



ASE374K

CONOPS and Attitude Control by Operation Modes

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Mission Patch





I. Review of Mission Scope

Mission Statement:

- Design Low-Earth-Orbit Solar Power Satellite 'Redstone' operation concept which receives solar power via solar panel and transmit energy to designated ground plant.

Primary Mission Objectives

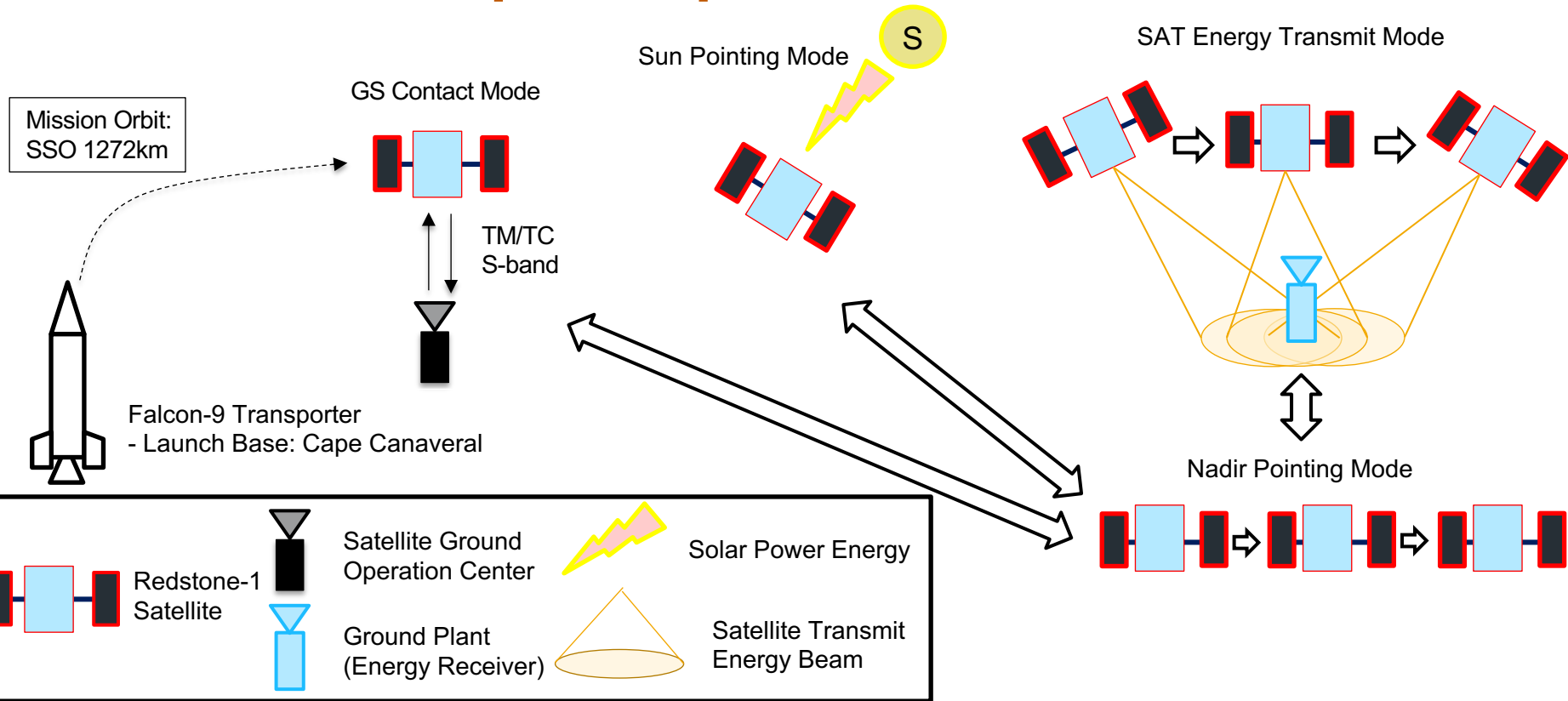
- Satellite shall receive solar energy from sun more than [1,TBD] kJ per [1, TBD] orbit .
- Satellite shall transmit stored solar energy to [3, TBD] ground stations [1,TBD]kJ each per [1, TBD]week.

Secondary Mission Objective

- Satellite can transmit stored solar energy to cislunar orbit satellite or other satellites. [Concept Study]
- Propose constellation strategy for continuous solar power reception and transmission. [Concept Study]

