RS-HL-14: Multi User Congestion Game

Hongseok Kim

UT Austin Oden Institute

08/02/24

Configuration of Congestion Game

Algorithm for *C*

I. Load the Dataset

```
clear;clc;
% Load the Satellite Contat Dataset
addpath('~/Desktop/Redstone_Project/RS_HL/RS_HL_10_TV_MDP_Functions')
load('/workspace/RS_Dataset/RS_HL_3_dataset.mat')
```

II. Destination Setting and Time Index Vector Setting

```
time_index_vector = 100:130;
start_time_index = 100:120;

number_of_agents = 100;
number_of_destinations = 5;
state_vector = 1:48;

start_state = state_vector(randi(numel(state_vector), 1, number_of_agents));
destination_values = randsample(state_vector,number_of_destinations);
destination_state = destination_values(randi(numel(destination_values), 1, number_of_agents));
start_time = start_time_index(randi(numel(start_time_index), 1, number_of_agents));
```

II.1 Run the MDP simulation for each destination

```
fprintf('Total Number of Destinations: %d\n', number_of_destinations);

Total Number of Destinations: 5

for destination_index = 1:number_of_destinations
    fprintf('-----\n')
```

```
fprintf('Running MDP %d / %d , Destination %d \n',
destination_index,number_of_destinations,destination_values(destination_index
));
    MDP.(['MDP', num2str(destination_values(destination_index))])
= runMDP(sat_to_sat_contact_3d_matrix,
time_index_vector,destination_values(destination_index));
end
```

```
Running MDP 1 / 5 , Destination 35
simulation set up complete!
Policy: 1 -> Value Iteration: 418
Policy: 2 -> Value Iteration: 14
Policy: 3 -> Value Iteration: 7
Policy: 4 -> Value Iteration: 5
Policy: 5 -> Value Iteration: 6
Policy: 6 -> Value Iteration: 11
Policy: 7 -> Value Iteration: 5
Policy: 8 -> Value Iteration: 1
______
Running MDP 2 / 5 , Destination 32
simulation set up complete!
Policy: 1 -> Value Iteration: 419
Policy: 2 -> Value Iteration: 13
Policy: 3 -> Value Iteration: 7
Policy: 4 -> Value Iteration: 5
Policy: 5 -> Value Iteration: 6
Policy: 6 -> Value Iteration: 10
Policy: 7 -> Value Iteration: 5
Policy: 8 -> Value Iteration: 5
Policy: 9 -> Value Iteration: 1
_____
Running MDP 3 / 5 , Destination 20
simulation set up complete!
Policy: 1 -> Value Iteration: 460
Policy: 2 -> Value Iteration: 14
Policy: 3 -> Value Iteration: 5
Policy: 4 -> Value Iteration: 5
Policy: 5 -> Value Iteration: 5
Policy: 6 -> Value Iteration: 11
Policy: 7 -> Value Iteration: 4
Policy: 8 -> Value Iteration: 5
Policy: 9 -> Value Iteration: 1
Policy: 10 -> Value Iteration: 1
Policy: 11 -> Value Iteration: 1
Policy: 12 -> Value Iteration: 1
Policy: 13 -> Value Iteration: 1
Policy: 14 -> Value Iteration: 1
Policy: 15 -> Value Iteration: 1
______
Running MDP 4 / 5 , Destination 40
simulation set up complete!
Policy: 1 -> Value Iteration: 441
Policy: 2 -> Value Iteration: 14
Policy: 3 -> Value Iteration: 6
Policy: 4 -> Value Iteration: 5
Policy: 5 -> Value Iteration: 8
Policy: 6 -> Value Iteration: 10
Policy: 7 -> Value Iteration: 9
Policy: 8 -> Value Iteration: 1
Policy: 9 -> Value Iteration: 1
```

```
Running MDP 5 / 5 , Destination 47

simulation set up complete!

Policy: 1 -> Value Iteration: 434

Policy: 2 -> Value Iteration: 14

Policy: 3 -> Value Iteration: 7

Policy: 4 -> Value Iteration: 5

Policy: 5 -> Value Iteration: 7

Policy: 6 -> Value Iteration: 9

Policy: 7 -> Value Iteration: 5

Policy: 8 -> Value Iteration: 1
```

