}$  and  $2\text{ kg}$  respectively, lie on a smooth horizontal plane. Initially  $B$  is at rest and  $A$  is moving towards  $B$  with speed  $10\text{ ms}^{-1}$ . After the spheres collide  $A$  continues to move in the same direction but with half the speed of  $B$ .

(a) Find the speed of  $B$  after the collision.

[2]



$$\text{Before} = \text{After}$$

$$(4)(10) + (2)(0) = 4\left(\frac{v}{2}\right) + (2)(v)$$

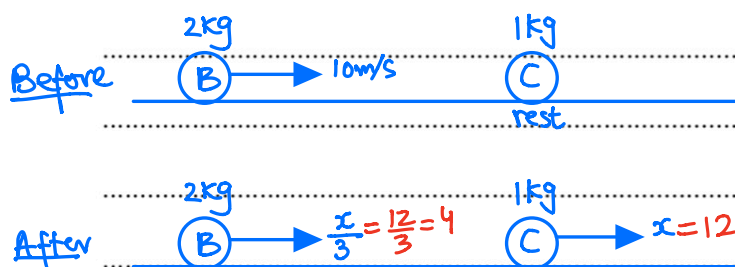
$$40 = 2v + 2v$$

$$v = 10$$

A third small smooth sphere  $C$ , of mass  $1\text{ kg}$  and with the same radius as  $A$  and  $B$ , is at rest on the plane.  $B$  now collides directly with  $C$ . After this collision  $B$  continues to move in the same direction but with one third the speed of  $C$ .

(b) Show that there is another collision between  $A$  and  $B$ .

[3]



$$\text{Before} = \text{After}$$

$$(2)(10) + (1)(0) = 2\left(\frac{x}{3}\right) + 1(x)$$

$$x = 12$$

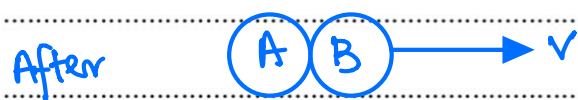
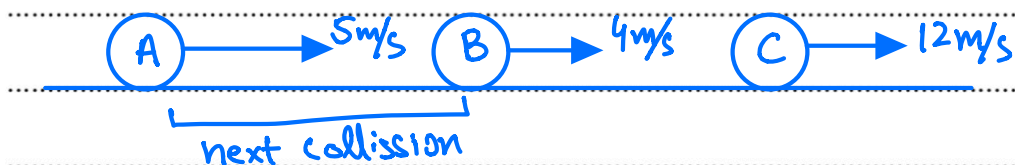


Since speed of  $A = 5$  and speed of  $B = 4$ ,  $A$  will catch up and there will be another collision.

(c) A and B coalesce during this collision.

Find the total loss of kinetic energy in the system due to the three collisions.

[5]



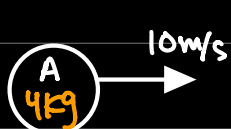
Before = After

$$(4)(5) + (2)(4) = (4+2)v$$

$$28 = 6v$$

$$v = 4.667$$

START



$$\text{TOTAL KE} = \frac{1}{2}(4)(10)^2 + \frac{1}{2}(2)(0)^2 + \frac{1}{2}(1)(0)^2 = 200 \text{ J}$$

END



$$\text{TOTAL KE} = \frac{1}{2}(4+2)(4.667)^2 + \frac{1}{2}(1)(12)^2 = 137.15 \text{ J}$$

$$\text{Loss in KE} = 200 - 137.15 = 62.85 \text{ J}.$$