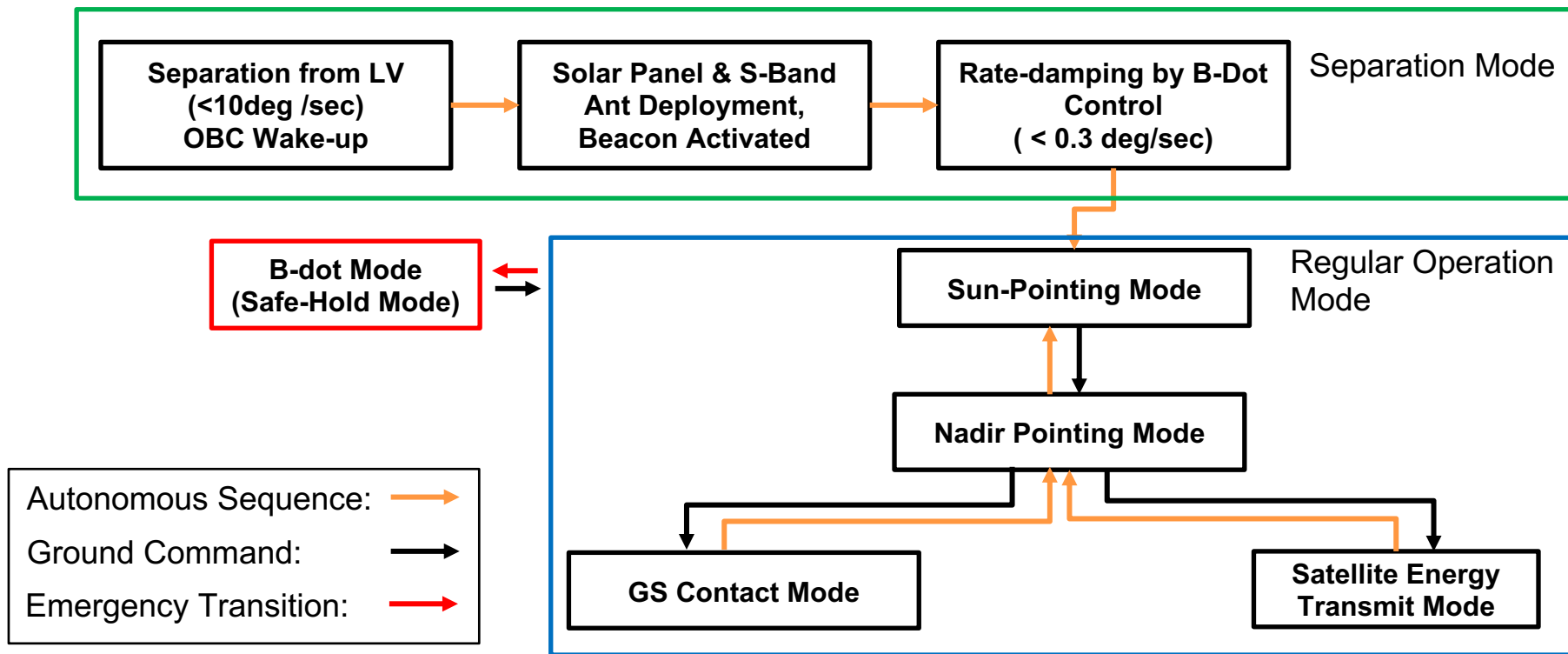


II. Satellite Concept of Operations





III. Operation Mode Definition (1/4)





III. Operation Mode Definition (2/4)

Separation Mode

- Pre-Launch Condition: No power will be provided before separation from launch vehicle
- After separation from launch vehicle, the max tip-off rate of 10deg/sec is anticipated and satellite OBC will wake up and start to send beacon signal
- Solar array will be deployed for the generation of solar power
- B-dot Controller will autonomously start to run to damp out high tip-off rate of 10deg/sec to 0.3deg/sec: predicted time duration for detumbling is less than about 4.2 hrs.
- After settling down to satellite rate of 0.3deg/sec, the sun pointing controller will autonomously start to run to make solar array face to the sun for taking solar power by three-axis control method

Sun Pointing Mode

- The sun pointing mode requires aligning $-y$ body axis to sun vector
- The sun-pointing controller will autonomously start from the “Post-Launch Mode” to make solar array face to the sun for taking solar power by three-axis control method.
- If no anomaly, most of the lifetime of satellite will be operated with “Sun Pointing Mode”
- Sun sensors, star tracker, gyro, three-axis magnetometer as sensors and RWAs, magnetic torque rod will be utilized for three axis control and momentum dumping
- Estimation algorithm will run to estimate to attitude and rate information



III. Operation Mode Definition (3/4)

Nadir Pointing Mode

- The Nadir Pointing Mode is aligning z vector to center of earth, and x vector to velocity of spacecraft
- Between transition to any normal operation mode (solar pointing mode, Nadir Pointing Mode, GS contact mode, Satellite Energy transmission mode), the satellite should transit to Nadir Pointing Mode
- The RWA shall comply performance requirements to transit from Nadir Point Mode to any operation mode and vice versa

GS contact Mode

- Since we are using S-band transceiver for TM/TC operation, the satellite will maintain Nadir Pointing mode while making communication with ground station.
- The S-band transceiver turns on this operation mode

Satellite Energy Transmit Mode

- Satellite z-axis will point designated ground energy plant and transmit the stored solar energy
- When this mode is planed, the satellite will point nadir direction and do roll-off and pitch-off maneuver if necessary
- Mode transition from “Sun-Pointing Mode” to “Satellite Energy Transmit Mode” will be performed by ground commands, NOT autonomously



III. Operation Mode Definition (4/4)

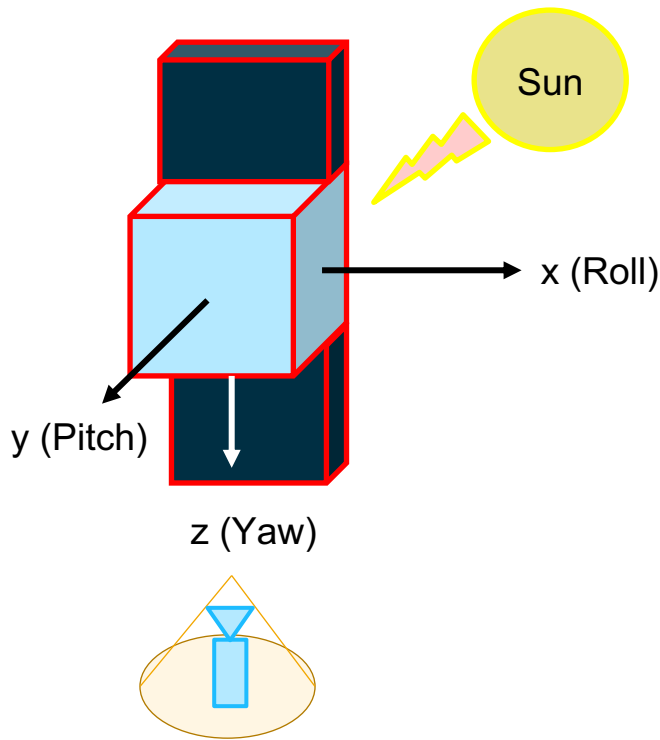
Safe-Hold Mode

- If there are some kinds of anomaly at hardware or software by unknown reason or SEU, satellite will enter from any mode to “Safe-Hold Mode” autonomously
- Once abnormal condition is detected, the satellite will be transition to the “Safe-Hold Mode” for survival of satellite, which makes first OBC power-reset and power-off unnecessary hardware for power-saving and satellite survival.
- Magnetic torque rods, sun sensors and magnetometer will be used for two axis control to save power. [TBD]
- Estimation algorithm will run to estimate the attitude and rate information. [TBD]
- Recovery from “Safe-Hold Mode” to “Sun-Pointing Mode” will be done by ground commands.