III. Configure each Agent's Setting

```
agents_input = [start_time', start_state', destination_state'];
```

IV. Configure the simulation structure setting

```
% Level 1: Initialize simulation structure
sim = struct();

for time_index = time_index_vector
    sim.(['time' num2str(time_index)]) = {};
end

% Level 2/3: Initialize Agent (Level 2) with States and Destination (Level 3)
number_of_agents = length(agents_input(:,1));

for agent_index = 1:number_of_agents
    sim.(['time' num2str(agents_input(agent_index,1))]).(['agent' num2str(agent_index)]).('state') = agents_input(agent_index,2);
    sim.(['time' num2str(agents_input(agent_index,1))]).(['agent' num2str(agent_index)]).('destination') = agents_input(agent_index,3);
end
```

V. Configuration of Action Value Structure and Simulation Structure

```
% Initialize Action Value Structure
action_value_struct = struct();
```

```
for time_index = time_index_vector
    % If there's no active agent, continue to next time step
    if isempty(sim.(['time' num2str(time_index)]))
       continue;
    end
    % Parse the number of active agents
    number_of_active_agents = length(fieldnames(sim.(['time'
num2str(time_index)]));
    % Make the status matrix represents current and next
    % [current_state, next_state, destination]
    status_matrix = zeros(3, number_of_active_agents);
    agents_list = fieldnames(sim.(['time' num2str(time_index)]));
    % Definine Original Policy Distribution Matrix
    original_policy_matrix =
zeros(number_of_active_agents,length(state_vector));
    % Find the Next state from Current Agent-State
    for active_agent_index = 1:number_of_active_agents
        % Find the Current State and Destination of given agent
        current_state = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('state');
        destination = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('destination');
        % Get the Action values and corresponding next states from given
state in given MDP
        action_value_vector = MDP.(['MDP' num2str(destination)]).
(['time' num2str(time_index)]).(['state' num2str(current_state)]).
('action_value_vector');
       next_state_vector = MDP.(['MDP' num2str(destination)]).
(['time' num2str(time_index)]).(['state' num2str(current_state)]).
('next_state_vector');
        % Action Value Matrix Config: [Action index, Action Value Q, Next
State S']
        vector_length = length(action_value_vector);
        action_value_matrix = [(1:vector_length)',action_value_vector,
next_state_vector, action_value_vector];
        action_value_matrix = sortrows(action_value_matrix,2, 'descend');
        action_value_struct.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('action_value_matrix') =
action_value_matrix;
```

```
% Find the Active Actoin Number from given Original MDP pi
distribution
        pi_dist = MDP.(['MDP' num2str(destination)]).(['time'
num2str(time_index)]).('policy_distribution');
        action_number = find(pi_dist(current_state,:) ~= 0);
        for action_number_index = 1:length(action_number)
original_policy_matrix(active_agent_index,action_number(action_number_index))
 = action_number(action_number_index);
        end
        % Get Activated Next States Vector (Which is from pi distribution)
        activated_next_states = action_number;
        action_value_struct.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('activated_next_states') =
activated_next_states;
        if length(action_number) > 1
        action_number = randsample(action_number,1);
        end
        next_state = MDP.(['MDP' num2str(destination)]).(['time'
num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('success').('next_state');
        reward = MDP.(['MDP' num2str(destination)]).(['time'
num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('success').('reward');
        state_value = MDP.(['MDP' num2str(destination)]).(['time'
num2str(time_index)]).(['state' num2str(current_state)]).('state_value');
        action_value = MDP.(['MDP' num2str(destination)]).
(['time' num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('action_value');
        % Configure Proposed status matrix for the collision test
        status_matrix(1,active_agent_index) = current_state;
        status_matrix(2,active_agent_index) = next_state;
        status_matrix(3,active_agent_index) = destination;
        % Add State Value
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('state_value') = state_value;
        % Save the Original Reward and action value to prepare the update
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('original_action_number') = action_number;
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('original_action_value') = action_value;
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('original_reward') = reward;
```

