#### Ch 10.3: Convolutional Neural Nets

Lecture 22 - CMSE 381

Michigan State University

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Dept of Computational Mathematics, Science & Engineering

Monday, April 15, 2024

#### Announcements

#### Last time:

- Multilayer
- pyTorch

#### This lecture:

CNNs

#### **Announcements:**

 last and this week's in-class assignments both due this week

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Grades conversion

Convert
4.0
3.5
3
2.5
2
1.5
1
0

## Section 1

Last time: Neural Nets

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## **MNIST**



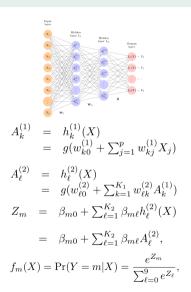






- Goal: Build a model to classify images into their correct digit class
- Each image has  $p = 28 \cdot 28 = 784$  pixels
- Each pixel is grayscale value in [0,255]
- Data converted into column order
- Output represented by one-hot vector  $Y = (Y_0, Y_1, \dots, Y_9)$
- 60K training images, 10K test images

### Neural network architecture for MNIST

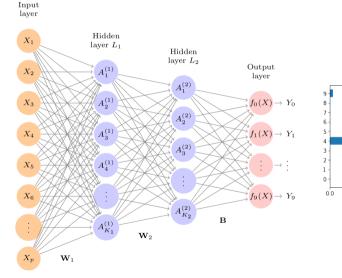


- Two hidden layers.
- Softmax for classification output
- In lab, we used L<sub>1</sub> has 128 units; L<sub>2</sub> has 64
- 10 output variables due to class labeling
- Result is we are training approx 110K weights

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# MNIST learning





0.2 0.4 0.6 0.8 1.0

Class Probability

## Section 2

## Convolutional Neural Network

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# When dealing with images with NN: Flattening the image

$$\begin{pmatrix} 1 & 1 & 0 \\ 4 & 2 & 1 \\ 0 & 2 & 1 \end{pmatrix} \longrightarrow \begin{pmatrix} 1 \\ 1 \\ 0 \\ 4 \\ 2 \\ 1 \\ 0 \\ 2 \\ 1 \end{pmatrix}$$

- Just ignore the fact that we have a picture
- Loses a lot of the structure that we might want for more complicated
- Answer is CNNs, which take in image data and build a neural net that specifically tracks that structure

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# Example data set: CIFAR100 Data

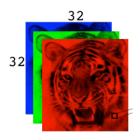


- 60,000 images: 50K training, 10K test
- Labels with 20 super classes (e.g. aquatic mammals)
- 5 classes per super class (beaver, dolphin, otter, seal, whale)
- Images are 32x32

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# Image channel data

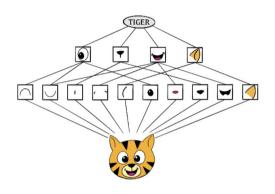
- 3 numbers per pixel (red, green, blue)
- Numbers are organized in a feature map, which is 3 dimensional array
- First two directions are spatial (32x32)
- Third is the *channel* axis representing teh three colors



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## **CNNs**

- Idea is to build a neural net that works on this data
- Identify low level features on the input image such as small edges, patches of color, etc
- Low level features combined into higher-level features (parts of ears, eyes, etc)
- Does this using special types of hidden layers: convolution layers and pooling layers



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#### 1D convolution

**Definition.** Let's start with 1D convolution (a 1D "image," is also known as a signal, and can be represented by a regular 1D vector in Matlab). Let's call our input vector f and our kernel g, and say that f has length n, and g has length m. The convolution f \* g of f and g is defined as:

$$(f * g)(i) = \sum_{j=1}^{m} g(j) \cdot f(i - j + m/2)$$

$$f = \boxed{10 \mid 50 \mid 60 \mid 10 \mid 20 \mid 40 \mid 30}$$

$$g = \boxed{1/3 \mid 1/3 \mid 1/3}$$

$$h = \boxed{20 \mid 40 \mid 40 \mid 30 \mid 20 \mid 30 \mid 23.333}$$

$$h = [20 \mid 40 \mid 40 \mid 30 \mid 20 \mid 30 \mid 23.333]$$

What is the output if using the kernel g = [0.2, 0.6, 0.2] instead? What about g = [0, 1, 0]

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#### 2D convolution

#### Convolution Filter

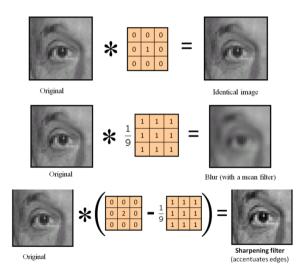
#### Original Image:



#### Convolution filter:

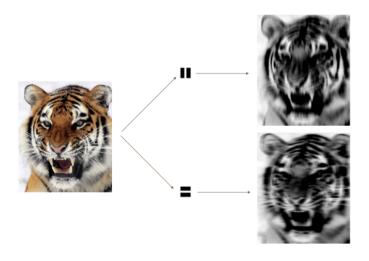
$$\longrightarrow \begin{bmatrix} \alpha & \beta \\ \gamma & \delta \end{bmatrix}$$

# Convolution Filter Example



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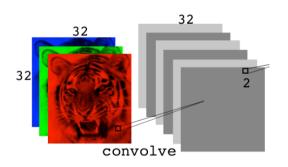
# Convolution filter: Bigger example



- 192×179 image of tiger
- Convolution filters are 15x15 images with mostly zero (black) narrow strip of ones (white)
- Highlights areas of the tiger that resemble the filter

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# Convolution layer -3D



- Image is in color, so 3 channels
- This means the convolution filter will have three channels, one per color, each of dimension 3x3
- Results are summed to form a 2-dimensional output. Color is "forgotton" at this point
- K different filters here means K 2-d output maps, which can then be treated as channels
- Padding to make the updated image the same size

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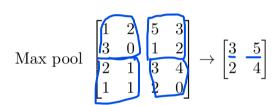
### More notes on convolution

- Filters idea from image processing
- Novelty in DL is that the choice of filters are learned
- Filter weights: one hidden unit per pixel in convolved image; but more constrained than that
- Applying ReLU to convolved image.
   Sometimes viewed as separate layer in CNN, and then called a detector layer.
- Kernels in CNN corresponds to weights in NN.

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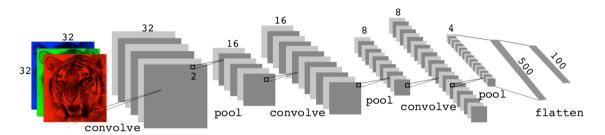
# Pooling layers

- Condense a large image into a smaller summary image
- Lots of options, but max pooling is common:
- For each 2x2 non-overlapping block of pixels, get a single new pixel with the maximum value from the block
- Provides location invariance: so long as large value in one of the four pixels, the whole block registers as a large value



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# Putting it together to make a CNN



- Start with three channels
- get a new channel at first hidden layer for each filter. Padding to keep the same size
- Next is max pool layer,
- convolve & pool several more times

- Since size of image decreased, we increase number of filters in the next convolve layer to compensate
- Flattened, then fed into 1 or more fully-connected layers
- Last is softmax activation for the 100 classes

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https://poloclub.github.io/cnn-explainer/