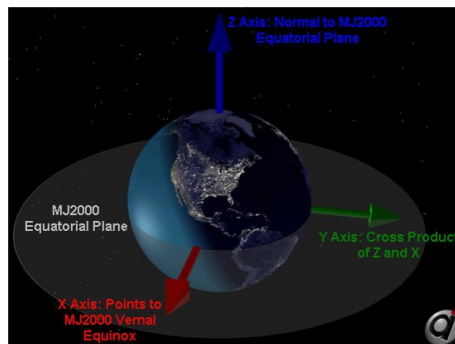
IV. Satellite Dynamics Modeling [1/4]

Satellite Body Frame Definition

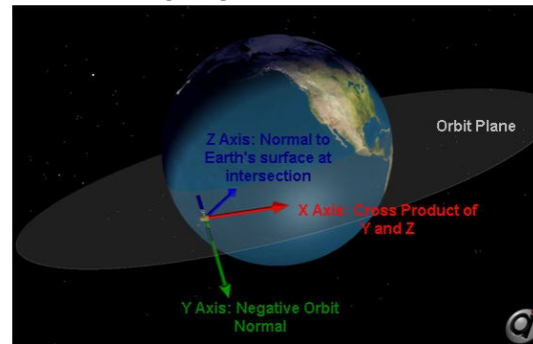


Satellite Orbit Frame Definition

MJ2000 Frame



LVLH Frame



https://ai-solutions.com/_freelyflyeruniversityguide/attitude_reference_frames.htm

- We are using Euler Angle 3-1-2 Rotation System for generating Direction-Cosine-Matrix (DCM)
- We are using ECI Frame as MJ2000 Equatorial Frame to get satellite, sun, star locations
- We are using LVLH frame to get Nadir direction
- Since our proposed orbit is circular orbit x axis of LVLH frame = velocity vector of satellite



IV. Satellite Dynamics Modeling [2/4]

Important Assumptions

J2 Perturbation

- J2 Perturbation by earth oblateness is the single perturbation factor calculating satellite orbit trajectory
- We assume the Satellite maintain two-body dynamics except J2 Perturbation

Low-Earth-Orbit Circular Orbit

- We assume satellite's orbit is LEO perfect Circular Orbit
- We assume Geodetic frame of satellite is exactly same as LVLH frame, and x axis of LVLH frame is same as velocity vector of satellite since it is circular orbit

Perfect Sphere Earth

- We assume Earth is perfect sphere with 6378km radius, but only assume oblateness for J2 perturbation
- Nadir pointing of the Earth is same as Satellite pointing to center of earth, and z body axis is normal to tangent plane of nadir pointing ground location

Ignorance of Precession and Nutation of Satellite

- We assume satellite's MOI is diagonal matrix which indicate one axis of rotation does not impact another axis rotation



IV. Satellite Dynamics Modeling [3/4]

Satellite State Vector

$$\mathbf{X}_{\text{SAT}} = \begin{bmatrix} \vec{r}_I \\ \vec{v}_I \\ R_{\text{BI}} \\ \vec{\omega}_B \\ \vec{\omega}_{\text{RWA}} \end{bmatrix}$$

\vec{r}_I : Satellite Position Vector in ECI frame

\vec{v}_I : Satellite Velocity Vector in ECI frame

R_{BI} : Rotation Matrix from ECI frame to Body Frame

$\vec{\omega}_B$: Satellite Angular Velocity Vector w. r. t Body Frame

$\vec{\omega}_{\text{RWA}}$: Satellite Reaction Wheels Angular Velocity vector

Satellite Dynamic Model

$$\dot{\mathbf{X}}_{\text{SAT}} = f_{\text{SAT}}\left(t, \mathbf{X}_{\text{SAT}}, \vec{e}_a, \vec{d}_I, P\right) : \text{Non - linear dynamic Model of } \dot{\mathbf{X}}_{\text{sat}}$$

t : Time

\mathbf{X}_{SAT} : Satellite State Vector

\vec{e}_a : Satellite Reaction Wheels Motor Voltage (Control input)

\vec{d}_I : Satellite Disturbance Force Vector (Disturbance)

P : Satellite Parameter Structure

m : Mass of Satellite

J : Satellite's Moment of Inertia

τ_m : Time constant for Motor Dynamics

c_m : Steady - State Parameter : voltage to angular rate ω (rad/s)

I_{RWA} : Momentum of Inertia of Reaction Wheel



IV. Satellite Dynamics Modeling [4/4]

Satellite Dynamic Model

$$\dot{\mathbf{X}}_{\text{SAT}} = f_{\text{SAT}}\left(t, \mathbf{X}_{\text{SAT}}, \vec{e}_a, \vec{d}_I, P\right) : \text{Non-linear dynamic Model of } \dot{\mathbf{X}}_{\text{sat}}$$

$$\mathbf{X}_{\text{SAT}} = \begin{bmatrix} \vec{r}_I \\ \vec{v}_I \\ R_{\text{BI}} \\ \vec{\omega}_B \\ \vec{\omega}_{\text{RWA}} \end{bmatrix}$$

\vec{r}_I : Satellite Position Vector in ECI frame

\vec{v}_I : Satellite Velocity Vector in ECI frame

R_{BI} : Rotation Matrix from ECI frame to Body Frame

$\vec{\omega}_B$: Satellite Angular Velocity Vector w. r. t Body Frame

$\vec{\omega}_{\text{RWA}}$: Satellite Reaction Wheels Angular Velocity vector

$$\dot{\mathbf{r}}_I = \mathbf{v}_I$$

$$\dot{\mathbf{v}}_I = \begin{bmatrix} -\mu \frac{r_{\text{xl}}}{r^3} \left[1 - \frac{3}{2} J_2 \left(\frac{R_{\text{Earth}}}{r} \right)^2 \left(5 \left(\frac{r_{\text{zl}}}{r} \right)^2 - 1 \right) \right] \\ -\mu \frac{r_{\text{yl}}}{r^3} \left[1 - \frac{3}{2} J_2 \left(\frac{R_{\text{Earth}}}{r} \right)^2 \left(5 \left(\frac{r_{\text{zl}}}{r} \right)^2 - 1 \right) \right] \\ -\mu \frac{r_{\text{zl}}}{r^3} \left[1 - \frac{3}{2} J_2 \left(\frac{R_{\text{Earth}}}{r} \right)^2 \left(5 \left(\frac{r_{\text{zl}}}{r} \right)^2 - 3 \right) \right] \end{bmatrix}$$

$$\dot{R}_{\text{BI}} = -\omega_B \times R_{\text{BI}}$$

$$\dot{\omega}_B = J^{-1} \left(\vec{N}_B - [\omega_B \times] J \omega_B \right)$$

$$\dot{\omega}_{\text{RWA}} = -\frac{\vec{\omega}_{\text{RWA}}}{\tau_m} + \frac{c_m}{\tau_m} \vec{e}_a$$