V.1 Policy Iteration By Updating Q values of potential Collision by given policy distribution

```
updated_policy_matrix =
zeros(number_of_active_agents,length(state_vector));
    policy_iteration = 0;
    congestion_cost_factor = 12;
    while true
    % while isequal(original_policy_matrix,updated_policy_matrix) == false
   policy_iteration = policy_iteration + 1;
    if policy_iteration > 1
        original_policy_matrix = updated_policy_matrix;
    end
    for active_agent_index = 1:number_of_active_agents
       action_value_matrix = action_value_struct.
(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('action_value_matrix');
       action_value_matrix_original = action_value_matrix;
       number_of_actions = length(action_value_matrix(:,1));
       for test_agent_index = 1:number_of_active_agents
          if active_agent_index == test_agent_index
              continue;
          end
```

```
index_starting_next_timestep = find(agents_input(:,1) ==
time_index+1);
          agents input extracted =
agents_input(index_starting_next_timestep,:);
          starting_state_list = agents_input_extracted(:,2)';
          test_activated_next_index =
original_policy_matrix(active_agent_index);
          text_activated_next_states =
test_activated_next_index(test_activated_next_index ~= 0);
          % test_activated_next_states
= action_value_struct.(['time' num2str(time_index)]).
(agents_list{test_agent_index}).('activated_next_states');
          test_activated_states = [text_activated_next_states,
starting_state_list];
          for action_index = 1:number_of_actions
              action_value_mat_next_state =
action_value_matrix(action_index,3);
              congestion_indicator = length(find(test_activated_states ==
action_value_mat_next_state));
              current_action_value = action_value_matrix(action_index,2);
              updated_action_value = current_action_value -
congestion_cost_factor * congestion_indicator;
              action_value_matrix(action_index,4) = updated_action_value;
          end
       end
       % if isequal(action_value_matrix(:,1),
action_value_matrix_updated(:,1)) == false
              fprintf('there was correctance \n')
       % end
       action_value_struct.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('action_value_matrix') =
action_value_matrix;
        % Policy Iteration Process -> Should Be Done
    end
    % Update The Action Number
    for active_agent_index = 1:number_of_active_agents
        % Find the Current State and Destination of given agent
        current_state = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('state');
```

```
destination = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('destination');
        % if current_state == destination
             continue;
        % end
        action_value_matrix = action_value_struct.
(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('action_value_matrix');
        updated_action_value_vector = max(action_value_matrix(:,4));
        updated_action_index = find(updated_action_value_vector ==
action_value_matrix(:,4));
        updated_action_policy = action_value_matrix(updated_action_index,1);
        for index = 1:length(updated_action_policy)
            updated_policy_matrix(active_agent_index,
updated_action_policy(index)) = updated_action_policy(index);
        end
        % Get Activated Next States Vector (Which is from pi distribution)
        activated_next_states_updated =
updated_policy_matrix(active_agent_index,:);
        activated_next_states_updated =
activated_next_states_updated(activated_next_states_updated ~= 0)';
        action_value_struct.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('activated_next_states') =
activated_next_states_updated';
        if length(updated_action_index) > 1
        updated_action_index = randsample(updated_action_index,1);
        end
        action_number = action_value_matrix(updated_action_index,1);
        action_value = action_value_matrix(updated_action_index,2);
        next_state = action_value_matrix(updated_action_index,3);
        reward = MDP.(['MDP' num2str(destination)]).(['time'
num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('success').('reward');
        % Modify Proposed status matrix for the collision test
        status_matrix(1,active_agent_index) = current_state;
        status_matrix(2,active_agent_index) = next_state;
        status_matrix(3,active_agent_index) = destination;
        % Modify the action number, reward, action value (may be changed)
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('action_number') = action_number;
```

```
sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('action_value') = action_value;
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('reward') = reward;
        sim.(['time' num2str(time_index)]).(agents_list{active_agent_index}).
('next_state') = next_state;
        % original_action_number = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('original_action_number');
        % Check the Update of the values
        % if isequal(action_number, original_action_number) == false
              fprintf('action_number changed from %d to %d
\n',original_action_number,action_number)
             time_index
              agents_list{active_agent_index}
              sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index})
        % end
    end
        if isequal(original_policy_matrix,updated_policy_matrix) == true
        break;
        end
    end
    fprintf('Policy Iteration Completed at time %d by %d iterations
\n',time_index, policy_iteration)
```

V.1 Propagation With Randomness

```
current_state = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('state');
    destination = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('destination');
    action_number = sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('action_number');
    transmission_probability = MDP.(['MDP' num2str(destination)]).
(['time' num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('success').('transition_probability');
        if random_factor > -1
        % if random factor > 1 - transmission probability
            % Update the time+1 for next state
            % Don't update the agent already arrived to destination
            if current_state == destination
                continue;
            end
            sim.(['time' num2str(time_index+1)]).
(agents_list{active_agent_index}).('state') =
status_matrix(2,active_agent_index);
            sim.(['time' num2str(time_index+1)]).
(agents_list{active_agent_index}).('destination') =
status_matrix(3,active_agent_index);
        else
            sim.(['time' num2str(time_index+1)]).
(agents_list{active_agent_index}).('state') = current_state;
            sim.(['time' num2str(time_index+1)]).
(agents_list{active_agent_index}).('destination') =
status_matrix(3,active_agent_index);
            % Since it is failure, we should replace reward as failure
penalty
            failure reward = MDP.(['MDP' num2str(destination)]).
(['time' num2str(time_index)]).(['state' num2str(current_state)]).(['action'
num2str(action_number)]).('fail').('reward');
            sim.(['time' num2str(time_index)]).
(agents_list{active_agent_index}).('reward') = failure_reward;
        end
    end
end
Policy Iteration Completed at time 100 by 1 iterations
Policy Iteration Completed at time 101 by 2 iterations
```

```
Policy Iteration Completed at time 100 by 1 iterations Policy Iteration Completed at time 101 by 2 iterations Policy Iteration Completed at time 102 by 1 iterations Policy Iteration Completed at time 103 by 2 iterations Policy Iteration Completed at time 104 by 2 iterations Policy Iteration Completed at time 105 by 2 iterations Policy Iteration Completed at time 105 by 2 iterations Policy Iteration Completed at time 106 by 2 iterations Policy Iteration Completed at time 107 by 2 iterations
```

```
Policy Iteration Completed at time 108 by 2 iterations
Policy Iteration Completed at time 109 by 2 iterations
Policy Iteration Completed at time 110 by 2 iterations
Policy Iteration Completed at time 111 by 2 iterations
Policy Iteration Completed at time 112 by 1 iterations
Policy Iteration Completed at time 113 by 2 iterations
Policy Iteration Completed at time 114 by 2 iterations
Policy Iteration Completed at time 115 by 2 iterations
Policy Iteration Completed at time 116 by 2 iterations
Policy Iteration Completed at time 117 by 2 iterations
Policy Iteration Completed at time 118 by 2 iterations
Policy Iteration Completed at time 119 by 2 iterations
Policy Iteration Completed at time 120 by 1 iterations
Policy Iteration Completed at time 121 by 1 iterations
Policy Iteration Completed at time 122 by 1 iterations
Policy Iteration Completed at time 123 by 1 iterations
Policy Iteration Completed at time 124 by 1 iterations
Policy Iteration Completed at time 125 by 1 iterations
Policy Iteration Completed at time 126 by 1 iterations
Policy Iteration Completed at time 127 by 1 iterations
Policy Iteration Completed at time 128 by 1 iterations
Policy Iteration Completed at time 129 by 1 iterations
Policy Iteration Completed at time 130 by 1 iterations
```