Assumption: Reaction Wheel is Mounted parallel to Each Body Axis

J_2 Perturbation Model

J_2 : J_2 Perturbation Constant

μ : Gravity Constant

R_{Earth} : Earth Radius

$r = |\mathbf{r}_I|$

$\mathbf{r}_I = (r_{\text{xl}}, r_{\text{yl}}, r_{\text{zl}})^T$

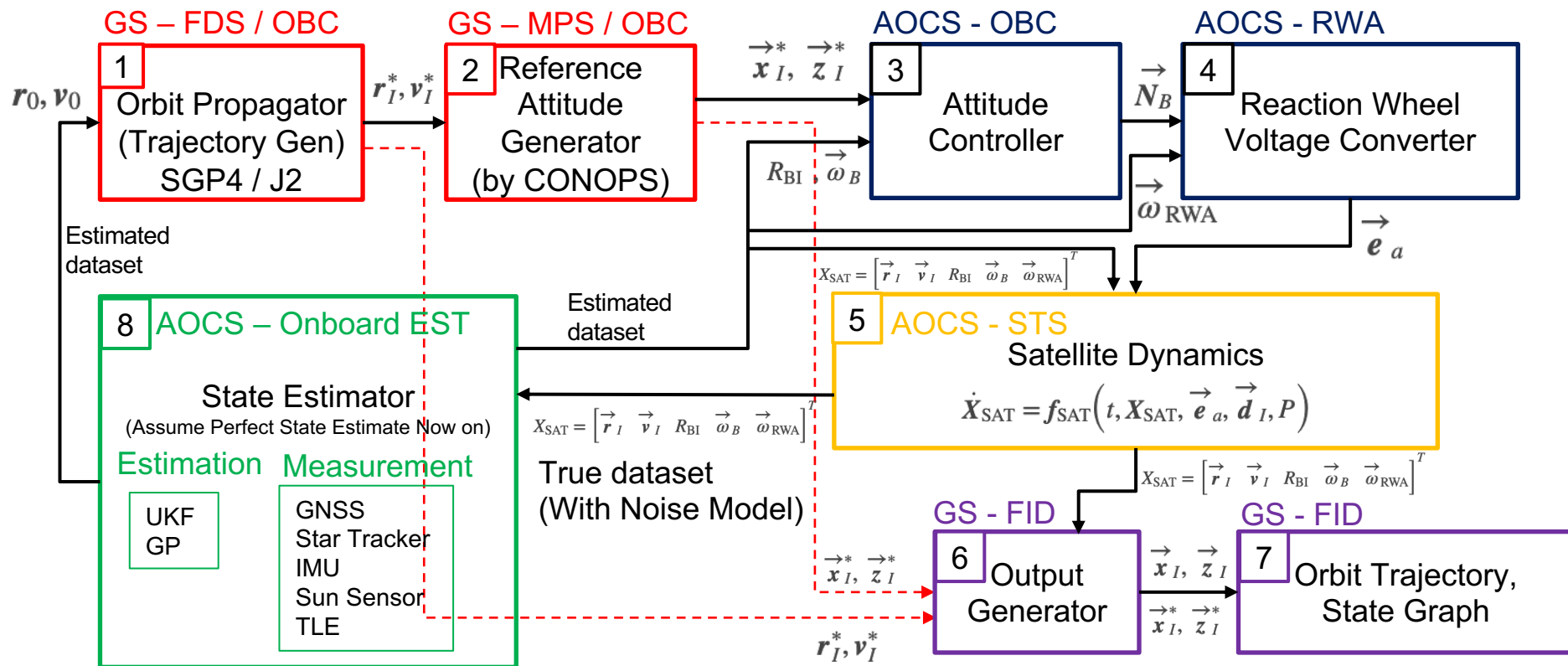
Body Torque Calculation RWA Dynamics

\vec{N}_B : Body Torque Vector

$$\vec{N}_B = -I_{\text{RWA}} \dot{\omega}_{\text{RWA}} = I_{\text{RWA}} \left(-\frac{\vec{\omega}_{\text{RWA}}}{\tau_m} + \frac{c_m}{\tau_m} \vec{e}_a \right)$$



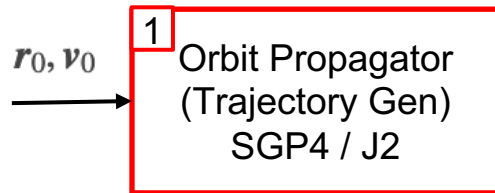
V. Satellite Controller Modeling [1/6]





V. Satellite Controller Modeling [2/6]

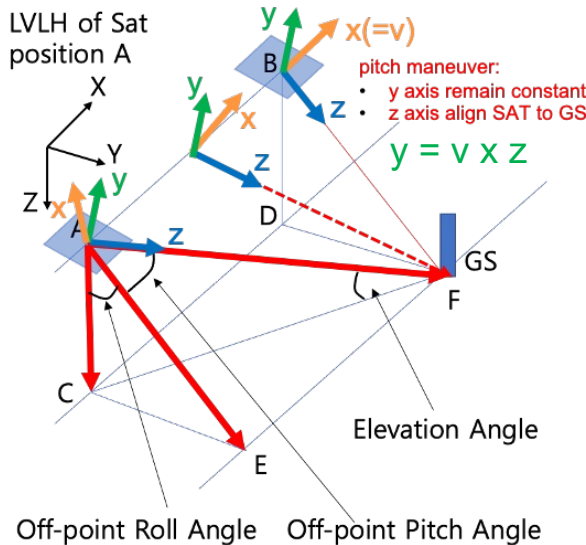
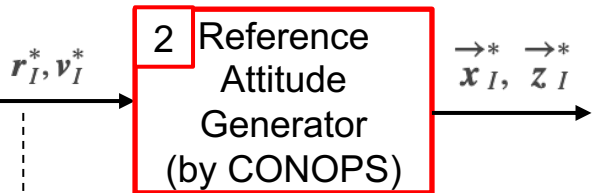
1. On-orbit Propagator