VI. result display

```
result matrix = zeros(length(time index vector), number of agents);
reward_matrix = zeros(length(time_index_vector),number_of_agents);
state_value_matrix = zeros(length(time_index_vector),number_of_agents);
action_value_matrix = zeros(length(time_index_vector),number_of_agents);
cumulative_reward_matrix = zeros(length(time_index_vector),number_of_agents);
for time_index = time_index_vector
    if isempty(sim.(['time' num2str(time_index)]))
     continue;
    end
    agents_list = fieldnames(sim.(['time' num2str(time_index)]));
    number_of_agents = length(agents_list);
    for agent_index = 1:number_of_agents
        agent_name = cell2mat(agents_list(agent_index));
        agent_no = regexp(agent_name, '\d+', 'match');
        agent_number = str2double(agent_no{1});
        result_matrix(time_index - min(time_index_vector) + 1,agent_number)
= sim.(['time' num2str(time_index)]).(agent_name).('state');
```

```
reward_matrix(time_index - min(time_index_vector) + 1,agent_number)
   sim.(['time' num2str(time_index)]).(agent_name).('reward');
          state_value_matrix(time_index - min(time_index_vector)
+ 1,agent_number) = sim.(['time' num2str(time_index)]).(agent_name).
('state_value');
          action_value_matrix(time_index - min(time_index_vector)
+ 1,agent_number) = sim.(['time' num2str(time_index)]).(agent_name).
('action_value');
          cumulative_reward_matrix(time_index - min(time_index_vector) +
1,agent_number) = sum(reward_matrix(1:time_index - min(time_index_vector) +
1,agent_number));
     end
end
result = [time_index_vector' , result_matrix]
result = 31 \times 101
                                                                                0 ...
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                             0
                                                                    0
                                                                          0
   100
           0
           0
                 0
   101
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                             0
                                                                   0
                                                                         19
                                                                                0
                                                             7
   102
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                                   0
                                                                         20
                                                                                0
   103
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                             6
                                                                   0
                                                                         46
                                                                                0
   104
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       5
                                                            28
                                                                    0
                                                                         47
                                                                                0
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       4
                                                            27
                                                                   0
                                                                          0
                                                                                0
   105
   106
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                      25
                                                            26
                                                                   0
                                                                          0
                                                                                0
   107
           0
                47
                       0
                              0
                                    0
                                          0
                                                 0
                                                      23
                                                            25
                                                                   0
                                                                          0
                                                                                0
           0
                                          0
                                                 0
                                                      22
                                                                   0
                                                                          0
                                                                                0
   108
                48
                       0
                              0
                                    0
                                                            48
                                                                                0
   109
                       0
                              0
                                          0
                                                 0
                                                      21
                                                            47
                                                                    0
                                                                          O
          25
                 3
                                    0
reward = [time index vector', reward matrix]
reward = 31 \times 101
                                          0
                                                 0
                                                                                0 • • •
   100
           0
                 Λ
                       0
                              0
                                    0
                                                       Λ
                                                             0
                                                                   Ω
                                                                          0
   101
           0
                 Ω
                                          0
                                                 0
                                                       0
                                                             0
                                                                                0
                       0
                              0
                                    0
                                                                   0
                                                                         -1
   102
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                            -1
                                                                   0
                                                                        -15
                                                                                0
   103
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                           -15
                                                                   0
                                                                         75
                                                                                0
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                      -1
                                                            -1
                                                                                0
   104
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                     -15
                                                            -1
                                                                          0
                                                                                0
   105
           0
                                    0
                                          0
                                                 0
                                                                                0
   106
                 0
                       0
                              0
                                                     -15
                                                            -1
   107
           0
                -1
                       0
                              0
                                    0
                                          0
                                                 0
                                                      -1
                                                            -1
                                                                   0
                                                                          0
                                                                                0
   108
           0
               -15
                       0
                              0
                                    0
                                          0
                                                 0
                                                      -1
                                                            75
                                                                   0
                                                                          0
                                                                                0
   109
          -5
                -1
                       0
                              0
                                    0
                                          0
                                                 0
                                                      -5
                                                             0
                                                                   0
                                                                          0
                                                                                0
cumulative_reward = [time_index_vector', cumulative_reward_matrix]
cumulative\_reward = 31 \times 101
                                                                                0 ...
   100
           0
                 Ω
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                             0
                                                                    0
                                                                          0
                                                                         -1
           0
                 0
                       0
   101
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                             0
                                                                   0
                                                                                0
   102
           0
                 0
                       0
                                          0
                                                 0
                                                       0
                                                            -1
                                                                        -16
                                                                                0
                              0
                                    0
                                                                   0
   103
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                       0
                                                           -16
                                                                   0
                                                                         59
                                                                                0
   104
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                      -1
                                                           -17
                                                                   0
                                                                         59
                                                                                0
   105
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                     -16
                                                           -18
                                                                   0
                                                                          0
                                                                                0
   106
           0
                 0
                       0
                              0
                                    0
                                          0
                                                 0
                                                     -31
                                                           -19
                                                                   0
                                                                          0
                                                                                0
   107
                                                           -20
                                                                                0
           0
                -1
                       0
                              0
                                    0
                                          0
                                                     -32
                                                                   0
```

```
0
   109
          -5
                -17
                         0
                               0
                                      0
                                            0
                                                   0
                                                       -38
                                                               55
                                                                       0
                                                                             0
state_value = [time_index_vector', state_value_matrix]
state_value = 31 \times 101
                                                                                      0 ...
  100.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
  101.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  102.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
                    0
                                                     0
  103.0000
                               0
                                          O
                                                                O
                                                                           O
                                                                                      0
  104.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  105.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  106.0000
                    Ω
                               Ω
                                          Ω
                                                     0
                                                                Ω
                                                                           Λ
                                                                                      Ω
  107.0000
                    Ω
                      -26.0000
                                          Ω
                                                     Ω
                                                                Ω
                                                                           Ω
                                                                                      0
                    0 -17.5000
                                          0
                                                                0
                                                                                      0
  108.0000
                                                     0
                                                                           Ω
  109.0000
              53.0000
                          2.5000
                                                     0
                                                                0
                                                                           0
                                                                                      0
action_value = [time_index_vector', action_value_matrix]
action_value = 31 \times 101
                                                                                      0 ...
 100.0000
                               0
                                          0
                                                     0
                                                                0
                                                                           0
  101.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  102.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  103.0000
                    0
                               0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  104.0000
                    0
                               0
                                                     0
                                                                0
                                                                           0
                                                                                      0
  105.0000
                    0
                               0
                                          0
                                                     0
                                                                0
                                                                           0
                                                                                      0
                                                                                      0
  106.0000
                    0
                               0
                                          0
                                                     Ω
                                                                0
                                                                           Ω
```