Input : Current Estimated \mathbf{r}, \mathbf{v}
Output: Propagated Trajectory
Using Existing J2 Model

- Can be substituted by SGP4 Model with TLE telemetry information
- Or can use more precise Propagation Model

2. Reference Attitude Generator



I/O Structure

Input : Propagated Trajectory $\mathbf{r}_I^*, \mathbf{v}_I^*$

Output : Reference Attitude Body Axis $\vec{\mathbf{z}}_I^*, \vec{\mathbf{x}}_I^*$

cf : $\vec{\mathbf{z}}_I^* = R_{BI}^T [0 \ 0 \ 1]^T$, $\vec{\mathbf{x}}_I^* = R_{BI}^T [1 \ 0 \ 0]^T$

Different Attitude Generation by Operating Mode

1) Nadir Pointing Mode

$$\Rightarrow \vec{\mathbf{x}}_I^* = \frac{\vec{\mathbf{v}}_I^*}{|\vec{\mathbf{v}}_I^*|}, \vec{\mathbf{z}}_I^* = -\frac{\vec{\mathbf{r}}_I^*}{|\vec{\mathbf{r}}_I^*|}$$

2) Energy Transmitting Mode

\Rightarrow Ground Location Vector $\vec{\mathbf{r}}_{GS}$

$$\Rightarrow \vec{\mathbf{z}}_I^* = \frac{\vec{\mathbf{r}}_{GS} - \vec{\mathbf{r}}_I^*}{|\vec{\mathbf{r}}_{GS} - \vec{\mathbf{r}}_I^*|}, \vec{\mathbf{y}}_I^* = \frac{\vec{\mathbf{z}}_I^* \times \vec{\mathbf{v}}_I^*}{|\vec{\mathbf{z}}_I^* \times \vec{\mathbf{v}}_I^*|}$$

$$\Rightarrow \vec{\mathbf{x}}_I^* = \vec{\mathbf{y}}_I^* \times \vec{\mathbf{z}}_I^*$$

3) Sun Pointing Mode

\Rightarrow Sun direction vector $\hat{\mathbf{r}}_{\text{sun}}$

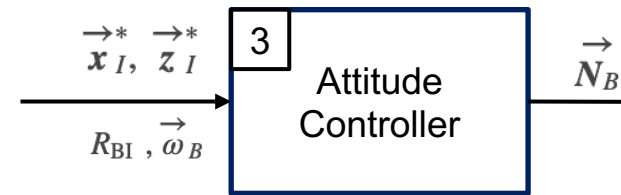
$$\Rightarrow \vec{\mathbf{y}}_I^* = -\hat{\mathbf{r}}_{\text{sun}}, \vec{\mathbf{z}}_I^* = \frac{\vec{\mathbf{v}}_I^* \times \vec{\mathbf{y}}_I^*}{|\vec{\mathbf{v}}_I^* \times \vec{\mathbf{y}}_I^*|}$$

$$\Rightarrow \vec{\mathbf{x}}_I^* = \vec{\mathbf{y}}_I^* \times \vec{\mathbf{z}}_I^*$$



V. Satellite Controller Modeling [3/6]

3. Attitude Controller



Calculate error vector \vec{e}

Use TRIAD Method to Determine R_{BI}^* R_{BI}^* : Reference Direction Cosine Matrix

\vec{x}_I, \vec{z}_I : Reference Attitude Input

$$\vec{b} = \frac{\vec{z}_I \times \vec{x}_I}{|\vec{z}_I \times \vec{x}_I|}$$

$$\text{if } \vec{z}_I \times \vec{x}_I = 0 \Rightarrow \vec{b} = \vec{0}$$

$$\vec{a} = \vec{b} \times \vec{z}_I$$

$$R_{BI}^* = \begin{bmatrix} | & | & | \\ \vec{a} & \vec{b} & \vec{z}_I \\ | & | & | \end{bmatrix}^T$$

R_E : Error Direction Cosine Matrix

$$R_{BI}^* = R_E R_{BI} \Leftrightarrow R_E = R_{BI}^* R_{BI}^T$$

$$R_E = \begin{bmatrix} e_{11} & e_{12} & e_{13} \\ e_{21} & e_{22} & e_{23} \\ e_{31} & e_{32} & e_{33} \end{bmatrix} \Rightarrow \vec{e} = \begin{bmatrix} e_{23} - e_{32} \\ e_{31} - e_{13} \\ e_{12} - e_{21} \end{bmatrix}$$

We assume $\dot{\vec{e}} = -\dot{\omega}_B$

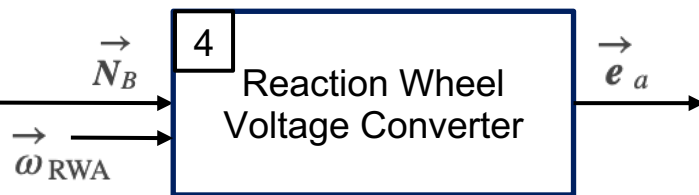
Design PD Controller

$$\vec{N}_B = K_p \vec{e} - K_d \dot{\omega}_B + [\dot{\omega}_B \times] J \dot{\omega}_B$$

K_p, K_d : PD gain matrix

\vec{N}_B : Required body torque (Control Input)

4. Reaction Wheel Voltage Converter



Reaction Wheel Motor Dynamics

$$\frac{\Omega(s)}{E_a(s)} = \frac{c_m}{\tau_m s + 1} : \text{1st order system}$$

$\Omega(s)$: RWA Angular Rate in s domain

$E_a(s)$: RWA Input Voltage in s domain

$$\Omega(s)(\tau_m s + 1) = c_m E_a(s)$$

$$s\Omega(s) = \frac{1}{\tau_m} (c_m E_a(s) - \Omega(s))$$

$$\therefore \dot{\omega}_{RWA}(t) = \frac{1}{\tau_m} (c_m e_a(t) - \omega_{RWA}(t))$$

Reaction Wheel Voltage Converter Design

Input: \vec{N}_B : Required body torque (Attitude Control output)