Ω

Ω

Ω

Ω

O

VI.1 Chack Congestion Factor in Result Matrix

0 -26.0000

0 -19.5000

2.5000

43.0000

-16

Ω

-33

```
congestion_factor_vector = zeros(length(result(:,1)),1);
active_data_packet= zeros(length(result(:,1)),1);
active_sats = zeros(length(result(:,1)),1);

for result_index = 1:length(result(:,1))
    states_vector = result(result_index,2:end);
    active_agent_vector = states_vector(states_vector ~= 0);
    unique_active_agent_vector = unique(active_agent_vector);
    active_sats(result_index) = length(unique_active_agent_vector);
    active_data_packet(result_index) = length(active_agent_vector);
    congestion_factor_vector(result_index) = length(active_agent_vector) -
    length(unique_active_agent_vector);
end

congestion_factor_vector'
```

ans = 1×31

107.0000

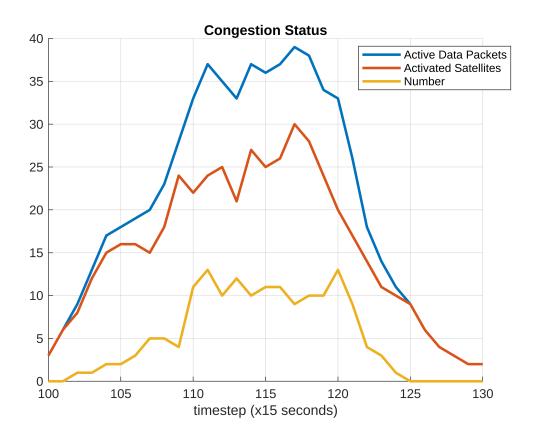
108.0000

109.0000

```
congestion_factor_sum = sum(congestion_factor_vector)
```

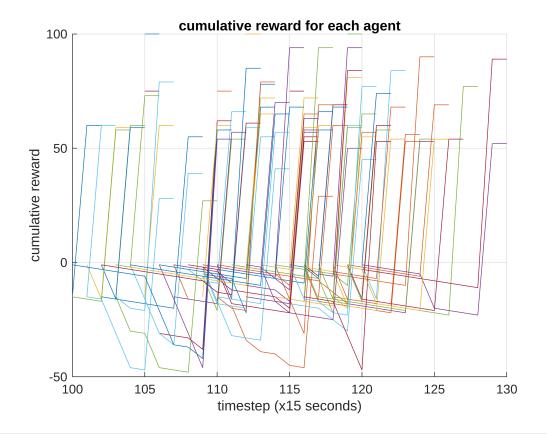
```
congestion_factor_sum = 160
```

```
figure;
hold on
plot(time_index_vector', active_data_packet,'LineWidth',2)
plot(time_index_vector', active_sats,'LineWidth',2)
plot(time_index_vector', congestion_factor_vector,'LineWidth',2)
grid on
title('Congestion Status')
xlabel('timestep (x15 seconds)')
legend('Active Data Packets',"Activated Satellites","Number")
```



VII. Result Graph

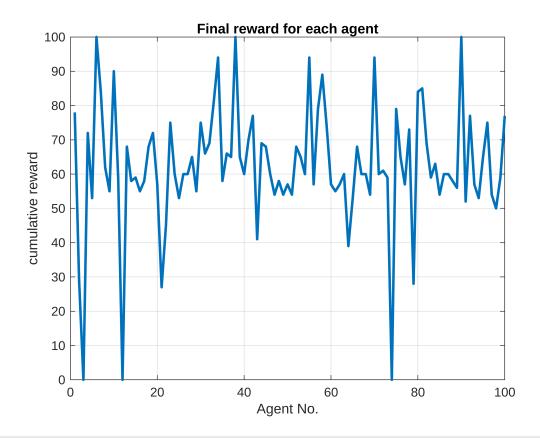
```
number_of_agents = length(agents_input(:,1));
final_cumulative_reward_vector = zeros(number_of_agents,1);
figure;
hold on
```



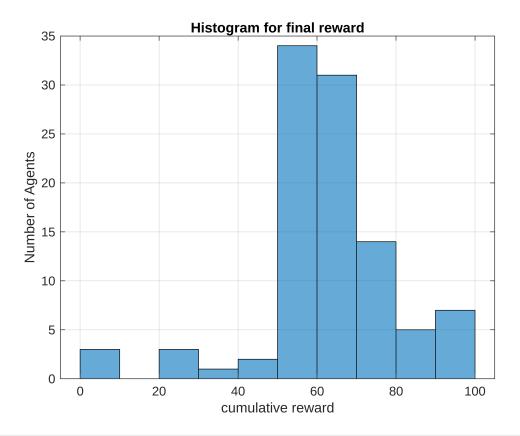
```
for agent_index = 1:number_of_agents
    each_agent_reward_vector = cumulative_reward_matrix(:,agent_index);
    each_agent_reward= each_agent_reward_vector(each_agent_reward_vector ~=
0);
    if isempty(each_agent_reward) == true
        continue;
    end
        final_cumulative_reward_vector(agent_index) = each_agent_reward(end);
end

figure;
plot((1:number_of_agents)',final_cumulative_reward_vector,"LineWidth",2)
grid on
```

```
title('Final reward for each agent')
xlabel('Agent No.')
ylabel('cumulative reward')
```