$\vec{\omega}_{RWA}$: Reaction wheel angular rate (From Estimator)

Output: \vec{e}_a Required motor voltage (Control Input to SAT)

$$\vec{N}_B = -I_{RWA} \dot{\omega}_{RWA} \Rightarrow -I_{RWA}^{-1} \vec{N}_B = \dot{\omega}_{RWA}$$

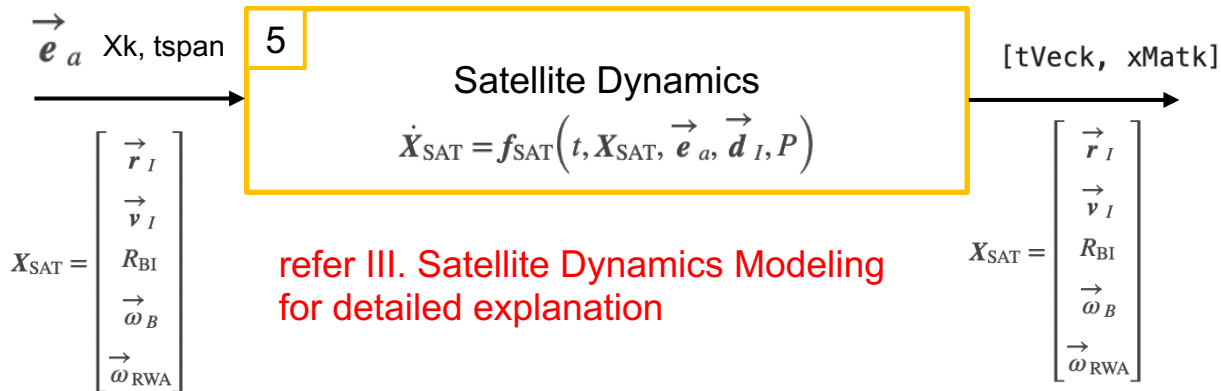
$$-I_{RWA}^{-1} \vec{N}_B = \frac{1}{\tau_m} (c_m \vec{e}_a - \vec{\omega}_{RWA})$$

$$\therefore \vec{e}_a = \frac{1}{c_m} [-I_{RWA}^{-1} \vec{N}_B \tau_m + \vec{\omega}_{RWA}]$$



V. Satellite Controller Modeling [4/6]

5. Satellite Dynamics



```
function [Xdot] = SAT0deFunctionHF(t,X,eaVec,distVec,P)

INPUTS

t ----- Scalar time input, as required by Matlab's ODE function
format.

X ----- Nx-by-1 SAT state, arranged as

X = [rI',vI',RBI(1,1),RBI(2,1),...,RBI(2,3),RBI(3,3),...
      omegaB',omegaVec']'

rI = 3x1 position vector in I in meters
vI = 3x1 velocity vector wrt I and in I, in meters/sec
RBI = 3x3 attitude matrix from I to B frame
omegaB = 3x1 angular rate vector of body wrt I, expressed in B
in rad/sec
omegaVec = 4x1 vector of rotor angular rates, in rad/sec.
omegaVec(i) is the angular rate of the ith rotor.

eaVec --- 4x1 vector of voltages applied to motors, in volts. eaVec(i)
is the constant voltage setpoint for the ith rotor.

distVec --- 3x1 vector of constant disturbance forces acting on the SAT's
center of mass, expressed in Newtons in I.

OUTPUTS

Xdot ----- Nx-by-1 time derivative of the input vector X
```

Generate oversampled, updated satellite dynamics using integrator function (ODE45 or RK4)

```
eak = voltageConverterSAT(NBk,omegaVec_k,P_voltage);
```

```
Xk = [r_k;v_k;RBI_k(:);omegaB_k;omegaVec_k];
```

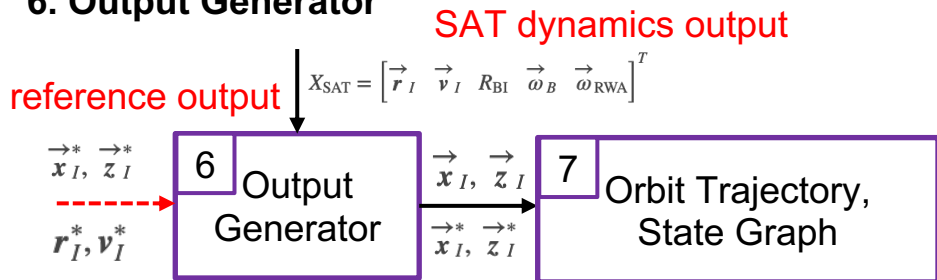
```
[tVeck, xMatk] = ode45(@(t,X) SAT0deFunctionHF(t,X,eak,distMat_k,Parameters), tspan,Xk);
```

Then Store the simulation output [tVeck, xMatk]



V. Satellite Controller Modeling [5/6]

6. Output Generator



List of Available Output

1. Satellite Trajectory with Body Axis Vector display

⇒ Reference Trajectory and attitude : $\vec{r}^*, \vec{x}_I^*, \vec{z}_I^*, \vec{y}_I^* (= \vec{z}_I^* \times \vec{x}_I^*)$

⇒ Output Trajectory and attitude : $\vec{r}, \vec{x}_I = R_{BI}^T \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \vec{y}_I = R_{BI}^T \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}, \vec{z}_I = R_{BI}^T \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$

⇒ We can use **quiver** function for display trajectory and attitude vector

2. Satellite Euler angle (Roll, Pitch, Yaw) display

$$\Rightarrow \text{Reference Euler Angle : } R_{BI}^* = \begin{bmatrix} | & | & | \\ \vec{a} & \vec{b} & \vec{z}_I^* \\ | & | & | \end{bmatrix}^T \begin{cases} \vec{b} = \frac{\vec{z}_I^* \times \vec{x}_I^*}{|\vec{z}_I^* \times \vec{x}_I^*|}, \text{ if } \vec{z}_I^* \times \vec{x}_I^* = 0 \Rightarrow \vec{b} = 0 \\ \vec{a} = \vec{b} \times \vec{z}_I^* \end{cases}$$

$$\phi^* = \sin^{-1}(R_{BI}^*(2, 3)), \theta^* = \tan^{-1}\left(-\frac{R_{BI}^*(1, 3)}{R_{BI}^*(3, 3)}\right), \psi^* = \tan^{-1}\left(-\frac{R_{BI}^*(2, 1)}{R_{BI}^*(2, 2)}\right)$$