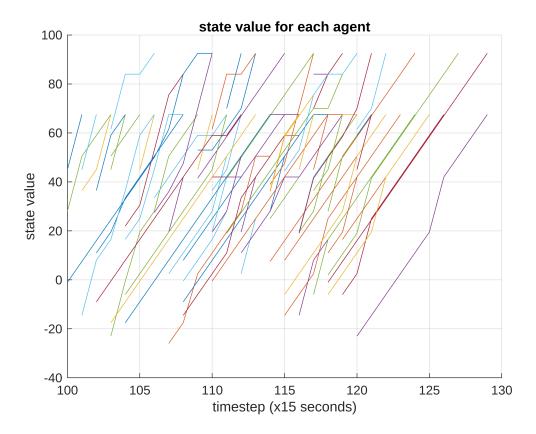
```
figure;
histogram(final_cumulative_reward_vector)
grid on
title('Histogram for final reward')
xlabel('cumulative reward')
ylabel('Number of Agents')
```



```
figure;
hold on
for agent_index = 1:number_of_agents

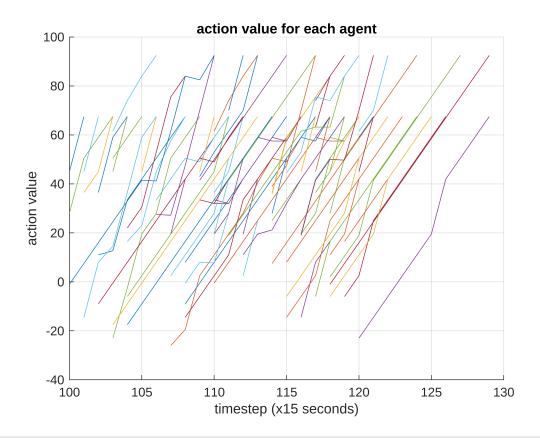
    state_value_each_agent = [time_index_vector',
    state_value_matrix(:,agent_index)];
    state_value_each_agent =
    state_value_each_agent(state_value_each_agent(:,2) ~= 0, :);

    plot(state_value_each_agent(:,1),state_value_each_agent(:,2))
end
hold off
grid on
title('state value for each agent')
xlabel('timestep (x15 seconds)')
ylabel('state value')
```



```
figure;
hold on
for agent_index = 1:number_of_agents

    action_value_each_agent = [time_index_vector',
action_value_matrix(:,agent_index)];
    action_value_each_agent =
action_value_each_agent(action_value_each_agent(:,2) ~= 0, :);
    plot(action_value_each_agent(:,1),action_value_each_agent(:,2))
end
hold off
grid on
title('action value for each agent')
xlabel('timestep (x15 seconds)')
ylabel('action value')
```



```
figure;
hold on
for agent_index = 1:number_of_agents

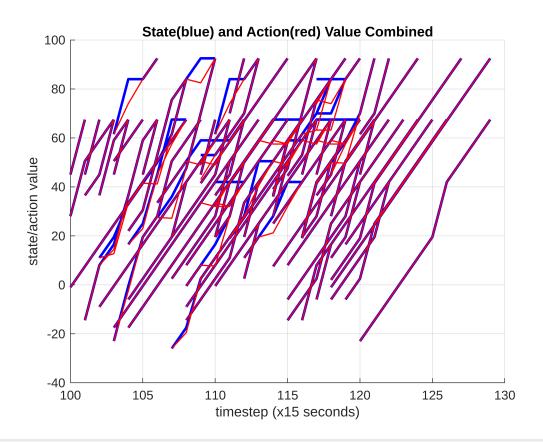
    state_value_each_agent = [time_index_vector',
state_value_matrix(:,agent_index)];
    state_value_each_agent =
state_value_each_agent(state_value_each_agent(:,2) ~= 0, :);

plot(state_value_each_agent(:,1),state_value_each_agent(:,2),'b','LineWidth',
2)
end

for agent_index = 1:number_of_agents

    action_value_each_agent = [time_index_vector',
action_value_matrix(:,agent_index)];
    action_value_each_agent =
action_value_each_agent =
action_value_each_agent(action_value_each_agent(:,2) ~= 0, :);
```

```
plot(action_value_each_agent(:,1),action_value_each_agent(:,2),'r','LineWidth
',1)
end
hold off
grid on
title('State(blue) and Action(red) Value Combined')
xlabel('timestep (x15 seconds)')
ylabel('state/action value')
```



```
figure;
hold on
for agent_index = 1:number_of_agents
    result_sorted = [result(:,1), result(:,1+agent_index)];
    result_sorted_nonzero = result_sorted(result_sorted(:,2) ~= 0,:);
    plot(result_sorted_nonzero(:,1),result_sorted_nonzero(:,2))
end
hold off
grid on
title('Network Trajectory By Each Agent')
xlabel('timestep (x15 seconds)')
ylabel('Satellite No.')
```