⇒ Output Euler Angle : Using R_{BI} from X_{SAT}

$$\phi = \sin^{-1}(R_{BI}(2, 3)), \theta = \tan^{-1}\left(-\frac{R_{BI}(1, 3)}{R_{BI}(3, 3)}\right), \psi = \tan^{-1}\left(-\frac{R_{BI}(2, 1)}{R_{BI}(2, 2)}\right)$$

3. Reaction Wheel Angular Rate display

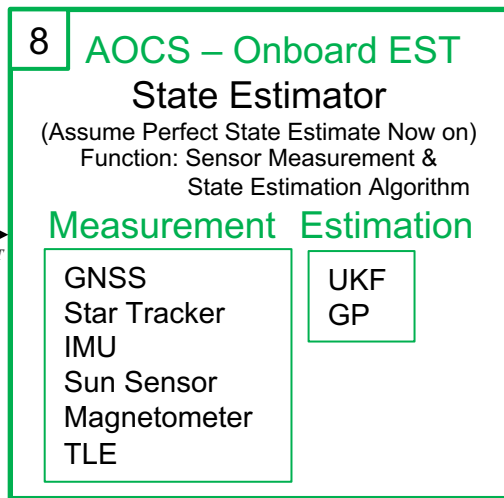
⇒ Use $\vec{\omega}_{RWA}$ from X_{SAT}

- We can make more visualized output from given dataset
- ECI to LLA map display, Pointing Display for GS Contact
- Sun Pointing Display, Nadir Pointing Display



V. Satellite Controller Modeling [6/6]

8. State Estimator



$$\mathbf{X}_{\text{SAT}} = \begin{bmatrix} \vec{r}_I & \vec{v}_I & R_{BI} & \vec{\omega}_B & \vec{\omega}_{RWA} \end{bmatrix}^T$$

True dataset
(With Noise Model)

$$\mathbf{X}_{\text{SAT}} = \begin{bmatrix} \vec{r}_I & \vec{v}_I & R_{BI} & \vec{\omega}_B & \vec{\omega}_{RWA} \end{bmatrix}^T$$

Estimated dataset

- Currently, assuming we have perfect estimation, so estimated dataset is same with True Dataset with no noise model
- In the future research we will develop the onboard sensor measurement model and estimation model

- Since the satellite does not receive the perfectly accurate dataset, for high-fidelity simulation, we should model the noised / biased state signal and sensor dynamics model
- The satellite uses multiple sensors for trajectory and attitude (GNSS, Star Tracker, IMU, Sun Sensor, TLE Telemetry, Magnetometer, etc.)
- By sensor fusion technique like Unscented Kalman Filter, satellite optimizes the state signal
- By optimization methodology such as Gaussian Process or Bayesian Optimization, Satellite Develops innate dynamic model for advanced adaptive control



VI. Simulation Parameters Modeling

Epoch :

Mar 21, 2024

Satellite Initial Location :

SMA = 7640km

eccentricity $e = 1.6e - 5$

inclination $i = 100.7$ deg

RAAN $\Omega = 90$ deg

AOP $\omega = 0$ deg

True Anomaly $\theta = 0$ deg

Designated Ground Station :

Austin, Texas :

Latitude = 30.285 deg

Longitude = -97.735 deg

Altitude = 70m

Satellite Initial Operation Mode : Nadir

Nadir Mode Simulation Specification :

Total Elapsed Time : 3600 sec

Energy Transmission Mode Simulation Specification :

Total Elapsed Time : 1000 sec

Slant Range Calculation Include

Sun Pointing Mode Simulation Specification

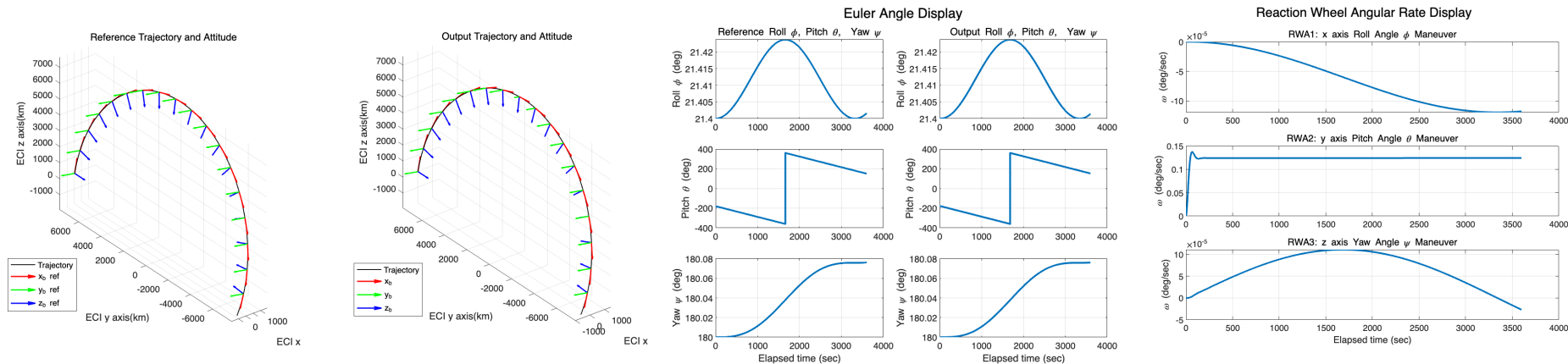
Total Elapsed Time : 3600 sec

Sun vector on 3/21/2024 : (1, 0, 0) \Rightarrow Changed by Day



VII. Simulation Results and Discussion [1/3]

Result 1: Nadir Pointing Mode

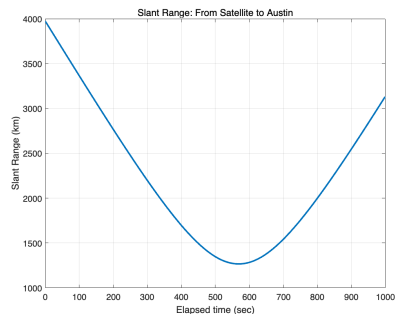
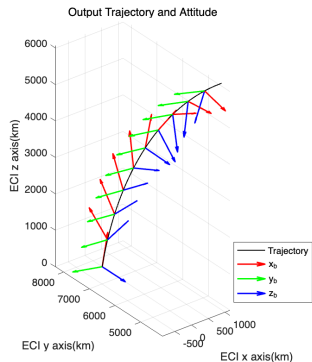
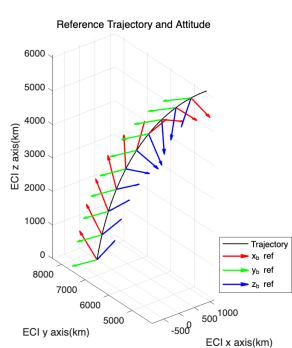


- The satellite has good tracking performance for Nadir Pointing Mode
- RWA #2 maintains steady-state non-zero angular velocity, which indicates there exist constant momentum for Nadir pointing mode
- RWA #1 and #3 almost remains zero rotational speed

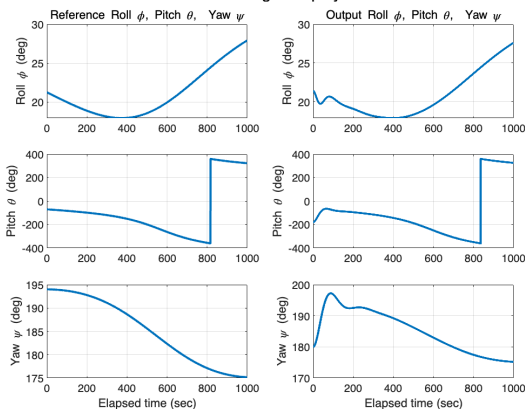


VII. Simulation Results and Discussion [2/3]

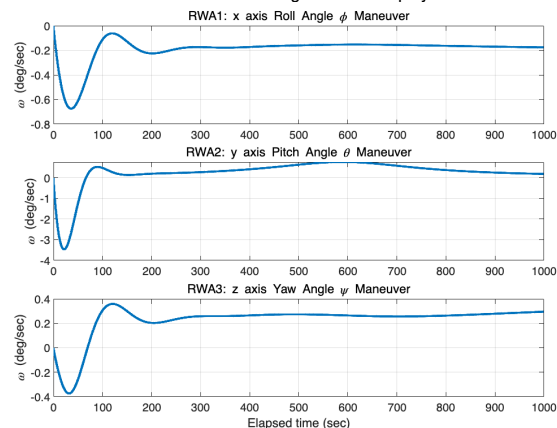
Result 2: Energy Transmission Mode



Euler Angle Display



Reaction Wheel Angular Rate Display

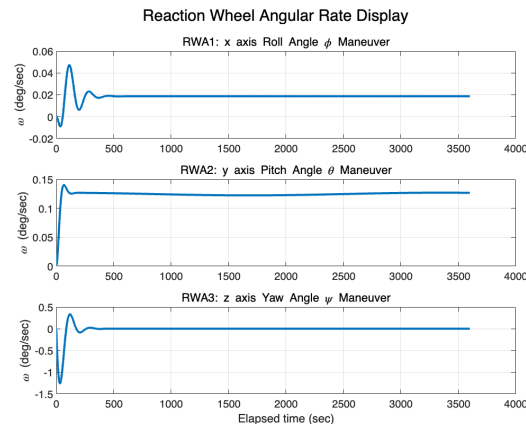
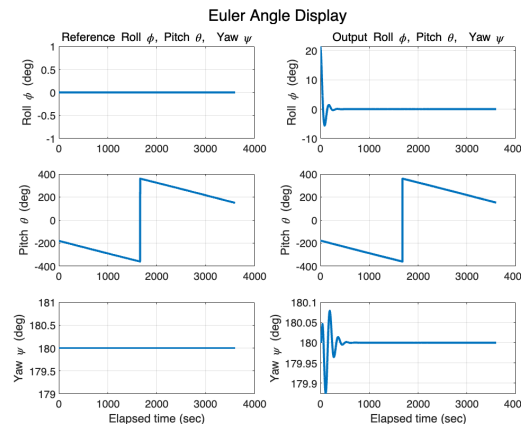
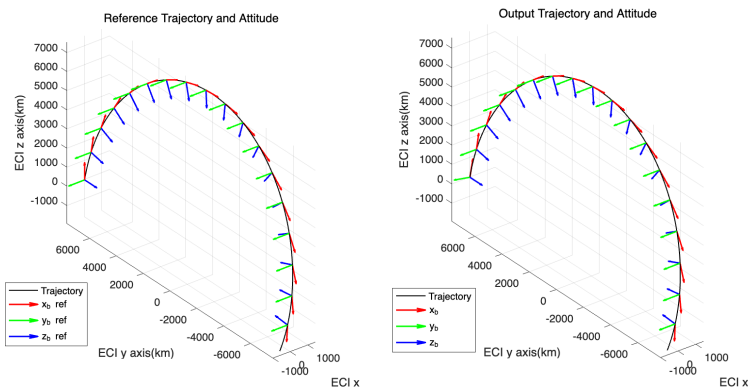


- The satellite requires 100 seconds to transit from Nadir pointing mode for Energy Transmission mode in given condition
- The satellite has good ground plant tracking performance after transition to Energy Transmission mode
- The Yaw-axis maneuver exists in Energy transmission mode
- The shortest slant range occurs around elapsed time 550 seconds



VII. Simulation Results and Discussion [3/3]

Result 3: Sun Pointing Mode



- The tracking performance of Sun-Pointing mode is good, maintaining constant roll and yaw angle.
- The satellite requires around 250 seconds for transition from nadir pointing mode to sun pointing mode in given simulation environment
- The RWA #1 and #2 maintains non-zero steady state angular rate, which indicates there exist steady-state angular momentum



VIII. Conclusion and Future Research

- In this session, we have discussed the Redstone-1's concept of operations and defined operation mode
- We have discussed the Redstone-1's attitude control mechanism
- We have discussed simulation of transition between normal operation modes in given initial condition
- In future research, we will investigate the satellite Sensor Measurement and Estimation Method



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